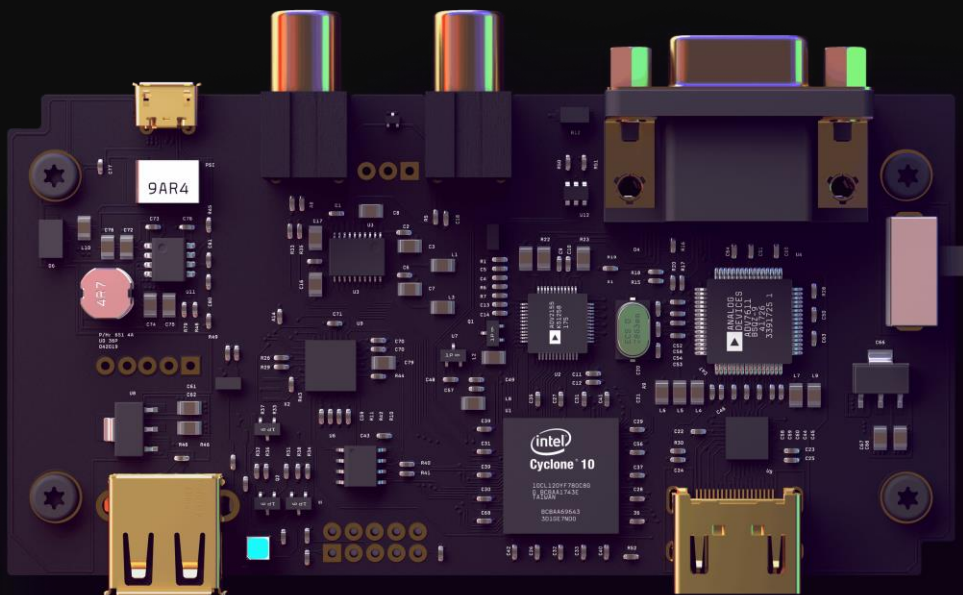


EC205

Analog Electronics Lab

Lab – 9



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Experiment 9: Second order Low-pass and High-pass filter

Aim: To design and study a $\mu A741$ based Sallen-Key Low-pass and High-pass filter

Circuit Diagram:

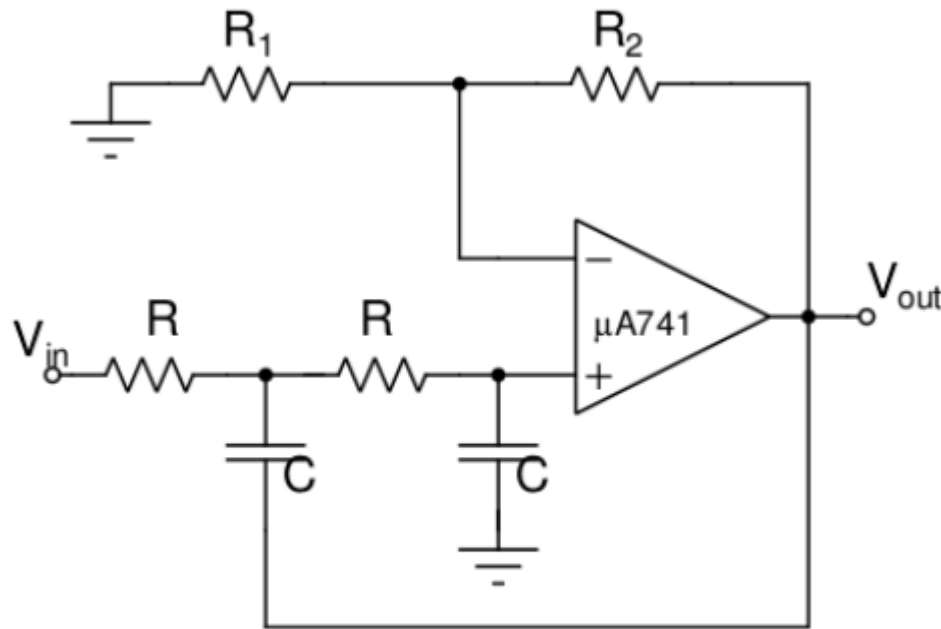


Figure 1: Sallen-key filter

1. Design the low-pass filter for three different Q values (0.5, 0.707 and 2) for a cut-off frequency = 1 kHz. Obtain the magnitude response and phase response. (For hardware lab: Note that the input signal should be such that the peak-to-peak value of the output is at least 100 mV when the filter attenuation increases to 40 dB)

->

Transfer Function for low pass filter $H(S) = \frac{K}{(RCS)^2 + (3-K)RCS + 1}$

We know that for the following circuit, we get

$$f_c = \frac{1}{2\pi RC}, \text{ and } Q = \frac{1}{3-K} \text{ where } K = 1 + \frac{R_2}{R_1}$$

considering $R=1\text{k}\Omega$ and using $f_c=1\text{ kHz}$.

$$C = \frac{1}{2\pi R f_c} = 0.1591\text{ }\mu\text{F}$$

From $-40\text{dB} = 20\log\left(\frac{V_{out}}{V_{in}}\right)$, since $V_{out} \geq 100\text{mV}$

$$V_{in} = 100V_{out} = 100 \times 100 \times 10^{-3}\text{ V} = 10\text{V}_{p2p}$$

For $Q=0.5$,

Let us consider $R_1 = 1\text{k}\Omega$

$K=1$, R_2 has to be 0Ω .

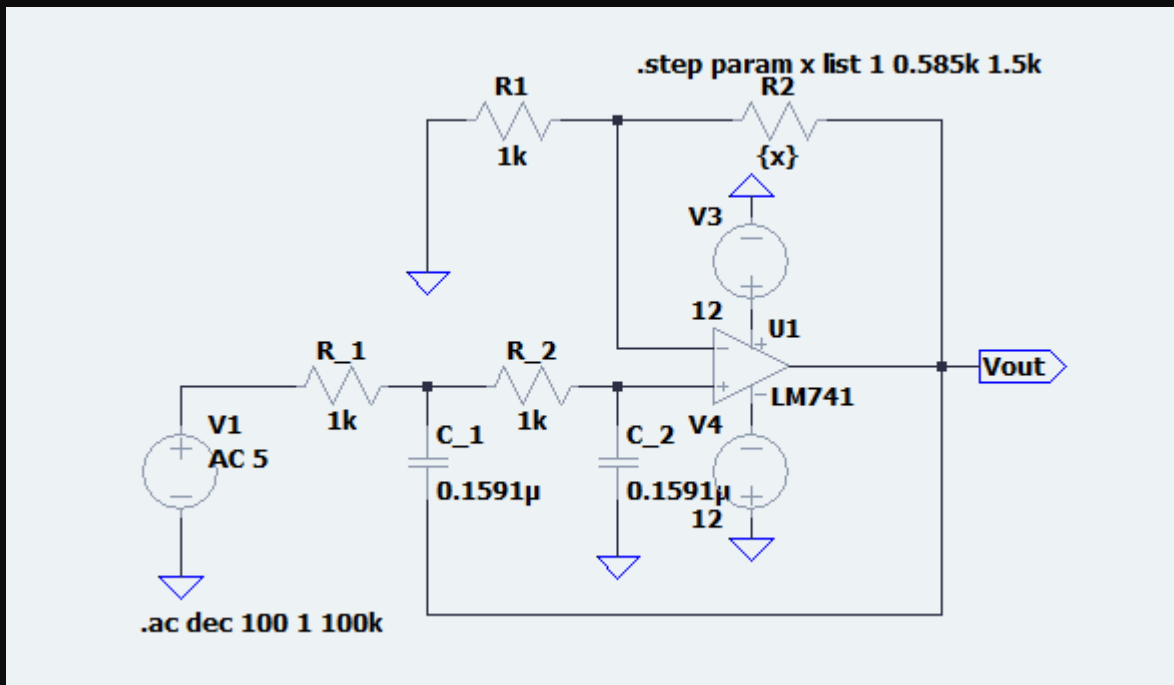
For $Q=0.707$,

$K=1.585$, $R_2=0.5855\text{k}\Omega$

For $Q=2$,

$K=2.5$, $R_2=1.5\text{k}\Omega$

Circuit in LTSpice:

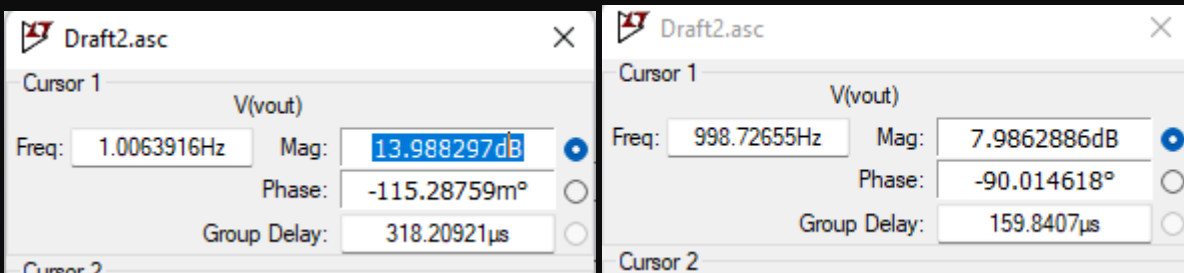


2. Simulate the circuit and obtain the frequency response. Determine the DC gain, the cut-off frequency and stop-band roll-off and compare with the designed.

Frequency/phase Response:



For $Q=0.5$,



Gain = 13.988297dB

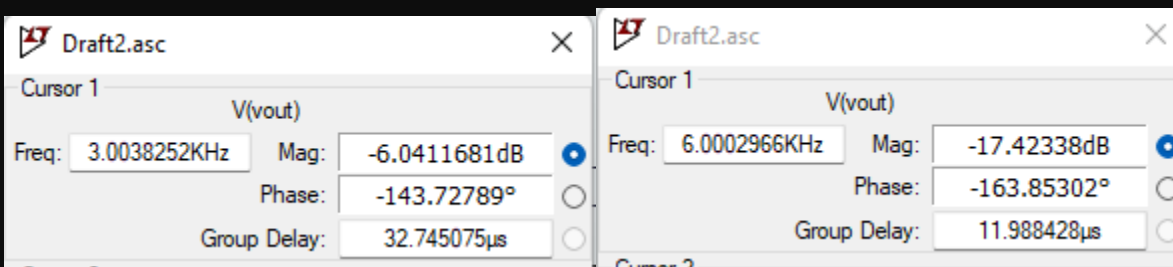
$F_c = 998.72655\text{Hz}$

$K=1$, R_2 has to be 0Ω .

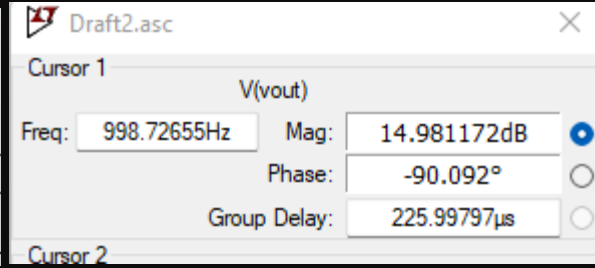
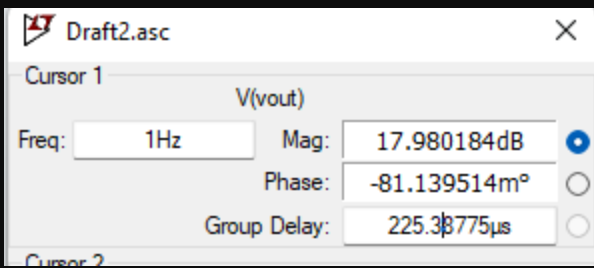
Stop band roll-off

$$= (-17.4233 + 6.041181) / ((5.9926 - 3.0038) \cdot 10^3)$$

$$= -0.036$$



For $Q=0.707$,



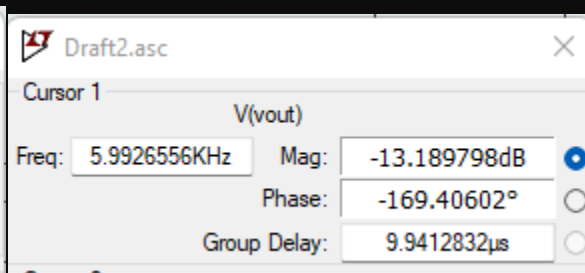
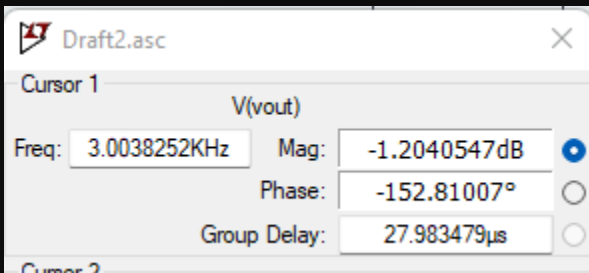
Gain = 17.980184dB

Fc= 998.72655Hz

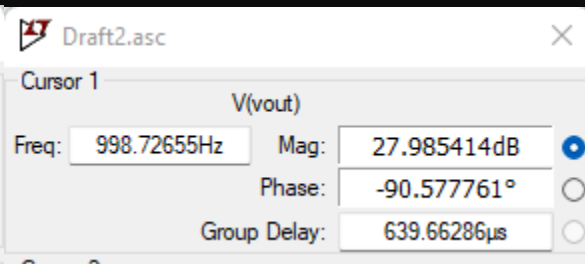
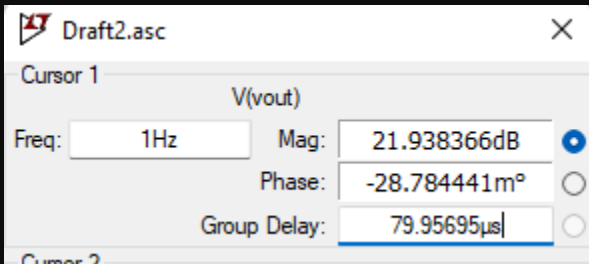
Stop band roll-off

$$= (-13.1897 + 1.2040) / ((5.9926 - 3.0038) * 10^3)$$

$$= -0.038$$



For Q=2,



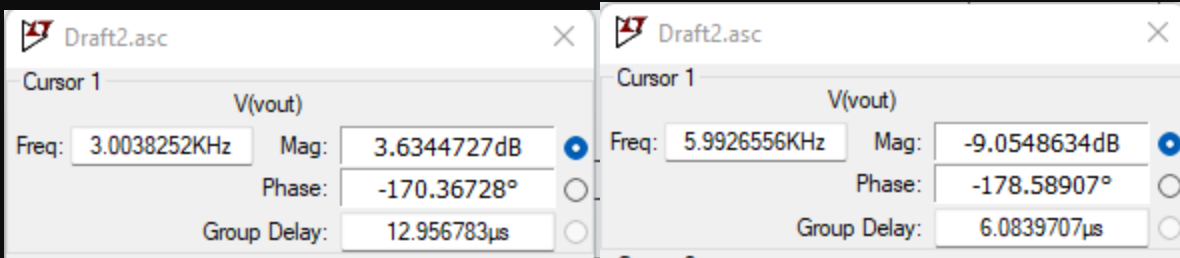
Gain = 21.938366dB

Fc= 998.72655Hz

Stop band roll-off

$$= (-9.0548 - 3.6344) / ((5.9926 - 3.0038) * 10^3)$$

$$= -0.041$$



$$F_{\text{maxgain}} = f_c \sqrt{1 - \frac{1}{2Q^2}} = 10^3 \sqrt{\frac{7}{8}} = 0.935 \text{ kHz}$$

$$|H(j\omega)|_{\text{max at } F_{\text{maxgain}}} = \frac{QK}{\sqrt{1 - \frac{1}{4Q^2}}} = \frac{5 \cdot 4}{\sqrt{15}} = 5.16$$

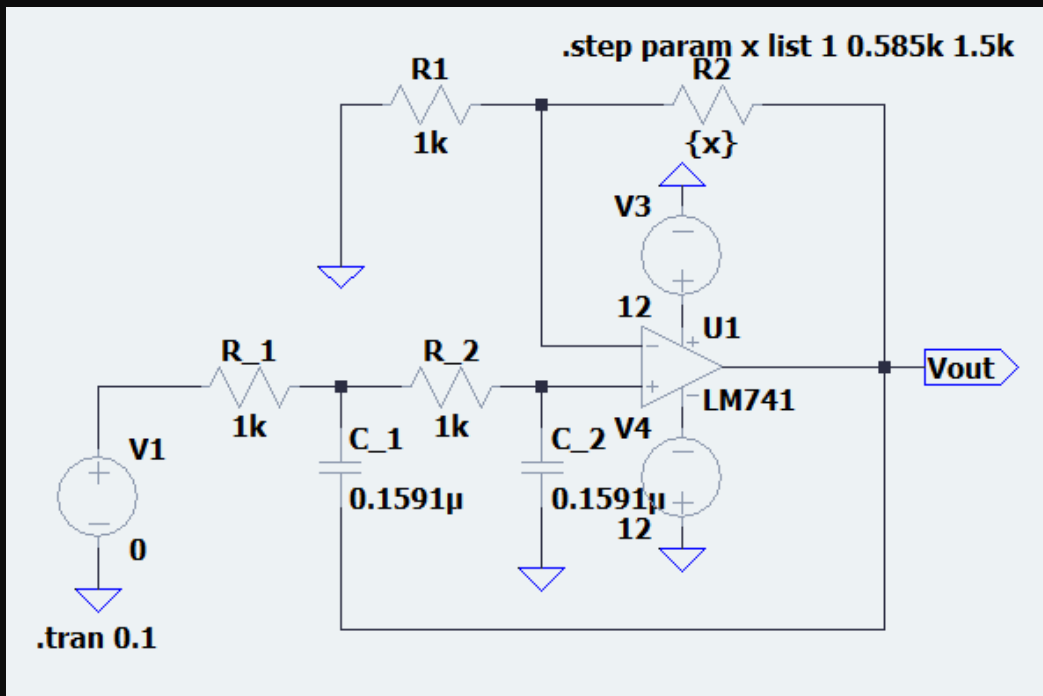
3. Tabulate the results in the format shown in Table 1 below.

Q	Ri	k	F0 Frequency at which gain = QK	Hp (max gain)	Fp Frequency at which max gain occurs	Stop band roll- off
0.5	1	2	998.72655	13.988297dB	1Hz	-0.036
0.707	0.585k	1.585	998.72655	17.980184dB	30.417337Hz	-0.038
2	1.5k	2.5	998.72655	28.275992dB	931.12805Hz	-0.041

4. Now, ground the input terminal of the filter (Remember to disconnect the Signal Generator in the hardware lab). Adjust R2 such that the gain $K = (1 + R2/R1)$ becomes slightly higher than 3. You will see the filter oscillating. What is the reason?

Let $K = 3.2$, We get $R = 2.2 \text{ K}\Omega$

Circuit in LTspice:



Observation: waveform:



When the gain value is greater than 3, the system become oscillatory because its tending towards system instability.

5. Convert the filter designed in step-1 to a high-pass filter. Observe and note down the salient features for $Q = 0.707$.

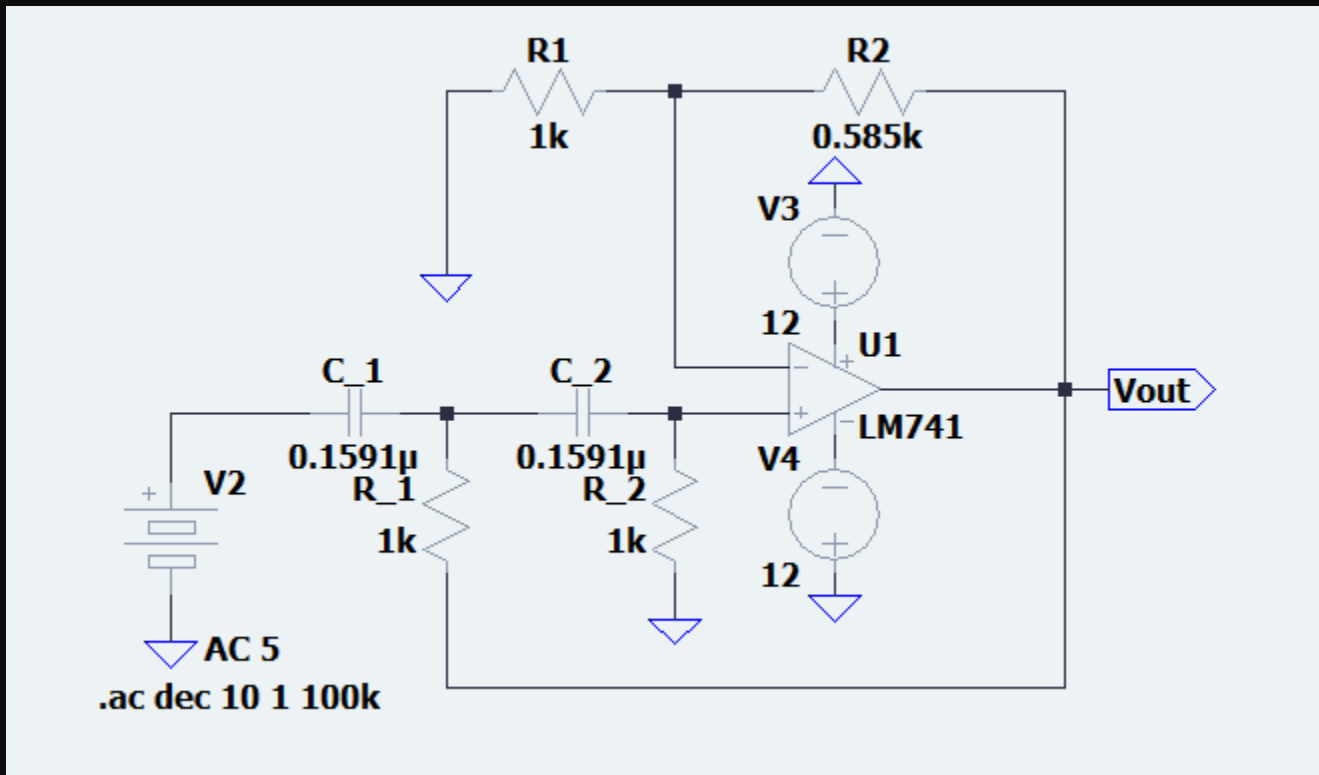
-> It can be easily made by just switching Capacitors and Resistors at the input.

As for $Q=2$, we will use the resistor values from above questions as it will be applicable here too.

$$\text{Transfer Function for high pass filter } H(S) = \frac{K(RCS)^2}{(RCS)^2 + (3-K)RCS + 1}$$

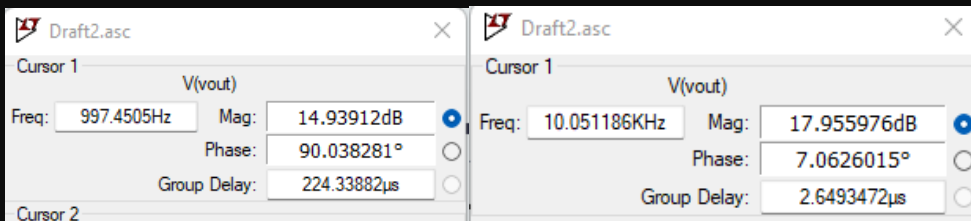
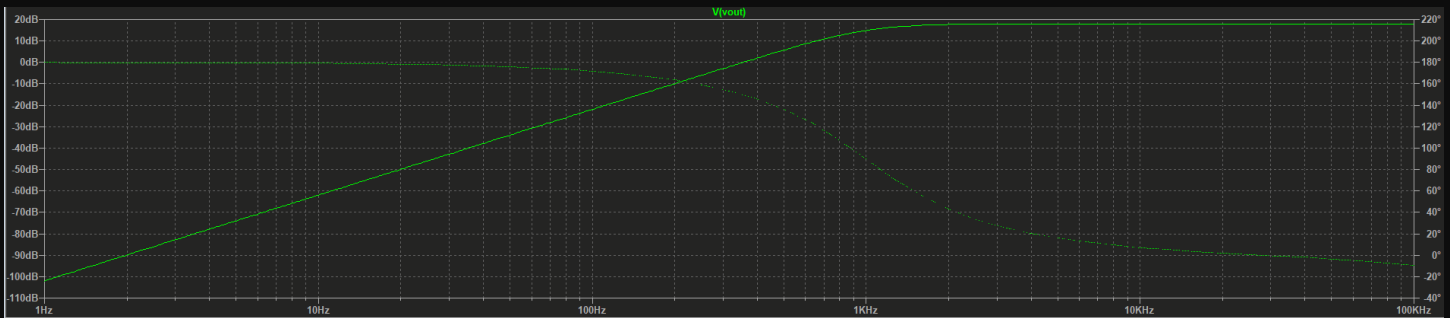
$$f_{\text{maxgain}} = \frac{fc}{\sqrt{1 - \frac{1}{2Q^2}}}$$

Circuit in LTspice:



Observations:

Frequency/phase Response:

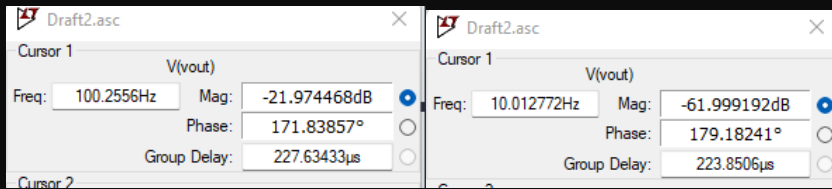


$f_c = 997.4505\text{Hz}$

For roll off factor:

$$= (-21.974468 + 61.999192) / (100.2556 - 10.012772)$$

$$= 0.44352249244$$



$H_{\max} = 17.955976\text{dB}$,

$f_{\max\text{gain}} = 10.0511\text{ kHz}$

$$f_{\max}(\text{expected}) = \frac{f_c}{\sqrt{1 - \frac{1}{2Q^2}}} = 1.00015\text{ kHz}$$