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Assignment-1 (12.13.5.5)

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- **5.)Question:** The probability that a bulb produced by a factory will fuse after 150 days of use is 0.05. Find the probability that out of 5 such bulbs
 - 1) none
 - 2) not more than one
 - 3) more than one
 - 4) at least one

will fuse after 150 days of use.

Solution: Let the **Probability** of i^{th} bulb to fuse after 150 days of use be Pr(i).

$$Pr(i) = 0.05 \ \forall i \in \{1, 2, 3, 4, 5\}$$

Probability of one bulb getting fused is independent of another

1) Probability that none of the 5 bulbs fuses is:

$$\Pr(\bar{1} \cap \bar{2} \cap \bar{3} \cap \bar{4} \cap \bar{5}) = \prod_{i=1}^{i=5} (1 - \Pr(i)) \quad (1)$$

form (1)

$$=(1-0.05)^5=0.95^5$$

$$= 0.7737809375$$

2) Probability that not more than one bulb fuses is same as exactly 0 bulb fuses or exactly one bulb fuses:

Probability of no bulb to fuse is:

$$(0.95)^5$$

Probability of exactly one bulb to fuse is:

$$\binom{5}{1} \times \Pr\left(1 \cap \bar{2} \cap \bar{3} \cap \bar{4} \cap \bar{5}\right) \tag{2}$$

(choosing which bulb is defective) form (2)

$$= 5 \times (0.95)^4 \times 0.05 = 0.2036265625$$

3) Let A be event that none of the bulbs is fused and B be event that exactly one bulb is fused

Probability that more than one bulb will fuse will be:

$$= 1 - \Pr(A) - \Pr(B) \tag{3}$$

form (3)

$$= 1 - (0.95)^5 - 5 \times 0.05 \times (0.95)^4$$

$$= 0.0225925$$

4) Probability that at least one bulb is fused is

1 – Probability that no bulb is fused (4)

form (4)

$$= 1 - (0.95)^5 = 0.2262190625$$