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Assignment-1 (12.13.5.5)

Uttam Paharia CS22BTECH11060

5.)Question:The probability that a bulb produced by a factory will fuse after 150 days of use is 0.05. Find the probability that out of 5 such bulbs

- 1) none
- 2) not more than one
- 3) more than one
- 4) at least one

will fuse after 150 days of use.

Solution: Let the **Probability** of i bulb to fuse after 150 days of use be Pr(i).

Probability of a bulb to fuse after 150 days is =0.05 Probability of one bulb getting fused is independent of another

Let Cumulative Distributive Function be:

$$F_X(i) = Pr(X \le i) \tag{1}$$

$$F_X(0) = Pr(X = 0) = \Pr(1'2'3'4'5') = \prod_{i=1}^{i=5} (1 - \Pr(i))$$
(2)

$$= 0.95^5 = 0.7737809375 \tag{3}$$

$$F_X(1) = F_X(0) + Pr(X = 1)$$
 (4)

$$= (0.95)^5 + {}^5C_1 \times (0.5) \times (0.95)^4 \qquad (5)$$

$$F_X(2) = F_X(1) + Pr(X = 2)$$
 (6)

$$= (0.95)^5 + {}^5C_1 \times (0.5) \times (0.95)^4 \tag{7}$$

$$+ {}^{5}C_{2} \times (0.5)^{2} \times (0.95)^{3}$$
 (8)

$$F_X(6) = 1 \tag{9}$$

1) Probability that none of the 5 bulbs fuses is:

$$F_X(0) \tag{10}$$

form (??)

$$= 0.95^5 \tag{11}$$

$$= 0.7737809375$$
 (12)

2) Probability that not more than one bulb fuses is same as exactly 0 bulb fuses or exactly one bulb fuses:

$$F_X(1) = 0.9774075 \tag{13}$$

3) Let A be event that none of the bulbs is fused and B be event that exactly one bulb is fused Probability that more than one bulb will fuse will be:

$$F_X(6) - F_X(1)$$
 (14)

form (??)

$$= 0.0225925$$
 (15)

4) Probability that at least one bulb is fused is

$$F_X(6) - F_X(0)$$
 (16)

form (??)

$$= 1 - (0.95)^5 = 0.2262190625 \tag{17}$$