

Note: Q1 is compulsory. Attempt one question each from the Units I, II, III & IV.

Q1

- a) The mean of 200 items was 50. Later on it was discovered that 2 items were misread as 92 and 8 instead of 192 and 88. Find out the corrected mean.
- b) A bag X contains 2 white and 3 red balls and a bag Y contains 4 white and 5 red balls. One ball is drawn at random from one of the bags and is found to be red. Find the probability that it was drawn from bag Y.
- c) In 4 tosses of a coin, let  $x$  be the number of heads. Calculate the expected values of  $x$ .
- d) The probability density function  $f(x)$  of a continuous random variable  $x$  is  $f(x) = A/x^2$   $1 \leq x \leq 4$ . Find the value of A.
- e) For 10 observations on price ( $x$ ) and supply( $y$ ), the following data were obtained  $\sum x = 130$ ,  $\sum y = 220$ ,  $\sum x^2 = 2288$ ,  $\sum y^2 = 5506$  and  $\sum xy = 3467$   
Obtain the regression line  $y$  on  $x$ .
- f) Find out the mean, variance and M.G.F of the exponential distribution.
- g) A machine produced 16 defective articles in a batch of 500. After overhauling it produced 3 defectives in a batch of 100. Has the machine improved?
- h) Define Sampling with its applications, Null Hypothesis, Type I and II error and level of significance.

## UNIT I

$$7+9 = 16$$

Q2

- a). In a certain distribution, the first four moments about the point  $x=4$  are -1.5, 17, -30 and 308. Find the moments about mean and about origin.
- b) The annual salaries of a group of employers are given in the following table. Find Standard deviation and coefficient of variation.

Salaries X in thousand	45	5	55	6	6	70	7	80
No of persons	3	5	8	7	9	7	4	7

Q3

- a) Calculate the mean and median from the following table:

Class interval	Frequency
6.5-7.5	5
7.5-8.5	12
8.5-9.5	25
9.5-10.5	48
10.5-11.5	32

Q4	<p>a) Let <math>(x,y)</math> be a 2-Dim continuous random variable having the joint density function <math>f(x,y) = \frac{x e^{-y}}{2}</math>, <math>0 &lt; x &lt; 2</math>, <math>y &gt; 0</math>. Find the distribution function of <math>X+Y</math>.</p> <p>b) The joint probability distribution of two random variables <math>X</math> and <math>Y</math> is given by: <math>P(X=0, Y=1) = 1/3</math>, <math>P(X=1, Y=-1) = 1/3</math> and <math>P(X=1, Y=1) = 1/3</math>. Find i) Marginal distribution of <math>X</math> and <math>Y</math>, and ii) the conditional probability distribution of <math>X</math> given <math>Y=1</math>.</p>
Q5	<p>a) A die is tossed thrice. A success is getting 1 or 6 on a toss. Find the mean and variance of the number of successes.</p> <p>b) Derive mean and variance using the given M.G.F of the random variable <math>X</math> <math>M_X(t) = (q + pe^t)^n</math>.</p>

### UNIT III (10)

Q6	<p>a). A manufacturer knows from experience that the resistance of resistors he produces is normal with mean 100 ohms and standard deviation 2 ohms. What percentage of resistors will have resistance between 98 ohms and 102 ohms?</p> <p>b). Obtain the rank correlation coefficient for the following data:</p> <table border="1" data-bbox="255 945 1421 1073"> <thead> <tr> <th>X</th><th>68</th><th>64</th><th>75</th><th>50</th><th>64</th><th>80</th><th>75</th><th>40</th><th>55</th><th>64</th></tr> </thead> <tbody> <tr> <th>Y</th><td>62</td><td>58</td><td>68</td><td>45</td><td>81</td><td>60</td><td>68</td><td>48</td><td>50</td><td>70</td></tr> </tbody> </table>	X	68	64	75	50	64	80	75	40	55	64	Y	62	58	68	45	81	60	68	48	50	70
X	68	64	75	50	64	80	75	40	55	64													
Y	62	58	68	45	81	60	68	48	50	70													
Q7	<p>a). Out of 800 families with 4 children each, how many families would be expected to have (i) 2 boys and 2 girls (ii) no girl (iii) atmost 2 girls? Assume equal probabilities for boys and girls.</p> <p>b). State the Central Limit Theorem. A coin is tossed 200 times. Find the approximate probability of the number of heads obtained is between 80 and 120 by CL theorem.</p>																						

### UNIT IV

(95)

Q8	<p>a). The nine items of a sample have the following values: 45, 47, 50, 52, 48, 47, 49, 53, 51. Does the mean of these values differ significantly from the assumed mean 47.5?</p> <p>b). The theory predicts the proportion of beans in the four groups G1, G2, G3, G4 should be in the ratio 9:3:3:1. In an experiment with 1600 beans the numbers in the four groups were 882, 313, 287 and 118. Does the experimental result support the theory?</p>
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Q9	<p>a). Can vaccination be regarded as preventive measure of small pox as evidenced by the following data of 1482 persons exposed to smallpox in a locality. 368 in all were attacked of these 1482 persons and 343 were vaccinated and of these only 35 were attacked.</p> <p>b). A machine is producing bolts of which a certain fraction is defective.</p>
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