PROBLEM SET 6

Reading:

- Kittel & Kroemer Ch. 4, pp. 102-110
- Kittel & Kroemer Ch. 5, pp. 117-144
- 1. K&K problem 4.8 (*Heat shields*).
- 2. K&K problem 4.19 (Reflective heat shield and Kirchoff's Law).
- 3. K&K problem 4.18 (Isentropic expansion of photon gas). Before answering (a) and (b), explain why $\tau V^{1/3}$ has been constant since the cosmic black-body radiation decoupled from matter. You may wish to read through problem 17.
- 4. K&K problem 4.12 (Heat capacity of photons and phonons)
- 5. K&K problem 4.14 (Heat capacity of liquid ⁴He at low temperatures)
- 6. Active transport (from K&K 5.4). The concentration of potassium K⁺ ions in the internal sap of a plant cell may exceed by a factor of 10⁴ the concentration of K⁺ ions in the pond water in which the cell is growing. The chemical potential of the K⁺ ions is higher in the sap because their concentration n is higher there. Estimate the difference in chemical potential at 300 K and show that it is equivalent to a voltage of 0.24 V across the cell wall.
- 7. States of positive and negative ionization (from K&K 5.7). Consider a lattice of fixed hydrogen atoms. Suppose that a neutral atom can exist in either its ground state, of energy $-\Delta/2$, or an excited state of energy $\Delta/2$. Alternatively, it can exist as a positive ion with energy $-\delta/2$ or a negative ion with energy $\delta/2$.
 - a. Show that the average number of electrons per atom can be calculated as $\langle N \rangle = \phi \, d(\ln \mathfrak{z})/d\phi$, where $\phi = e^{\beta \mu}$ and μ is the chemical potential. Find \mathfrak{z} .
 - b. Find a condition for the average number of electrons per atom to be unity in terms of δ , β , and ϕ .
 - c. If the average number of electrons per atom is unity, what is the value of the chemical potential?
 - d. Give a physical explanation for the value of the chemical potential that you found. Does it depend on the energies of the ground and excited states? Why or why not?