

# GATE ASSIGNMENT-3

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Download all python codes from

[https://github.com/V-Gopireddy/EE3900/blob/main/GATE\\_Assignment3/codes/GateAssignment-3.py](https://github.com/V-Gopireddy/EE3900/blob/main/GATE_Assignment3/codes/GateAssignment-3.py)

And all latex-tikz from

[https://github.com/V-gopireddy/EE3900/blob/main/GATE\\_Assignment3/GateAssignment-3.tex](https://github.com/V-gopireddy/EE3900/blob/main/GATE_Assignment3/GateAssignment-3.tex)

## 1 QUESTION EC-2001/Q.1.3

The transfer function of a system is given by

$$H(s) = \frac{1}{s^2(s-2)} \quad (1.0.1)$$

The impulse response of the system is

- 1)  $(t^2 * e^{-2t})U(t)$
- 2)  $(t * e^{2t})U(t)$
- 3)  $(te^{-2t})U(t)$
- 4)  $(te^{-2t})U(t)$

## 2 SOLUTION

**Lemma 2.1** (Table of Laplace Transforms).

Time Function $f(t) = \mathcal{L}^{-1}\{F(s)\}$	Laplace transform of $f(t)$ $F(s) = \mathcal{L}\{f(t)\}$
$t^n U(t), n \geq 1$	$\frac{n!}{s^{n+1}}, s > 0$
$\frac{t^{n-1}}{(n-1)!} U(t), n \geq 2$	$\frac{1}{s^n}, s > 0$
$e^{-at} U(t)$	$\frac{1}{s+a}, s+a > 0$

**Theorem 2.1** (Convolution theorem). Suppose  $F(s) = \mathcal{L}\{f(t)\}$ ,  $G(s) = \mathcal{L}\{g(t)\}$  exist, then,

$$\mathcal{L}^{-1}\{F(s)G(s)\} = f(t) * g(t) \quad (2.0.1)$$

Let,

$$F(s) = \frac{1}{s^2}, G(s) = \frac{1}{s-2} \quad (2.0.2)$$

$$\Rightarrow f(t) = \mathcal{L}^{-1}\left\{\frac{1}{s^2}\right\} = \frac{t}{1!} = tU(t) \quad (2.0.3)$$

$$\Rightarrow g(t) = \mathcal{L}^{-1}\left\{\frac{1}{s-2}\right\} = e^{2t}U(t) \quad (2.0.4)$$

Given transfer function,

$$H(s) = \frac{1}{s^2(s-2)} \quad (2.0.5)$$

$$\Rightarrow h(t) = \mathcal{L}^{-1}\{H(s)\} \quad (2.0.6)$$

$$= \mathcal{L}^{-1}\left\{\frac{1}{s^2(s-2)}\right\} \quad (2.0.7)$$

$$= \mathcal{L}^{-1}\{F(s)G(s)\} \quad (2.0.8)$$

$$= f(t) * g(t) = (t * e^{2t})U(t) \quad (2.0.9)$$

Correct Option is (2)

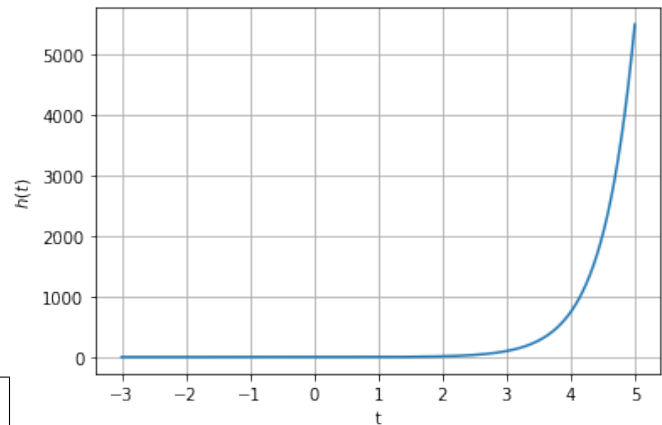


Fig. 4: Plot of  $h(t) = (t * e^{2t})U(t)$