

# QUIZ-1

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Download all latex-tikz codes from

<https://github.com/V-gopireddy/EE3900/blob/main/Quiz1/Quiz-1.tex>

Therefore

$$S = \sum_{n=-\infty}^{\infty} |h[n]| \quad (2.0.5)$$

$$= \sum_{n=0}^{\infty} \left| \sin\left(\frac{n\pi}{3}\right) \right| \quad (2.0.6)$$

$$= \sum_{n=0}^{\infty} \sqrt{3} = \infty \quad (2.0.7)$$

## 1 QUESTION 2.19 (D,E,F)

For each of the following impulse responses of LTI systems, indicate whether or not the system is stable:

- 1)  $h[n] = \sin(n\pi/3)u[n]$
- 2)  $h[n] = (3/4)^{|n|} \cos(n\pi/4 + \pi/4)$
- 3)  $h[n] = 2u[n+5] - u[n] - u[n-5]$

Since,

$$S = \infty \quad (2.0.8)$$

The system is unstable □

**Lemma 2.3.** LTI system with impulse response

$$h[n] = (3/4)^{|n|} \cos(n\pi/4 + \pi/4) \quad (2.0.9)$$

is stable

*Proof.* Since  $-1 \leq \cos(n\pi/4 + \pi/4) \leq 1$

$$S = \sum_{n=-\infty}^{\infty} |h[n]| \quad (2.0.10)$$

$$= \sum_{n=-\infty}^{\infty} |(3/4)^{|n|} \cos(n\pi/4 + \pi/4)| \quad (2.0.11)$$

$$\leq \sum_{n=-\infty}^{\infty} \left| \left(\frac{3}{4}\right)^{|n|} \right| \quad (2.0.12)$$

$$= 1 + 2 \sum_{n=1}^{\infty} \left| \left(\frac{3}{4}\right)^n \right| = 7 \quad (2.0.13)$$

Since,

$$S = 7 < \infty \quad (2.0.14)$$

The system is stable □

**Lemma 2.4.** LTI system with impulse response

$$h[n] = 2u[n+5] - u[n] - u[n-5] \quad (2.0.15)$$

is stable

## 2 SOLUTION

**Definition 1.** We say that a system is **stable** if it produces a bounded output for every possible bounded input, i.e it satisfies the BIBO(Bounded-input-Bounded-output) condition.

**Lemma 2.1.** A system with impulse response  $h[n]$  is said to be BIBO stable if and only if  $h[n]$  is absolutely summable

$$S = \sum_{n=-\infty}^{\infty} |h[n]| < \infty \quad (2.0.1)$$

**Lemma 2.2.** LTI system with impulse response

$$h[n] = \sin(n\pi/3)u[n] \quad (2.0.2)$$

is unstable

*Proof.* We have,

$$h[n] = \sin\left(\frac{n\pi}{3}\right)u[n] \quad (2.0.3)$$

$$= \begin{cases} \sin\left(\frac{n\pi}{3}\right), & n \geq 0 \\ 0, & n < 0 \end{cases} \quad (2.0.4)$$

*Proof.* We have

$$h[n] = 2u[n + 5] - u[n] - u[n - 5] \quad (2.0.16)$$

$$= \begin{cases} 2, & -5 \leq n < 0 \\ 1, & 0 \leq n < 5 \\ 0, & \text{otherwise} \end{cases} \quad (2.0.17)$$

Therefore

$$S = \sum_{n=-\infty}^{\infty} |h[n]| \quad (2.0.18)$$

$$= \sum_{n=-5}^0 |2| + \sum_{n=0}^{-5} |1| = 15 \quad (2.0.19)$$

Since,

$$S = 15 < \infty \quad (2.0.20)$$

The system is stable □