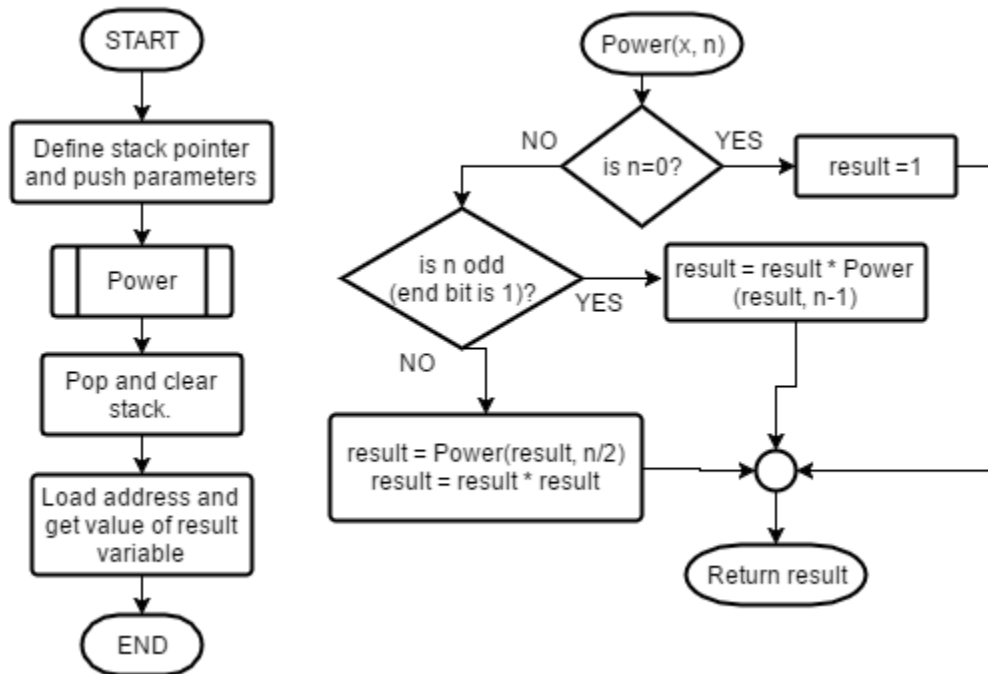


**Question 1**



;Vivian Lam

;program to recursively compute factorial. uses the stack

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AREA power, CODE, READONLY

n EQU 12

x EQU 2

ENTRY

Main LDR sp, =stackk ;define the stack by setting a pointer to  
it

MOV r0, #n ;prepare the parameter

MOV r2, #x

STR r0, [sp, #-4]! ;push the parameter (n) on the stack

STR r2, [sp, #-4]! ;pushing x

SUB sp, sp, #4 ;reserve a place in the stack for the return  
value

BL Power ;call the power subroutine

LDR r0, [sp], #4 ;load the result in r0 and pop it from the  
stack

ADD sp, sp, #8 ;also remove the parameter from the stack

ADR r1, result ;get the address of the result variable

```
        STR    r0,[r1]        ;store the final result in the result
variable
```

```
Loop B    Loop                ;infinite loop so no error
```

```
;-----
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```

```
        AREA power, CODE, READONLY
```

```
Power STMFD sp!,{r0,r1,r2,fp,lr} ;push general registers, as well as
fp and lr
```

```
        MOV    fp,sp          ;set the fp for this call
```

```
        SUB    sp,sp,#4        ;create space for the y local variable
```

```
        LDR    r0,[fp,#28];load n: 5 registers*4 + 4(from result return
address) + 4 (from x) + (we do not consider the 4 from n cus we
already pointing to top) = 28 forward
```

```
        LDR    r2,[fp,#24];load x
```

```
        CMP    r0,#0           ;if (n = 0)
```

```
        MOVEQ  r0,#1           ;{ prepare the value to be returned
```

```
        STREQ  r0,[fp,#20] ; store the returned value in the stack
```

```
        BEQ    ret             ; branch to the return section
```

```
        ;}
```

```
        ;is n odd?
```

```
        TST    r0, #1 ;AND to check last bit: if it's a 1 then the register
contains an odd number
```

```

;BNE Odd ;n is odd (zero flag not set) return x * power(x, n -
1);

```

```

BEQ Even;n is even (zzero flag set), y= power(x, n >> 1); return
y * y

```

```

;      LDR    r0,[fp,#0x18] ;get the parameter from the stack (get
n)

```

```

;      LDR    r2,[] ;load x

```

```

Odd ;n is odd (zero flag not set) return x * power(x, n - 1);

```

```

;prepare the value to be returned (x, n-1)

```

```

SUB r0,r0,#1 ;preparing n-1 and storing result into r0

```

```

;push parameters to the stack (push x and n-1)

```

```

STR r0,[sp,#-4]! ;pushin n-1

```

```

STR r2,[sp,#-4]!;push x to the stack

```

```

SUB sp,sp,#4;reserve space in stack for return value

```

```

BL Power ;call power subroutine

```

```

LDR r0,[sp],#4;load result (the empty space we created above) and
pop

```

```

ADD    sp,sp,#8      ;also remove the parameters (there's two:n
and x, so use 8) from the stack

```

```

MUL r2,r0,r2;calculating: return x * fact(x,n-1);

```

```

STR r2,[fp,#20];store the returned value in the stack

```

```

B ret;branch to return (so that we don't calculate the Even case)

```

```

Even ;n is even (ztero flag set), y= power(x, n >> 1); return y * y
    ;preparing new parameter: divide n by 2 by shifting right by 1
    LSR r0,r0, #1
    ;push parameters to the stack
    STR r0,[sp,#-4]! ;pushin n/2
    STR r2,[sp,#-4]!;push x to the stack
    SUB sp,sp,#4;reserve space in stack for return value

    BL Power ;call power subroutine

    LDR r0,[sp],#4;load result (the empty space we created above) and
pop

    ADD    sp,sp,#8      ;also remove the parameters (there's two:n
and x, so use 8) from the stack

    STR r0,[fp,#-4] ;set y equal to the result (store r0 into the
location of y, which is fp-4<offset cus stack type is FD)

    MUL r1,r0,r0 ;calculate y*y

    STR r1,[fp,#20];store the returned value in the stack

ret MOV    sp,fp      ;collapse all working spaces for this
function call

    LDMFD sp!,{r0,r1,r2,fp,pc} ;load all registers and return to the
caller

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    AREA power, DATA, READWRITE

result DCD    0x00      ;the final result

```

```
        SPACE 0x200          ;declare the space for stack

        ALIGN

stackk  DCD    0x00          ;initial stack position (FD model)
;-----
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        END
```

%%

How many stack frames are needed to calculate  $x^n$ , when  $n = 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11$ , and  $12$ ?

n=0: 1 frame needed  
n=1: 2 frames needed  
n=2: 3 frames needed  
n=3: 4 frames needed  
n=4: 4 frames needed  
n=5: 5 frames needed  
n=6: 5 frames needed  
n=7: 6 frames needed  
n=8: 5 frames needed  
n=9: 6 frames needed  
n=10: 6 frames needed  
n=11: 7 frames needed  
n=12: 6 frames needed