

P: myarr: [0 1 2 -1 4 5]

myres: [ - - ]

size = 2  
size = 2

allvec: [x0 x1 x2 x3]

vector size and vector offset ①

size = 2  
size = 0

[2 0] | [0 2 4]

myarr = [0 2 2 4 8]

row + 1 or col + 1

[2 6 0] | [0 2 8]

allvec: [x0 x1 x2 x3]

P1: size = 2, size = 2

myres: [x2 x3]

(myarr) = 6

myarr = [ - - - ] = [ 2 4 ]

myarr = 2.

i = 0

[myarr[i]] = 2 - 2 = 0 [ 0 4 ]

i = 1: [myarr[i]] = 4 - 2 = 2

[myarr[i]] = 6

[0 2]

Hybrid:

Scatter:  $\begin{bmatrix} 0 \\ 2 \\ 2 \\ 3 \\ 0 \\ 1 \\ 2 \\ 3 \end{bmatrix}$

Scatter Hybrid

$\begin{bmatrix} 2 \\ 2 \\ 0 \\ 1 \\ 2 \\ 3 \end{bmatrix}$

$\begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 2 & 3 \\ 4 & 4 & 4 & 4 \end{bmatrix}$   
(Hybrid)

Node:

$\begin{bmatrix} 1 \\ 1 \\ 2 \\ 2 \\ 4 \\ 4 \\ 4 \\ 4 \end{bmatrix}$

Scatter

(Hybrid)

$\begin{bmatrix} 2 \\ 2 \\ 4 \\ 4 \\ 4 \\ 4 \end{bmatrix}$

Prepare senders:

$\hookrightarrow$  Hybrid:  $\begin{bmatrix} 2 & 3 & 0 & 1 & 2 & 3 \end{bmatrix}$

Hybrid = 6  
rows = 4

size = 2  
Hybrid =  $\begin{bmatrix} x_1 & x_3 \end{bmatrix}$

$\Rightarrow$  size = 2, left = 2, total = 4.

Prepare senders:  $\begin{bmatrix} 1 & - & - & - \end{bmatrix}$

senders:  $\begin{bmatrix} 0 & 0 & 0 \end{bmatrix} \rightarrow \begin{bmatrix} 1 & 0 & 0 \end{bmatrix} \rightarrow \begin{bmatrix} 1 & 0 & 0 \end{bmatrix}$

NRV = 1.

NRV = 2.

senders:  $\begin{bmatrix} 1 & - & - & - & - & - \end{bmatrix}$

then  $vec = D$ .

$i = 0 \rightarrow 5$

(i)  $i = 0$ : if  $((2 < 2) \vee (2 > 4)) \times$

(ii)  $i = 1$ : if  $((3 < 2) \vee (3 > 4)) \times$

(iii)  $i = 2$ : if  $((0 < 2) \vee (0 > 4)) \checkmark$

(iv)  $i = 3$ : if  $((1 < 2) \vee (1 > 4)) \checkmark$

(v)  $i = 4$ : if  $((2 < 2) \vee (2 > 4)) \times$

(vi)  $i = 5$ : if  $((3 < 2) \vee (3 > 4)) \times$

reverse iter:  $[0 \ 2 \ 2] \rightarrow [0 \ 2 \ 2] \rightarrow [0 \ 2 \ 2]$

compress vector:  $[0 \ 2 \ 2] \rightarrow [0 \ 0 \ 2] \rightarrow [2 \ 0 \ 0]$

my vector:  $[x_1 \ x_2 \ x_3 \ \dots]$

$prod = D$

$i = 0 \rightarrow 5$

(i)  $i = 0$ :  
if  $((2 < 2) \vee (2 > 4)) \times$

(ii)  $i = 1$ :  
if  $((3 < 2) \vee (3 > 4)) \times$

(iii)  $i = 2$ :  
if  $((0 < 2) \vee (0 > 4)) \checkmark$

$prod = D$

reverse iter:  $[0 + 0] = 0$ . reverse iter:  $[0] = 0$ .

my vector:  $[2 + 0 + 0 = 2]$

my vector:  $[2 \ 3 \ 0 \ 1 \ 2 \ 3]$

↓

$[0 \ 3 \ 0 \ 1 \ 2 \ 3]$

↓

$[0 \ 1 \ 0 \ 1 \ 2 \ 3]$

↓

$[0 \ 1 \ 2 \ 1 \ 2 \ 3]$

$CD \ i=3$   
 $\text{if } ((1 < 2) \vee (1 > 4)) \checkmark$        $[0 \ 1 \ 2 \ 3 \ 2 \ 3]$   
 $proc = 0$   
 $\text{save index } [0 + 1] = 1$        $\text{save index } [1] = 1$

$CD \ i=4$   
 $\text{if } ((2 < 2) \vee (2 > 4)) \times$        $[0 \ 1 \ 2 \ 3 \ 0 \ 3]$

$CD \ i=5$   
 $\text{if } ((3 < 2) \vee (3 > 4)) \times$        $[0 \ 1 \ 2 \ 3 \ 0 \ 1]$

New modified mycviatna:  $([0 \ 1 \ 2 \ 3 \ 0 \ 1])$

$NR = 2$   
 $\text{delete } vrc \text{ } [0] = [2 \ 0 \ 0]$   
 $\text{save } Pr = [0 \ 2 \ 2]$   
 $\text{save } Index = [0 \ 1 \ - \ - \ - \ -]$  (10)

Proc 0:

vector size and vector type

$[2 \ 2 \ 0]$        $[0 \ 2 \ 4]$

PCD + 1      ED 4/15      size = 2

$[2 \ 6 \ 0]$        $[0 \ 2 \ 8]$   
 $\uparrow$        $\uparrow$   
 $\text{all vector: } [x_0 \ x_1 \ x_2 \ x_3 \ x_4 \ x_5]$

[illegible]

$proc = 0$   
 $i = 0$   
 $i+1 = 0$ : if  $((0 < 0) || (0 > 2)) \times$   
 $i+1 = 1$ : if  $((1 < 0) || (1 > 2)) \checkmark$   
 $proc = 1$   
 $getVecIndex[0 + 0] = 2$   
 $getVecIndex[0] = 2$   
 $myval[1] = 2 + 0 + 0 = 2$   
 $RV = 1$

$RV \neq 1$   
 $myval[0] = [0 \ 2]$   
 $reverseArr = [0 \ 0 \ 1]$   
 $undoVecIndex = [2 \ -]$   
 $getVecIndex = [0 \ 1 \ 0]$   
 $myVecDone = [x_0 \ x_1 \ -]$

$P_2$ :  
 $vecDone$  size and  $vecDone$  size  
 $[2 \ 2 \ 0] \mid [0 \ 2 \ 4]$

$vecDone$  or  $vecDone$   
 $[2 \ 6 \ 0] \quad [2 \ 2 \ 8]$

$vecDone = 0$       Alternative:  $[x_0 \ x_1 \ x_2 \ x_3]$   
 $size = 2$   
 $myVecDone = [ ]_0$

$$\text{myRowP} = \underline{\underline{0}}$$

$$\text{myRowP} = \underline{\underline{0}}$$

$$(\text{myRowP}) = \underline{\underline{0}}$$

WIDUP

$$[\text{myRowP} \underline{\underline{0}}] = \underline{\underline{0}}$$

$$\Rightarrow \text{myRowP} = \underline{\underline{0}}$$

$$\text{myRowP} = \underline{\underline{0}}$$

$$\text{myRowP} = \underline{\underline{0}}$$

↓

Pre-reverse:

$$\text{size} = 3$$

$$\text{ls} = 4$$

$$\text{le} = 6$$

$$\text{pre-reverse} = \underline{\underline{0}}$$

$$\text{reverse} = \underline{\underline{0}}$$

$$\text{reverse} = \underline{\underline{0}}$$

$$\text{rev} = \underline{\underline{0}}$$

$$\text{rev} = \underline{\underline{0}}$$

$$\text{myRowP} = \underline{\underline{0}}$$

$$\text{myRowP} = \underline{\underline{0}}$$

$$\text{myRowP} = \underline{\underline{0}}$$

$$\text{myRowP} = \underline{\underline{0}}$$

$$\text{myRowP} = \underline{\underline{0}}$$

$$\text{myRowP} = \underline{\underline{0}}$$

$$\text{myRowP} = \underline{\underline{0}}$$

$$\text{dense } P^T r = \begin{bmatrix} 0 & -1 \\ 0 & -1 \end{bmatrix} \rightarrow \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix} \rightarrow$$

$$\text{myrecorr}: \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$\text{vsize} = 0$$

$$\text{addDC}: 0 + 0$$

$$\text{myrecorr}: \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

$$\text{proc} = 0$$

$$\text{I} = 0 - 0$$

$$\Rightarrow \text{dense } \text{corr} = \begin{bmatrix} 0 & 0 & 0 \end{bmatrix}$$

$$\text{dense } P^T r = \begin{bmatrix} 0 & 0 & 0 \end{bmatrix}$$

$$\text{dense } \text{corr} = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

$$\text{myrecorr} = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

$$\text{mycorr} = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$





P1: result:  $\begin{bmatrix} - & - \end{bmatrix}$

value=2, mycolptr:  $\begin{bmatrix} 0 & 2 & 2 \end{bmatrix}$

mycolind:  $\begin{bmatrix} 0 & 2 \end{bmatrix}$

myrow:  $\begin{bmatrix} 1 & 1 \end{bmatrix}$

myrowcol:  $\begin{bmatrix} x_0 & x_1 & x_2 \end{bmatrix}$

⇒ i:0, i+1:im

(i) i:0:  $\text{res}[i] \rightarrow j = 0 \text{ to } 2$ .

$$\text{res}[i] = \text{val}[0] * \text{vec}[\text{colind}[0]] +$$

$$\text{val}[1] * \text{vec}[\text{colind}[1]]$$

$$\Rightarrow \text{res}[i] = 1 * \text{vec}[0] + 1 * \text{vec}[2]$$

$$\text{res}[i] = 1 * x_0 + 1 * x_2 \quad \text{--- (1)}$$

(ii) i:1:

$\text{res}[i] \rightarrow j = 1 \text{ to } 2 \times$

$$\text{res}[i] = 0 \quad \text{--- (1)}$$

P1: result:  $\begin{bmatrix} - & - \end{bmatrix}$  value=2, mycolptr:  $\begin{bmatrix} 0 & 2 & 6 \end{bmatrix}$

mycolind:  $\begin{bmatrix} 0 & 1 & 2 & 3 & 0 & 1 \end{bmatrix}$  myrow:  $\begin{bmatrix} 3 & 3 & 4 & 4 & 2 & 4 \end{bmatrix}$

myrowcol:  $\begin{bmatrix} x_1 & x_2 & x_0 & x_1 \end{bmatrix}$

i = 0 to 5, ~~loop = 0 1 2 3 4~~

(i) i:0:  $\text{res}[i] : j = 0 \text{ to } 1$ .

$$\text{res}[i] = \text{val}[0] * \text{vec}[\text{colind}[0]] + \text{val}[1] * \text{vec}[\text{colind}[1]]$$

(ii) i:1:  $j = 2 \text{ to } 5$ . (1, 3, 4, 5)

$$\text{res}[i] = \text{val}[2] * \text{vec}[\text{colind}[2]] + \text{val}[3] * \text{vec}[\text{colind}[3]] +$$

$$\text{val}[4] * \text{vec}[\text{colind}[4]] + \text{val}[5] * \text{vec}[\text{colind}[5]]$$

$$\text{res}[i] = 3 * \text{vec}[0] + 3 * \text{vec}[1] = 3x_1 + 3x_2 \quad \text{--- (1)}$$

$$\text{res}[i] = 4 * \text{vec}[2] + 4 * \text{vec}[3] + 4 * \text{vec}[0] + 4 * \text{vec}[1]$$

$$= 4x_0 + 4x_1 + 4x_1 + 4x_2 \quad \text{--- (1)}$$

P1  
res:  $\begin{bmatrix} 1x_0 + 1x_2 \\ 0 \end{bmatrix}$

P1  
res:  $\begin{bmatrix} 3x_1 + 3x_2 \\ 4(x_0 + x_2) \end{bmatrix}$  res:  $\begin{bmatrix} 6 \end{bmatrix}$  (empty)

res row col:  $\begin{bmatrix} 0 & 2 & 4 \end{bmatrix}$

res row col:  $\begin{bmatrix} 2 & 2 & 0 \end{bmatrix}$

$$\begin{bmatrix} - \\ - \\ - \\ - \end{bmatrix} \begin{bmatrix} x_0 + x_1 \\ 0 \\ 3x_1 + 3x_2 \\ 4(x_0 + x_2) \end{bmatrix} \xrightarrow{\text{(Total result)}} =$$