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## Problem Sheet #04

### Problem 4.1:

- a-). the function  $f$  is injective since every number in the domain maps to a distinct number in the codomain. if  $f(x_1) = f(x_2)$ , then  $x_1 = x_2$ .
- the fct  $f$  is surjective, ~~there is a  $y$  such that~~  
for any real number  $y$ , you can find an  $x$  such that  $f(x) = y$ .
  - Since the function is both injective and surjective it is indeed bijective.
- b-). the function  $g$  is injective because every number in the domain maps to a distinct number in the codomain. if  $g(x_1) = g(x_2)$ , then  $x_1 = x_2$ .
- this fct is not surjective since it only maps to odd natural numbers.
  - Since this fct is injective but not surjective, it is not bijective.



c-). The function  $h$  is injective, every number in the domain maps to a distinct number in the codomain.

• it is surjective,  $\forall y \in [-1, 1]$ , you can find an  $x$  such as  $h(x) = \sin(x) = y$

• Since the fct is both injective and surjective it's bijective.

### Problem 4.3:

a-)  $C := \text{Customers}$  ;  ~~$T := \text{Tickets}$~~

$T := \text{tickets (representing set of all tickets)}$

$CA := \text{Cashiers}$

$M := \text{movie theaters}$

$E := \text{cinema employees}$

$D := \text{drink menu}$  ;  $TT := \text{ticket takers}$

b-)  $\text{is-a}(\text{cashier} \times \text{employees}) \Rightarrow (CA \times E)$

-  $\text{Order} \subseteq (C \times T)$

-  $\text{Entrance} \subseteq (T \times M)$

-  $\text{Server} \subseteq (E \times D)$  (relation between cinema employees and the drinks they serve)



- Drink order  $\subseteq (C \times D)$

- is a  $(TT \times E)$

- ~~check~~  $\subseteq (TT \times T)$

### c-7) \* Partial Order Relation:

- Denoted as  $V$  (validity),  $V \subseteq (T \times M)$

represents the relation indicating whether one ticket is valid for the same movie theater as another ticket. Relation is reflexive, antisymmetric and transitive.

### \* Equivalence Relation:

- Denoted as  $C$  (capacity),  $C \subseteq (M \times M)$

represents the relation indicating whether or not two movie theaters have the same seating capacity. This relation is reflexive, transitive and symmetric. Hence, it is an equivalence relation.

### \* Strict Partial Order Relation:

- Denoted as  $H$  (Hierarchy),  $H \subseteq (E \times E)$

represents the relation indicating a hierarchy among employees. This relation is irreflexive, asymmetric and transitive. Hence, it is a strict partial order relation.



### \* Equivalence Relation:

- Denoted as  $T(\text{taste})$ ,  $T \subseteq (C \times C)$

represents the relation indicating whether two customers have the same preference to the same movie theater. the relation is reflexive, transitive and symmetric.

### \* Partial Order Relation:

- Denoted as  $P(\text{price order})$ ,  $P \subseteq (D \times D)$

represents the relation indicating different drinks with different associated prices, meaning a drink can be priced higher than or equal ~~than~~ to another drink. the later relation is reflexive, antisymmetric and transitive.

### Problem 4.4:

a-7 import Data.Char

main :: IO ()

main = print (ord '=')

- the following code would print the char code of '=' which is 61.



5-7 import Data.Char

main :: IO()

main = print (chr 128119)

- the char with the code point 128119 represents emoji  
(hugging face emoji)