# **MT251P - Foundations of Euclidean Geometry**

**Assignment #4** 

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### **Question 1**

In each case below, state whether the statement is true or false. Justify your answer in each case.

#### Part A

There are infinitely many  $4 \times 4$  matrices that are not invertible.

#### **Solution**

#### Part B

There is a  $4 \times 4$  invertible matrix A such that  $A^3 = 2A^2$  and det A = 2.

#### **Solution**

#### Part C

There is a 4 × 4 matrix A such that 
$$A^2 = \begin{pmatrix} -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

#### **Solution**

### **Question 2**

#### Part A

Prove that  $det(A^{-1}BA) = det(B)$ , for all  $n \times n$  matrices A, B where A is invertible and n > 1.

#### **Solution**

#### Part B

Suppose  $\underline{a} = i + 2j - k$ ,  $\underline{b} = i + 3j + k$  and  $\underline{c} = 3i + 8j + 4k$ . Find  $||\underline{w}||^2$  if  $\underline{w} \in \mathbb{R}^3$  such that  $\underline{w}.\underline{a} = 3$ ,  $\underline{w}.\underline{b} = 5$  and  $\underline{w}.\underline{c} = 17$ .

#### **Solution**

## **Question 3**

Find the solution set of the following system of linear equations:

$$x_1 - 4x_2 + 3x_3 = 0$$

$$2x_1 - 6x_2 + 10x_3 = 6$$

$$x_1 - 2x_2 + 7x_3 = 5$$

#### **Solution**

# **Question 4**

Find the solution set of the following system of linear equations:

$$4x - 6y + 8z = 8$$

$$x + 2y - 5z = 2$$

$$y + 4x - 6z = 8$$

#### **Solution**

## **Question 5**

Find 
$$A^{-1}$$
 if  $A = \begin{pmatrix} 0 & 1 & 2 \\ 1 & 0 & 3 \\ 4 & -3 & 8 \end{pmatrix}$ 

#### **Solution**