

DEPARTMENT OF MATHEMATICS & STATISTICS

MT251P

Homework 3

Due by 4 p.m. on November 25, 2022

1. Suppose  $\underline{u} = 3i + j - 3k$  and  $\underline{w} = 6j + 2k$ . Find  $2\underline{w} - 4\underline{u}$ ,  $\|\underline{u} - \underline{w}\|$ ,  $\underline{u} \cdot \underline{w}$  and the angle between  $\underline{u}$  and  $\underline{w}$ .
2. Prove that  $\|\underline{u} - \underline{w}\| \geq \|\underline{u}\| - \|\underline{w}\|$ , for all  $\underline{u}, \underline{w} \in \mathbb{R}^n$ , for  $n \geq 1$ .
3. In each case below, state whether the statement is true or false. Justify your answer in each case.
  - (i)  $(\underline{a} \times \underline{b}) + (\underline{b} \times \underline{a}) = \underline{a} \times 2\underline{a}$ , for all  $\underline{a}, \underline{b} \in \mathbb{R}^3$ .
  - (ii) There are vectors  $\underline{a}, \underline{b} \in \mathbb{R}^3$  such that  $(\underline{a} \times \underline{b}) \cdot (\underline{a} \times \underline{b}) < 0$ .
4. Find the equation of the plane containing the points  $(2, 1, -1)$ ,  $(0, -2, 0)$ ,  $(1, -1, 2)$ .
5. Find the parametric equation of the line that is the intersection of the planes  $2x + 4y - 4z + 16 = 0$  and  $5z - 2y + 2x = -4$ .