

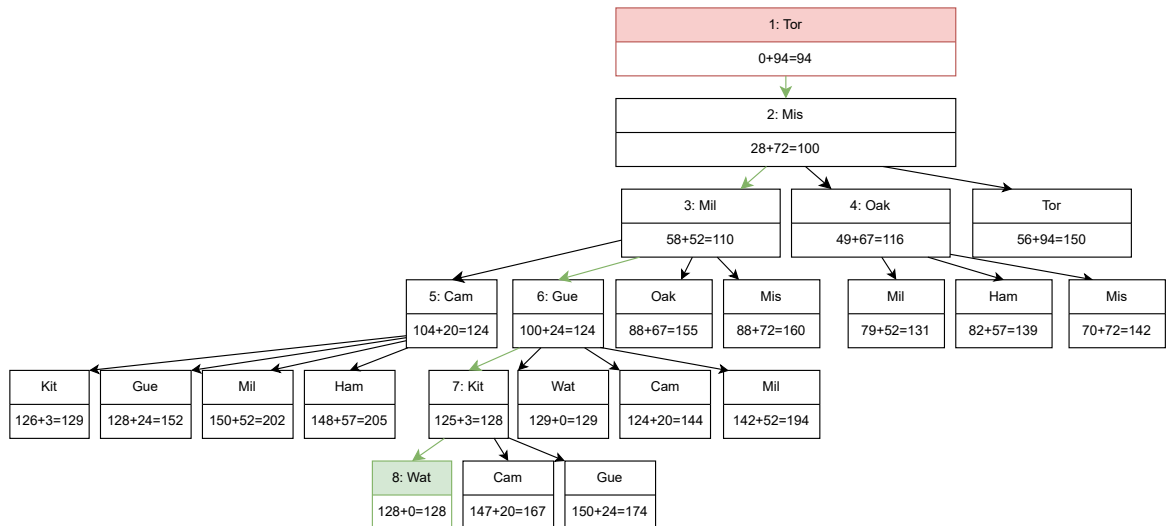
University of Waterloo

CS 486, Winter 2024

Assignment 1

Problem 1

- a) The Euclidean distance to the destination is an admissible heuristic function because it never overestimates the actual shortest path cost, as the shortest possible path between two cities is the straight line (Euclidean) distance between them, thus the only possible case is the Euclidean distance equals or **underestimates** the shortest path cost.
- b) The Euclidean distance to the destination is a consistent heuristic function because it satisfies the monotone restriction: **heuristic estimate of the path cost is always less than or equal to the actual cost**. As previously stated the Euclidean distance could only equals or **underestimates** the shortest path cost.
- c) Decision Tree:



Problem 2

a) minimax:

```
1     if depth == 0 or node.state.is_terminal:
2         # Base case: evaluate the state using the heuristic function
3         node.value = heuristic_fn(node.state, max_role)
4         return node.value
5     if node.state.turn == max_role:
6         # Maximizing player
7         max_eval = float('-inf')
8         for move in node.state.get_legal_moves():
9             # Create a successor node
10            successor_state = deepcopy(node.state)
11            successor_state.advance_state(move)
12            successor_node = MinimaxNode(successor_state)
13            # Recursively call minimax on the successor
14            eval = minimax(successor_node, depth - 1, max_role, ←
heuristic_fn)
15            # max_eval is the maximum evaluation value for the player.
16            max_eval = max(max_eval, eval)
17            # Store successor node and its value
18            node.successors[move] = successor_node
19            # Assign the maximum value found to the current node
20            node.value = max_eval
21        return max_eval
22    else:
23        # Minimizing player
24        min_eval = float('inf')
25        for move in node.state.get_legal_moves():
26            # Create a successor node
27            successor_state = deepcopy(node.state)
28            successor_state.advance_state(move)
29            successor_node = MinimaxNode(successor_state)
30            # Recursively call minimax on the successor
31            eval = minimax(successor_node, depth - 1, max_role, ←
heuristic_fn)
32            # min_eval is the minimum evaluation value for the player.
33            min_eval = min(min_eval, eval)
34            # Store successor node and its value
35            node.successors[move] = successor_node
36            # Assign the minimum value found to the current node
37            node.value = min_eval
38        return min_eval
39
```

- b) The game always terminates in less than 10 seconds (around 0.04s to 0.05s) on my laptop for RandomPlayer vs. MinimaxHeuristicPlayer with depth 2.

The first depth number i encountered for the game not terminating within 10 seconds is depth=6, which takes around 34s on my Laptop.

c) my_heuristic:

```
1      #If the state is terminal, give the true evaluation
2      if state.is_terminal:
3          if state.winner == '':
4              return 0
5          elif state.winner == max_role:
6              return 100
7          else:
8              return -100
9      #If the state is not terminal, give the heuristic evaluation
10     score_board = [
11         [1, 2, 3, 3, 2, 1],
12         [2, 4, 6, 6, 4, 2],
13         [3, 6, 9, 9, 6, 3],
14         [4, 8, 12, 12, 8, 4],
15         [3, 7, 10, 10, 7, 3],
16         [2, 4, 6, 6, 4, 2],
17         [1, 2, 3, 3, 2, 1],
18     ]
19     score = 0
20     # Calculate the score for each piece based on its distance from the center ←
       column
21     for col in range(state.num_cols):
22         for row in range(state.num_rows):
23             if state.board[col][row] == max_role:
24                 # Assign higher score to pieces closer to the center
25                 # The maximum score is given to the center column and decreases ←
       as it moves away from the center
26                 score += score_board[col][row]
27             else:
28                 score -= score_board[col][row]
29     return score
30
```

my_heuristic evaluates the board state by calculating a score based on the pieces' location on the board. Each spot on the board is given a score, with higher scores for spots closer to the centre. In the end, it returns the score as the difference between the total scores of the two players.

I believe `my_heuristic` will outperform `three_line_heur` because my heuristic function assign scores based on board positions, more precisely based on the pieces' distance from the centre of the board. The closer a piece is to the centre, the higher its score, as closer a piece is to the centre, higher the chance that it will contribute to a connect-4, or stop a connect-4 attempt for the opponent. And `three_line_heur` only based scores on number of 3-in-a-row, without considering how easy is that 3-in-a-row to become an actual connect-4.

d) Diagram (each run 20 games):

Agent 1	Agent 2	Wins	Draws	Losses
Minimax Player, depth 3 <code>three_line_heur</code>	RandomPlayer	20	0	0
Minimax Player, depth 3 <code>my_heuristic</code>	RandomPlayer	20	0	0
Minimax Player, depth 5 <code>three_line_heur</code>	Minimax Player, depth 2 <code>three_line_heur</code>	16	1	3
Minimax Player, depth 5 <code>my_heuristic</code>	Minimax Player, depth 2 <code>my_heuristic</code>	20	0	0
Minimax Player, depth 5 <code>my_heuristic</code>	Minimax Player, depth 5 <code>three_line_heur</code>	15	0	5

Problem 3

- 1) We will denote the i 'th Queen's coordinate in the form (X_i, Y_i) . And the domain for them is $1 \leq X_i \leq N$ and $1 \leq Y_i \leq N$ for all $i \in \{1, 2, \dots, N\}$.

And the constraints are:

- Row Constraint: $X_i \neq X_j$ for all $i \neq j$ where $i, j \in \{1, 2, \dots, N\}$.
- Column Constraint: $Y_i \neq Y_j$ for all $i \neq j$ where $i, j \in \{1, 2, \dots, N\}$.
- Diagonal Constraint: $|X_i - X_j| \neq |Y_i - Y_j|$ for all $i \neq j$ where $i, j \in \{1, 2, \dots, N\}$.

- 2) We will denote the i 'th Octopi's coordinate in the form (X_i, Y_i) . And the domain for them is $1 \leq X_i \leq N$ and $1 \leq Y_i \leq N$ for all $i \in \{1, 2, \dots, N\}$.

And the constraints are:

- Row Constraint: $X_i \neq X_j$ for all $i \neq j$ where $i, j \in \{1, 2, \dots, N\}$.
- Column Constraint: $Y_i \neq Y_j$ for all $i \neq j$ where $i, j \in \{1, 2, \dots, N\}$.
- Block Constraint: $\lfloor \frac{X_i-1}{M} \rfloor \neq \lfloor \frac{X_j-1}{M} \rfloor$ or $\lfloor \frac{Y_i-1}{M} \rfloor \neq \lfloor \frac{Y_j-1}{M} \rfloor$ for all $i \neq j$ where $i, j \in \{1, 2, \dots, N\}$.