

# Precise predictions for same sign W-bosons scattering at the LHC

Michele Grossi<sup>X,\*</sup>, Alexander Karlberg, Mathieu Pellen<sup>3,†</sup>, Giovanni Pelliccioli, Michael Rauch,  
Jürgen Reuter, Vincent Rothe, Christopher Schwan, Pascal Stienemeier, Marco Zaro.

<sup>1</sup>*University X, Institut Y,  
Street X, XXXX city, Country*

<sup>3</sup>*Universität Würzburg, Institut für Theoretische Physik und Astrophysik,  
Emil-Hilb-Weg 22, 97074 Würzburg, Germany*

## Abstract

Abstract to be written here.

---

\*E-mail: YY@email.com

†E-mail: mathieu.pellen@physik.uni-wuerzburg.de

# Contents

<b>1</b>	<b>Introduction</b>	<b>2</b>
<b>2</b>	<b>Definition of the process</b>	<b>2</b>
<b>3</b>	<b>Details of the calculations</b>	<b>2</b>
3.1	Description of the predictions . . . . .	2
3.2	Input parameters . . . . .	4
<b>4</b>	<b>Fixed order comparisons</b>	<b>5</b>
4.1	Cross sections . . . . .	5
4.2	Differential distributions . . . . .	6
<b>5</b>	<b>Influence of the fiducial region</b>	<b>6</b>
<b>6</b>	<b>Matching to parton shower</b>	<b>6</b>
<b>7</b>	<b>Conclusion</b>	<b>6</b>
<b>A</b>	<b>Appendix one</b>	<b>7</b>

# 1 Introduction

The measurements are [1–3].

In the last decade many codes capable of performing VBS simulations have appeared. Within a network such as VBSCan it is therefore natural to perform a quantitative comparison of these codes, both to cross-validate the results and to assess the impact of the different approximations which are used. In fact, already at LO, when considering the process  $pp \rightarrow \mu^+ \nu_\mu e^+ \nu_e jj$  at order  $\mathcal{O}(\alpha^6)$ , the various implementations VBS simulations are different. They differ, for example by the (non-)inclusion of diagrams with vector bosons in the  $s$ -channel or by the treatment of interferences between diagrams. The reason of these differences is that, when typical signal cuts for VBS are imposed, these effects turn to be small on rates and distributions.

## 2 Definition of the process

## 3 Details of the calculations

### 3.1 Description of the predictions

In the comparison, the following codes are used:

- The program BONSAY consists of a general-purpose Monte Carlo integrator and matrix elements taken from several sources: Born matrix elements are adapted from the program LUSIFER [4] for the partonic processes, real matrix elements are written by Marina Billoni, and virtual matrix elements by Stefan Dittmaier. One loop integrals are evaluated using the COLLIER library [5, 6].
- MADGRAPH5\_AMC@NLO [7] is an automatic meta-code (a code that generates codes) which makes it possible to simulate any scattering process including NLO QCD corrections both at fixed order and including matching to parton showers. It makes use of the FKS subtraction method [8, 9] (automated in the module MADFKS [10, 11]) for regulating IR singularities. The computations of one-loop amplitudes are carried out by switching dynamically between two integral-reduction techniques, OPP [12] or Laurent-series expansion [13], and TIR [14–16]. These have been automated in the module MADLOOP [17], which in turn exploits CUTTOOLS [18], NINJA [19, 20], or IREGI [21], together with an in-house implementation of the OPENLOOPS optimisation [22].

The simulation of VBS at NLO-QCD accuracy can be performed by issuing the following commands in the program interface:

```
> set complex_mass_scheme #1
> import model loop_qcd_qed_sm_Gmu #2
> generate p p > e+ ve mu+ vm j j QCD=0 [QCD] #3
> output #4
```

With these commands the complex-mass scheme is turned on #1, then the NLO-capable model is loaded #2<sup>1</sup>, finally the process code is generated #3 (note the QCD=0 syntax to select the purely-electroweak process) and written to disk #4. Because of some internal

---

<sup>1</sup>Despite the `loop_qcd_qed_sm_Gmu` model also includes NLO counterterms for computing electro-weak corrections, it is not yet possible to compute such corrections with the current version of the code.

limitations, which will be lifted in the future version capable of computing both QCD and EW corrections, only loops with QCD-interacting particles are generated.

- PHANTOM [23] is a dedicated tree-level Monte Carlo for six parton final states at  $pp$ ,  $p\bar{p}$  and  $e^+e^-$  colliders at  $\alpha_{ew}^6$  and  $\alpha_{ew}^4\alpha_s^2$  including interferences between the two sets of diagrams. It employs complete tree-level matrix elements in the complex-mass scheme [24] computed via the modular helicity formalism [25, 26]. The integration uses a multichannel approach [27] and an adaptive strategy [28]. PHANTOM generates unweighted events at parton-level for both the SM and a few instances of BSM theories..
- The POWHEG-BOX [29, 30] is a framework for matching NLO-QCD calculations with parton showers. It relies on the user providing the matrix elements and Born phase space, but will automatically construct FKS [8] subtraction terms and the phase space for the real emission. For the VBS processes all matrix elements are being provided by a previous version of VBFNLO [31–33] and hence the approximations used in the POWHEG-BOX are the similar to those used in VBFNLO.
- The program RECOLA+MoCANLO is made of a flexible Monte Carlo program dubbed MoCANLO [34] and the general matrix element generator RECOLA [35, 36]. To numerically evaluate the one-loop scalar and tensor integrals, RECOLA relies on the COLLIER library [5, 6], These tools have been successfully used for the computation of NLO corrections for VBS [37, 38].
- VBFNLO [31–33] is a flexible parton-level Monte Carlo for processes with electroweak bosons. It allows the calculation of VBS processes at NLO QCD in the VBF approximation and including the s-channel triboson contribution, neglecting interferences between the two. Besides the SM, also anomalous couplings of the Higgs and gauge bosons can be simulated.
- WHIZARD [39, 40] is a multi-purpose event generator with the LO matrix element generator O’MEGA. It provides FKS subtraction terms for any NLO process, while virtual matrix elements are provided externally by OPENLOOPS [22] (alternatively, RECOLA [35, 36] (cf. above) can be used as well). WHIZARD allows to simulate a huge number of BSM models as well, in particular for new physics in the VBS channel in terms of both higher-dimensional operators as well as explicit resonances.

The complete comparison of the codes will be published in a separate work. Here, we present some preliminary results obtained at LO ( $\mathcal{O}(\alpha^6)$ ) and including NLO QCD corrections at fixed-order  $\mathcal{O}(\alpha^6\alpha_s)$ , for the process  $pp \rightarrow \mu^+\nu_\mu e^+\nu_e jj$ . In Tab. 1 the details of the various codes are reported. In particular, it is specified whether

- all  $s$ – and  $t/u$ –channel diagrams that lead to the considered final state are included;
- interferences between diagrams are included at LO;
- diagrams which do not feature two resonant vector bosons are included;
- the so-called non-factorizable (NF) QCD corrections, that is the corrections where (real or virtual) gluons are exchanged between different quark lines, are included;
- EW corrections to the  $\mathcal{O}(\alpha^5\alpha_s)$  interference are included. These corrections are of the same order as the NLO QCD corrections to the  $\mathcal{O}(\alpha^6)$  term.

Contact person	Code	$\mathcal{O}(\alpha^6)$ $ s ^2/ t ^2/ u ^2$	$\mathcal{O}(\alpha^6)$ in- terf.	Non-res.	NF QCD	EW corr. to $\mathcal{O}(\alpha^5\alpha_s)$
A. Karlberg	POWHEG	$t/u$	No	Yes	No	No
M. Pellen	RECOLA+MoCANLO	Yes	Yes	Yes	Yes	Yes
M. Rauch	VBFNLO	Yes	No	Yes	No	No
C. Schwan	BONSAY	$t/u$	No	Yes, virt. No	No	No
M. Zaro	MG5_AMC	Yes	Yes	No virt.	No	No
V. Rothe	WHIZARD	Yes	Yes	Yes	Yes	Yes

Table 1: Summary of the different properties of the codes employed in the comparison.

### 3.2 Input parameters

We simulate VBS production at the LHC, with a center-of-mass energy  $\sqrt{s} = 13$  TeV. We assume five massless flavours in the proton, and employ the NNPDF 3.0 parton density [41] with NLO QCD evolution (the `lhaid` in LHAPDF6 [42] for this set is 260000) and strong coupling constant  $\alpha_s(M_Z) = 0.118$ . Since the employed PDF set has no photonic density, photon-induced processes are not considered. Initial-state collinear singularity are factorised with the  $\overline{\text{MS}}$  scheme, consistently with what is done in NNPDF.

We use the following values for the mass and width of the massive particles:

$$\begin{aligned}
m_t &= 173.21 \text{ GeV}, & \Gamma_t &= 0 \text{ GeV}, \\
M_Z^{\text{OS}} &= 91.1876 \text{ GeV}, & \Gamma_Z^{\text{OS}} &= 2.4952 \text{ GeV}, \\
M_W^{\text{OS}} &= 80.385 \text{ GeV}, & \Gamma_W^{\text{OS}} &= 2.085 \text{ GeV}, \\
M_H &= 125.0 \text{ GeV}, & \Gamma_H &= 4.07 \times 10^{-3} \text{ GeV},
\end{aligned} \tag{1}$$

and renormalise the EW coupling in the  $G_\mu$  scheme [43] where

$$G_\mu = 1.16637 \times 10^{-5} \text{ GeV}^{-2}. \tag{2}$$

The derived value of the EW coupling  $\alpha$ , corresponding to our choice of input parameters, is

$$\alpha = 7.555310522369 \times 10^{-3}. \tag{3}$$

We employ the complex-mass scheme [44, 45] to treat unstable intermediate particles in a gauge-invariant manner **CHECK THAT ALL CODES USE THE CMS**.

Cross sections and distribution are computed within the following VBS cuts inspired from experimental measurements [1–3, 46]:

- The two same-sign charged leptons are required to have

$$p_{\text{T},\ell} > 20 \text{ GeV}, \quad |y_\ell| < 2.5, \quad \Delta R_{\ell\ell} > 0.3. \tag{4}$$

- The total missing transverse energy, computed from the vectorial sum of the transverse momenta of the two neutrinos in the event, is required to be

$$E_{\text{T,miss}} = p_{\text{T,miss}} > 40 \text{ GeV}. \tag{5}$$

- QCD partons (quark and gluons) are clustered together using the anti- $k_T$  algorithm [47] with distance parameter  $R = 0.4$ . Jets are required to have

$$p_{T,j} > 30 \text{ GeV}, \quad |y_j| < 4.5, \quad \Delta R_{j\ell} > 0.3. \quad (6)$$

On the two jets with largest transverse-momentum the following invariant-mass and rapidity-separation cuts are imposed

$$m_{jj} > 500 \text{ GeV}, \quad |\Delta y_{jj}| > 2.5. \quad (7)$$

- When EW corrections are computed, real photons and charged fermion are clustered together using the anti- $k_T$  algorithm with radius parameter  $R = 0.1$ . In this case, leptons and quarks mentioned above must be understood as *dressed fermions*. Photons which are not combined at this step are clustered with QCD partons to form jets as it is described previously.

## 4 Fixed order comparisons

### 4.1 Cross sections

In Tab. 2 we report the total rates at LO accuracy obtained with the set-up described above, and in Fig. 1 we show the results for the tagging-jet (left) and lepton-pair (right) invariant-mass distribution. In both case we show the absolute distributions in the main frame of the figures, while in the inset the ratio over VBFNLO is displayed. For both observables we find an excellent agreement among the various tools, which confirms the fact that contributions from  $s$ -channel diagrams as well as from non-resonant configurations are strongly suppressed in the fiducial region.

Code	$\sigma[\text{fb}]$
BONSAY	$1.5524 \pm 0.0002$
MG5_AMC	$1.547 \pm 0.001$
POWHEG	$1.5573 \pm 0.0003$
RECOLA+MoCANLO	$1.5503 \pm 0.0003$
VBFNLO	$1.5538 \pm 0.0002$
WHIZARD	$1.5539 \pm 0.0004$

Table 2: Rates at LO accuracy within VBS cuts obtained with the different codes used in this comparison, for the  $pp \rightarrow \mu^+ \nu_\mu e^+ \nu_e jj$  process.

At NLO, rates show slightly larger discrepancies, as it can be observed in Tab. 3. This is most likely due to low dijet invariant-mass configurations, where  $s$ -channel diagrams and interferences are less suppressed than at LO, because of the presence of extra QCD radiation.

Code	$\sigma[\text{fb}]$
BONSAY	$1.3366 \pm 0.0009$
MG5_aMC	$1.318 \pm 0.003$
POWHEG	$1.334 \pm 0.0003$
RECOLA+MoCANLO	$1.317 \pm 0.004$
VBFNLO	$1.3531 \pm 0.0003$

Table 3: Rates at NLO-QCD accuracy within VBS cuts obtained with the different codes used in this comparison, for the  $pp \rightarrow \mu^+ \nu_\mu e^+ \nu_e jj$  process.

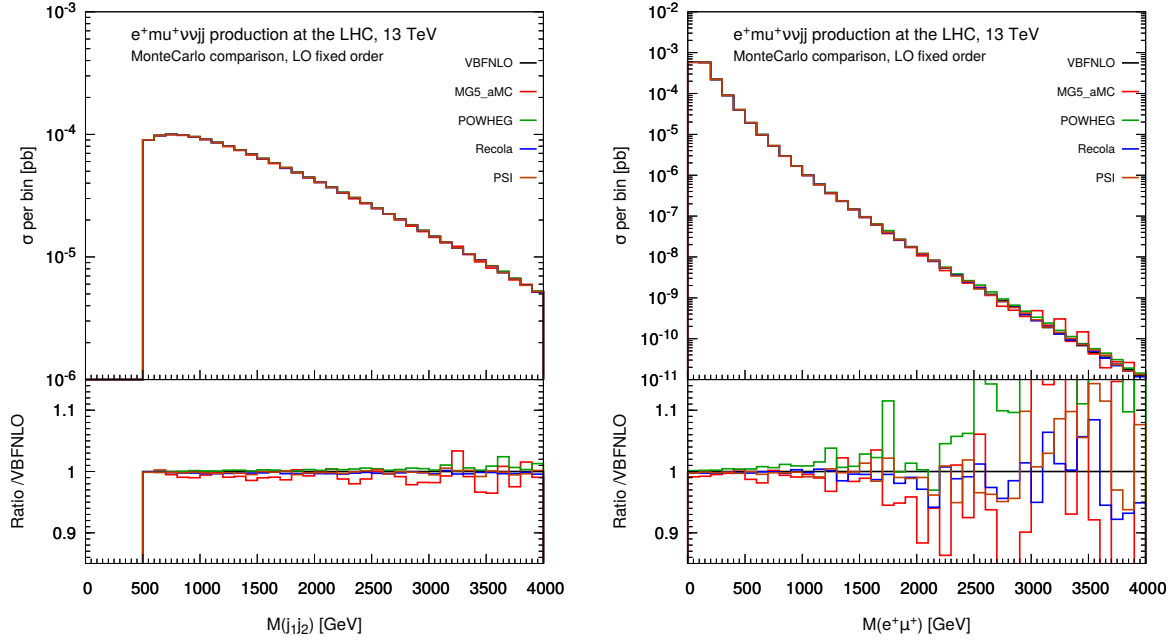


Figure 1: Invariant-mass of the two tagging jets (left) and of the two leptons (right), at LO accuracy, computed with the different codes used in this comparison. The inset shows the ratio over VBFNLO.

## 4.2 Differential distributions

## 5 Influence of the fiducial region

## 6 Matching to parton shower

## 7 Conclusion

## Acknowledgements

We thank ... Acknowledgement of VBSCAN COST action.

Figure 2: Caption of the plot.

## A Appendix one

### References

- [1] **ATLAS** Collaboration, G. Aad *et al.*, *Evidence for Electroweak Production of  $W^\pm W^\pm jj$  in  $pp$  Collisions at  $\sqrt{s} = 8$  TeV with the ATLAS Detector*. Phys. Rev. Lett. **113** (2014) no. 14, 141803, [arXiv:1405.6241 \[hep-ex\]](#).
- [2] **ATLAS** Collaboration, M. Aaboud *et al.*, *Measurement of  $W^\pm W^\pm$  vector-boson scattering and limits on anomalous quartic gauge couplings with the ATLAS detector*. Phys. Rev. **D96** (2017) 012007, [arXiv:1611.02428 \[hep-ex\]](#).
- [3] **CMS** Collaboration, V. Khachatryan *et al.*, *Study of vector boson scattering and search for new physics in events with two same-sign leptons and two jets*. Phys. Rev. Lett. **114** (2015) no. 5, 051801, [arXiv:1410.6315 \[hep-ex\]](#).
- [4] S. Dittmaier and M. Roth, *LUSIFER: A LUCid approach to six FERMion production*. Nucl. Phys. **B642** (2002) 307–343, [arXiv:hep-ph/0206070 \[hep-ph\]](#).
- [5] A. Denner, S. Dittmaier, and L. Hofer, *COLLIER - A fortran-library for one-loop integrals*. PoS **LL2014** (2014) 071, [arXiv:1407.0087 \[hep-ph\]](#).
- [6] A. Denner, S. Dittmaier, and L. Hofer, *COLLIER: a fortran-based Complex One-Loop Library in Extended Regularizations*. Comput. Phys. Commun. **212** (2017) 220–238, [arXiv:1604.06792 \[hep-ph\]](#).
- [7] J. Alwall *et al.*, *The automated computation of tree-level and next-to-leading order differential cross sections, and their matching to parton shower simulations*. JHEP **07** (2014) 079, [arXiv:1405.0301 \[hep-ph\]](#).
- [8] S. Frixione, Z. Kunszt, and A. Signer, *Three jet cross-sections to next-to-leading order*. Nucl. Phys. **B467** (1996) 399–442, [arXiv:hep-ph/9512328 \[hep-ph\]](#).
- [9] S. Frixione, *A General approach to jet cross-sections in QCD*. Nucl. Phys. **B507** (1997) 295–314, [arXiv:hep-ph/9706545 \[hep-ph\]](#).
- [10] R. Frederix, S. Frixione, F. Maltoni, and T. Stelzer, *Automation of next-to-leading order computations in QCD: The FKS subtraction*. JHEP **10** (2009) 003, [arXiv:0908.4272 \[hep-ph\]](#).
- [11] R. Frederix, S. Frixione, A. S. Papanastasiou, S. Prestel, and P. Torrielli, *Off-shell single-top production at NLO matched to parton showers*. JHEP **06** (2016) 027, [arXiv:1603.01178 \[hep-ph\]](#).
- [12] G. Ossola, C. G. Papadopoulos, and R. Pittau, *Reducing full one-loop amplitudes to scalar integrals at the integrand level*. Nucl. Phys. **B763** (2007) 147–169, [arXiv:hep-ph/0609007 \[hep-ph\]](#).



- [13] P. Mastrolia, E. Mirabella, and T. Peraro, *Integrand reduction of one-loop scattering amplitudes through Laurent series expansion*. JHEP **06** (2012) 095, [arXiv:1203.0291 \[hep-ph\]](#). [Erratum: JHEP11,128(2012)].
- [14] G. Passarino and M. J. G. Veltman, *One-loop corrections for  $e^+e^-$  annihilation into  $\mu^+\mu^-$  in the Weinberg model*. Nucl. Phys. **B160** (1979) 151–207.
- [15] A. I. Davydychev, *A Simple formula for reducing Feynman diagrams to scalar integrals*. Phys. Lett. **B263** (1991) 107–111.
- [16] A. Denner and S. Dittmaier, *Reduction schemes for one-loop tensor integrals*. Nucl. Phys. **B734** (2006) 62–115, [hep-ph/0509141](#).
- [17] V. Hirschi, R. Frederix, S. Frixione, M. V. Garzelli, F. Maltoni, and R. Pittau, *Automation of one-loop QCD corrections*. JHEP **05** (2011) 044, [arXiv:1103.0621 \[hep-ph\]](#).
- [18] G. Ossola, C. G. Papadopoulos, and R. Pittau, *CutTools: A Program implementing the OPP reduction method to compute one-loop amplitudes*. JHEP **03** (2008) 042, [arXiv:0711.3596 \[hep-ph\]](#).
- [19] T. Peraro, *Ninja: Automated Integrand Reduction via Laurent Expansion for One-Loop Amplitudes*. Comput. Phys. Commun. **185** (2014) 2771–2797, [arXiv:1403.1229 \[hep-ph\]](#).
- [20] V. Hirschi and T. Peraro, *Tensor integrand reduction via Laurent expansion*. JHEP **06** (2016) 060, [arXiv:1604.01363 \[hep-ph\]](#).
- [21] H.-S. Shao, *Iregi user manual, unpublished*.
- [22] F. Cascioli, P. Maierhofer, and S. Pozzorini, *Scattering Amplitudes with Open Loops*. Phys. Rev. Lett. **108** (2012) 111601, [arXiv:1111.5206 \[hep-ph\]](#).
- [23] A. Ballestrero, A. Belhouari, G. Bevilacqua, V. Kashkan, and E. Maina, *PHANTOM: A Monte Carlo event generator for six parton final states at high energy colliders*. Comput. Phys. Commun. **180** (2009) 401–417, [arXiv:0801.3359 \[hep-ph\]](#).
- [24] A. Denner and S. Dittmaier, *The Complex-mass scheme for perturbative calculations with unstable particles*. Nucl. Phys. Proc. Suppl. **160** (2006) 22–26, [arXiv:hep-ph/0605312 \[hep-ph\]](#). [,22(2006)].
- [25] A. Ballestrero, “PHACT: Helicity amplitudes for present and future colliders,” in *High energy physics and quantum field theory. Proceedings, 14th International Workshop, QFTHEP’99, Moscow, Russia, May 27-June 2, 1999*, pp. 303–309. 1999. [arXiv:hep-ph/9911318 \[hep-ph\]](#).
- [26] A. Ballestrero and E. Maina, *A New method for helicity calculations*. Phys. Lett. **B350** (1995) 225–233, [arXiv:hep-ph/9403244 \[hep-ph\]](#).
- [27] F. Berends, P. Daverveldt, and R. Kleiss, *Complete lowest-order calculations for four-lepton final states in electron-positron collisions*. Nuclear Physics B **253** (1985) no. Supplement C, 441 – 463.  
<http://www.sciencedirect.com/science/article/pii/0550321385905413>.

- [28] G. P. Lepage, *A new algorithm for adaptive multidimensional integration*. Journal of Computational Physics **27** (1978) no. 2, 192 – 203.  
<http://www.sciencedirect.com/science/article/pii/0021999178900049>.
- [29] S. Alioli, P. Nason, C. Oleari, and E. Re, *A general framework for implementing NLO calculations in shower Monte Carlo programs: the POWHEG BOX*. JHEP **06** (2010) 043, [arXiv:1002.2581 \[hep-ph\]](#).
- [30] S. Frixione, P. Nason, and C. Oleari, *Matching NLO QCD computations with Parton Shower simulations: the POWHEG method*. JHEP **11** (2007) 070, [arXiv:0709.2092 \[hep-ph\]](#).
- [31] K. Arnold *et al.*, *VBFNLO: A Parton level Monte Carlo for processes with electroweak bosons*. Comput. Phys. Commun. **180** (2009) 1661–1670, [arXiv:0811.4559 \[hep-ph\]](#).
- [32] K. Arnold *et al.*, *VBFNLO: A Parton Level Monte Carlo for Processes with Electroweak Bosons – Manual for Version 2.5.0*. [arXiv:1107.4038 \[hep-ph\]](#).
- [33] J. Baglio *et al.*, *Release Note - VBFNLO 2.7.0*. [arXiv:1404.3940 \[hep-ph\]](#).
- [34] R. Feger, “MoCaNLO: a generic Monte Carlo event generator for NLO calculations of hadron-collider processes.” unpublished, 2015.
- [35] S. Actis *et al.*, *Recursive generation of one-loop amplitudes in the Standard Model*. JHEP **04** (2013) 037, [arXiv:1211.6316 \[hep-ph\]](#).
- [36] S. Actis *et al.*, *RECOLA: REcursive Computation of One-Loop Amplitudes*. Comput. Phys. Commun. **214** (2017) 140–173, [arXiv:1605.01090 \[hep-ph\]](#).
- [37] B. Biedermann, A. Denner, and M. Pellen, *Large electroweak corrections to vector-boson scattering at the Large Hadron Collider*. Phys. Rev. Lett. **118** (2017) no. 26, 261801, [arXiv:1611.02951 \[hep-ph\]](#).
- [38] B. Biedermann, A. Denner, and M. Pellen, *Complete NLO corrections to  $W^+W^+$  scattering and its irreducible background at the LHC*. [arXiv:1708.00268 \[hep-ph\]](#).
- [39] M. Moretti, T. Ohl, and J. Reuter, *O’Mega: An Optimizing matrix element generator*. [arXiv:hep-ph/0102195 \[hep-ph\]](#).
- [40] W. Kilian, T. Ohl, and J. Reuter, *WHIZARD: Simulating Multi-Particle Processes at LHC and ILC*. Eur. Phys. J. **C71** (2011) 1742, [arXiv:0708.4233 \[hep-ph\]](#).
- [41] **NNPDF** Collaboration, R. D. Ball *et al.*, *Parton distributions for the LHC Run II*. JHEP **04** (2015) 040, [arXiv:1410.8849 \[hep-ph\]](#).
- [42] A. Buckley, J. Ferrando, S. Lloyd, K. Nordström, B. Page, M. Rüfenacht, M. Schönherr, and G. Watt, *LHAPDF6: parton density access in the LHC precision era*. Eur. Phys. J. **C75** (2015) 132, [arXiv:1412.7420 \[hep-ph\]](#).
- [43] A. Denner, S. Dittmaier, M. Roth, and D. Wackeroth, *Electroweak radiative corrections to  $e^+e^- \rightarrow WW \rightarrow 4$  fermions in double-pole approximation: The RACOONWW approach*. Nucl. Phys. **B587** (2000) 67–117, [arXiv:hep-ph/0006307 \[hep-ph\]](#).

- [44] A. Denner *et al.*, *Predictions for all processes  $e^+e^- \rightarrow 4 \text{ fermions} + \gamma$* . Nucl. Phys. **B560** (1999) 33–65, [arXiv:hep-ph/9904472](#).
- [45] A. Denner *et al.*, *Electroweak corrections to charged-current  $e^+e^- \rightarrow 4 \text{ fermion processes}$ : Technical details and further results*. Nucl. Phys. **B724** (2005) 247–294, [arXiv:hep-ph/0505042](#).
- [46] **CMS** Collaboration, *Observation of electroweak production of same-sign  $W$  boson pairs in the two jet and two same-sign lepton final state in proton-proton collisions at 13 TeV*. CMS-PAS-SMP-17-004.
- [47] M. Cacciari, G. P. Salam, and G. Soyez, *The anti- $k_t$  jet clustering algorithm*. JHEP **04** (2008) 063, [arXiv:0802.1189 \[hep-ph\]](#).