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Course facilitator: Dr M Pourbehi



**Project : Two-Way Slab System with Lateral Loads  
(Wind & Seismic)**

**EVODIE MWANGE KIBAMBO**  
**220074852**

Team Members	Student Numbers
MIHLALI NKOMO	222047178
LINDOKUHLE MBUYAZI	216071402
EVODIE MWANGE KIBAMBO	220074852

## Assignment Submittal & Identification

Student Number	220074852
Surname & Initials	KIBAMBO EM
Program	Bachelor of Engineering Technology Honours Civil Engineering
Subject Name	Design of Multi-Storey Buildings
Subject Code	D M B 5 8 1 S

Assignment Number : 0 1

Due date: 1 2 / 1 1 / 2 0 2 5

Lecturer: Dr. Mohammed Pourbehi

### DECLARATION OF OWN WORK:

I, student name \_\_ Evodie Mwange Kibambo \_\_, student number \_\_ 220074852 \_\_

declare that this report compiled is my own work, that it has not been submitted for any other degree at CPUT or any other University or any higher education institution, and that all resources that I have used or quoted are indicated in the text and acknowledged in the list of references.

Signed: EM KIBAMBO

Date: 01/11/2025

## Abstract

This report represents the structural analysis and design of a two-way concrete slab system of a multiple storey building subjected to both gravity and lateral loads, in accordance with the South African National Standards (SANS 10160 and SANS 10100-1). The analysis was conducted for a structure located in Durban, KwaZulu-Natal, where wind and seismic actions were determined based on site-specific parameters, including basic wind speed, terrain category, and peak ground acceleration.

The structure was modelled as a reinforced concrete frame and slab system using PROKON finite element software. The analysis considered ultimate and serviceability limit states, with verification of wind and seismic responses against simplified hand methods. The two-way slab was designed using the Direct Design Method, and beams and columns were detailed to meet the requirements of strength and serviceability.

The results demonstrate that the proposed structural system meets safety and serviceability criteria, with all member forces within acceptable limits.

In addition to technical outcomes, the report reflects professional practice through ethical decision-making, self-management, and quality assurance. The project highlights the importance of integrating engineering judgement in modern structural design under combined gravity and lateral actions.

## Table of Content

Abstract .....	2
1. INTRODUCTION .....	4
1.1 Project Background.....	4
1.2 Objectives .....	4
2. Site Selection & Justification.....	5
3. Phase 1 – Analysis (Two-Way Slab + Lateral Actions) .....	6
3.1 Actions and Load Combinations (SANS 10160) .....	6
3.1.1 Tabulated load combinations.....	6
3.1.2 Load Cases and Combinations Diagram.....	8
3.2 Two-Way Slab Analysis (Gravity) .....	12
3.3 Wind Actions (SANS 10160-3) .....	20
3.5 Finite Element Modelling & Verification (PROKON) .....	28
4. Phase 2 – Design & Detailing.....	29
4.1 Two-Way Slab Design .....	29
5. Discussion .....	51
6. Conclusion and recommendations .....	52
7. Reflection.....	52
8. Reference .....	53
9. Appendix .....	53

## List of figures

Figure 1: Building plan view and elevation .....	4
Figure 2 : Aerial view of site.....	5
Figure 3: Storey shear force from wind loading .....	24
Figure 4: Moments diagrams under wind loading .....	24
Figure 5: Axial forces diagram under wind loading .....	25
Figure 6 : Beam plan and elevation .....	34
Figure 1: Chat from Robert and Marshal .....	50

## List of tables

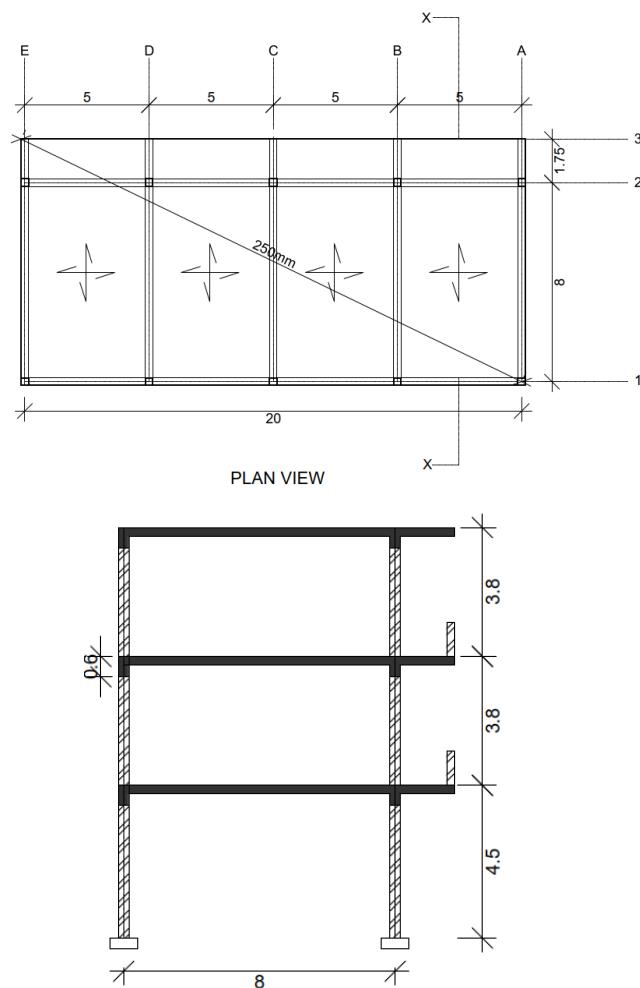
Table 1 STR-P ULS load combinations .....	6
Table 2: STR ULS Load combinations .....	7
Table 3: Accidental ULS Load Combinations .....	7

Table 4 : Irreversible serviceability SLS combinations .....	7
Table 5: Column moment distribution .....	19

## 1. INTRODUCTION

### 1.1 Project Background

This report presented the structural analysis and design of a reinforced concrete two-way slab system subjected to both gravity and lateral loads, including wind and seismic actions. The structure represented a typical reinforced concrete classroom block consisting of spans in each direction, supported by beams and columns (as shown in Figure 1). The project was done to demonstrate competence in integrated structural analysis, design, and professional engineering practice in accordance with South African standards.



*Figure 1: Building plan view and elevation*

### 1.2 Objectives

The primary objective of the project was to analyse and design the structural floor system to safely resist gravity, wind, and seismic actions while maintaining an adequate serviceability state. The objectives included:

- The analysis of the two-way slab using the procedures outlined in SANS 10100-1.

- The determination of wind and seismic actions in accordance with SANS 10160-3 and SANS 10160-4, using site-specific parameters based on the selected project location.
- To develop a 3D finite element (FE) model of the structure in PROKON,
- Verification of results through simplified hand calculations and ensuring consistency within provided limits.
- The design of slab, beams, and columns for ultimate and serviceability limit states, including reinforcement detailing, deflection checks, and crack control.

The study adopted a systematic approach beginning with the identification of the project site and corresponding design inputs, followed by gravity load estimation, lateral load derivation, finite element modelling, and component design. The structure was modelled as a two-way slab system supported on beams located along gridlines 1 and 2, forming a fully supported floor panel. Wind and seismic actions were incorporated alongside gravity loads to evaluate the building's overall behaviour under lateral actions.

All analysis and design work adhered to the relevant provisions of the South African National Standards (SANS), ensuring that the final solution met the fundamental requirements of strength, stability, and serviceability. The outcomes of this project provided an integrated understanding of how wind and seismic effects influence slab, beam, and column systems, reinforcing the importance of combining compliance to code and professional responsibility in structural engineering practice.

## 2. Site Selection & Justification

The project site was located in Geduld, within the City of Ekurhuleni in the Gauteng Province of South Africa. This location was selected due to its strategic location and the availability of geotechnical information that is crucial for wind load and seismic analysis. The surrounding area of Geduld is predominantly urban with a mixture of residential and industrial developments. Based on the built environment and the level of surface roughness, the site was classified as Terrain Category C. Based on the site characteristics, Terrain Category C was selected as it represents areas with regular vegetation cover, buildings, or isolated obstacles, which aligns with the suburban context of the project location.



*Figure 2 : Aerial view of site*

### 3. Phase 1 – Analysis (Two-Way Slab + Lateral Actions)

#### 3.1 Actions and Load Combinations (SANS 10160)

This section presents the gravity (G) and variable (Q) actions applied to the slab, beams, and columns. All load values were determined in accordance with SANS 10160-1 and SANS 10160-2.

The following steps were carried out:

- Permanent actions (self-weight, finishes, partitions) were calculated based on material densities and element dimensions.
- Variable actions were selected according to the occupancy category of the building.
- Ultimate Limit State (ULS) and Serviceability Limit State (SLS) combinations were established by referencing SANS 10160-1
- Lateral actions were included by adding wind (W) and seismic (E) to combinations where relevant.
- Load-case diagrams and load-combination diagrams were prepared to illustrate the applied actions.

##### 3.1.1 Tabulated load combinations

Load Combination	Permanent Load (Gk)	Live Load(Qk)	Wind Load (Wk)
STR-P (ULS)			
<b>Unfavorable</b>			
C1	Permanent load with live load only		
	1.35	1	
C2	Permanent load with wind load only		
	1.35		1
C3	Permanent load with live load leading and wind load accompanying		
	1.35	1	0x1
C4	Permanent load with wind load leading and live load accompanying		
	1.35	0.3 x 1.0	1

Table 1 STR-P ULS load combinations

Load Combination	Permanent Load (Gk)	Live Load(Qk)	Wind Load (Wk)
STR (ULS)			
<b>Favorable</b>			
C1	Permanent load only		
	0.9		
<b>Unfavorable</b>			

C2	Permanent load and live load only		
	1.2	1.6	
C3	Permanent load and live load leading and wind load accompanying		
	1.2	1.6	0.0 x 1.6
C4	Permanent load and wind load only		
	1.2		1.6
C5	Permanent load and wind load leading and live load accompanying		
	1.2	0.3 x 1.6	1.6

Table 2: STR ULS Load combinations

Load Combination	Permanent Load (Gk)	Live Load(Qk)	Wind Load (Wk)	Seismic Load (E)
ACC (ULS)				
<b>Unfavorable</b>				
C1	Permanent load and seismic load only			
	1			1
C2	Permanent load and seismic load leading and live load accompanying			
	1	0.3 x 1		1
C3	Permanent load and live load leading and wind load accompanying			
	1	1	0.0 x 1	
C4	Permanent load and wind load leading and live load accompanying			
	1	0.3 x 1	1	

Table 3: Accidental ULS Load Combinations

Load Combination	Permanent Load (Gk)	Live Load(Qk)	Wind Load (Wk)
Irreversible serviceability (SLS)			
<b>Un-favorable</b>			
C1	Permanent load only		
	1.1		
<b>Favorable</b>			
C2	Permanent load and live load only		
	1	1	
C3	Permanent load and live load leading and wind load accompanying		
	1	1	0.3 x 0.6
C4	Permanent load and wind load only		
	1		0.6
C5	Permanent load and wind load leading and live load accompanying		
	1	0.3 x 1	0.6

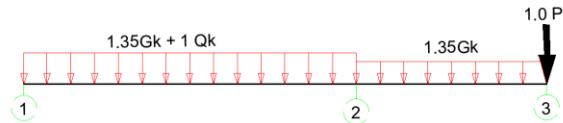
Table 4 : Irreversible serviceability SLS combinations

### 3.1.2 Load Cases and Combinations Diagram

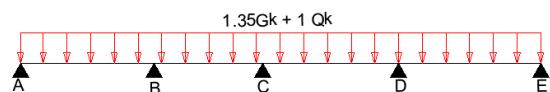
The diagrams below were developed using the different combinations

#### a) STR-P Combination diagrams

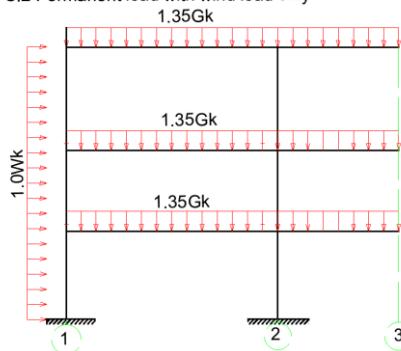
C.1 Permanent load with live load only ( same as C.3)



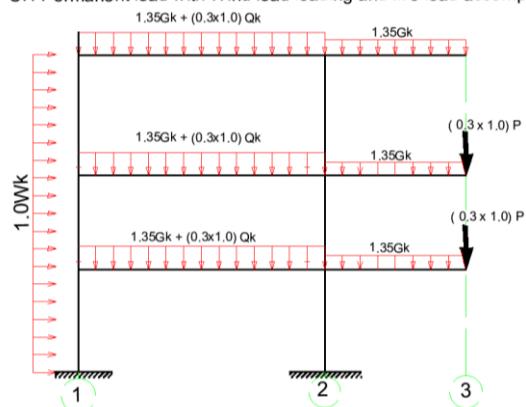
for the floor Slab



C.2 Permanent load with wind load only

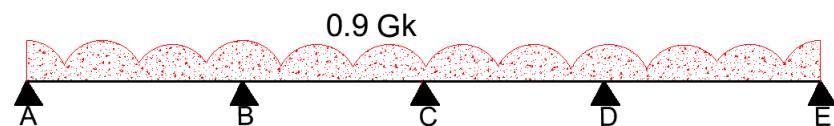


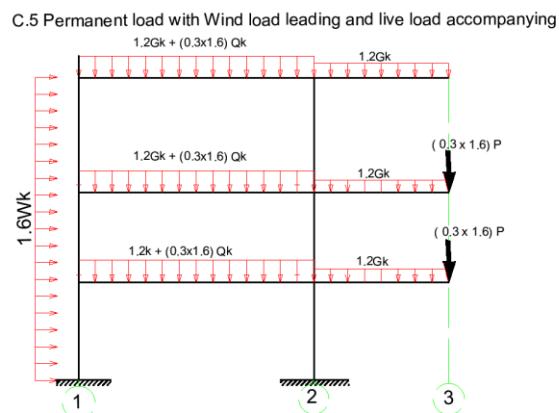
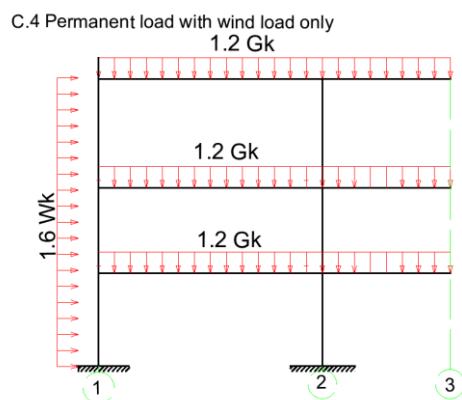
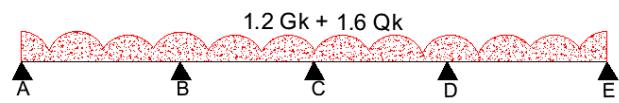
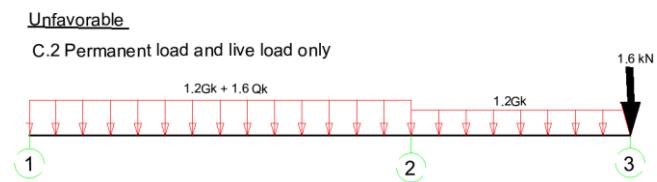
C.4 Permanent load with Wind load leading and live load accompanying



#### b) STR combination diagrams

C.1 (Favorable) Permanent load only

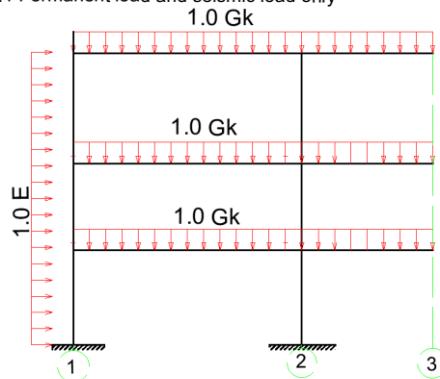




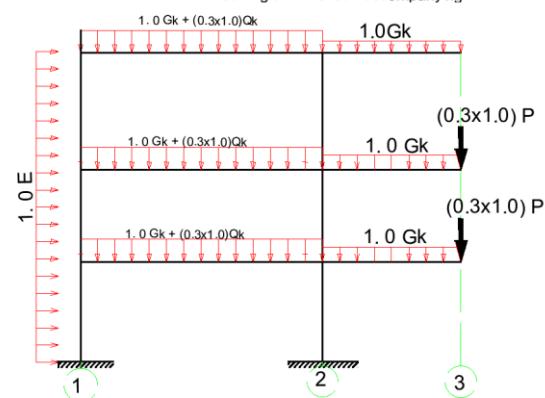
c) Accidental Combination diagrams

ACC (ULS)

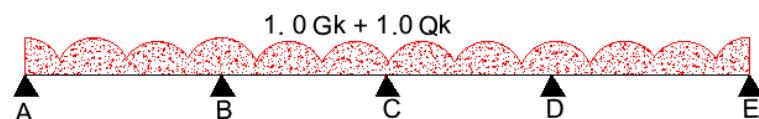
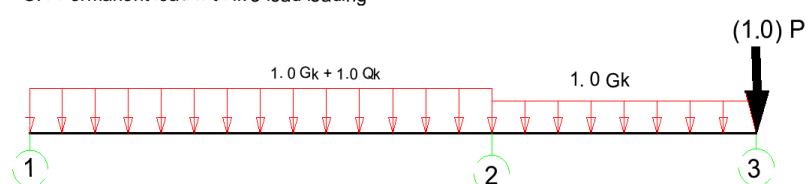
C.1 Permanent load and seismic load only



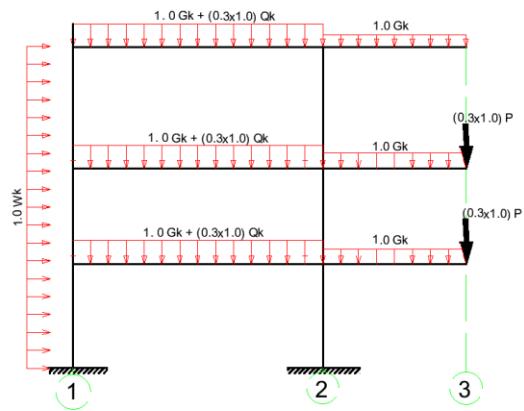
C.2 Permanent load with seismic load leading and live load accompanying



C.4 Permanent load with live load leading

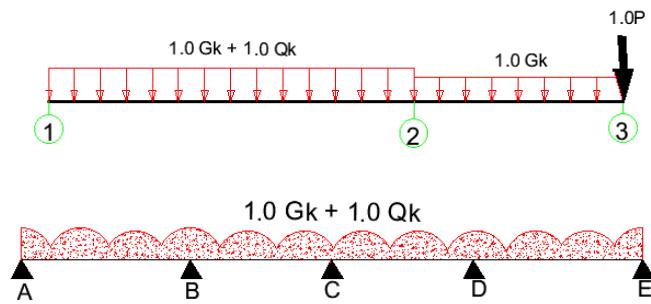


C.4 Permanent load with wind load leading and live load accompanying

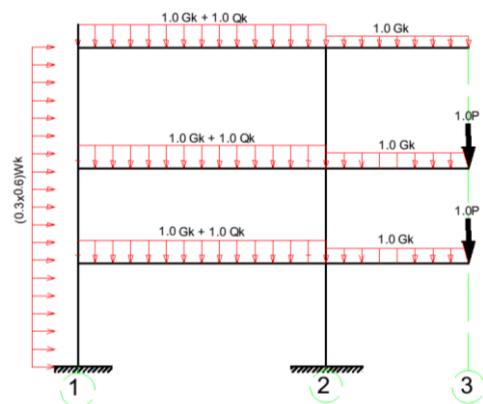


#### d) Irreversible Combination Diagrams

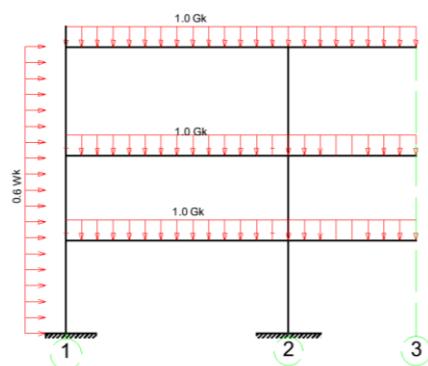
C.2 Permanent load and live load



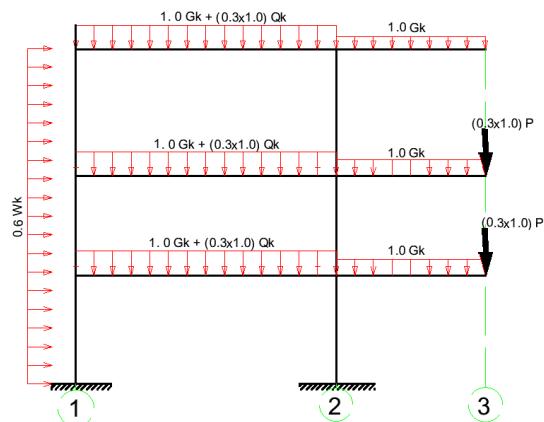
C.3 Permanent load with live load leading and wind load accompanying



C.4 Permanent load with wind only



C.5 Permanent load with wind load leading and live load accompanying



### 3.2 Two-Way Slab Analysis (Gravity)

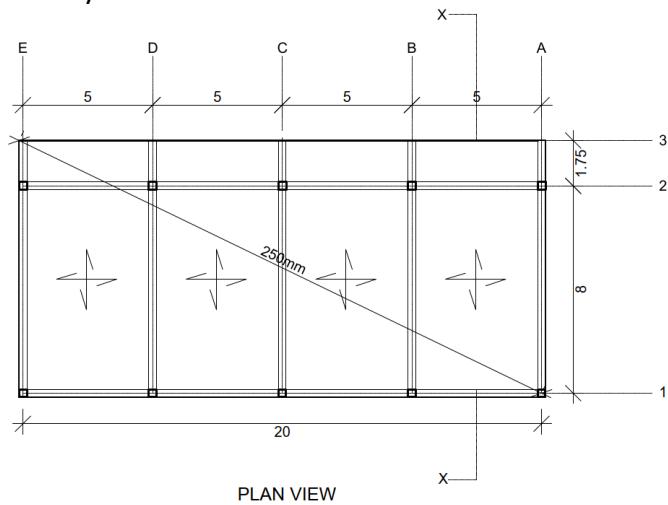
- The two-way slab system was analysed under gravity loads using the Direct Design Method (DDM) in accordance with SANS 10100-1. The slab was supported on all four edges by beams on gridlines 1 and 2, and span from grid A to E, forming a continuous panel. Below is displayed gravity load analysis and distribution on the slab, which will serve as basis for the design.

References	Calculations
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SANS  
10160-1

- **Slab Load Calculations**

#### Plan Layout



**Spans:**

A–B–C–D–E

Each span = 5 m

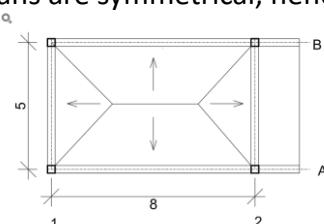
Width of slab = 8 m

- **Material Properties**

Element	Property	Value
Slab	Density	24 kN/m <sup>3</sup>
	Thickness	0.250 m
Wall	Weight	5 kN/m <sup>2</sup>
	Thickness	0.230 m
Scred	Density	23 kN/m <sup>3</sup>
	Thickness	0.050 m
Surface	Density	0.15 kN/m <sup>2</sup>

- **Load distribution on Span 1 and 4**

Both spans are symmetrical, hence they will have the same load distribution.



#### 1. Classroom Load

##### (a) Self-weight: Classroom

Element	Density (kN/m <sup>3</sup> )	Thickness (m)	Distributed Load (kN/m <sup>2</sup> )
Slab	24	0.25	6
Scred	23	0.05	1.15
Service	-	-	0.15
Wall	-	-	5
<b>Total</b>			<b>12.3 kN/m<sup>2</sup></b>

(B) Imposed Load: Classroom

Occupancy	Distributed Load (kN/m <sup>2</sup> )
Classroom	3

- Factored Load

$$n=1.2Gk+1.6Qk$$

$$n=19.56 \text{ kN/m}^2$$

- Span check  $\frac{ly}{lx} = \frac{8}{5} = 1.6 < 2$

This is a two-way slab, hence the load will be distributed as follows:

a.1 Trapezoidal load

$$w = \frac{n lx}{6} \left[ 3 - \left( \frac{lx}{ly} \right)^2 \right]$$

$$w = 42.53 \text{ kN/m}$$

a.2 Triangular load

$$w = \frac{n lx}{3}$$

$$w = 32.6 \text{ kN/m}$$

## 2. Balcony Load

(a) Self-weight: Balcony

Element	Density (kN/m <sup>3</sup> )	Thickness (m)	Distributed Load (kN/m <sup>2</sup> )
Slab	24	0.25	6
Screed	23	0.05	1.15
Services	-	-	0.15
<b>Total</b>			<b>7.3 kN/m<sup>2</sup></b>

(b) Imposed Load: Balcony

Occupancy	Distributed Load (kN/m <sup>2</sup> )
corridors	5

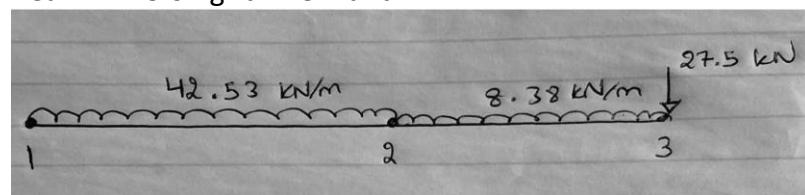
- Factored Load

$$n=1.2Gk+1.6Qk$$

$$n=16.76 \text{ kN/m}^2$$

$$\text{-Balustrade Load} = 5 \times 1.1 \times 5 = 27.5 \text{ kN}$$

- Beam 1-2-3 on grid line A and E



- Load distribution on Span 2 and 3

Factored Load

$$n=1.2Gk+1.6Qk$$

$$n=19.56 \text{ kN/m}^2$$

$$\text{Span check } \frac{ly}{lx} = \frac{8}{5} = 1.6 < 2$$

This is a two-way slab, hence the load will be distributed as follows:

a.1 Trapezoidal load

$$w = \frac{nlx}{6} \left[ 3 - \left( \frac{lx}{ly} \right)^2 \right]$$

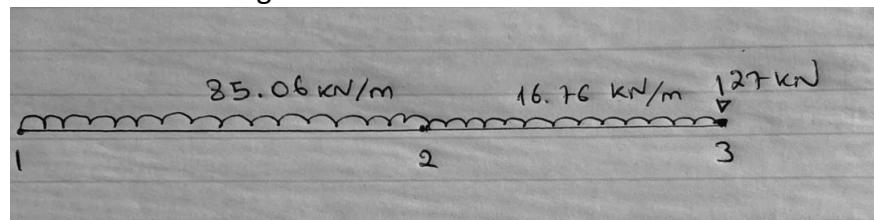
$$w = 42.53 \text{ kN/m}$$

a.2 Triangular load

$$w = \frac{nlx}{3}$$

$$w = 32.6 \text{ kN/m}$$

- Beam 1-2-3 on grid line A and E



- Beam on grid 1 and 2

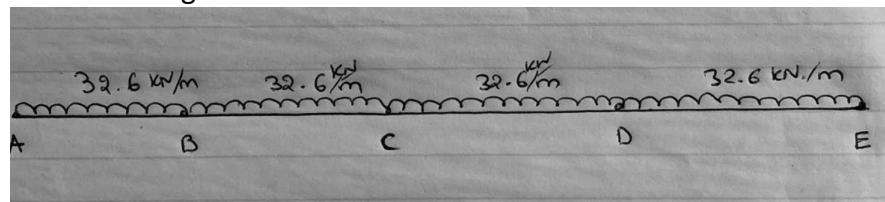
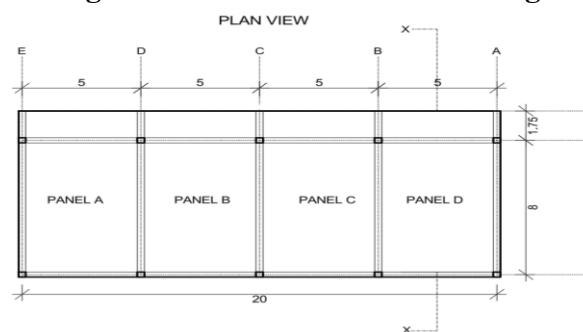


Table 15  
(SABS 0100-1)

#### Bending moment coefficients for rectangular panels



The nominal self-weight and live load are the same on adjacent panels, and the spans of adjacent panels are the same.

$$\frac{ly}{lx} = \frac{8 \text{ m}}{5 \text{ m}} = 1.6$$

In Table 15,  $\frac{ly}{lx} = 1.6$  is not available, so interpolation will be applied between 1.5 and 1.75 to calculate the bending moment coefficients.

Table 15  
(SABS 0100-1 )

• **Panel A and D**

The two panels will have the same configuration as they are symmetrical.

Panel A has three discontinuous edges with one long edge continuous hence, Case 7 will be used

Interpolation:

1.5	<b>1.6</b>	1.7
0.084	<b>0.0872</b>	0.092
0.063	<b>0.065</b>	0.069

❖ Short span lx direction

Sagging (+) moment in mid span

$$\beta_{sx} = 0.065$$

$$m_{sx.a1} = \beta_{sx} \cdot n \cdot l_x^2 = 0.065 \times 19.53 \times (8)^2 \\ = 81.24 \text{ kN}\cdot\text{m}$$

Hogging (-) moment at support

$$\beta_{sx} = -0.0872$$

$$m_{sx.a2} = \beta_{sx} \cdot n \cdot l_x^2 = -0.0872 \times 19.53 \times 5 \times 8^2 \\ = -108.99 \approx 147 \text{ kN}\cdot\text{m}$$

❖ Long span ly direction

Sagging (+) moment in mid span

$$\beta_{sy} = 0.0654$$

$$m_{sy.a1} = \beta_{sy} \cdot n \cdot l_y^2 = 0.065 \times 19.53 \times (5)^2 \\ = 31.73 \text{ kN}\cdot\text{m}$$

Hogging (-) moment at support

$$\beta_{sy} = -0.0872$$

$$m_{sy.a2} = \beta_{sy} \cdot n \cdot l_y^2 = -0.0872 \times 19.53 \times 5 \times 5^2 \\ = -42.47 \text{ kN}\cdot\text{m}$$

• **Panel B and C**

The two panels will have the same configuration as they are symmetrical.

Panel B has two short edges that are discontinuous, so case 5 will be used.

Interpolation:

1.5	<b>1.6</b>	1.7
0.062	<b>0.064</b>	0.067
0.045	<b>0.045</b>	0.047

❖ Short span lx direction

Sagging (+) moment in mid span

$$\beta_{sx} = 0.045$$

$$m_{sx.b1} = \beta_{sx} \cdot n \cdot l_x^2 = 0.045 \times 19.53 \times (8)^2 \\ = 56.25 \text{ kN}\cdot\text{m}$$

SANS 10100-1  
Clause 4.4.4.2.3

Hogging (-) moment at support  
 $\beta_{sx} = -0.0872$   
 $m_{sx,b2} = \beta_{sx} \cdot n \cdot l_x^2 = -0.064 \times 19.53 \times 8^2$   
 $= -77.99 \text{ kN}\cdot\text{m}$

❖ Long span ly direction  
Sagging (+) moment in mid span  
 $\beta_{sy} = 0.045$   
 $m_{sy,b1} = \beta_{sy} \cdot n \cdot l_y^2 = 0.045 \times 19.53 \times (5)^2$   
 $= 21.97 \text{ kN}\cdot\text{m}$

Hogging (-) moment at support  
 $\beta_{sy} = -0.064$   
 $m_{sy,b2} = \beta_{sy} \cdot n \cdot l_y^2 = -0.0664 \times 19.53 \times 5^2$   
 $= -31.248 \text{ kN}\cdot\text{m}$

There is a large difference at the joint support moment of panels A and B, hence some adjustments are required:

a)  $\Sigma |M| = m_{xa} + \frac{m_{xa}a_2}{2} = 31.24 + \frac{102.93}{2} = 135.735 \text{ kN}\cdot\text{m}$

b) Fixed end moment  
Panel A:  $m_{I1a} = -102.33 \text{ kN}/\text{m}$   
Panel B:  $m_{I1b} = -49.32 \text{ kN}/\text{m}$

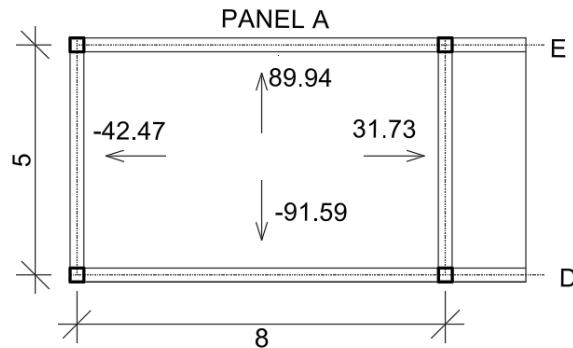
c) Moment Redistribution at Support  
 $D_a = \frac{3}{2+3} = 0.6, D_b = 0.4$

d) Unbalanced Moment:  
 $M_o = -m_{Ia} - m_{Ib} = -108.99 - (-79.99) = -29 \text{ kN}/\text{m}$

e) Moment Distribution:  
 $m_{xa,a2} = -102.99 - (0.6)(-53) = -91.59 \text{ kN}\cdot\text{m}$   
 $m_{xb,A} = -49.33 + (0.4)(-53) = -91.59 \text{ kN}\cdot\text{m}$

f) Adjusted Midspan Moment for Panel A

$$m_{sx,a2} = \left( 135.735 - \left| \frac{(-91.59)}{2} \right| \right) = 135.735 - \frac{91.59}{2} \\ = 89.94 \text{kN/m}$$



- Going from the loading obtained , a moment distribution was done for the columns, that helped in determining the worst case scenario to use for the design. Below is displayed the summarised moment distribution on the column, the details calculations are attached under the appendix D

Joint	K – per Member	$\sum k$	Distribution factor
A (Fixed)	AB: 0.8EI	---	$D_{AB} = 0$
B	AB: 0.8EI, BC:0.8EI	1.6EI	$D_{AB} = 0.5, D_{BC} = 0.5$
C	BC:0.8EI, CD: 0.8EI	1.6EI	$D_{CB} = 0.5, D_{CD} = 0.5$
D	CD: 0.8EI, DE:0.8EI	1.6EI	$D_{DC} = 0.5, D_{DE} = 0.5$
E (Fixed)	DE: 0.8EI	--	$D_{ED} = 0$

Joint	A	B		C		D		E
DF	0	0,5	0,5	0,5	0,5	0,5	0,5	0
FEM	-67,92	-67,92	-67,92	-67,92	-67,92	-67,92	-67,92	-67,92
Balance		67,92	67,92	67,92	67,92	67,92	67,92	
C,O	33,96		33,96	33,96	33,96	33,96	33,96	33,96
Bal.		-16,98	-16,98	-33,96	-33,96	-16,98	-16,98	
C.O	-8,49		-16,98	-8,49	-8,49	-16,98	-8,49	
Bal.		8,49	8,49	8,49	8,49	8,49	8,49	
C.O	4,245		4,245	4,245	4,245	4,245	4,245	4,245
Bal.		-2,122	-2,122	-4,245	-4,245	-2,122	-2,122	
C.O	-1,061		-2,122	-1,061	-1,061	-2,122	-1,061	
Bal.		1,061	1,061	1,061	1,061	1,061	1,061	
C.O	0,531		0,531	0,531	0,531	0,531	0,531	0,531
Bal.		-0,266	-0,266	-0,531	-0,531	-0,266	-0,266	
C.O	-0,133		-0,266	-0,138	-0,138	-0,266	-0,133	-0,133
Bal		0,133	0,133	0,133	0,133	0,133	0,133	
	-38,868	-9,684	9,684	0	0	9,684	-9,684	-38,868

Joint	A		BA	B		CB	C		DC	D		ED	E	
	Col. I.M	AB		Col. I.M	BC		Col. I.M	CD		Col. I.M	DE		Col. I.M	ED
	DF	0,233		0,767	0,434		0,434	0,132		0,434	0,132		0,467	0,233
Load (kN)			163		163		163		163		163		163	
FEM	-67,92	-67,92	58,953	17,931	58,953	58,955	17,931	58,955	58,953	17,931	58,953	52,095	15,825	
Balance	15,825	52,095	26,048	26,048	26,048	26,078	26,078	26,078	26,048	26,048	26,048	26,048	26,048	
C,O			-22,609	-6,877	-22,609	-22,609	-6,877	-22,609	-22,609	-6,877	-22,609	-19,979	-6,069	
Bal.	-6,069	-19,979				-11,305	-11,305	-11,305	-11,305	-11,305	-11,305	-9,989	-11,305	
C.O			-9,989			9,242	9,242	9,242	9,242	9,242	9,242	8,671	2,634	
Bal.	2,634	8,671				4,907	4,907	4,907	4,907	4,907	4,907	4,621		
C.O			4,621			4,621	4,621	4,621	4,621	4,621	4,621			
Bal.	-1,077	-3,544				-4,011	-4,011	-4,011	-4,011	-4,011	-4,011	-3,544	-1,077	
C.O			-2,006			-1,772	-2,045	-2,006	-2,006	-2,045	-1,772	-2,006		
Bal.	0,467	1,539				1,657	0,504	1,657	1,741	0,529	1,741	1,539	0,467	
M (kNm)	11,78	-11,78		-6,065	13,149	-7,083		-8,754	13,324	-6,754		-7,083	13,149	-6,065
													-11,78	11,78

Table 5: Column moment distribution

- Moment in each column is given by:

$$M_{col} = \sum M_{col} \times \frac{k_{col}}{\sum k_{col}}$$

$$M_{AK} = M_{EO} = 11.78 \times \frac{1.776 \times 10^{-4}}{3.276 \times 10^{-4}} = -6.386 \text{ kNm}$$

$$M_{AF} = M_{EJ} = 11.78 \times \frac{1.5 \times 10^{-4}}{3.276 \times 10^{-4}} = 5.39 \text{ kNm}$$

$$M_{BL} = M_{DN} = 13.149 \times \frac{1.776 \times 10^{-4}}{3.276 \times 10^{-4}} = 7.128 \text{ kNm}$$

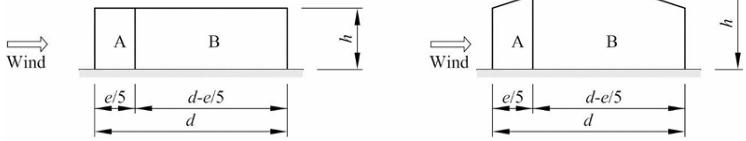
$$M_{BG} = M_{DI} = 13.149 \times \frac{1.776 \times 10^{-4}}{3.276 \times 10^{-4}} = 6.02 kNm$$

### 3.3 Wind Actions (SANS 10160-3)

Wind loads were evaluated using the following site-specific parameters:

- **Location:** Geduld, Ekurhuleni, Gauteng
- **Terrain Category:** C
- **Elevation:** 1600 m
- **Building Height:** 12.1 m
- **Basic Wind Speed:**  $v_{b,0} = 36 \text{ m/s}$
- **Design Working Life:** 50 years

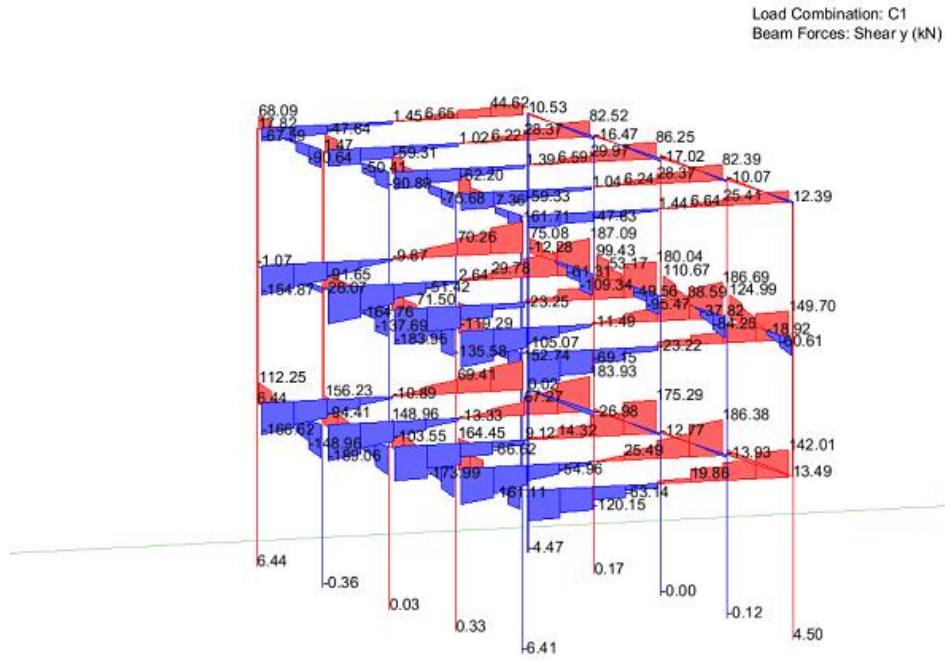
Reference	Calculations	Outcomes
SANS 10160-3  Sans 10160-1 (Annexure A) Sans 10160-1 (Table 1)	<p style="text-align: center;"><u>Load Calculations</u></p> <p><u>Wind loading</u></p> <p><b>Given:</b></p> <ul style="list-style-type: none"> <li>• Location : Geduld in the City of Ekurhuleni, Gauteng Province.</li> <li>• Terrain Category C</li> <li>• Elevation : 1600 meters</li> <li>• Height: 12.1 m</li> <li>• wind speed : 36 m/s</li> <li>• Design working life: 50 years</li> </ul>	
7.2.2 7.2.3	<ul style="list-style-type: none"> <li>• <b>Wind speed and wind pressure</b></li> </ul> $V_b = C_{prob} \times V_{b,0}$ $C_{prob} = \left[ \frac{1 - K \times \ln \{-\ln(1 - p)\}}{1 - K \times \ln \{-\ln 0,98\}} \right]^n$ $K = 0.2 \quad P = \frac{1}{50} \quad n = 0.5$ <p>Therefore, <math>C_{prob} = 1</math></p> $V_b = 1 \times 36 \text{ m/s} = 36 \text{ m/s}$	$V_b = 36 \text{ m/s}$
7.3 7.3.1.1	<ul style="list-style-type: none"> <li>• <b>Peak wind speed</b></li> </ul> $V_p(Z) = C_r(Z) \times C_o(Z) \times V_{b,peak}$ $V_{b,peak} = 1.0 \times V_b = 1.0 \times 36 \text{ m/s} = 36 \text{ m/s}$	

7.3.2.1 Table 1	$c_r(z) = 1,36 \left( \frac{z - z_o}{z_g - z_o} \right)^\alpha$ $Cr(z) = 1.0$ <p>At terrain category C:  <math>Zg = 350 \quad Z_o = 3 \quad Z_c = 5 \quad a = 0.120</math>  At <math>z = 12.1 \text{ m}</math>  <math>Cr = 1.36 ((12.1-3)/(350-3))0.120 = 0.88</math>  <math>V_p(z) = 0.88 \times 1.0 \times 36 = 31.68 \text{ m/s}</math></p>	$Cr(z) = 1.0$ $V_p(z) = 31.68 \text{ m/s}$						
7.4	<ul style="list-style-type: none"> <li><b>Peak wind speed pressure</b></li> </ul> $q_p(z) = \frac{1}{2} \times \rho \times V_p^2(z)$  <p>At Geduld in the City of Ekurhuleni, Gauteng Province, the site altitude above sea level is 1600m.</p> <p>Using interpolation, the air density (<math>\rho</math>) = <math>0.988 \text{ kg/m}^3</math></p> <p>At <math>z = 12.1 \text{ m}</math>  <math>V_p(z) = 31.68 \text{ m/s}</math>  <math>q_p(z) = \frac{1}{2} \times 0.988 \times 31.68^2 = 495.789 \text{ N/m}^2</math></p>							
8 8.10 8.10.1	<p><b>External wind pressure</b></p> <p>b=20.3m  h=12.1m  e=b or 2h the lesser  e=20.3 m or e= 24.2m  e=20.3 m  d=9.9m  e&gt;d</p>  <p>c) Elevation for <math>e \geq d</math></p>	$q_p(z) = 495.789 \text{ N/m}^2$						
8.10.1.1	<p>Area = <math>12.1 \times 20.3 = 245.63 \text{ m}^2</math>  <math>B \times h &gt; 10 \text{ m}^2</math> use <math>C_{pe}</math></p> <p>Area of openings = 30% Area of wall  = 30% of <math>245.63 \text{ m}^2</math>  = <math>73.69 \text{ m}^2</math></p> <p><math>h/d = \frac{12.1}{9.9} = 1.22</math></p> <table border="1" data-bbox="346 1785 1124 1904"> <thead> <tr> <th>Zone</th> <th><math>C_{pe10}</math></th> </tr> </thead> <tbody> <tr> <td>A</td> <td>-1.2</td> </tr> <tr> <td>B</td> <td>-0.8</td> </tr> </tbody> </table> <ul style="list-style-type: none"> <li><b>Internal pressure</b></li> </ul>	Zone	$C_{pe10}$	A	-1.2	B	-0.8	
Zone	$C_{pe10}$							
A	-1.2							
B	-0.8							
8.3.9.6								

	<p>With reference to clause 8.3.9.6, the building has no dominant wall, hence Cpi is determined using Figure 16.</p> <p>Area of openings = 30% Area of wall  <math>= 30\% \text{ of } 245.63 \text{ m}^2</math>  <math>= 73.69 \text{ m}^2</math></p> $\mu = \frac{\text{sum of openings where cpe is negative or 0}}{\text{sum of openings}}$ $\mu = 1$ $h/d = \frac{12.1}{9.9} = 1.22$ <p>from the graph, Cpi = -0.5</p> <ul style="list-style-type: none"> <li>Internal Wind pressure  <math>Wi = qp(z) \times Cpi</math>  <math>= 495.789 \times (-0.5)</math>  <math>= -247.89 \text{ N/m}^2</math></li> <li>External Wind pressure  <math>We = qp(z) \times Cpe</math></li> </ul> <p>For Zone A  <math>We = 495.789 \times (-1.2)</math>  <math>= -594.95 \text{ N/m}^2</math></p> <p>For Zone B  <math>We = 495.789 \times (-0.8)</math>  <math>= -396.62 \text{ N/m}^2</math></p>	
7.5.3	<ul style="list-style-type: none"> <li><b>Calculation of wind force</b></li> </ul> <p>The wind force Fw is given by :</p> $F_w = c_s \times c_d \times c_f \times q_p (z_e) \times A_{ref}$	
7.5.3.5	<ul style="list-style-type: none"> <li>Force Coefficient Calculation</li> </ul> $C_f = C_{f0} \times \psi_m \times \psi_r$ $\frac{L}{b} = \frac{20.3}{9.9} = 2.05$ $\frac{d}{b} = \frac{10.3}{9.9} = 1.04$	
<b>Figure 25</b>	$C_{f0} = 1.65$ $\psi_r = 1$ (Reduction factor for sharp corners – Figure 26) $\frac{r}{b} = 0$ <p><b>Solidity Ratio:</b></p> $\frac{A}{A_c} = 1$ (Solid rectangular wall, Cl. 8.13.3)	
<b>Table 22</b>	<p><b>Effective Slenderness</b></p> $L \geq 50m, \quad \lambda = \frac{1.4 \times 20.3}{9.9} = 2.87 < 70$	

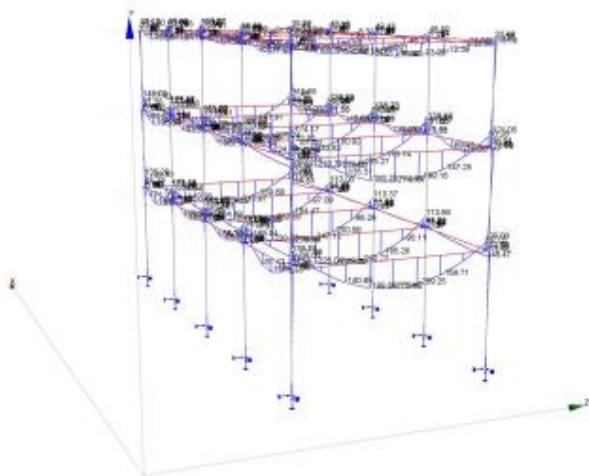
<b>Figure 38</b>	$L = 15 \text{ m}, \quad \lambda = \frac{2 \times 20.3}{9.9} = 4.10 < 70$ <p><b>Interpolation:</b></p> <table border="0"> <thead> <tr> <th>L (m)</th> <th><math>\lambda</math> (Slenderness)</th> </tr> </thead> <tbody> <tr> <td>50</td> <td>2.87</td> </tr> <tr> <td>20.3</td> <td>3.914</td> </tr> <tr> <td>15</td> <td>4.10</td> </tr> </tbody> </table> <p>Thus,  <math>\lambda = 3.914</math></p> $\psi_m = 0.651$	L (m)	$\lambda$ (Slenderness)	50	2.87	20.3	3.914	15	4.10	
L (m)	$\lambda$ (Slenderness)									
50	2.87									
20.3	3.914									
15	4.10									
	<p><b>Final Calculation</b></p> $C_f = C_{f0} \times \psi_r \times \psi_m$ $C_f = (1.65)(1)(0.65) = 1.074$									
8.7.2 Equation 22	<p><b>Reference Area Calculation</b></p> $A_{ref} = L \times b$ $A_{ref} = (20.3 \times 9.9) = 200.97 \text{ m}^2$ <p>The wind force is calculated as follows: <math>F_w = 1 \times 1 \times 495.789 \text{ N/m}^2 \times 200.97</math></p> $F_w = 99638.715 \text{ N}$ $= 99.638 \text{ kN}$									

- A 3D model was developed to analyse the effect of the combined actions of wind and gravity load on the building. When modelling on prokon, the required input use for hand calculations was applied on the model to derive storey shear forces as shown under figure 3,4, and 5. The complete prokon analysis of the building is attached under the appendix C.



*Figure 3: Storey shear force from wind loading*

## X-Moments: Load Case Load Combination C1



*Figure 4: Moments diagrams under wind loading*

### Axial Forces: Load Case Load Combination C1

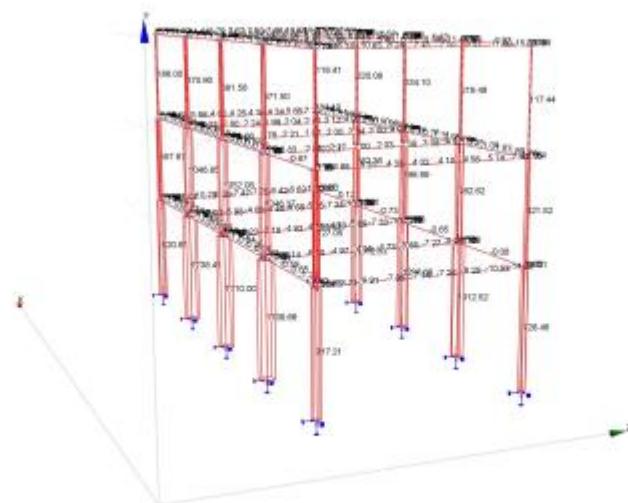


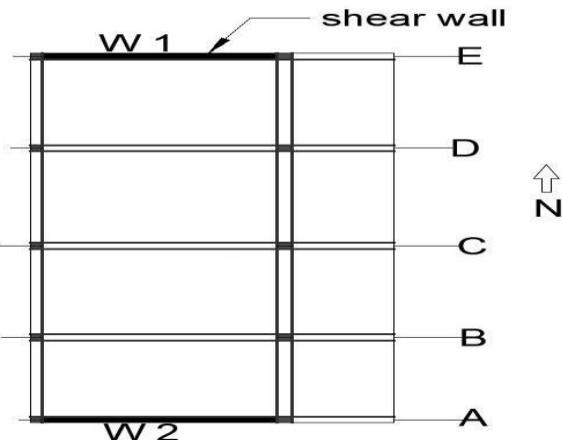
Figure 5: Axial forces diagram under wind loading

### 3.4 Seismic Actions (SANS 10160-4)

Although Gauteng is a region of low seismic activity, It was required to evaluate the potential effect on the structure. The analysis was based on the Equivalent Lateral Force (ELF) method because the building Satisfy the conditions stipulated under clause 8.4.3 . The system chosen was a moment resisting frame with two shear walls added on the perimeter to improve the building's lateral strength and stability. They help the structure resist earthquake forces and reduce movement or drift in the frame.

Reference	Calculations	Answer
Tutorial -2	<p><b><u>SELF-WEIGHTS</u></b></p> <p><b>Slab:</b></p> $W = \gamma_{concrete} \cdot t \cdot A_{slab}, \quad L = 8m \quad W = 20m$ $= 24 \times 0.25 \times (8 \times 20), \quad \gamma_{concrete.} = 24kN/m^3$ $= 960kN$ <p><b>Scree:</b></p> $W = \gamma_{scree} \cdot t \cdot A_{slab}$ $= 23 \times (0.05) \times (8 \times 20)$ $= 184 kN$ <p><b>Services:</b></p> $0.15kPa$ $W = 0.15 \times (8 \times 20)$ $= 24kN$ <p><b><u>Masonry Walls:</u></b></p>	

SANS 10160-1, Table 2	<p><b>(1) Gridline A-E</b></p> $W = 5kN/m^2 (7.7 \times 3.2)(5\text{no.}) \\ = 616 kN$ <p><b>(2) Gridline 1 &amp; 2:</b></p> $W = 5kN/m^2(4.7 \times 3.2)(8\text{no.}) \\ = 601.6kN$ <p><b>Balustrade:</b></p> $W = 5kN/m^2(1.1)(0.23) \\ = 1.265kN$ <p><b>Balcony:</b></p> $W_{slab} = \gamma_{concrete}.t \cdot A_{slab} \\ = 210kN$ <p><b>TOTAL (<math>G_n</math>): Slab + Balcony + Masonry Walls+ Screed +Services</b></p> $G_n = 2595.6 kN$	2595.6 kN
SANS10160-1, Table 2	<p><b>IMPOSED LOADS</b></p> <p><b>Classroom</b>, C1 - <math>q_k = 3kN/m^2</math></p> $Q_1 = 3(8 \times 20) \\ = 480kN$ <p><b>Balcony</b></p> $Q_2 = 5 (1.75 \times 20) \\ = 175 kN$ <p><b>TOTAL (Q): Classroom + Balcony</b></p> $Q = 655 kN$ <p><i>Combination Factor, <math>\psi_i = 0.3</math></i></p>	655 kN
SANS10160-4,CL 8.3	$W_{n1} = G_n + \psi_i Q_n \\ = 2595.6 + 0.3(655) \\ = 2792.1kN \times 2\text{no} \\ = 5584.2kN$ <p><b>ROOF</b></p> <p><b>Self-weight</b></p> $G_n = (24)(9.75 \times 20) \\ = 1170kN$ <p>Screed-roof: 184 kN</p>	5584.2kN

SANS10160-2, Table 5	<p>Services: 29.25 kN          Screed-Balcony: 40.25 kN  <b>Sub-total = 1423.5 kN</b></p> <p><b>Imposed load</b>          Category J, <math>q_k = 2 \text{ kN}/\text{m}^2</math>  <math>Q = 2(9.75 \times 20)</math>  <math>= 390 \text{ kN}</math></p> $W_{n2} = G_n + \psi_i Q_n$ $= 1423.5 + 0.3(390)$ $= 1540.5 \text{ kN}$ $W_{n-TOTAL} = 5584.2 \text{ kN} + 1540.5 \text{ kN}$ $= 7124.7 \text{ kN}$ <p><math>a_g = 0.1</math></p>	
SANS10160-4, Figure 1	$q = 5$ (With reinforced concrete shear walls)	$W_n =$ <b>7124.7 kN</b>
SANS10160-4, Table 4	Ground type = 4	
SANS10160-4, Table 1	$S = 1.35$	
SANS10160-4, Table 2	$T_B = 0.2$ $T_c = 0.8$ $T_D = 2$	
	 <p>Thickness of the RC shear wall = 270mm</p>	

	Wall	$L_{wi}$ (m)	$b_w$ (m)	$A_i$ ( $m^2$ )	$h_t$ (m)	$L_{wi}/h_t$	
<b>W<sub>1</sub></b>	7.7	0.27		2.079	12.1	0.636	
<b>W<sub>2</sub></b>	7.7	0.27		2.079	12.1	0.636	
				<b>4.158</b>		<b>1.272</b>	

SANS10160-4,  
Cl 8.5.2.2

$$A_c \sum A_i \left[ 0.2 + \left( \frac{L_{wi}}{h_t} \right)^2 \right] = 7.559 m^2$$

$$C_T = 0.075 \sqrt{A_c} = 0.20620$$

$$T = 1.34 \text{ sec}$$

8.5.2.1

$$T_c \leq T \leq T_D \quad S_d(T) \left\{ = a_g \times S_q^{2.5} \left[ \frac{T_c}{T} \right] \right\} \text{ but } \geq \beta \times a_g$$

$$S_d(T) = 0.1 \times 1.35 \times \frac{2.5}{5} \left[ \frac{0.8}{1.34} \right]$$

$$= 0.0403$$

SANS10160-4,  
Cl 5.3.4

$$V_n = S_d(T) \times W$$

$$= (0.0403 \times 7124.7)$$

$$= \mathbf{287.125 kN}$$

SANS10160-4,  
Cl 8.5.1

$$F_{xn} = \frac{W_x \times h_x}{\sum_{i=1}^n W_i \times h_i} \times V_n$$

SANS10160-4,  
Cl 8.5.3

Floor	h (m)	W <sub>e</sub> (kN)	W <sub>h</sub> (kNm)	F (kN)	Cum. F (kN)
3	12.1	1540.5	18640.05	98.421	98.421
2	8.3	2792.1	23174.43	122.363	220.784
1	4.5	2792.1	12564.45	66.341	287.125
			<b>54378.93</b>		

**287.125kN**

### 3.5 Finite Element Modelling & Verification (PROKON)

For the purpose of this project, the software used was Prokon, where the entire 3D building was modelled. The model was analysed as a whole, and using the analysis results, the most critical results were further developed for design. The slabs were modelled as two-way plate elements supported by continuous beams.

The model geometry and element properties were based on the structural drawings and section sizes used in the hand calculations. This work represented Foundation supports were modelled as pinned bases, providing vertical restraint while allowing horizontal reactions to be taken directly from the Prokon output. For the Load Cases and Combinations Load cases modelled in Prokon correspond to gravity, wind (+/-) and seismic (ELF). The results displayed under Appendix C are from the worse combination case.

The following results were extracted:

- Bending moments and shear forces for critical beams
- Slab moment contours ( $M_x$  and  $M_y$ )
- Storey shear
- Deflections under service loads

## 4. Phase 2 – Design & Detailing

### 4.1 Two-Way Slab Design

Using moments obtained from the analysis, the Top and bottom reinforcement were designed for column and middle strips, then the minimum reinforcement and spacing limits of SANS 10100-1 were checked, and Torsion reinforcement was provided at discontinuous corners.

#### ❖ Input

Materials properties	Value
$f_{cu}$	30 MPa
$f_y$	450 MPa
Cover	20mm
$L_x$	5m
$L_y$	8m
$n$	19.53 kN/m <sup>2</sup>
$h$	250mm
$b_s$	300mm

REFERENCES	CALCULATIONS
<b>I. <u>PANEL A DESIGN</u></b>	
( SABS 0100-1)	<p><b>Assumptions:</b>  <math>b = 1 \text{ m}</math>  <math>\emptyset x = 16 \text{ mm}</math> (main reinforcement)  <math>\emptyset y = 12 \text{ mm}</math> (transverse reinforcement)</p> <p><b>Check for Reinforcement:</b></p> $d_x = h - \text{cover} - \frac{\emptyset x}{2} = 250 - 20 - \frac{16}{2} = 222 \text{ mm}$ $d_y = h - \text{cover} - \emptyset x - \frac{S_x}{2} = 250 - 20 - 16 - \frac{16}{2} = 208 \text{ mm}$ <p><b>Assumption:</b> Redistribution = 10%  <math>K' = 0.156</math></p>

Clause 4.3.3.4.1

#### A. Short Span Reinforcement

##### (i) At Midspan:

$$M = 89.94 \text{ kNm}$$

$$K = \frac{89.94 \times 10^6}{1000 \times 222^2 \times 30} = 0.061$$

Since  $K < K'$ , only tension reinforcement is required.

$$Z = 222[0.5 + \sqrt{0.25 - \frac{0.061}{0.9}}] = 205.76 \text{ mm} < 0.95d \checkmark$$

Area of Steel Required

$$A_s = \frac{89.94 \times 10^6}{0.87 \times 450 \times 205.76} = 1116.50 \text{ mm}^2$$

Provide: Y16 @ spacing

$$Nbars = \frac{1116.50}{\pi \times (16)^2 / 4} = 6bars$$

$$\text{Spacing} = \frac{1000}{6} = 166 \text{ mm c/c}$$

Provide: Y16 @ 150 mm c/c

$$A_{s,prov} = \frac{1000}{150} \times \frac{\pi}{4} \times 16^2 = 1340 \text{ mm}^2$$

##### (ii) At Support:

$$M = 91.59 \text{ kN m}$$

$$K = \frac{91.59 \times 10^6}{1000 \times 222^2 \times 30} = 0.062$$

$$Z = 222[0.5 + \sqrt{0.25 - \frac{0.062}{0.5}}] = 205.48 \text{ mm} < 0.95d$$

$$A_s = \frac{91.59 \times 10^6}{0.87 \times 450 \times 205.48} = 1138.54 \text{ mm}^2$$

Provide: Y16 @ 150 mm c/c

$$A_{s,prov} = 1340 \text{ mm}^2$$

#### B. Long Span Reinforcement

##### (i) At Midspan

$$M = 31.73 \text{ kN m}$$

$$d_g = 208 \text{ mm}$$

$$K = \frac{31.73 \times 10^6}{1000 \times 208^2 \times 30} = 0.024$$

<p>Table 23, Clause 4.11</p> <p>Clause 4.11.8.2.2(b)</p>	<p><math>z = 208 \left( 0.5 + \sqrt{0.25 - \frac{0.024}{0.9}} \right) = 202.30 &gt; 0.95d</math></p> <p>Hence, use <math>z = 0.95d = 197.6 \text{ mm}</math></p> $A_{s,req} = \frac{31.73 \times 10^6}{0.87 \times 450 \times 197.6} = 410.16 \text{ mm}^2$ <p><b>Provide:</b> Y12 @ 250 mm c/c  <math>A_{s,prov} = 452 \text{ mm}^2</math></p> <p><b>(ii) At Support</b></p> $M = 42.47 \text{ kN m}$ $K = \frac{42.47 \times 10^6}{1000 \times 208^2 \times 30} = 0.033$ $z = 208(0.5 + \sqrt{0.25 - \frac{0.033}{0.9}}) = 200.07 \text{ mm} > 0.95d$ <p>Hence, use <math>z = 0.95d = 197.6 \text{ mm}</math></p> $A_{s,req} = \frac{42.47 \times 10^6}{0.87 \times 450 \times 197.6} = 410.16 \text{ mm}^2$ <p><b>Provide:</b> Y12 @ 250 mm c/c  <math>A_{s,prov} = 452 \text{ mm}^2</math></p> <ul style="list-style-type: none"> <li>• <b>Minimum Reinforcement</b>  For high yield steel, the minimum reinforcement is:  <math>A_{s,min} = \frac{0.13 b h}{100}</math>  <math>A_{s,min} = \frac{0.13 \times 1000 \times 250}{100} = 325 \text{ mm}^2/\text{m width}</math></li> <li>• OK for all reinforcement  Provide: Y12 @ 250 mm c/c  <math>A_{s,prov} = 452 \text{ mm}^2/\text{m width}</math></li> <li>• <b>Maximum Spacing of Reinforcement</b>  Short span: <math>f_y = 450 \text{ MPa}</math>, <math>h = 250 \text{ mm}</math>  Slab depth &lt; 200 mm ⇒ additional check required  <math>\frac{100 A_{s,prov}}{b d_x} = \frac{100 \times 1340}{1000 \times 222} = 0.6 &lt; 3 \checkmark</math>  the maximum spacing should not exceed the lesser of</li> </ul>
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Claude 4.11.8.2.2  Clause 4.3.6.3	<p><math>3x(222) = 196 \text{ mm or } 180 \text{ mm}</math></p> <p>max spacing <math>&lt; 3x222</math></p> <p><b>C. Torsion Reinforcement</b></p> <p>(i) At the corner</p> $\frac{3}{4}A_{sx} = \frac{3}{4} \times 1340 = 1005 \text{ mm}^2$ <p>Provide Y16 @ 200 mm c/c</p> <p>(iii) Along edge:</p> $\frac{2}{8}A_{sx} = 502.5 \text{ mm}^2$ <p>Provide Y12 @ 225 mm c/c</p> <p><i>(Placed in corners of <math>0.2Lx = 1 \text{ m}</math>)</i></p> <p><b>D. Reinforcement at Discontinuous Ends:</b></p> <p>(i) Short span:</p> $\frac{1}{2} \times 1340 = 670 \text{ mm}^2 \Rightarrow \text{Provide Y16 @ 300 mm c/c}$ <p>(ii) Long span:</p> $\frac{1}{2} \times 452 = 325 \text{ mm}^2 < A_{s,min}$ <p>Use <math>A_s = 325 \text{ mm}^2 \Rightarrow \text{Provide Y12 @ 325 mm c/c}</math></p> <p><b>E. Span effective depth ratio , short span deflection</b></p> $\frac{M_{sx} \cdot a}{b dx^2} = \frac{89.94}{1000 \times 222^2} = 1.85 \times 10^2 \text{ kN/mm}^2 \approx 1.82 \text{ MPa}$ <ul style="list-style-type: none"> <li>Modification factor</li> </ul> $f_s = 0.87 f_y \times \frac{\gamma_1 + \gamma_2}{\gamma_3 + \gamma_4} \times \frac{A_{sreq}}{A_{s,prov}} \times \frac{1}{B_b}$ <p><math>\gamma_1 = 1.0</math> (SLS),  <math>\gamma_2 = 1.0</math> (SLS)  <math>\gamma_3 = 1.2</math> (ULS)  <math>\gamma_4 = 1.6</math> (ULS)</p> $A_{s,req} = 1116.45, A_{s,prov} = 1340$ $f_s = 0.87(450) + \frac{(1+1)}{(1.2+1.6)} \times \frac{1116.45}{1340} = 232 \text{ MPa}$ $F_1 = 0.55 + \frac{(477 - 232)}{120(0.97 + 0.9)} = 1.3 < 2.0 \text{ OK } \checkmark$ $\frac{lx}{dx} = \frac{5000}{222} = 22.52 < 24F_1 \text{ OK}$
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### E. Load Distribution and Shear

- Shear Check

$$v = \frac{19.53 \times 5}{2} = 48.825 \text{ kN}$$

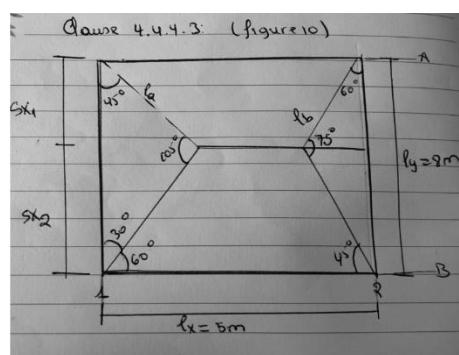
$$v = \frac{48.825 \times 10^3}{1000 \times 222} = 0.219 \text{ MPa}$$

$$V_c = 0.75 \left( \frac{30}{25} \right)^{1/3} \left( \frac{100 \times 1340}{1000 \times 222} \right)^{1/3} \left( \frac{400}{222} \right)^{1/4} \frac{1}{1.4}$$

$$V_c = 0.55 \text{ MPa}$$

$$\therefore v < V_c \Rightarrow \text{OK}$$

Load Distribution on Beam:



#### Short Span:

$$l_a = \frac{\sin 30 \times 8}{\sin 105} = 4.141 \text{ m}$$

$$S_{x1} = 4.141 \times \sin 45 = 2.928 \text{ m}, S_{x2} = 5.072 \text{ m}$$

#### Long Span:

$$l_b = \frac{\sin 45 \times 8}{\sin 75} = 5.856 \text{ m}$$

$$S_{y2} = 5.071 \text{ m}, S_{y2} = 2.928 \text{ m},$$

#### Shear on beam along Grid line A on short span

$$V_a = 19.53 \times 2.928 = 57.18 \text{ kN/m}$$

$$\frac{V_a}{d_x} = \frac{57.18}{222} = 0.258 \text{ MPa} < V_c \text{ OK } \checkmark$$

#### Shear on beam along Grid line B on short span

$$\frac{V_b}{d_x} = \frac{99.056}{222} = 0.446 \text{ OK } \checkmark$$

Shear at Beam along Long Span

Grid 1:

$$V_1 = 19.53 \times 2.928 = 57.18 \text{ kN/m}$$

$$\frac{V_1}{d_x} = \frac{57.18}{208} = 0.275 < V_c \text{ OK } \checkmark$$

Grid 2:

$$V_2 = \frac{19.53 \times 5.072}{208} = 0.476 < 0.55 \text{ OK } \checkmark$$

- Following above design, a bar bending schedule was generated and is as displayed under the appendix B

#### 4.2 Beam Design (Gridlines A–E and 1–2)

The structural design process of the beam covered several key aspects to ensure both safety and efficiency. Flexural design at mid-span and supports was carried out under ultimate limit state (ULS) conditions, while shear design followed the provisions outlined in SANS 10100-1. Compression reinforcement was added where necessary to enhance structural performance. Moment redistribution was reviewed and verified in cases where it was applied. In addition, anchorage lengths, lap lengths, and bar curtailments were carefully checked to meet code requirements. Finally, detailed reinforcement layouts and bar schedules were developed to provide clear guidance for construction and compliance with design standards.

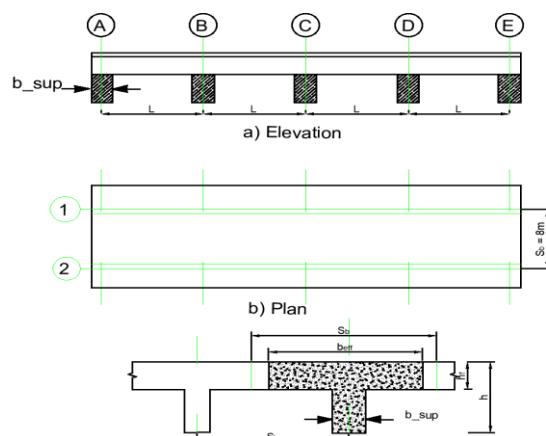


Figure 6 : Beam plan and elevation

- Input:**

Effective span length	L	5.0 m
Spacing of beams	S <sub>b</sub>	8.0 m
Width of supports	b <sub>sup</sub>	300 mm

Cross section dimensions:		
Width of web	$b_w$	300 mm
Total height	$h$	600 mm
Height of slab	$h_f$	250 mm
Loading:		
Nominal live load	$q_n$	3.0 kN/m <sup>2</sup> (class rooms)
Superimposed dead load	$g_{sdl}$	0.15 kN/m <sup>2</sup> + 5 kN/m <sup>2</sup> = 5.15 kN/m <sup>2</sup> (services + walls)
<b>The use of the structure requires a fire resistance of 1.5 hours (typically used for buildings between 5m to 18m high)</b>		
<b>Assuming moderate exposure conditions</b>		
Concrete:		
Characteristic cube strength	$f_{cu}$	25 MPa
Ultimate strain in concrete	$\varepsilon_{cu}$	0.0035
Unit weight of concrete	$\gamma_c$	24 kN/m <sup>3</sup>
Unit weight of screed	$\gamma_{screed}$	23 kN/m <sup>3</sup>
Maximum aggregate size	$h_{agg}$	26.5 mm (For deep suspended slabs)
Reinforcing steel:		
Yield strength in tension	$f_y$	450 MPa (hot-rolled high-yield steel from SABS 0100-1 Table 3)
Yield strength in shear	$f_{yv}$	450 MPa
Modulus of elasticity	$E_s$	200 GPa (SABS 0100-1 clause 3.4.2.3)
Material safety factor for shear	$\gamma_{mv}$	1.4 (SABS 0100-1 clause 3.3.3.2.c)

References	Calculations
Robberts and Marshall Textbook Table 10.1	<p><b>Concrete cover</b></p> <p><b>Fire resistance</b></p> <p>For fire resistance, for siliceous aggregates:        Minimum width of section = 140 mm , therefore <math>b_w = 300</math> mm <b>OK</b>        Minimum required cover to main reinforcing bars is 35 mm</p> <p>For a minimum possible link size of 8mm, cover should be greater than, 35 mm – 8 mm = 27 mm.</p>

Table 9.1  SABS 01001-1 Table 4	<p><b>Exposure conditions</b>  For moderate exposure conditions:  Cover = 30 mm &gt; h<sub>agg</sub> = 26.5 mm <b>OK</b></p> <p><b>Design loads: ULS</b></p> <p>Live load on beam: Q<sub>n</sub> = q<sub>n</sub> x s<sub>b</sub> = 3.0 kN/m<sup>2</sup> x 8.0 m = 24 kN/m  Self-weight of beam and slab : G<sub>self</sub> = [0.35 m x 0.3 m + 0.25m x 8.0 m] 24 kN/m<sup>3</sup>  = 50.52 kN/m  Screed : G<sub>screed</sub> = 0.05 m x 23 kN/m<sup>3</sup> x 8.0 m = 9.2 kN/m  Superimposed DL: G<sub>sdl</sub> = g<sub>sdl</sub> x s<sub>b</sub> = 5.15 kN/m<sup>2</sup> x 8.0 m = 41.2 kN/m</p> <p>Total self-weight: G<sub>n</sub> = G<sub>self</sub> + G<sub>screed</sub> + G<sub>sdl</sub> = 100.92 kN/m</p> <p>Design load: w<sub>u</sub> = 1.2 G<sub>n</sub> + 1.6 Q<sub>n</sub> = 159.50 kN/m</p> <p><b>Bending moments and shear forces</b></p> <p>Checking if simplified analysis method may be used:</p> <ul style="list-style-type: none"> <li>(a) <math>\frac{Q_n}{G_n} = \frac{24}{100.92} = 0.24 &lt; 1.25</math></li> <li>(b) The loads are mainly uniformly distributed.</li> <li>(c) There are 4 spans.</li> <li>(d) The spans are equal.</li> </ul> <p>Therefore, the simplified method in Table 4 may be used:  Total load on span: F = w<sub>u</sub> x L = 159.50 kN/m x 5.0 m = 792.52 kN</p> <p>Bending moments:</p> <p>Near mid-end span @F, M<sub>F</sub> = <math>\frac{FL}{11} = \frac{792.52 \text{ kN} \times 5 \text{ m}}{11} = 360.2 \text{ kNm}</math></p> <p>First interior support @B, M<sub>B</sub> = <math>\frac{-FL}{9} = \frac{-792.52 \text{ kN} \times 5 \text{ m}}{9} = -440.3 \text{ kNm}</math></p> <p>Interior support @C, M<sub>C</sub> = <math>\frac{-FL}{12} = \frac{-792.52 \text{ kN} \times 5 \text{ m}}{12} = -330.2 \text{ kNm}</math></p> <p>Shear forces:</p> <p>V<sub>A</sub> = 0.45 F = 0.45 x 792.52 kN = 356.6 kN  V<sub>B</sub> = 0.6 F = 0.6 x 792.52 kN = 475.5 kN  V<sub>C</sub> = 0.55 F = 0.55 x 792.52 kN = 435.9 kN</p> <p><b>Design for Flexure</b></p> <p><b>Midspan (at F)</b></p> <p>Tension bar size: Ø = 25 mm</p>
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	Link size: $\phi_v = 10 \text{ mm}$
4.3.1.5	<p>Effective depth: <math>d_F = h - \text{cover} - \frac{\phi}{2}</math>  <math>= 600 - 30 - 10 - \frac{25}{2} = 547.5 \text{ mm}</math></p> <p>Effective flange width: <math>b_{\text{eff}} = b_w + \frac{0.7L}{5} = 0.3 + \frac{0.7 \times 5}{5} = 1 \text{ m}</math>  <math>b_{\text{eff}} = 1 \text{ m} &lt; s_b = 8.0 \text{ m } \textbf{OK}</math></p> <p>Finding reinforcement, assuming <math>s &lt; h_f</math>:  At midspan, assume <math>\beta_b = 1.0</math></p>
4.3.3.4.1	<p><math>K' = 0.402 (\beta_b - 0.4) - 0.18 (\beta_b - 0.4)^2</math>  <math>= 0.402 (1 - 0.4) - 0.18 (1 - 0.4)^2 = 0.176</math></p> <p><math>K' = 0.176 &gt; 0.156</math>, therefore use <math>K' = 0.156</math></p> <p><math>K = \frac{M_F}{b_{\text{eff}} \times d_F^2 \times f_{cu}} = \frac{360.2}{1 \times (0.5475)^2 \times (25 \times 10^3)} = 0.048</math></p> <p><math>K = 0.048 &lt; K' = 0.156</math>, compression reinforcement is not required.</p> <p><math>z = d_F \left( 0.5 + \sqrt{0.25 - \frac{K}{0.9}} \right) = d_F \left( 0.5 + \sqrt{0.25 - \frac{0.048}{0.9}} \right) = 0.943 d_F</math></p> <p><math>z = 0.943 d_F &lt; z = 0.95d</math>, therefore use <math>z = 0.943 d_F</math>.  <math>z = 0.943 d_F = 0.943 \times 547.5 \text{ mm} = 516.3 \text{ mm}</math></p> <p><math>s = 2(d_F - z) = 2(547.5 \text{ mm} - 516.3 \text{ mm}) = 62.4 \text{ mm} &lt; h_f = 250 \text{ mm } \textbf{OK}</math></p> <p><math>A_{s.\text{req.F}} = \frac{M_F}{0.87 \times f_y \times z} = \frac{360.2 \times 10^6}{0.87 \times 450 \times 516.3} = 1782 \text{ mm}^2</math></p> <p><b>Therefore, Provide 3Y25 and 1Y20</b></p> <p><math>A_{s.\text{prov.F}} = 1473 \text{ mm}^2 + 314.2 \text{ mm}^2 = 1787 \text{ mm}^2</math></p> <p>The actual depth calculated to the centroid of the reinforcement will be slightly greater than assumed, OK.</p> <p>Minimum reinforcement:  <math>\frac{b_w}{b_{\text{eff}}} = \frac{300}{1000} = 0.3 &lt; 0.4</math></p> <p>Therefore, <math>\frac{100 \times A_{s.\text{prov.F}}}{b_w h} = \frac{100 \times 1787}{300 \times 600} = 0.99 &gt; 0.18 \text{ } \textbf{OK}</math></p> <p>Maximum area of reinforcement = 4%, OK</p>
Table 23	

	<p>Maximum horizontal spacing of bars:  <math>\frac{1}{2}[b_w - 2\text{cover} - 2\emptyset_v - (3 \times 25 \text{ mm}) - 20 \text{ mm}] = 62.5 \text{ mm}</math></p> <p><math>62.5 \text{ mm} &lt; h_{\text{agg}} + 5 \text{ mm} = 31.5 \text{ mm} \quad \text{OK}</math></p> <p>Maximum spacing between bars ( assuming 0% redistribution):  <math>s_{\max} = 170 \text{ mm} \quad \text{OK}</math></p>
Table 25	<p><b>Support B</b></p> <p>Tension bar size: <math>\emptyset = 25 \text{ mm}</math>  Link size: <math>\emptyset_v = 10 \text{ mm}</math></p> <p>Assuming that the tension bars will probably be placed in two layers to fit into the web.</p> <p>Effective depth: <math>d_B = h - \text{cover} - \emptyset_v - \emptyset</math>  <math>= 600 - 30 - 10 - 25 = 535 \text{ mm}</math></p> <p>Finding reinforcement, noting that <math>b = b_w</math>:</p> <p>At the support, assume <math>\beta_b = 0.9</math></p>
4.3.1.5	
4.3.3.4.1	<p><math>K' = 0.402(\beta_b - 0.4) - 0.18(\beta_b - 0.4)^2</math>  <math>= 0.402(0.9 - 0.4) - 0.18(0.9 - 0.4)^2 = 0.156</math></p> <p><math>K = \frac{M_B}{b_w \times d_B^2 \times f_{cu}} = \frac{440.3}{0.3 \times (0.535)^2 \times (25 \times 10^3)} = 0.205</math></p> <p><math>K = 0.205 &gt; K' = 0.156</math>, compression reinforcement is required.</p> <p><math>d' = \text{cover} + \emptyset_v + \frac{\emptyset}{2} = 30 + 10 + \frac{25}{2} = 52.5 \text{ mm}</math></p> <p>Yield stress for compression reinforcement:</p> <p><math>f_{yc} = \frac{f_y}{1.15 + \frac{f_y}{2000 \text{ MPa}}} = \frac{450 \text{ MPa}}{1.15 + \frac{450 \text{ MPa}}{2000 \text{ MPa}}} = 327.3 \text{ MPa}</math></p> <p><math>\frac{d'}{d_B} = \frac{52.5}{535} = 0.098 &lt; (\beta_b - 0.4)(1 - \frac{f_{yc}}{E_s \times \varepsilon_{cu}}) = 0.266</math>, the compression will yield at ultimate.</p> <p>Internal lever arm:</p> <p><math>z = d_B \left( 0.5 + \sqrt{0.25 - \frac{K'}{0.9}} \right) = d_B \left( 0.5 + \sqrt{0.25 - \frac{0.156}{0.9}} \right) = 0.777 d_B</math></p> <p><math>z = 0.777 \times 535 \text{ mm} = 415.7 \text{ mm}</math></p>
Figure 2	
4.3.3.4.1	

4.3.3.4.1	<p>Required area of compression reinforcement:</p> $A'_{s,\text{req},B} = \frac{(K-K')f_{cu}b_w d_B^2}{f_{yc} \times (d_B - d')} = \frac{(0.205-0.156) \times 25 \times 300 \times (535)^2}{327.3 \times (535-52.5)} = 666 \text{ mm}^2$ <p>Required area of tension reinforcement:</p> $A_{s,\text{req},B} = \frac{K' f_{cu} b_w d_B^2}{0.87 f_y z} + \frac{f_{yc}}{0.87 f_y} A'_{s,\text{req},B}$ $= \frac{0.156 \times 25 \times 300 \times (535)^2}{0.87 \times 450 \times 415.7} + \frac{327.3}{0.87 \times 450} \times 666 = 2614 \text{ mm}^2$ <p>For compression reinforcement at the support the tension reinforcement at midspan is extended into the support.</p> <p><b>Therefore, Provide 3Y25 and 1Y20</b>      <math>A'_{s,\text{prov},B} = 1787 \text{ mm}^2</math></p> <p>Tension reinforcement:  <b>Provide 4Y25 and 3Y20</b>  <math>A_{s,\text{prov},B} = 1963 \text{ mm}^2 + 942 \text{ mm}^2 = 2905 \text{ mm}^2</math></p> <p>The actual depth calculated to the centroid of the reinforcement will be slightly greater than assumed, OK.</p> <p>Minimum reinforcement:</p> <p>Table 23</p> <p>Tension: <math>\frac{100 \times A_{s,\text{prov},B}}{b_w h} = \frac{100 \times 2905}{300 \times 600} = 1.61 &gt; 0.26 \text{ OK}</math></p> <p>Compression: <math>\frac{100 \times A'_{s,\text{prov},B}}{b_w h} = \frac{100 \times 1787}{300 \times 600} = 0.99 &gt; 0.20 \text{ OK}</math></p> <p>Maximum area of reinforcement = 4%, OK</p> <p>Maximum horizontal spacing of bars in top beam:  <math>\frac{1}{2}(b_w - 2\text{cover} - 2\emptyset_v - (3 \times 25 \text{ mm}) - 20 \text{ mm}) = 62.5 \text{ mm}</math></p> <p><math>62.5 \text{ mm} &lt; h_{agg} + 5 \text{ mm} = 31.5 \text{ mm} \text{ OK}</math></p> <p>Care should be taken here to compact the concrete during placing. There is not enough space in the top beam to allow for the standard 75 mm diameter vibrator to pass between reinforcements.</p> <p>Table 25</p> <p>Maximum spacing between bars (assuming 10% redistribution):  <math>s_{\max} = 155 \text{ mm} \text{ OK}</math></p> <p>The reinforcement at support B can be curtailed:  Anchorage curtailment length the greatest of 0.25 L = 1250 mm and 45 Ø = 45 x 25 mm = 1125 mm</p>
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4.11.7.2.3 (a)	<p>Say <math>L_{ac,B} = 1350</math> mm</p> <p>20% of the reinforcement at the support must extend into the span:  <math>20\% A_{s,req,B} = 0.2 \times 2614 \text{ mm}^2 = 523 \text{ mm}^2</math>      Extend 2Y20 (<math>628 \text{ mm}^2</math>) of the top reinforcement into the span</p> <p><b>Support C</b></p> <p>Tension bar size: <math>\emptyset = 25 \text{ mm}</math>      Link size: <math>\emptyset_v = 10 \text{ mm}</math></p> <p>Finding reinforcement, assuming <math>s &lt; h_f</math> :      Assuming that the tension bars will probably be placed in two layers to fit into the web.</p> <p>Effective depth: <math>d_c = h - \text{cover} - \emptyset_v - \emptyset</math>  <math>= 600 - 30 - 10 - 25 = 535 \text{ mm}</math></p> <p>Finding reinforcement, noting that <math>b = b_w</math> :</p> <p>4.3.1.5 At the support, assume <math>\beta_b = 0.9</math></p> <p><math>K' = 0.156</math></p> <p>4.3.3.4.1 <math>K = \frac{M_c}{b_w \times d_c^2 \times f_{cu}} = \frac{330.2}{0.3 \times (0.535)^2 \times (25 \times 10^3)} = 0.154</math></p> <p><math>K = 0.154 &lt; K' = 0.156</math>, compression reinforcement is not required.</p> $z = d_c \left( 0.5 + \sqrt{0.25 - \frac{K}{0.9}} \right) = d_c \left( 0.5 + \sqrt{0.25 - \frac{0.154}{0.9}} \right) = 0.781 d_c$ <p><math>z = 0.781 d_c &lt; z = 0.95d</math>, therefore use <math>z = 0.781 d_c</math>.  <math>z = 0.781 d_c = 0.781 \times 535 \text{ mm} = 417.8 \text{ mm}</math></p> <p><math>s = 2(d_c - z) = 2(535 \text{ mm} - 417.8 \text{ mm}) = 234.4 \text{ mm} &lt; h_f = 250 \text{ mm } \textbf{OK}</math></p> $A_{s,req,c} = \frac{M_c}{0.87 \times f_y \times z} = \frac{330.2 \times 10^6}{0.87 \times 450 \times 417.8} = 2019 \text{ mm}^2$ <p><b>Therefore, Provide 3Y25 and 2Y20</b></p> <p><math>A_{s,prov,c} = 1473 \text{ mm}^2 + 628 \text{ mm}^2 = 2101 \text{ mm}^2</math></p> <p>The actual depth calculated to the centroid of the reinforcement will be slightly greater than assumed, OK.</p>
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Table 23	<p>Minimum reinforcement:</p> $\frac{b_w}{b_{eff}} = \frac{300}{1000} = 0.3 < 0.4$ <p>Therefore, <math>\frac{100 \times A_{s,prov.c}}{b_w h} = \frac{100 \times 2101}{300 \times 600} = 1.17 &gt; 0.18 \quad \text{OK}</math></p> <p>Maximum area of reinforcement = 4%, <b>OK</b></p> <p>Maximum horizontal spacing of bars:</p> $\frac{1}{2} [b_w - 2\text{cover} - 2\emptyset_v - (3 \times 25 \text{ mm}) - (2 \times 20 \text{ mm})] = 52.5 \text{ mm}$ <p><math>52.5 \text{ mm} &lt; h_{agg} + 5 \text{ mm} = 31.5 \text{ mm} \quad \text{OK}</math></p> <p>Maximum spacing between bars ( assuming 0% redistribution):  <math>s_{max} = 170 \text{ mm} \quad \text{OK}</math></p>
Table 25	<p><b>Minimum transverse reinforcement in flange</b></p> <p>To transfer shear in flange: <math>A_{s,trans} = \frac{0.15}{100} h_f (1\text{m}) = 375 \text{ mm}^2</math></p> <p><u>Provide Y10@175 mm c/c</u></p> <p><math>A_{s,trans.prov} = 449 \text{ mm}^2</math> over a length of <math>b_{eff} = 1000 \text{ mm}</math></p>
4.3.4.1.1	<p><b>Design for Shear</b></p> <p><b>Maximum shear</b></p> <p>Maximum shear force will occur at the face of support B.</p> $V_{sup.B} = V_B - w_u \cdot \frac{b_{sup}}{2} = 475.5 - 159.50 \times \frac{0.3}{2} = 451.6 \text{ kN}$ $V_{max} = \frac{V_{sup.B}}{b_w d_B} = \frac{451.6 \times 10^3}{300 \times 535} = 2.81 \text{ MPa}$ $V_{max} = 2.81 \text{ MPa} < 0.75 \sqrt{f_{cu}} = 3.75 \text{ MPa} \text{ and } 4.75 \text{ MPa}, \text{OK}$ <p><b>Nominal shear reinforcement</b></p> <p>Nominal shear reinforcement to be provided for <math>f_{sv} = 450 \text{ MPa}</math></p> $\left( \frac{A_{sv}}{s_v} \right)_{min} = 0.0012 b_w = 0.36 \frac{\text{mm}^2}{\text{mm}}$ <p>For two legs of a Y10 link <math>A_{sv,min} = 224 \text{ mm}^2</math></p> <p>Maximum spacing is: <math>0.75d_f = 0.75 \times 547.5 \text{ mm} = 410.6 \text{ mm}</math></p> <p>Selecting a spacing of <math>s_{v,min} = 350 \text{ mm}</math></p>
4.11.4.5.3	

$$\left(\frac{A_{sv}}{s_v}\right)_{min} = \frac{143 \text{ mm}^2}{350 \text{ mm}} = 0.41 \frac{\text{mm}^2}{\text{mm}}, \text{OK}$$

**Provide Y10 links @350 mm c/c.**

Assuming that nominal links will always be placed in areas of sagging bending, reinforcement at midspan is considered.

4.3.4.1.2  $\rho_F = \frac{100 \times A_{s,prov,F}}{b_w d_F} = \frac{100 \times 1787}{300 \times 547.5} = 1.09 < 3, \text{OK}$

$$f_{cu} = 25 \text{ MPa} < 40 \text{ MPa}, \text{OK}$$

Shear resistance of concrete:

$$V_{c,F} = \frac{0.75 \text{ MPa}}{\gamma_{mv}} \cdot \left[ \rho_F \left( \frac{f_{cu}}{25 \text{ MPa}} \right) \right]^{\frac{1}{3}} \cdot \left( \frac{400 \text{ mm}}{d_F} \right)^{\frac{1}{4}}$$

$$= \frac{0.75 \text{ MPa}}{1.4} \cdot \left[ 1.09 \left( \frac{25 \text{ MPa}}{25 \text{ MPa}} \right) \right]^{\frac{1}{3}} \cdot \left( \frac{400 \text{ mm}}{547.5 \text{ mm}} \right)^{\frac{1}{4}} = 0.51 \text{ MPa}$$

The resistance given by the nominal shear reinforcement is:

$$V_{s,min} = \frac{A_{sv,min}}{s_{v,min}} \cdot \frac{0.87 f_{yv}}{b_w} = \frac{224}{350} \times \frac{0.87 \times 450}{300} = 0.84 \text{ MPa}$$

$$V_n = V_{s,min} + V_{c,F} = 1.35 \text{ MPa}$$

$$V_n = v_n b_w d_F = 1.35 \text{ MPa} \times 300 \text{ mm} \times 547.5 \text{ mm} \times 10^{-3} = 221.7 \text{ kN}$$

### Shear reinforcement at support A

Considering a critical section at a distance  $d_F = 547.5 \text{ mm}$  from the face of the support.

4.3.4.1.2  $V_{sup,A} = V_A - w_u \cdot \frac{b_{sup}}{2} = 356.6 - 159.5 \times \frac{0.3}{2} = 332.7 \text{ kN}$

$$V = V_{sup,A} - w_u \cdot d_F = 332.7 - 159.5 \times 0.5475 = 246.4 \text{ kN}$$

$$v = \frac{V}{b_w d_F} = \frac{246.4 \times 10^3}{300 \times 547.5} = 1.5 \text{ MPa}$$

Tension reinforcement is not curtailed at support A, the full area will be used:

$$v_{c,F} = 0.51 \text{ MPa}$$

4.3.4.1.3 Required  $\frac{A_{sv}}{s_v} = \frac{(v - v_{c,F}) \cdot b_w}{0.87 f_{yv}} = \frac{(1.5 - 0.51) \times 300}{0.87 \times 450} = 0.759 \frac{\text{mm}^2}{\text{mm}}$

For two legs of a Y10 link  $A_{sv} = 224 \text{ mm}^2$

$$\text{Required spacing } s_v = \frac{0.87 f_{yv} \cdot A_{sv}}{(v - v_{c,F}) \cdot b_w} = \frac{0.87 \times 450 \times 224}{(1.5 - 0.51) \times 300} = 295 \text{ mm}$$

Say  $s_v = 250$  mm.

$$\text{Provide Y10 links @250 mm c/c } \frac{A_{sv}}{s_v} = \frac{224 \text{ mm}^2}{250 \text{ m}} = 0.896 \frac{\text{mm}^2}{\text{mm}}, \text{OK}$$

Maximum spacing is:  $0.75d_f = 0.75 \times 547.5 \text{ mm} = 410.6 \text{ mm}$  OK

Extend this reinforcement the following distance:

$$s = \frac{V_{sup.A} - V_n}{w_u} = \frac{332.7 - 221.7}{159.5} = 696 \text{ mm from the face of the support}$$

### **Shear reinforcement at support B**

Considering a critical section at a distance  $d_B = 535$  mm from the face of the support.

4.3.4.1.2

$$V_{sup.B} = V_B - w_u \cdot \frac{b_{sup}}{2} = 475.5 - 159.5 \times \frac{0.3}{2} = 451.6 \text{ kN}$$

$$V = V_{sup.B} - w_u \cdot d_B = 451.6 - 159.5 \times 0.535 = 366.3 \text{ kN}$$

$$v = \frac{V}{b_w d_B} = \frac{366.3 \times 10^3}{300 \times 535} = 2.282 \text{ MPa}$$

4.3.4.1.3 Shear resistance of the concrete:

$$\rho_B = \frac{100 \times A_{s.prov.B}}{b_w d_B} = \frac{100 \times 2905}{300 \times 535} = 1.81 < 3, \text{OK}$$

All reinforcement in this critical section extend at a distance  $d$  beyond the critical section.

$$v_{c.B} = \frac{0.75 \text{ MPa}}{\gamma_{mv}} \cdot \left[ \rho_B \left( \frac{f_{cu}}{25 \text{ MPa}} \right) \right]^{\frac{1}{3}} \cdot \left( \frac{400 \text{ mm}}{d_B} \right)^{\frac{1}{4}}$$

$$= \frac{0.75 \text{ MPa}}{1.4} \cdot \left[ 1.81 \left( \frac{25 \text{ MPa}}{25 \text{ MPa}} \right) \right]^{\frac{1}{3}} \cdot \left( \frac{400 \text{ mm}}{535 \text{ mm}} \right)^{\frac{1}{4}} = 0.607 \text{ MPa}$$

$$\text{Required } \frac{A_{sv}}{s_v} = \frac{(v - v_{c.B}) \cdot b_w}{0.87 f_{yv}} = \frac{(2.282 - 0.607) \times 300}{0.87 \times 450} = 1.284 \frac{\text{mm}^2}{\text{mm}}$$

For Y8 link in pairs (4 legs)  $A_{sv} = 449 \text{ mm}^2$

$$\text{Required spacing } s_v = \frac{0.87 f_{yv} \cdot A_{sv}}{(v - v_{c.B}) \cdot b_w} = \frac{0.87 \times 450 \times 449}{(2.282 - 0.607) \times 300} = 350 \text{ mm}$$

Say  $s_v = 300$  mm.

Provide Y10 links @300 mm c/c  $\frac{A_{sv}}{s_v} = \frac{449 \text{ mm}^2}{300 \text{ m}} = 1.497 \frac{\text{mm}^2}{\text{mm}}$ , OK

Maximum spacing is:  $0.75d_B = 0.75 \times 535 \text{ mm} = 401 \text{ mm}$  OK

Extend this reinforcement the following distance:

$$s = \frac{V_{sup.B} - V_n}{w_u} = \frac{451.6 - 221.7}{159.5} = 1441 \text{ mm from the face of the support}$$

A more economical alternative would be to consider a further critical section (G) at a distance  $L_{ac.B} - d_B = 1350 \text{ mm} - 535 \text{ mm} = 815 \text{ mm}$ .

$$V = V_{sup.B} - w_u \cdot (L_{ac.B} - d_B) = 451.6 - 159.5 \times 0.815 = 321.6 \text{ kN}$$

$$v = \frac{V}{b_w d_B} = \frac{321.6 \times 10^3}{300 \times 535} = 2.004 \text{ MPa}$$

Shear resistance of the concrete:

$$A_{s,G} = 628 \text{ mm}^2 (2Y20 bars)$$

$$v_{c,G} = \frac{0.75 \text{ MPa}}{\gamma_{mv}} \cdot \left[ \left( \frac{100 \cdot A_{s,G}}{b_w d_B} \right) \left( \frac{f_{cu}}{25 \text{ MPa}} \right) \right]^{\frac{1}{3}} \cdot \left( \frac{400 \text{ mm}}{d_B} \right)^{\frac{1}{4}}$$

$$= \frac{0.75 \text{ MPa}}{1.4} \cdot \left[ \left( \frac{100 \times 628}{300 \times 535} \right) \left( \frac{25 \text{ MPa}}{25 \text{ MPa}} \right) \right]^{\frac{1}{3}} \cdot \left( \frac{400 \text{ mm}}{535 \text{ mm}} \right)^{\frac{1}{4}} = 0.364 \text{ MPa}$$

$$\text{Required } \frac{A_{sv}}{s_v} = \frac{(v - v_{c,G}) \cdot b_w}{0.87 f_{yv}} = \frac{(2.004 - 0.364) \times 300}{0.87 \times 450} = 1.257 \frac{\text{mm}^2}{\text{mm}}$$

For 2 legs of a Y10 link in pairs  $A_{sv} = 224 \text{ mm}^2$

$$\text{Required spacing } s_v = \frac{0.87 f_{yv} \cdot A_{sv}}{(v - v_{c,G}) \cdot b_w} = \frac{0.87 \times 450 \times 224}{(2.004 - 0.364) \times 300} = 178 \text{ mm}$$

Say  $s_v = 175 \text{ mm}$ .

Provide Y10 links @100 mm c/c  $\frac{A_{sv}}{s_v} = \frac{224 \text{ mm}^2}{175 \text{ m}} = 1.28 \frac{\text{mm}^2}{\text{mm}}$ , OK

Between 1.441 m and  $(L_{ac.B} - d_B) = 0.815 \text{ m}$  from the face of the support.

### Shear reinforcement at support C

Considering a critical section at a distance  $d_C = 535 \text{ mm}$  from the face of the support.

$$V_{sup.C} = V_C - w_u \cdot \frac{b_{sup}}{2} = 435.9 - 159.5 \times \frac{0.3}{2} = 412 \text{ kN}$$

$$V = V_{\text{sup.C}} - w_u \cdot d_c = 412 - 159.5 \times 0.535 = 326.7 \text{ kN}$$

$$v = \frac{V}{b_w d_c} = \frac{326.7 \times 10^3}{300 \times 535} = 2.036 \text{ MPa}$$

Tension reinforcement is not curtailed at support C, the full area will be used:

$$v_{c,F} = 0.51 \text{ MPa}$$

$$\text{Required } \frac{A_{sv}}{s_v} = \frac{(v - v_{c,F}) \cdot b_w}{0.87 f_{yv}} = \frac{(2.036 - 0.51) \times 300}{0.87 \times 450} = 1.17 \frac{\text{mm}^2}{\text{mm}}$$

For two legs of a Y10 link  $A_{sv} = 224 \text{ mm}^2$

$$\text{Required spacing } s_v = \frac{0.87 f_{yv} \cdot A_{sv}}{(v - v_{c,F}) \cdot b_w} = \frac{0.87 \times 450 \times 224}{(2.036 - 0.51) \times 300} = 192 \text{ mm}$$

Say  $s_v = 150 \text{ mm}$ .

$$\text{Provide Y10 links @150 mm c/c } \frac{A_{sv}}{s_v} = \frac{224 \text{ mm}^2}{150 \text{ mm}} = 1.49 \frac{\text{mm}^2}{\text{mm}}, \text{OK}$$

Maximum spacing is:  $0.75d_c = 0.75 \times 535 \text{ mm} = 401.2 \text{ mm}$  OK

Extend this reinforcement the following distance:

$$s = \frac{V_{\text{sup.C}} - V_n}{w_u} = \frac{412 - 221.7}{159.5} = 1193 \text{ mm from the face of the support}$$

### ***Confinement of compression reinforcement***

At support B:

Smallest compression bar is  $\emptyset_{min} = 20 \text{ mm}$

Maximum spacing of links  $s_{v,max} = 12 \times \emptyset_{min} = 240 \text{ mm}$ , OK all links spacings are less

Largest compression bar is  $\emptyset_{max} = 25 \text{ mm}$

Minimum link size is  $\frac{\emptyset_{max}}{4} = 6.3 \text{ mm}$ , OK all links diameter are greater than this

### **Check Span-Effective Depth Ratio**

#### **Basic L/d ratio**

For a beam with one end continuous:

$$\left(\frac{L}{d}\right)_{basic} = 24$$

Table 10

	Since the span is less than 10m, the L/d ratio will not be adjusted.
	<b><i>Modification factor for tension reinforcement</i></b>
4.3.6.3.1	Assuming $\beta_b = 1.0$
Table 11	$f_s = 0.87 f_y \cdot \left(\frac{1.1+1.0}{1.2+1.6}\right) \cdot \left(\frac{A_{s.req.F}}{A_{s.prov.F}}\right) \cdot \frac{1}{\beta_b}$ $= 0.87 \times 450 \cdot \left(\frac{1.1+1.0}{1.2+1.6}\right) \cdot \left(\frac{1782}{1787}\right) \cdot \frac{1}{1} = 292.8 \text{ MPa}$ <p>Modification factor for tension reinforcement:</p> $MF_{AS} = 0.55 + \frac{477 \text{ MPa} - f_s}{120 \cdot \left( 0.9 \text{ MPa} + \frac{M_F}{b_{eff} \cdot d_F} \right)}$ $= 0.55 + \frac{477 \text{ MPa} - 292.8 \text{ MPa}}{120 \cdot \left( 0.9 \text{ MPa} + \frac{360.2 \times 10^6}{1000 \times (547.5)^2} \right)} = 1.28$
4.3.6.3.2	<b><i>Modification factor for compression reinforcement</i></b>
Table 12	$A'_{prov.F} = 628 \text{ mm}^2$ (2Y20 bars) <p>For a section at midspan <math>\rho' = \frac{100 \times A'_{s.prov.F}}{b_{eff} d_F} = \frac{100 \times 628}{1000 \times 547.5} = 0.115</math></p> <p>Modification factor for compression reinforcement:</p> $MF_{A'S} = 1 + \frac{\rho'}{3 + \rho'} = 1.037$ <p><b>Check L/d ratio:</b></p> <p>Maximum allowable L/d ratio:</p> $L\_over\_d\_allow = MF_{AS} \times MF_{A'S} \times \left(\frac{L}{d}\right)_{basic} = 31.86$ <p>Provided L/d</p> $L\_over\_d\_prov = \frac{L}{d_F} = \frac{5000}{547.5} = 9.13$ $L\_over\_d\_prov = 9.13 < L\_over\_d\_allow = 31.86 \text{ OK}$

- ❖ Following above design, a bar bending schedule was generated and is as displayed under the appendix B

#### 4.3 Column Design

Using the updated loads derived from both gravity and lateral load combinations, the column design was carried out comprehensively. Slenderness limits were checked in accordance with code standards. Both longitudinal and transverse reinforcement were appropriately sized and detailed to satisfy strength and serviceability requirements.

For the gridline 2 columns analysed in Phase 1, the structure produced the following result for the column to be the most critical.

**Maximum Vertical Force  $N = 1683.083kN$**

**Moments :  $M_1 = 3.01kNm$  ;  $M_2 = 3.561kNm$**

### Slenderness Classification

**Given :**

Column Size: 300 x 300 mm

Beam Size: 600 x 300 mm

Slab Thickness: 250mm

Reference	Calculations
SABS 0100-1 Table 18  4.7.1.4	<p><b>Major axis ( X-X) Braced</b></p> $L_{ox} = 4500 - 600 = 3900mm$ <p>Condition at top = 1</p> <p>Condition at bottom = 3 {<b>Assumed that the pad footing is not designed to resist any moment</b>}</p> $\beta = 0.9 \quad \therefore L_{ex} = 0.9(3900) = 3510mm$ $\text{Limit} = 17 - \frac{7M_1}{M_2}$ $= 17 - \frac{7(3.01)}{3.561} = 11.08$ $\frac{L_{ex}}{h} = \frac{3510}{300} = 11.7 > 11.08 \quad \therefore \text{Slender}$ <p><b>Minor Axis (Y-Y) -Unbraced</b></p> $L_{oy} = 4500 - 600 = 3900mm$ <p>Condition at top = 1</p> <p>Condition Bottom = 3 (Previously assumed)</p> $\beta = 1.6 \quad \therefore L_{ey} = 1.6(3900) = 6240mm$
Table 19	

4.7.1.4	<p>Limit = 10</p> $\frac{L_{eY}}{h} = \frac{6240}{300} = 20.8 > 10 \quad \therefore \text{Slender}$ <p><b>Check slenderness ultimate Limit:</b></p> $l_o < 60b = 60 \times 0.3 = 18m$ $b \geq 0.25h = 75mm \quad \therefore \text{OK!!}$
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### Design Moment

Reference	Calculations
4.7.3.1, Eqn(12)	<p><b>X-AXIS (Braced)</b></p> $\beta_a = \frac{(\text{slenderness ratio})^2}{2000}$ $h = 300mm$ $K = 1.0 \text{ (assumed for initial calculations)}$ $a_u = \beta_a K h = (0.068)(1.0)(300) = 20.4mm$ $M_{add} = N_{a_u} = (1699.5)(0.0204) = 34.669 \text{ kNm}$
4.7.3.2.1	$M_i = 0.4M_1 + 0.6M_2$ $= 0.4(0) + 0.6(9.551) = 5.731 \text{ kNm}$ $0.4M_2 = 0.4(9.551) = 3.820 \text{ kNm}$ <p>a) <math>M_2 = 9.551 \text{ kNm}</math></p> <p>b) <math>M_i + M_{add} = 5.731 + 34.669 = \mathbf{40.4 \text{ kNm}}</math></p> <p>c) <math>e_{min} = 0.05h = 0.05(300) = 15mm (&lt; 20)</math></p> <p><math>e_{min}N = (0.015)(1699.5) = 25.493 \text{ kNm}</math></p> <div style="border: 1px solid black; padding: 5px; text-align: center;"><b><math>\mathbf{M_{design \ xx} = 40.4 \text{ kNm}}</math></b></div> <p><b>Y-AXIS (Unbraced)</b></p>
4.7.3.1 Eqn(12)	$\beta_a = \frac{(\text{slenderness ratio})^2}{2000}$ $h = 300mm$

	<p><math>K = 1.0</math> (assumed for initial calculations)</p> <p><math>a_u = \beta_a Kh = (0.21632)(1.0)(300) = 64.896 \text{ mm}</math></p> <p><math>M_{add} = N_{a_u} = (1699.5)(0.06489) = 110.281 \text{ kNm}</math></p> <p><math>M_i = 0.4M_1 + 0.6M_2</math></p> <p><math>M_i = 0.4(0) + 0.6(237.468) = 142.481 \text{ kNm}</math></p> <p>4.7.2.3</p> <p>a) <math>M_2 = 237.468 \text{ kNm}</math></p> <p>b) <math>M_i + M_{add} = 142.481 + 110.281 = 252.762 \text{ kNm}</math></p> <p>c) <math>e_{min} = 0.05h = 0.05(300) = 15 \text{ mm} (&lt; 20)</math></p> <p><math>e_{min}N = 0.015(1699.5) = 25.49 \text{ kNm}</math></p> <p style="border: 1px solid black; padding: 5px;"><b><math>M_{design\ yy} = 252.762 \text{ kNm}</math></b></p>
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## Reinforcement Design

References	Calculations
Table 21 SANS0100	<p><math>N = 1699.5 \text{ kN}</math></p> <p><math>M_{x\ top} = 9.551 \text{ kNm}</math></p> <p><math>M_{x\ bottom} = 0 \text{ kNm}</math></p> <p><math>M_{y\ top} = 237.468 \text{ kNm}</math></p> <p><math>M_{y\ bottom} = 0 \text{ kNm}</math></p> <p>Bi-Axial Bending with:</p> <p><i>Design as for the short column</i> <math>\begin{cases} N = 1699.5 \text{ kN} \\ M_{xx} = 40.4 \text{ kNm} \\ M_{yy} = 252.762 \text{ kNm} \end{cases}</math></p> <p>DESIGN FOR UNI-AXIAL BENDING</p> <p><math>\frac{M_x}{h} = \frac{40.4}{300} = 0.13</math></p> <p><math>\frac{M_y}{b} = \frac{252.762}{300} = 0.84 &gt; 0.13</math></p> <p><math>\therefore</math> Design for <math>y - \text{axis bending}</math></p> <p>Enhance moment for uniaxial design</p> <p><math>\frac{N}{bhf_{cu}} = \frac{1699.5 \times 10^3}{(300)(300)(30)} = 0.63</math></p> <p><math>\therefore \beta_b = 0.3</math></p>

4.7.4.4

$$M'_y = M_y + \beta_b \frac{b}{h} M_x$$

$$= 252.762 + (0.3) \left( \frac{300}{300} \right) (40.4) = 264.882 kNm$$

$$\frac{N}{bh f_{cu}} = \frac{1699.5 \times 10^3}{(300)(300)(30)} = 0.63$$

$$\frac{M'_y}{bh f_{cu}} = \frac{264.882 \times 10^6}{(300)(300)(30)} = 0.327$$

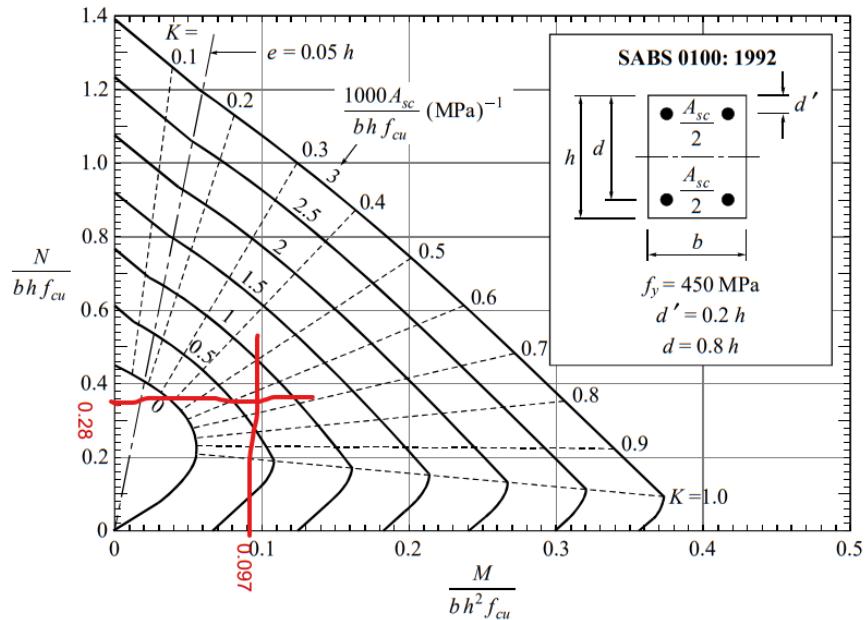


Figure 7: Chat from Robert and Marshal

For 300 × 300 column is not adequate

$$\begin{cases} \frac{N}{bh f_{cu}} = 0.63 \\ \frac{M'_y}{bh f_{cu}} = 0.327 \end{cases}$$

Try (450 × 450)

$$\begin{cases} \frac{N}{bh f_{cu}} = 0.28 \\ \frac{M'_y}{bh f_{cu}} = 0.097 \\ \frac{1000 A_{sc}}{bh f_{cu}} = 0.65 \end{cases}$$

Min.  $A_{sc} = 0.4\% \therefore OK$ Max.  $A_{sc} = 6\% \therefore OK$ 

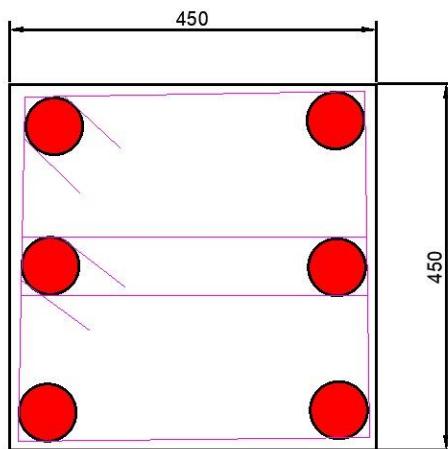
$$A_{sc} = \frac{0.65(450)(450)(30)}{1000} = 3290.625 mm^2$$

Provide 6Y32 bars =  $4825 mm^2 > 3290.625 mm^2 \therefore OK$ 

Links as per SANS

$$\left. \begin{array}{l} \emptyset > \frac{32}{4} = 8\text{mm} \\ \text{--- --- ---} \\ \text{Spacing} < 12 \times 32 = 384\text{mm} \end{array} \right\} \text{Provide R10@300 stirrups}$$

$$K = 0.65 < 1 \text{ (assumed)} \therefore Ok$$



$$\text{Dist. To unrestrained bar} = \frac{450 - 90 - 90 - 32}{1} \\ = 236 \text{ mm} (> 150 \therefore \text{additional restraint req})$$

Following above design, a bar bending schedule was generated and is as displayed under the appendix

## 5. Discussion

The structural analysis and design process successfully demonstrated the integration of theoretical and practical design principles in accordance with SANS 10100 and SANS 10160. Both hand calculations and finite element (FE) analysis in Prokon produced consistent results, confirming the reliability of the modelling approach. However, in throughout comparison between hand calculations and prokon, it could be observed that the results obtained from hand calculations were over designed, which although it is safe and reliable, it is not cost effective. The inclusion of two perimeter shear walls proved effective in improving the building's lateral stiffness, reducing storey drift, and enhancing overall stability under wind and seismic actions. Material selection, load combinations, and reinforcement detailing were all aligned with code requirements to ensure safety and serviceability. Minor differences observed between FE and hand results were attributed to simplifications in manual assumptions and differences in load application methods. Overall, the design achieved the intended objectives of strength, stability, and constructability.

## 6. Conclusion and recommendations

The project achieved its goal of designing a safe and efficient reinforced concrete structure capable of withstanding combined gravity and lateral loads. The slab, beams, and columns all satisfied the ultimate and serviceability limit state requirements, and the reinforcement layouts were optimized to ensure practicality in construction.

For future improvement, it is recommended to perform a more detailed foundation design to ensure full load transfer to the ground and to include long-term checks for deflection and cracking. It would also be beneficial to run additional simulations using different software or load scenarios to compare results and improve accuracy. Lastly, maintaining close coordination between analysis, detailing, and construction stages will help reduce errors and improve overall project quality.

## 7. Reflection

This project provided a meaningful learning experience by combining theoretical understanding with practical application. Throughout the process, I developed a deeper appreciation of how structural elements such as slabs, beams, and columns connect to form a stable system capable of resisting gravity and lateral forces. Using Prokon for the finite element modelling was a challenging, because the concept of 3D modelling was new, but it allowed me to visualize how loads are distributed and how stiffness assumptions influence the overall behaviour of the building.

The process also taught me the importance of verifying computer-based results with manual calculations. At times, discrepancies between the two methods required revisiting assumptions and adjusting load cases, which helped strengthen my problem-solving and critical thinking skills. I learned that accuracy in structural design does not only depend on software outputs, but also on understanding the reasoning behind each step and applying sound engineering judgement.

Additionally, working with South African design codes (SANS 10100 and SANS 10160) helped me gain confidence in applying local standards correctly to a real-life situation and interpreting code. It also showed me how design codes need to be consistently used to justify every assumption made.

Working with the group members have been an good experience, as the was a good communication an arrangement among us, making the learning experience not stressful.

Overall, this project has improved my technical knowledge, time management, and analytical abilities. More importantly, it reinforced the responsibility that comes with being a civil engineer to design safe, practical, and sustainable structures while upholding integrity and ethical decision. Making in every stage of the design process.

## 8. Reference

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## 9. Appendix