Experiment Simulation <u>CLARA</u> GPT Covariance Matrix Setup Optics Match beam divergence (obtain function to optimise the quad 1 and 2 strengths that produce beam with waist at reconstruction point (beam approximately round and convenient size at the camera) Performing a quad scan Quad Currents (strengths) of quads 3, 4, 5 Beam sizes and coupling xy terms obtained from the N cameras Set initial set of quads from the array of quad strengths (quads 3, 4, 5) Determine beam size at observation point for each set of quad strengths Calculate the transfer matrix at the reconstruction point using the optimum quad 1 and 2 strenghts the scan If experiment N< length of the array of quad strengths If simulation Recalculated covariant matrix ∑ at reconstruction point Total array of beam sizes for the set of quad strengths (quads 3, 4, 5 Determine Quad Strengths to be used during the quad scan Split total range into the number of steps strengths to scan for quad 3 For a Quad 3 strength , adjust quad 4 and quad 5 to get the beam at observation point which will be "round" enough and not "too big" or "too small" (as it would appear in the camera). choose number of ste Nscan < number of Data analysis to compute the emittance and optics steps Nscan > number of Calculate the D matrix (3N×10) from the quad strengths (quads 3, 4, 5) and 5 strengths Total set of quad strengths (for quad 3, 4 and 5 Construct the vector of beam sizes from measurements or simulations (obtained at the end of quad scan step), $\sigma_{x,y}$ (3N× 1) Find the covariance matrix Σ'' at reconstruction point from the D matrix and the vector of beam sizes as $\Sigma'' = pseudoinverse(D) \times \sigma_{x, y}$ $S_{matrix} = [0 1 0 0]$ -1 0 0 0 0 0 0 1 Calculate emittances and optics from the eigenvalues and 0 0 -1 0] eigenvectors of $\Sigma'' \cdot S$ matrix