Assignment_3

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Objective Function Minimize TC = 622x11+614x12+630x13+641x21+645x22+649x23These are subject to following constraints supply constraints: x11+x12+x13 >= 100x21+x22+x23 >= 120 demand constraints: x11+x21 >= 80 x12+x22 >= 60 x13+x23 >= 70

Now allare subjected to non-negativity where xij>=0 where i=1,2 and j= 1,2,3

#loading packages

```
library(Matrix)
library("lpSolve")
## Warning: package 'lpSolve' was built under R version 4.1.3
display \leftarrow matrix(c(22,14,30,600,100,
                   16,20,24,625,120,
                  80,60,70,"-","210/220"),ncol=5,nrow=3,byrow=TRUE)
 colnames(display) <- c("Warehouse1","Warehouse2","Warehouse3","Production</pre>
Cost", "Production Capacity")
 rownames(display) <- c("PlantA", "PlantB", "Monthly Demand")</pre>
 display <- as.table(display)</pre>
 display
##
                  Warehouse1 Warehouse2 Warehouse3 Production Cost
## PlantA
                  22
                              14
                                         30
                                                     600
## PlantB
                              20
                                         24
                                                     625
                  16
## Monthly Demand 80
                              60
                                         70
##
                  Production Capacity
## PlantA
                  100
## PlantB
                  120
## Monthly Demand 210/220
  display1 <- matrix(c(622,614,630,0,100,
                   641,645,649,0,120,
                   80,60,70,10,220),ncol=5,nrow=3,byrow=TRUE)
 colnames(display1) <-</pre>
c("Warehouse1","Warehouse2","Warehouse3","Dummy","Production Capacity")
 rownames(display1) <- c("PlantA", "PlantB", "Monthly Demand")</pre>
 display1 <- as.table(display1)</pre>
 display1
##
                  Warehouse1 Warehouse2 Warehouse3 Dummy Production Capacity
## PlantA
                          622
                                     614 630 0
```

## PlantB	641	645	649	0	120
## Monthly Demand	80	60	70	10	220

#The balanced problem will be satisfied by this table. Below is a cost totals matrix that we created.

```
totalcosts <- matrix(c(622,614,630,0,
641,645,649,0),nrow=2, byrow = TRUE)
```

#finding the production capacity in the matrix's row

```
row.rhs <- c(100,120)
row.signs <- rep("<=", 2)
```

#using the double variable 10 at the end to determine the monthly demand.

```
col.rhs <- c(80,60,70,10)
col.signs <- rep(">=", 4)
```

#now we are ready to run LP Transport command

```
lp.transport(totalcosts,"min",row.signs,row.rhs,col.signs,col.rhs)
## Success: the objective function is 132790
```

solution matrix

```
lp.transport(totalcosts, "min", row.signs, row.rhs, col.signs,
col.rhs)$solution

## [,1] [,2] [,3] [,4]
## [1,] 0 60 40 0
## [2,] 80 0 30 10
```

We can conclude from this that Z = \$132790. The results are as follows for each of the variables: 60x12 which is the Warehouse 2 from plant A. 40x13 which is the Warehouse 3 from plant A. 80x21 which is the Warehouse 1 from plant B. 30x23 which is the Warehouse 3 from plant B. and because "10" shows up in the 4th Variable 10x24 is a "throw away variable".

Question 2) We are aware that the number of constants in dual and the number of variables in primal are the same. The primary of the LP is asked in the first question. We shall maximize in the dual because we choose to minimize in the primal. Let's utilize "m" and "n" as our variables for the dual problem.

```
display2 <- as.table(display2)
display2

## W1 W2 W3 Prod Cap Supply (Dual)

## PlantA 622 614 630 100 m_1

## PlantB 641 645 649 120 m_2

## Monthly Demand 80 60 70 220 -

## Demand (Dual) n_1 n_2 n_3 - -</pre>
```

Now we are going to create our objective function based on the constraints from the primal. Later we will use the objective function from the primal to find the constants of the dual.

Maximize Z = 100m1+120m2+80n1+60n2+70n3

This objective function is subject to following constraints:

```
m1+n1 <= 622
m1+n2 <= 614
m1+n3 <= 630
m2+n1 <= 641
m2+n2 <= 645
m2+n3 <= 649
```

These variables were extracted from the linear programming function's transposed primal matrix. Transposing the f.con into the matrix and comparing it to the primal's above constants is an easy way to verify. These are confined where m=1,2 & n=1,2,3 and mk, nl

#Constants of the primal are now the objective function variables.

```
## Success: the objective function is 139120
lp ("max", f.obj, f.con, f.dir, f.rhs)$solution
## [1] 614 633 8 0 16
```

So Z=139,120 dollars and variables are: m1 = 614 which represents plant A m2 = 633 which represents Plant B m1 = 8 which represents Warehouse 1 m3 = 16 which represents Warehouse 3

OBSERVATION

The minimal Z=132790 (Primal) and the maximum Z=139120(Dual). What are we trying to max/min in this problem. We found that we should not be shipping from Plant(A/B) to all three Warehouses. We should be shipping from:

60x12 which is 60 Units from Plant A to Warehouse 2. 40x13 which is 40 Units from Plant A to Warehouse 3. 80x21 which is 60 Units from Plant B to Warehouse 1. 30x23 which is 60 Units from Plant B to Warehouse 3. Now we want to Max the profits from each distribution in respect to capacity.

Question 3)

```
m1 - n1 \le 622
```

then we subtract n1 to the other side to get m1 \leq 622 - n1

To compute that value it would be \$614<=(-8+622) which is true. We would continue to evaluate these equations:

```
m1 <= 622-n1===614<=622-8=614 = TRUE m1 <= 614-n2===614<=614-0=614 = TRUE m1 <= 630-n3===614<=630-16=614 = TRUE m2 <= 641-n1===633<=641-8=633 = TRUE m2 <= 645-n2===633<=645-0=645 = NOT TRUE m2 <= 649-n3===633<=649-16=633 = TRUE
```

#By updating each column, we can test for the shadow price while also learning from the Duality-and-Sensitivity. We change the 100 to 101 and 120 to 121 in our LP Transport.

```
row.rhs1 <- c(101,120)
row.signs1 <- rep("<=", 2)
col.rhs1 <- c(80,60,70,10)
col.signs1 <- rep(">=", 4)
row.rhs2 <- c(100,121)
row.signs2 <- rep("<=", 2)
col.rhs2 <- c(80,60,70,10)
col.signs2 <- rep(">=", 4)
lp.transport(totalcosts, "min", row.signs, row.rhs, col.signs, col.rhs)
## Success: the objective function is 132790
lp.transport(totalcosts, "min", row.signs1, row.rhs1, col.signs1, col.rhs1)
```

```
## Success: the objective function is 132771
lp.transport(totalcosts,"min",row.signs2,row.rhs2,col.signs2,col.rhs2)
## Success: the objective function is 132790
```

Since we are taking the minimum of this particular function, the fact that the number decreases by 19 indicates that the shadow price, which was determined by adding 1 to each of the Plants and the primordial, is 19. Plant B, on the other hand, doesn't have a shadow price. Additionally, we discovered that the dual variable n2 with the relationship Marginal Revenue (MR) = Marginal Cost (MC). Considering the equation that was It was determined that m2 = 645 - n2 = = 633 = 645 - 0 = 645 = NOT TRUE by utilizing m1 - n1 = 622.

```
lp ("max", f.obj, f.con, f.dir, f.rhs)$solution
## [1] 614 633 8 0 16
```

n 2 was = 0.

CONCLUSION: from the primal: 60x12 which is 60 Units from Plant A to Warehouse 2. 40x13 which is 40 Units from Plant A to Warehouse 3. 80x21 which is 60 Units from Plant B to Warehouse 1. 30x23 which is 60 Units from Plant B to Warehouse 3. from the dual We want the MR=MC. Five of the six MR<=MC. The only equation that does not satisfy this requirement is Plant B to Warehouse 2. We can see that from the primal that we will not be shipping any AED device there.