

### EE5103 Computer Control Systems: Homework #3

(Due date: 15/10/2023)

#### Q1. (10 Marks)

Consider the system given by the transfer function

$$H(z) = \frac{z + 0.9}{z^2 - 2.5z + 1}$$

Use polynomial design to determine a controller in the form of

$$R(q)u(k) = T(q)u_c(k) - S(q)y(k)$$

such that the closed-loop system has the characteristic polynomial

$$A_m(z) = z^2 - 1.8z + 0.9$$

Let the polynomial  $A_o(z)$  have as low order as possible and place all of its poles in the origin. Design the controller such that the steady-state gain from the command signal  $u_c(k)$  to the output  $y(k)$  is one. Consider the following two cases:

- a) The process zero is canceled.

(4 Marks)

- b) The process zero is not canceled.

(4 Marks)

Simulate the step responses of the two cases (letting  $u_c(k) = 1$ ), and plot out the corresponding output and input signals. Discuss the differences between the two controllers. Which one should be preferred?

(2 Marks)

#### Q2. (10 Marks)

Assume that the process is described by the transfer function

$$H(z) = \frac{z - 0.8}{z^2 - 4z + 4}$$

The reference model is specified as

$$H_m(z) = \frac{1}{z^2}$$

- a) Design a controller in the form of

$$R(q)u(k) = T(q)u_c(k) - S(q)y(k)$$

to make the closed-loop transfer function match the reference model as close as possible. Also try to make the controller reject constant disturbance.

(5 Marks)

b) Design a two-degree-of-freedom controller in the form of

$$u(k) = u_{fb}(k) + u_{ff}(k)$$

where the feedback control signal  $u_{fb}(k)$  is generated by the feedback controller

$$U_{fb}(z) = -\frac{S(z)}{R(z)}Y(z)$$

and the feed-forward control signal  $u_{ff}(k)$  is produced by the feed-forward controller

$$U_{ff}(z) = H_{ff}(z)U_c(z)$$

Design the feedback controller and feed-forward controller properly to follow the same reference model and to reject constant disturbance.

(5 Marks)

**Q3. (20 Marks)**

Consider a vehicle, which has a weight  $m = 1000$  kg. Assuming the average friction coefficient  $b = 200$ . Let  $y$  denote the displacement of the vehicle, then the dynamics of the vehicle can be described by the following equation

$$m\ddot{y}(t) + b\dot{y}(t) = u(t)$$

where  $m=1000$ , and  $b=200$ . Assume that the sampling period is 0.5s. Design a two-degree-of-freedom digital controller in the form of

$$R(q)u(k) = T(q)u_c(k) - S(q)y(k)$$

to meet the following performance requirements on its step response for position control system:

1. The overshoot is less than 10%.
2. The settling time is less than 10 s.
3. The controller can reject the influence of unknown constant disturbance.

**Q4. (10 Marks)**

A nonlinear process is described by the input-output model

$$y(k+1) = y(k) + \frac{cu(k-1)}{y^2(k-1) + 1}$$

where  $c$  is a constant parameter.

- a) Design a one-step-ahead controller to make the output of the system,  $y(k)$ , follow any arbitrary desired output,  $r(k)$ .

(7 Marks)

- b) Discuss the condition on the parameter  $c$  such that perfect tracking is attainable.

(3 Marks)