

Today's class.

- ① At the end we want to get dynamic Model of AC machine in form.

## Rotating Field machines

$$[\dot{x}] = [F(x)] [u]$$

- (2) The model will be based on space vectors

## Must Know

- Principle behind Space Vectors
  - Definition
  - Conversion.

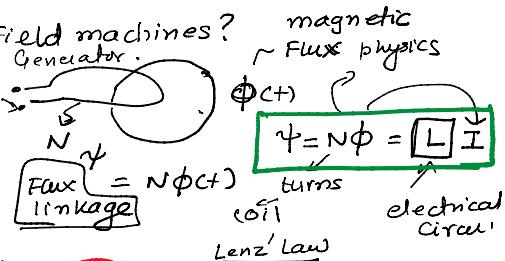


- ① What do we mean by Rotating Field machines? Generator.

- Rotating magnetic field

$$\vec{v}_i = \frac{d\psi}{dt} = N \frac{d\phi}{dE}$$

## Faradays law



- ① 2 windings minimum required.  
and ✓ → why?

$$\text{and } \quad (2) \quad I_a = \underline{I_m \cdot \cos(\omega t)} \quad |$$

$\checkmark$

$$I_b = \underline{I_m \cdot \sin(\omega t)} \quad ?$$

$\checkmark$

① Rotating magnetic field means = Flux linkage.

$$\Psi(t) = Lg \cdot Im \cdot \cos(\omega t)$$

$$\psi_b^{(+)} = Lb \operatorname{Im} \cos(\omega t)$$

Resultant Flux linkage  
is a vector

not yet complete

$$\Psi_s(t) = \Psi_a(t) + e^{j\phi} + \Psi_b(t) \cdot e^{j\frac{\pi}{2}}$$

Space Vector

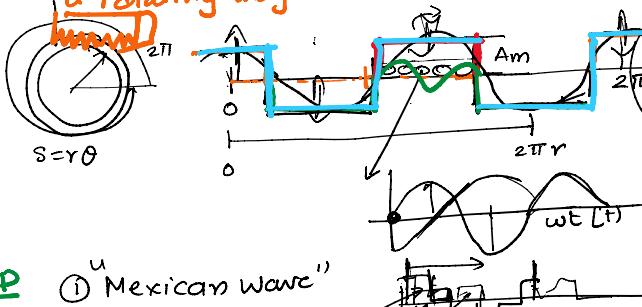
$$\Sigma \text{ Spatial orientations of resultant flux linkage at any given time.} \quad \Psi_s(t) = \Psi_a(t) + j \Psi_b(t)$$

$$L_a = L_b = L_m$$

$$\therefore \Psi_s(t) = L_m \cdot I_m \cdot \cos(\omega t) \quad \therefore \tau = \sin(\omega t)$$

flux linkage  
at any given  
time.

We need 2 quadrature winding fed with 2 phase currents ( $90^\circ$  phase shift) to produce a resultant flux linkage vector whose tip .. follows a circular trajectory to signify a rotating magnetic field.



## Distributed Windings

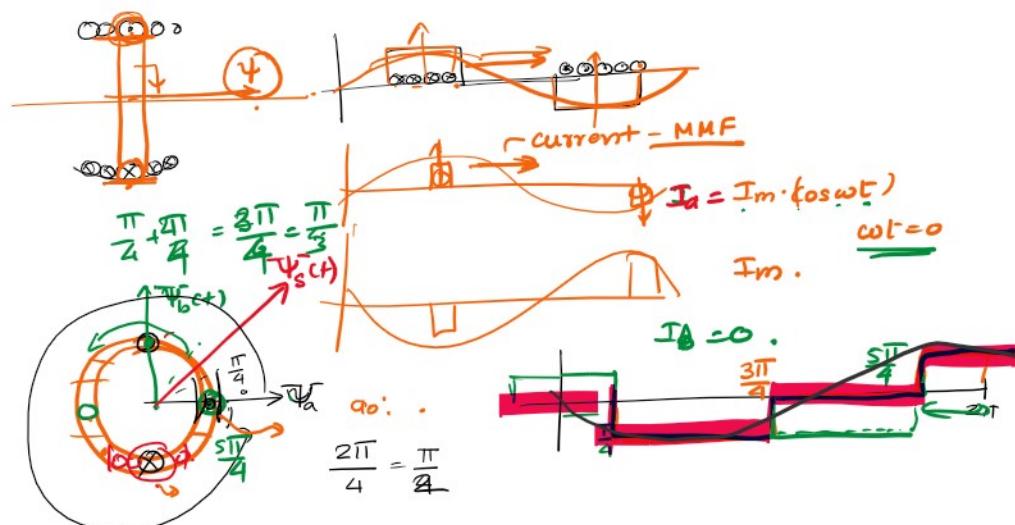
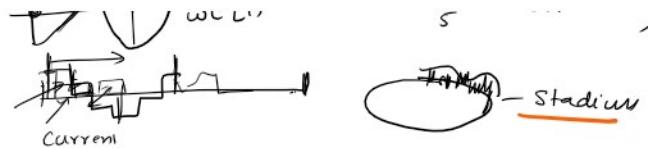
$\Rightarrow MMF = N.I$

$$= \frac{4Am}{\pi} (\cos(5\theta) - \frac{1}{3}\cos(3\theta) + \frac{1}{5}\cos(\theta)) \dots$$

Imp ① "Mexican Wave"

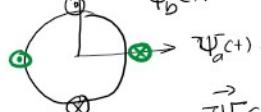
Imp

① "Mexican Wave"



$$\frac{3\pi}{4} + \frac{\pi}{2} = \frac{5\pi}{4} \quad \Psi_s(t) = L_m I_m \sin(\omega t)$$

$$\frac{5\pi}{4} + \frac{\pi}{4} = \frac{6\pi}{4} = \frac{3\pi}{2}$$



$$I_m = 1$$

$$\cos(\omega t)$$

$$\sin(\omega t)$$

$$\boxed{\Psi_s(t) = L_m I_m e^{j\omega t}}$$

I can define this in a complex plane.

Q3 But we have 3 phase windings - 3 phase currents.

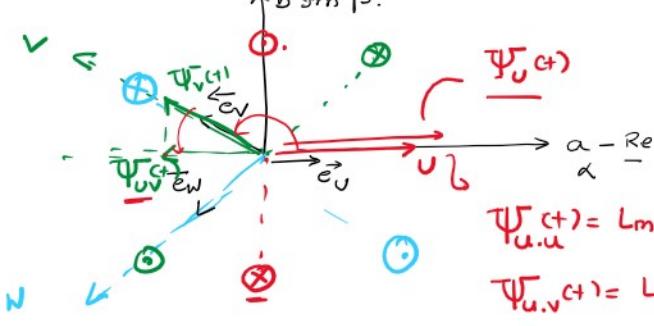
$$I_u(t) = I_m \cos(\omega t)$$

$$I_v(t) = I_m \cos(\omega t - 2\pi/3)$$

$$I_w(t) = I_m \cos(\omega t - 4\pi/3)$$

How do we produce a rotating magnetic field ... Same as 3 RMF produced by 2 quadrature Winding systems.

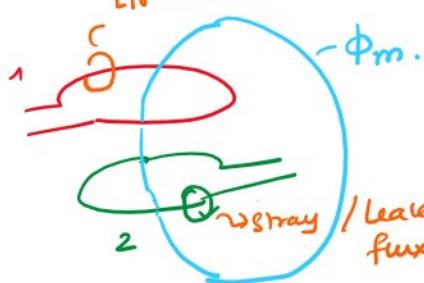
3 RMF produced by 2 quadrature Winding systems.



$$\Psi_{u,u}(t) = L_m I_u(t)$$

$$\Psi_{u,v}(t) = L_m I_v(t)$$

$$\Psi_{u,w}(t) = L_m I_w(t)$$



$$L_m = \Phi_m = \frac{\Phi}{I}$$

Φ<sub>m</sub> - mutual flux is flux linking

Any 2 coils Mutual.

$$\Phi_T = \Phi_m + \Phi_{1,\sigma}$$

2   $\phi_r = \phi_m + \phi_{r\sigma}$   
 $L_{\text{self inductance}} = L_m + L_\sigma$

## Space vectors for 3phase Machines

- The resultant flux linkage vector produced by 3 phase windings (with 3 phase currents) ... which would be same as that produced by 2 phase quadrature axis winding.

1. Thought experiment

$$L_m = 1.0, I_{V\sigma} = 1 \cdot \cos(\omega t), I_V = 1 \cdot \cos(\omega t - 2\pi/3), I_W = 1 \cdot \cos(\omega t - 4\pi/3).$$

$$\omega t = 0$$

$$\vec{\Psi}_s = \vec{\Psi}_U^{(+)}) + \vec{\Psi}_V^{(+)}) \cdot \vec{e}_V + \vec{\Psi}_W^{(+)}) \cdot \vec{e}_W$$

$$\vec{e}_V = e^{j2\pi/3} = -\frac{1}{2} + j\frac{\sqrt{3}}{2} \quad \vec{e}_W = e^{j4\pi/3} = -\frac{1}{2} - j\frac{\sqrt{3}}{2}.$$

$$\boxed{\vec{\Psi}_s = \frac{3}{2}}$$

$\therefore$  Definition of Space vector is

$$\vec{\Psi}_s^{(+)}) = \frac{2}{3} \left( \vec{\Psi}_U^{(+)}) \cdot \vec{e}_V + \vec{\Psi}_V^{(+)}) \cdot \vec{e}_V + \vec{\Psi}_W^{(+)}) \cdot \vec{e}_W \right)$$

$$\vec{a} = \vec{e}_V = e^{j2\pi/3} \quad \therefore \vec{e}_W = \vec{a}^2$$

$$\therefore \vec{\Psi}_s^{(+)}) = \frac{2}{3} \left( \vec{\Psi}_U^{(+)}) + \vec{\Psi}_V^{(+)}) \cdot \vec{a} + \vec{\Psi}_W^{(+)}) \vec{a}^2 \right)$$

## Complex phasor

$$r = A \cdot \cos(\omega t) \quad r_2 = A \cdot \cos(\omega t - \phi)$$

$$= \frac{|A| e^{j\omega t}}{\sqrt{2} R_{\text{MS}}} \quad = \frac{|A| \cdot \vec{e}^{j\phi}}{\sqrt{2}}$$

What the hell is Park's Transform?

$$\begin{bmatrix} \Psi_{s\alpha} \\ \Psi_{s\beta} \end{bmatrix}_{2 \times 1} = \frac{2}{3} \begin{bmatrix} 1 & -\frac{1}{2} & -\frac{1}{2} \\ 0 & \frac{\sqrt{3}}{2} & -\frac{\sqrt{3}}{2} \end{bmatrix}_{2 \times 3} \begin{bmatrix} \Psi_U \\ \Psi_V \\ \Psi_W \end{bmatrix}_{3 \times 1}$$

$$\begin{bmatrix} \Psi_U \\ \Psi_V \\ \Psi_W \end{bmatrix}_{3 \times 1} = \frac{1}{2} \begin{bmatrix} 1 & 0 \\ -\frac{1}{2} & \sqrt{3} \end{bmatrix}_{2 \times 2} \begin{bmatrix} \Psi_{s\alpha} \\ \Psi_{s\beta} \end{bmatrix}_{2 \times 1} \Rightarrow \vec{C}_{sp} = \vec{C}_{sv}^T$$

$$\frac{2}{3} (\vec{\Psi}_U^{(+)}) + \vec{a} \vec{\Psi}_V^{(+)}) + \vec{a}^2 \vec{\Psi}_W^{(+)})$$

$$\begin{bmatrix} \Psi_u \\ \Psi_v \\ \Psi_w \end{bmatrix} = \frac{2}{3} \begin{bmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{1}{2} & -\frac{\sqrt{3}}{2} \end{bmatrix} \begin{bmatrix} \Psi_{SA} \\ \Psi_{SP} \end{bmatrix}$$

Home work → solve how to convert space vectors → 3phas  
 Ⓛ use  $x_u + x_v + x_w = 0 \rightarrow \Psi_{SA} = \Psi_u$ .  
 $\Psi_v, \Psi_w$

$$\textcircled{\psi} \rightarrow \text{Faradays} \quad \vec{v} = \frac{d\vec{\psi}}{dt}$$

mathematical models.

$$\vec{V}_s = \frac{2}{3} (V_u(t) + \vec{\alpha} V_v(t) + \vec{\alpha}^2 V_w(t)).$$

$$\vec{I}_s = \frac{2}{3} (I_u(t) + \vec{\alpha} I_v(t) + \vec{\alpha}^2 I_w(t))$$

$$v = \frac{d\psi}{dt}, \quad \text{ohm-} v = R_i$$

$$V_u = R_u \cdot I_u + \underbrace{\frac{d\Psi_u}{dt}}_{\sim}.$$

whole stator winding 3p.

$$\vec{V}_s = R_s \cdot \vec{I}_s + \frac{d\Psi_s}{dt}$$

Rotor

$$\vec{V}_R = R_R \cdot \vec{I}_r + \frac{d\Psi_r}{dt}.$$