

# EE5703 Industrial Drives Project

## Industrial Robot Position Control

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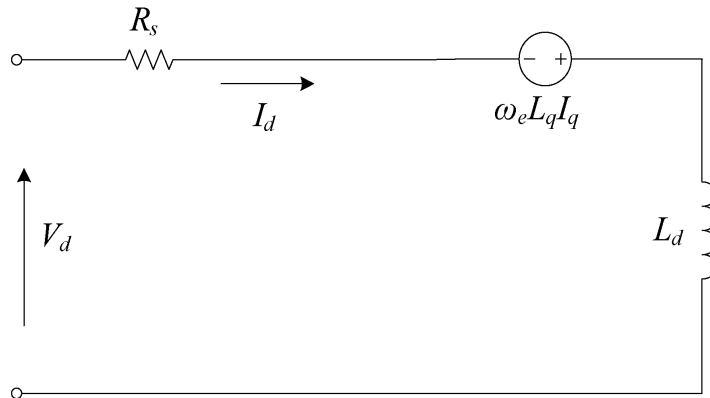
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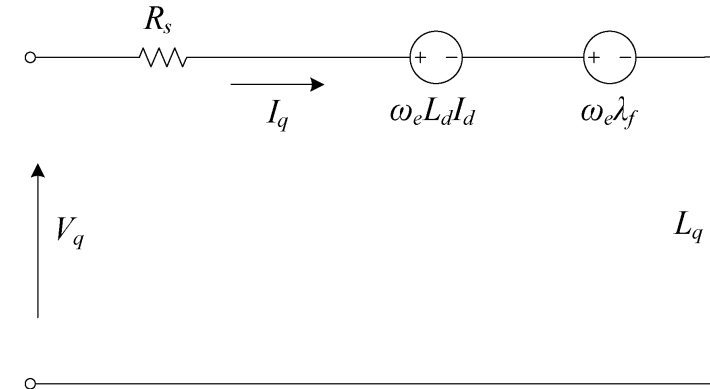
# Mathematic model

We apply d-q axis coordinate model

The rotor lacks electromagnetic dynamics since the flux is generated by permanent magnets.



(a)



(b)

Equivalent circuit

$$\vec{v}_{sd} = \vec{i}_{sd} r_s - \omega_s \psi_{sq} + \frac{d\psi_{sd}}{d\tau}$$

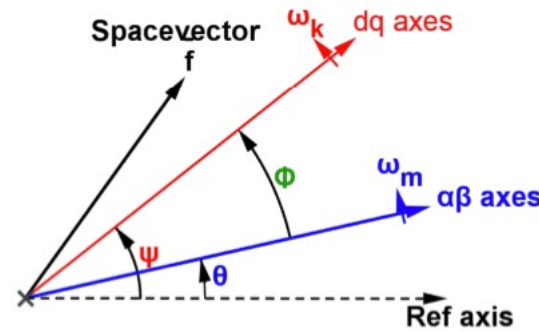
$$\vec{v}_{sd} = \vec{i}_{sd} r_s - \omega_s l_q i_{sq} + l_d \frac{di_{sd}}{d\tau}$$

$$\vec{v}_{sq} = \vec{i}_{sq} r_s + \omega_s \psi_{sd} + \frac{d\psi_{sq}}{d\tau}$$

$$\vec{v}_{sq} = \vec{i}_{sq} r_s + \omega_s l_q i_{sq} + \omega_s \psi_{r,m} + l_q \frac{di_{sq}}{d\tau}$$

# Mathematic model

$$\begin{aligned}\frac{di_{sd}}{d\tau} &= -\frac{r_s}{l_d}i_{sd} + w_s \frac{l_q}{l_d}i_{sq} + \frac{v_{sd}}{l_d} \\ \frac{di_{sq}}{d\tau} &= -\frac{r_s}{l_q}i_{sq} - w_s \frac{l_d}{l_q}i_{sd} - w_s \frac{\psi_{r,m}}{l_q} + \frac{v_{sq}}{l_q} \\ m_e &= \vec{\psi}_s \times \vec{i}_s = \text{Im}[\vec{\psi}_s^* \vec{i}_s] \\ &= \psi_{r,m}i_{sq} + (l_d - l_q)i_{sd}i_{sq} \\ w_s &= pw \\ \frac{dw}{d\tau} &= \frac{m_e - m_L}{\tau_m}\end{aligned}$$



$$\begin{aligned}\vec{v}_s &= r_s \vec{i}_s + l_s \frac{d\vec{i}_s}{d\tau} + \frac{d\vec{\psi}_{r,m}}{d\tau} \\ \vec{\psi}_{r,m} &= |\psi_{r,m}|e^{j\delta} = \psi_{r,m\alpha} + j\psi_{r,m\beta} \\ \vec{v}_s &= r_s \vec{i}_s + l_s \frac{d\vec{i}_s}{d\tau} + j\omega_s \vec{\psi}_{r,m} \\ v_{s\alpha} &= r_s i_{s\alpha} + l_s \frac{di_{s\alpha}}{d\tau} - \omega_s \psi_{r,m\beta} \\ v_{s\beta} &= r_s i_{s\beta} + l_s \frac{di_{s\beta}}{d\tau} + \omega_s \psi_{r,m\alpha} \\ \frac{di_{sa}}{d\tau} &= -\frac{r_s}{l_s}i_{sa} + \frac{v_{sa}}{l_s} - \frac{d\psi_a}{l_s d\tau} \\ \frac{di_{sb}}{d\tau} &= -\frac{r_s}{l_s}i_{sb} + \frac{v_{sb}}{l_s} - \frac{d\psi_b}{l_s d\tau}\end{aligned}$$

- d-q coordinate dynamic model is a commonly adopted and relatively straightforward.
- In our efforts to gain a deeper understanding of the PMSM and help us study we tried to model in stator coordinates.
- We can transform the equation on the d-q axis coordinate system to the  $\alpha$ - $\beta$  axis coordinate system using the **rotation velocity relationship**.
- Therefore, the voltage equation in the  $\alpha - \beta$  coordinate system can be expressed as

# PMSM Steady State Model

In real practice, the motor almost work in steady state.

Hence, we need to keep torque output constant.

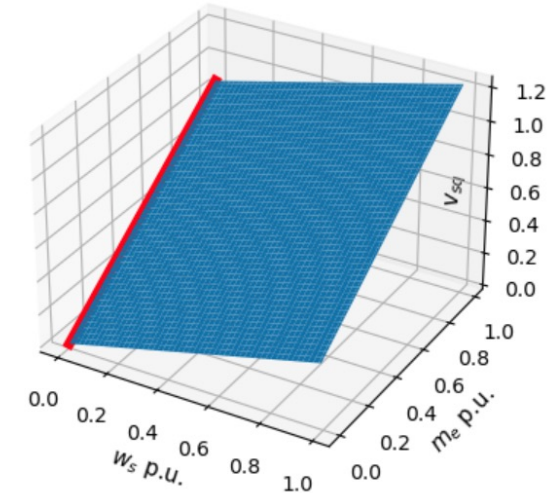
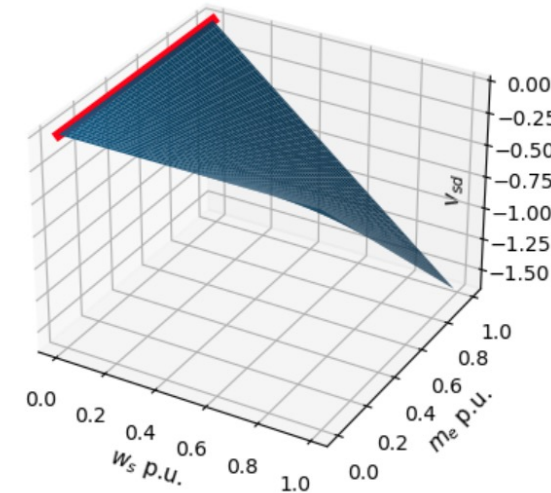
For steady state,  $\frac{di_{sd}}{d\tau} = 0$ ,  $\frac{di_{sq}}{d\tau} = 0$ ,  $\frac{dw}{d\tau} = 0$

$$\vec{v}_{sd} = \vec{i}_{sd}r_s - w_s\psi_{sd}$$

$$\vec{v}_{sd} = \vec{i}_{sd}r_s - w_sl_qi_{sq}$$

$$\vec{v}_{sq} = \vec{i}_{sq}r_s + w_s\psi_{sd}$$

$$\vec{v}_{sq} = \vec{i}_{sq}r_s + w_sl_di_{sd} + w_s\psi_{r,m}$$

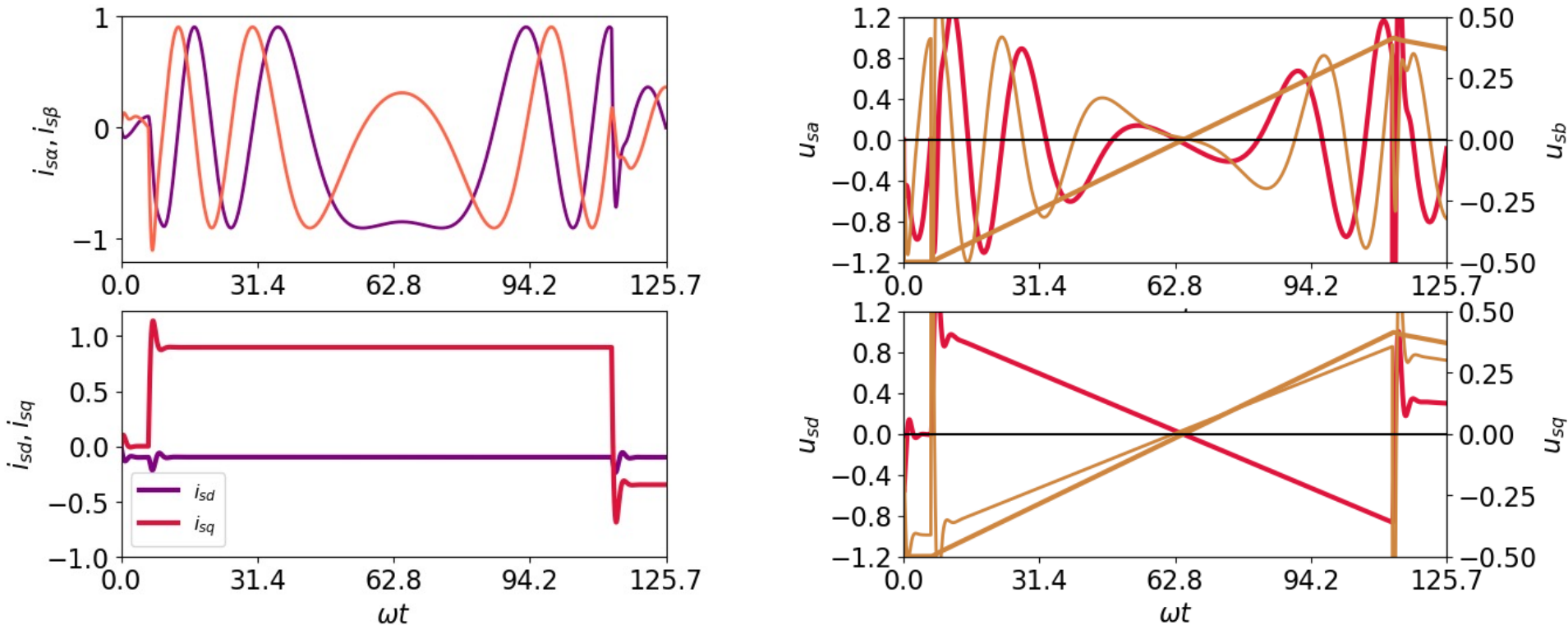


- Respective variation of  $\vec{v}_{sd}$  and  $\vec{v}_{sq}$  to  $w_s$  and  $m_e$
- Servo steady state ( $w_s = 0$ ) is indicated by red line



# Dynamic simulation

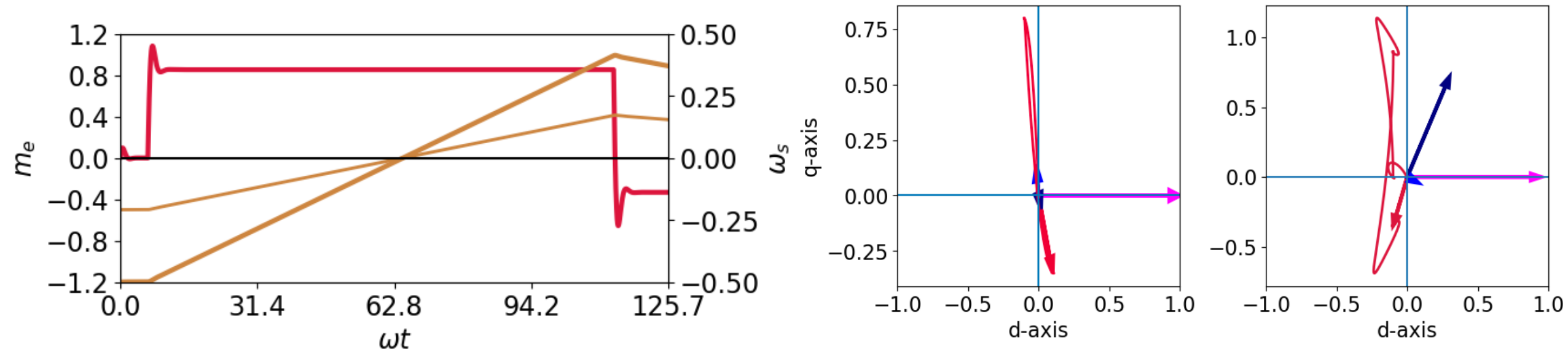
Initial rotational velocity of -5 rad/s. Current  $i_q$  to 0.8 then to -0.35.



$$\begin{aligned} r_s &= 0.1729, \\ l_q &= 0.6986, \\ l_d &= 0.4347, \\ \tau_m &= 50.5 \end{aligned}$$

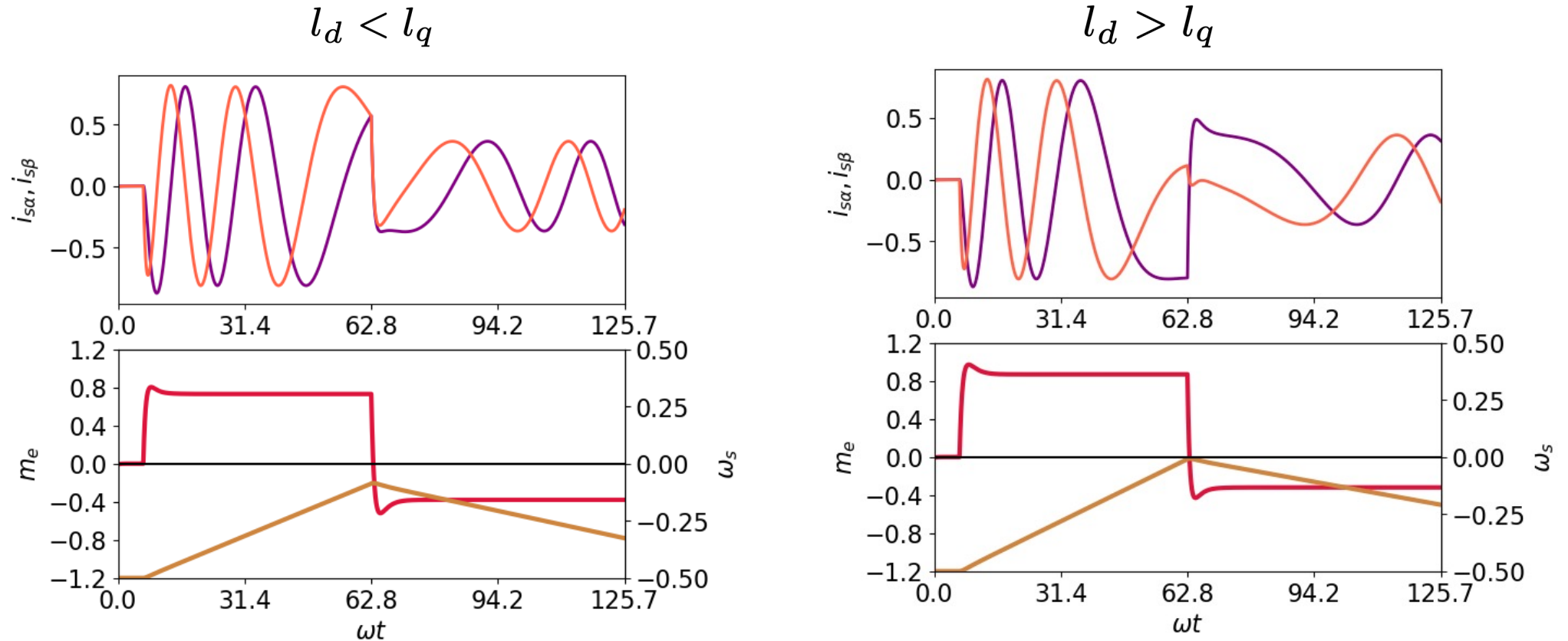
- For both models we can see the the rotational speed initiates from -0.5 and progressively accelerates, reversing direction.
- It also proves that the d-q coordinates method is much more straightforward for accomplishing precise current control compared with Stator coordinate model.

# Dynamic simulation



- Even though there is a smooth and slightly overshooting current initiation, the output torque and rotational speed exhibit seamless transitions without significant overshooting or oscillations.
- For current trajectory the q-axis current undergoes significant changes, underscoring its primary role in torque control.
- It demonstrates the q-axis current is the main contributor to torque regulation.

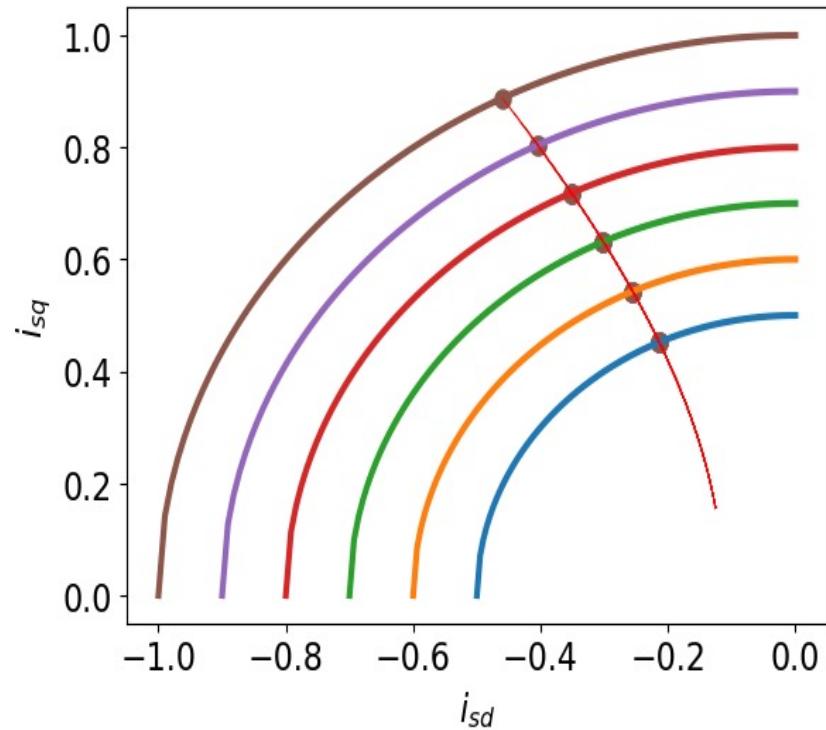
# Dynamic simulation



- For the other two situations, demonstrate effective control of current and rotation speed.
- The primary distinction lies in the rotational acceleration. when  $l_d > l_q$ , the acceleration is notably higher compared to the scenario with  $l_d < l_q$ .
- A larger  $l_d$  results in a more robust field along the d-axis, augmenting the motor's torque production capacity.

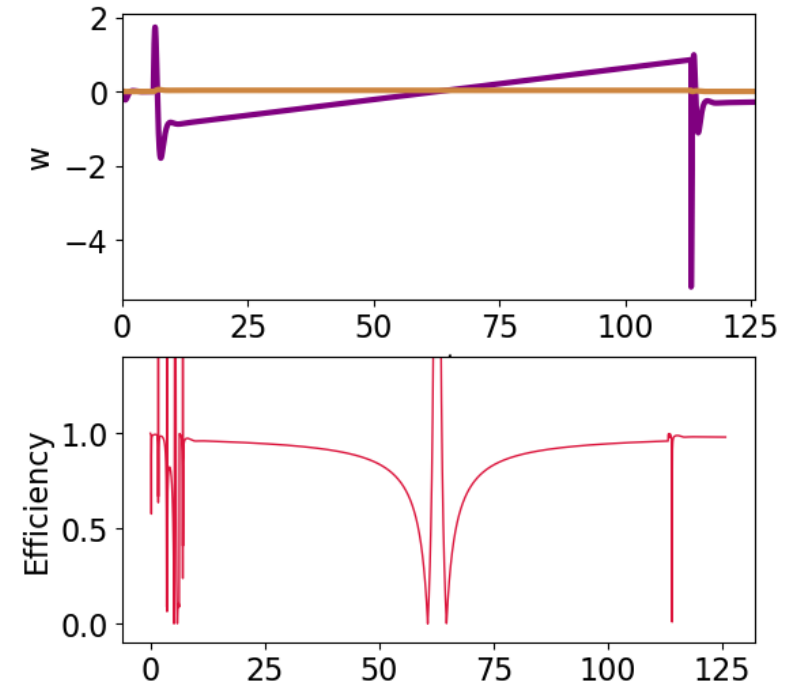
# Mathematic model

Maximum Torque per Ampere(MPTA)



- The simulation reveals that the MPTA position is not linearly related to  $i_d$  and  $i_q$ .
- So it's crucial to find the MPTA point in reality to improve the overall efficiency of robot operations.

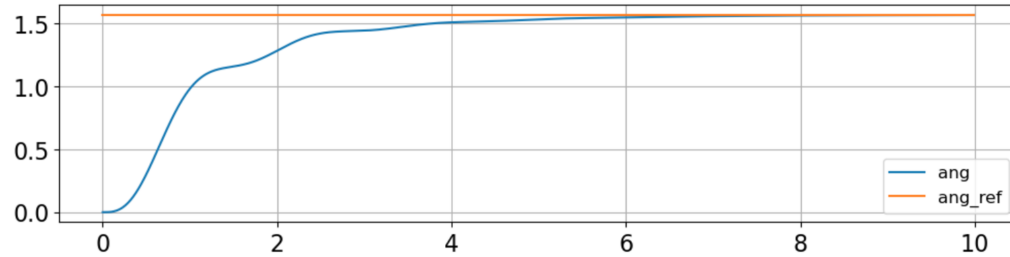
Power and efficiency



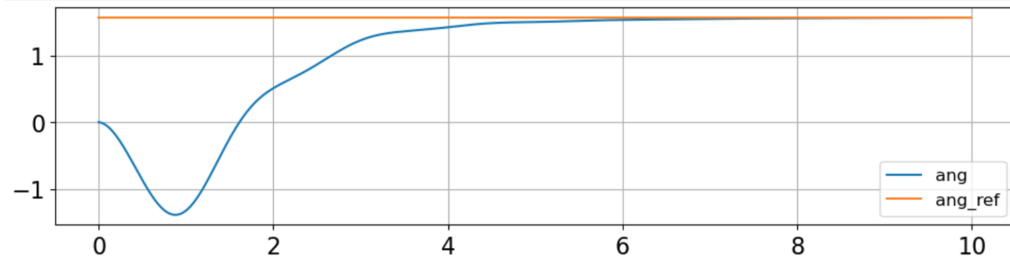
- The efficiency remains consistently high, nearing 1 in most conditions.
- However, fluctuations are observed when the current or rotor changes direction.



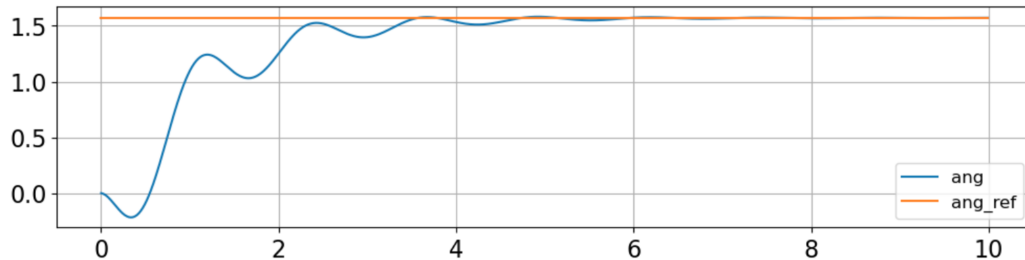
# Cascade PID Control



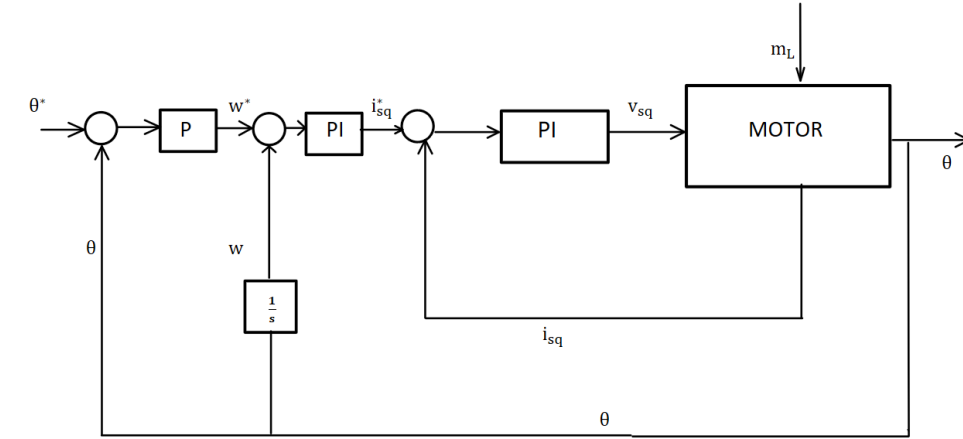
Position step  
response:  $\angle 90^\circ$ ,  
no load



Position step  
response:  $\angle 90^\circ$ ,  
 $m_L = 0.15$  p.u.



Position step  
response:  $\angle 90^\circ$ ,  
 $m_L = 0.15$  p.u.,  
extended voltage limit



Angular position-velocity cascade control

$$r_s = 0.3264, l_q = 1.459, \\ l_d = 3.622, \tau_m = 4.488$$

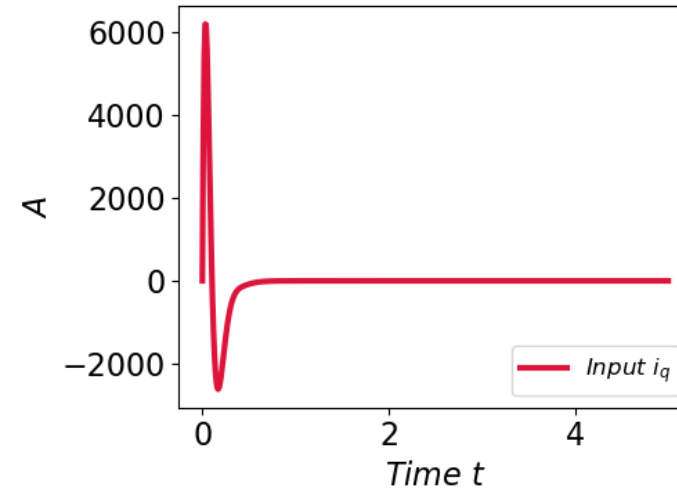
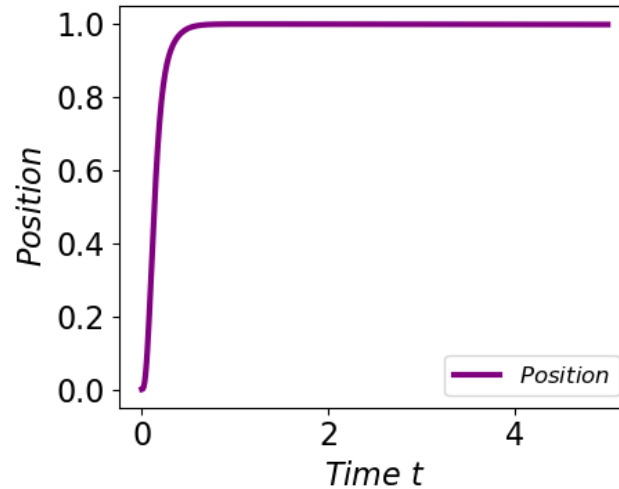
- No overshoot, but long settling time;
- Slow recovery from load torque;
- Less undershoot caused by load if voltage limit is extended to 5 p.u.;

# Augmented matrix LQR

In order to get better performance of controller we applied augmented matrix control

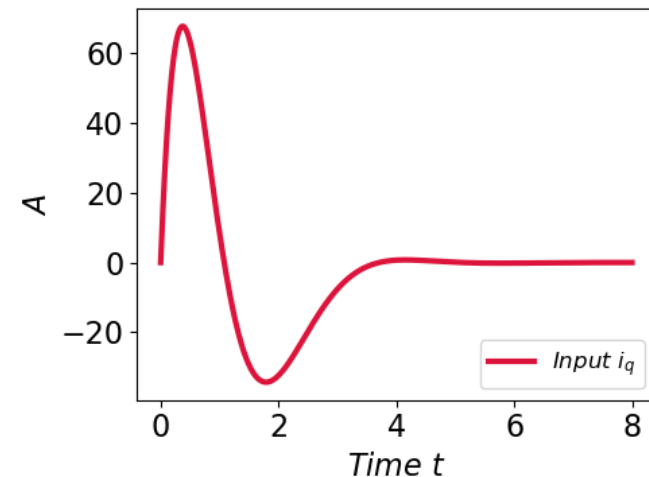
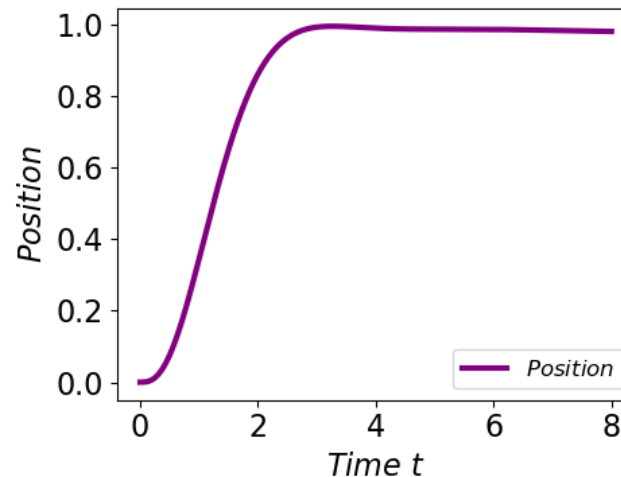
$$\begin{aligned} r_s &= 0.1729, \\ l_q &= 0.6986, \\ l_d &= 0.4347, \\ \tau_m &= 50.5 \end{aligned}$$

The control result is ideal, fast response and precise position.



The control input signal requirement is too high to meet in reality.

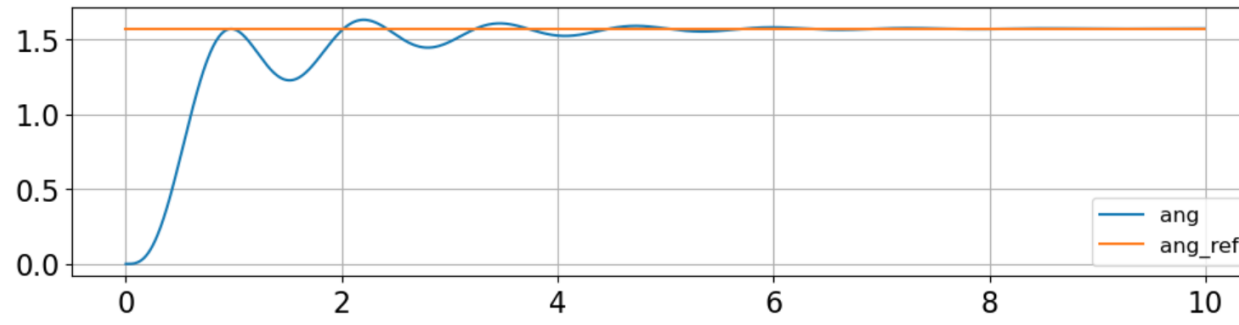
Change to another pair of Q and R, the result is still good.



The input signal is reachable.

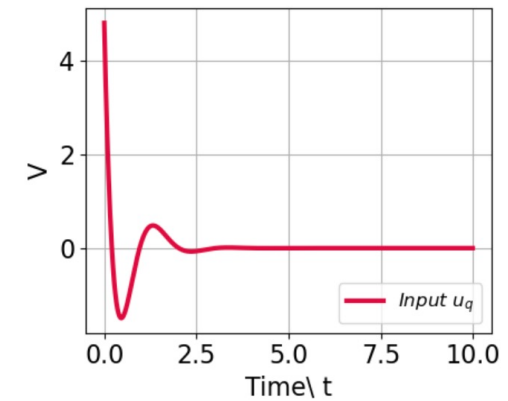
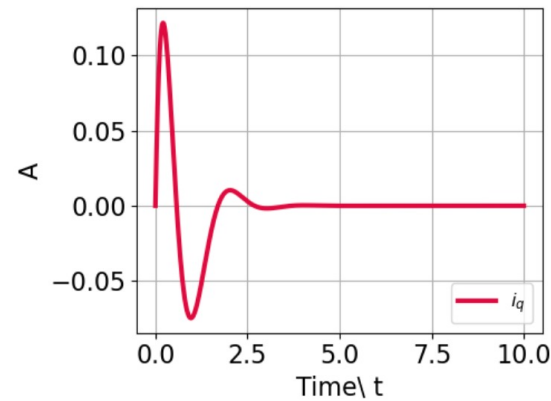
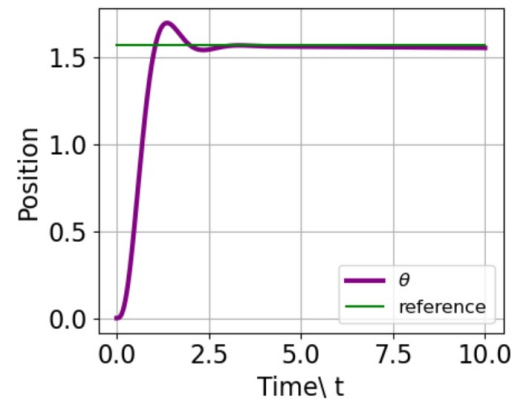
# Comparison

**PID**



$$r_s = 0.3264, l_q = 1.459, \\ l_d = 3.622, \tau_m = 4.488$$

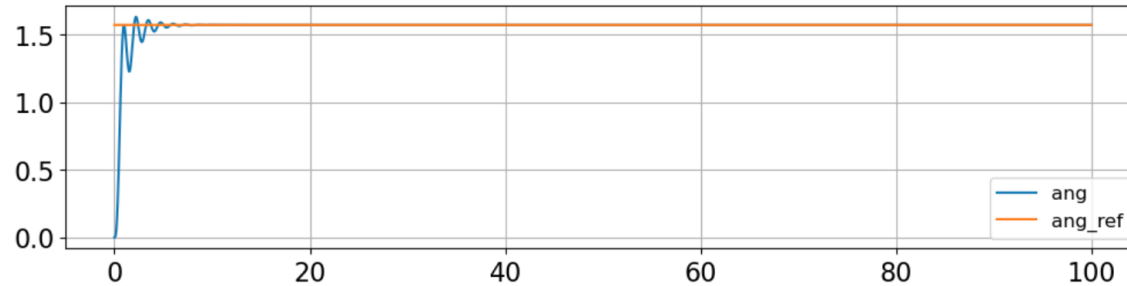
**LQR**



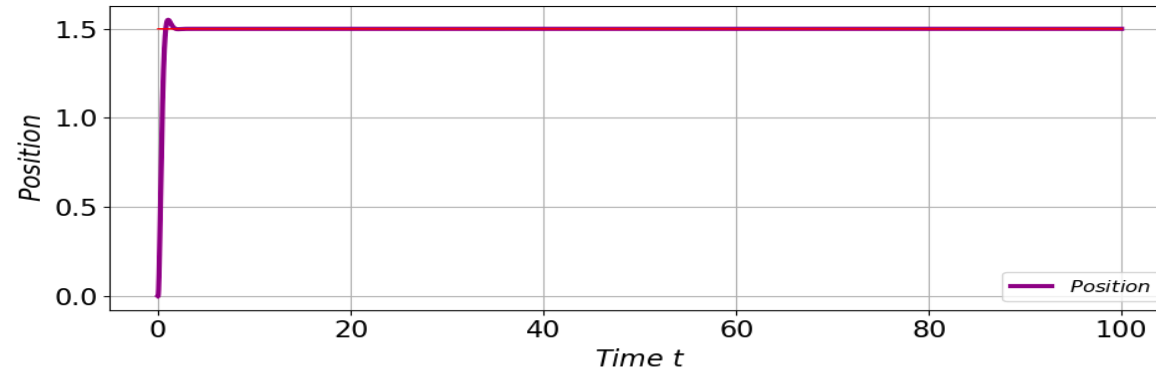
- Carefully tuned Q and R helps to overcome the problem of LQR control signal;
- LQR performs much better than PID.

# Comparison

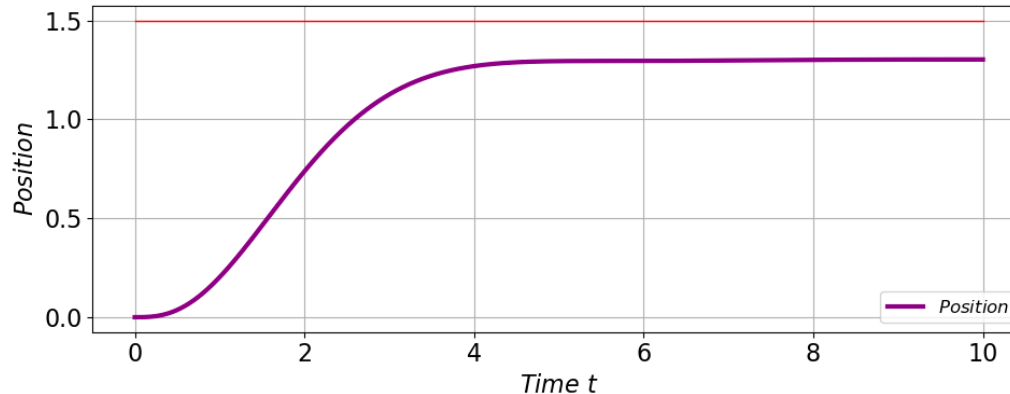
## PID



## LQR



## LQR, disturbance



- For long time simulation two methods Still work well

- For LQR part, we try to build a disturbance reject system but not work well this can be the future research direction for us.

# Conclusion

- This project evaluates a PMSM for industrial robot position control, covering dynamic equations, steady-state analysis, and key motor characteristics.
- The report compares position control using PID and LQR methods.
- In the end we compared two position control PID and LQR and get the conclusion that LQR is a better choice for precise position control despite some unsolved defects.
- Most importantly, these practice enhances our theoretical understanding learnt in class.