



Se tiene una fuerza $F = (2y^2x^3 + 2x^2y^3) \mathbf{j} \text{ N}$
 verifique si la fuerza es o no conservativa

$C_1 \Rightarrow$ Recta $(Y = A + Bx)$

$C_2 \Rightarrow$ Parabola $(Y = ax^b)$

$b = 2$

Ecuación Recta que pasa por dos puntos

$$\begin{cases} F_x = 2y^2x \\ F_y = 2x^2y \end{cases}$$

Pendiente.

$$B = \frac{\Delta Y}{\Delta x} \quad B = \frac{Y_f - Y_i}{X_f - X_i} = \frac{3 - 0}{4 - 0} = \frac{3}{4}$$

$$Y = 0 + \frac{3}{4}x$$

$$W = \int F_x dx + \int F_y dy + \int F_z dz$$

$$\begin{cases} Y = \frac{3}{4}x \\ X = \frac{4}{3}Y \end{cases}$$

$$W_{C1} = \int 2y^2x dx + \int 2x^2y dy$$

$$W_{C1} = 2 \int \left(\frac{3x}{4}\right)^2 x dx + 2 \int \left(\frac{4}{3}y\right)^2 y dy$$

$$W_{C1} = \frac{9}{8} \int_0^4 x^3 dx + \frac{32}{9} \int_0^3 y^3 dy$$

$$W_{C1} = \frac{9}{8} \left[\frac{x^4}{4} \right] + \frac{32}{9} \left[\frac{y^4}{4} \right]_0^3 = \frac{9}{8} \cdot \frac{1}{4} (4^4 - 0^4) + \frac{32}{9} \cdot \frac{1}{4} (3^4 - 0^4)$$

$$\Rightarrow \frac{9}{32} (256) + \frac{8}{9} (81) \quad W = 72 + 72 \rightarrow \underline{W = 144 \text{ J}}$$

$$y = \frac{3}{4}x$$

$$y = f(x) \Rightarrow \frac{dy}{dx} = \frac{d(\frac{3}{4}x)}{dx} = \frac{3}{4} \frac{dx}{dx} \rightarrow \frac{dy}{dx} = \frac{3}{4}$$

Pendiente

$$\boxed{\frac{dy}{dx} = \frac{3}{4}}$$

$$W_{C_2} = 2 \int y^2 x dx + 2 \int x^2 y dy$$

$$y = \frac{3}{4}x \quad \int_0^0 dy = \frac{3}{4}dx$$

$$W_{C_2} = 2 \int \left(\frac{3}{4}x\right)^2 x dx + 2 \int x^2 \cdot \frac{3}{4} dx, \frac{3}{4}x$$

$$W_{C_2} = \cancel{2} \cdot \frac{9}{16} \int x^3 dx + \cancel{2} \cdot \frac{9}{16} \int x^3 dx$$

$$W_{C_2} = \frac{9}{8} \int x^3 dx + \frac{9}{8} \int x^3 dx = \frac{18}{16} \int x^3 dx = \frac{9}{4} \int_0^4 x^3 dx$$

$$W_{C_2} = \frac{9}{4} \left[\frac{x^4}{4} \right]_0^4 = \frac{9}{16} (4^4 - 0^4) = 144 \rightarrow \underline{\underline{144 J}}$$