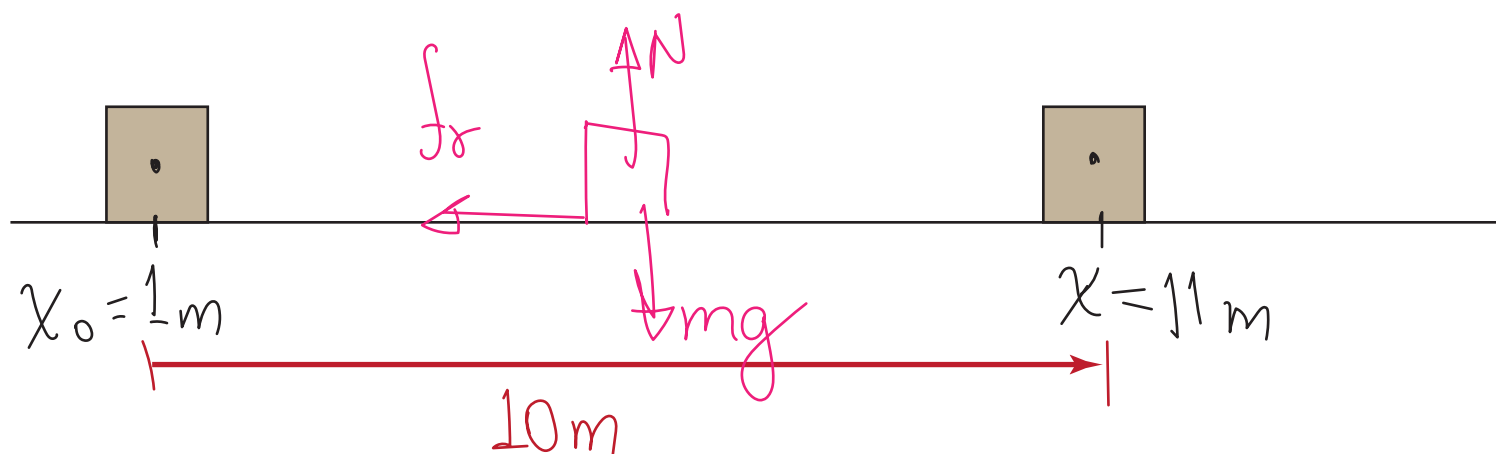


1.- A un bloque de 20 kg que se encuentra sobre un plano horizontal liso en el punto $x_0 = 1$ m y $y_0 = 0$ se le aplica una fuerza que depende de la posición según la ecuación $\vec{P} = 10(x^2) \hat{i}$ N. Para un desplazamiento de 10 m calcule el trabajo realizado por: a) \vec{P} . b) la fuerza de fricción, $\mu_c = 0,3$ c) el trabajo total realizado

R. a) 4433,3 J ; b) -588 J ; c) 3845,3 J



$$\Delta x = x - x_0 \Rightarrow x = \Delta x + x_0 = 10 + 1 = 11 \text{ m}$$

$$\vec{P} = 10x^2 \hat{i}$$

$$P_x = 10x^2$$

$$W = \int F_x dx + \int F_y dy + \int F_z dz$$

$$W_p = \int P_x dx = \int (10x^2) dx = 10 \int_1^{11} x^2 dx = 10 \left[\frac{x^3}{3} \right]_1^{11}$$

$$W_p = \frac{10}{3} (11^3 - 1^3) \Rightarrow \underline{W_p = 4433,33 \text{ J}}$$

$$W_p = 4,43 \times 10^3 = 4,43 \text{ kJ}$$

$$b) W_{fr} = - \int f_r dx = - \int \mu N dx$$

$$W_{fr} = - \int \mu mg dx = - \mu mg \int_1^{11} dx$$

$$W_{fr} = - \mu mg x \Big|_{x_0=1}^{x=11} = - \mu mg (x - x_0) = - \mu mg \Delta x$$

$$W_{fr} = -0,3(20)9,8(10) \Rightarrow \underline{W_{fr} = -588 \text{ J}}$$

$$\sum F_y = 0$$

$$N - mg = 0$$

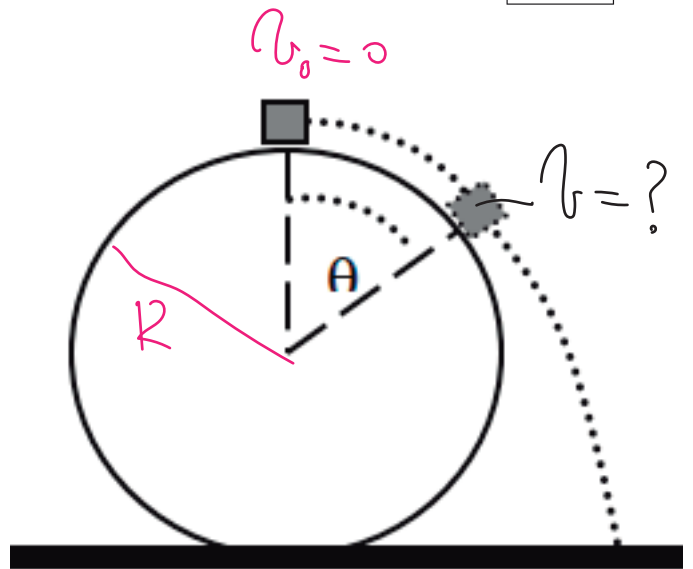
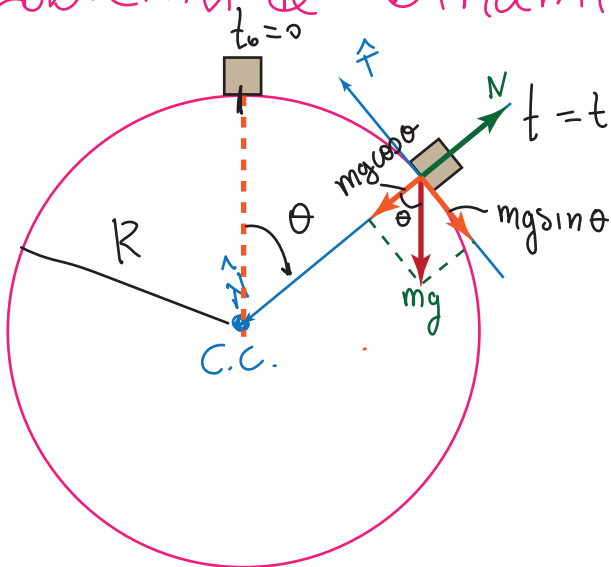
$$N = mg$$

$$W_T = W_p + W_{fr} = 4433,33 + (-588)$$

$$W_T = 3845,33 \text{ J}$$

9.- Una partícula de masa m descansa en la parte superior de una esfera lisa de radio R . si se deja deslizar desde el reposo, para que valor del ángulo θ se desprende de la esfera. R.48.18°

Problema de Dinamica



$$\sum F_N = m \frac{v^2}{R}$$

$$mg \cos \theta - N = m \frac{v^2}{R}$$

$$Rg \cos \theta = v^2$$

$$\frac{v^2}{Rg} = \cos \theta \quad \dots (1)$$

$$\sum F_T = m a_T$$

$$mg \sin \theta = m \frac{dv}{dt}$$

$$dv = g \sin \theta dt \frac{d\theta}{d\theta}$$

$$dv = g \sin \theta \frac{d\theta}{\frac{d\theta}{dt}}$$

$$\int_0^v dv = g \sin \theta \frac{d\theta}{\frac{v}{R}} \Rightarrow \int_0^v R dv = Rg \int_0^\theta \sin \theta d\theta$$

$$a_T = \frac{dv}{dt}$$

$$\frac{d\theta}{dt} = \omega = \dot{\theta}$$

$$v = R\omega$$

$$\omega = \frac{v}{R}$$

$$\frac{d\theta}{dt} = \frac{v}{R}$$

$$\Rightarrow \frac{v^2}{2} \Big|_0^v = Rg (-\cos \theta \Big|_0^\theta) \Rightarrow \frac{1}{2} (v^2 - 0^2) = -Rg (\cos \theta - \cos 0)$$

$$\frac{v^2}{2} = + Rg (1 - \cos \theta) \Rightarrow \frac{v^2}{Rg} = 2 - 2 \cos \theta \quad \dots (2)$$

$$\text{Ec. (1) = (2)}$$

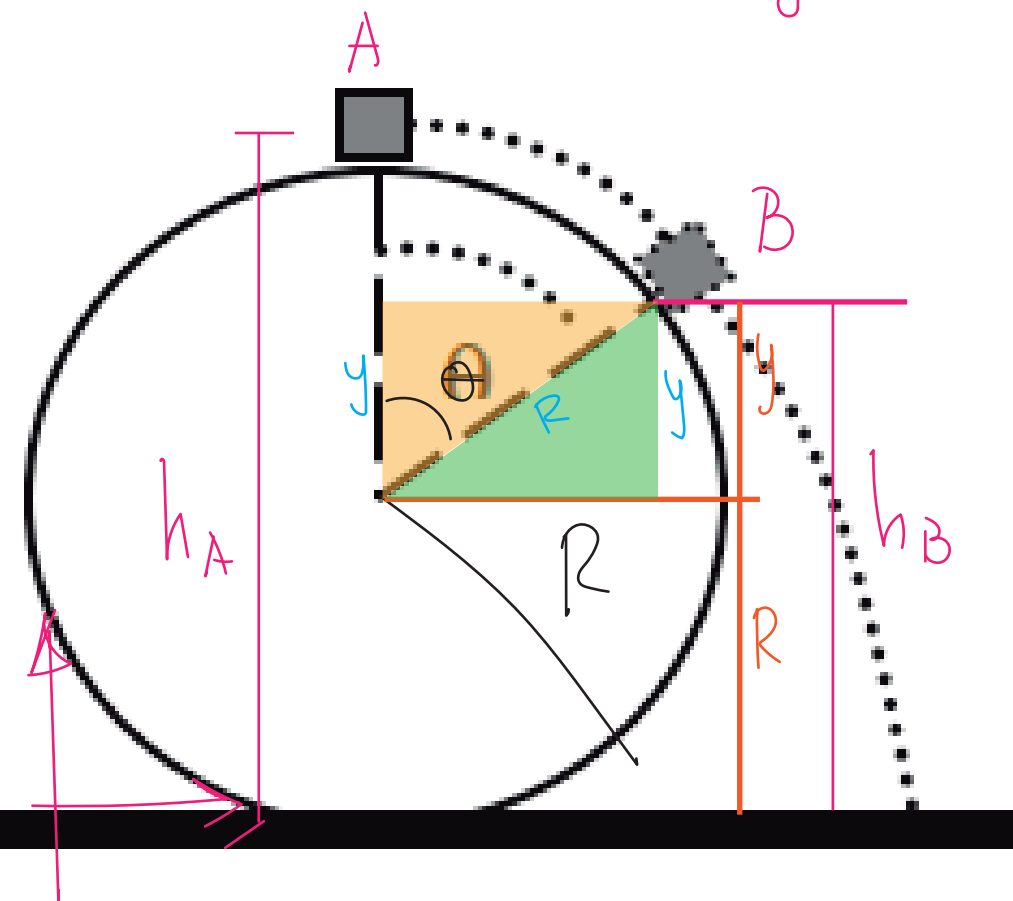
$$\cos \theta = 2 - 2 \cos \theta$$

$$3 \cos \theta = 2$$

$$\cos \theta = \frac{2}{3}$$

$$\theta = \cos^{-1}\left(\frac{2}{3}\right) \Rightarrow \theta = 48,19^\circ$$

Metodo por Energias



$$v = ?$$

$$v_B = \dot{\theta} = ?$$

$$h_A = 2R \quad \checkmark$$

$$h_B = y + R$$

$$\cos \theta = \frac{y}{R}$$

$$y = R \cos \theta$$

$$h_B = R \cos \theta + R \quad \checkmark$$

$$\sum E_A = \sum E_B + \cancel{W}^0$$

$$\cancel{E_C^A} + \cancel{E_P^A} + \cancel{E_E^A} = E_C^B + E_P^B + \cancel{E_E^B}$$

$$\cancel{mgh_A} = \frac{1}{2} m \cancel{v_B^2} + \cancel{mgh_B}$$

$$\frac{1}{2} v^2 = g(h_A - h_B)$$

$$\frac{1}{2} v^2 = g(2R - (R \cos \theta + R))$$

$$\frac{1}{2} v^2 = g(2R - R \cos \theta - R) \Rightarrow \frac{1}{2} v^2 = g(R - R \cos \theta)$$

$$\frac{1}{2} v^2 = Rg(1 - \cos \theta)$$

$$\frac{v^2}{Rg} = 2 - 2 \cos \theta \quad \dots (3)$$

$$\theta = 48,19^\circ$$

Sol.

