

1 $T(n) = 8T(n/2) + 1000n^2$

WKT $T(n) = aT(n/b) + f(n)$

$a = 8$; $b = 2$; $f(n) = cn^d$
 $= 1000n^2$

$c = 1000, d = 2$

Since $a > b^d$
 i.e. $8 > 2^2$

using master theorem

$T(n) = O(n^{\log_b a})$
 $= O(n^{\log_2 8})$
 $= O(n^{\log_2 2^3}) = O(n^3)$

2 $T(n) = 2T(n/2) + n^2$

$a = 2$; $b = 2$; $c = 1$; $d = 2$

since $a < b^d$
 $2 < 2^2$

$T(n) = O(n^d)$
 $T(n) = O(n^2)$

3 $T(n) = 2T(n/2) + 10n$

$a = 2$, $b = 2$, $c = 10$, $d = 1$

since $a = b^d$
 $2 = 2^1$

using master theorem

$T(n) = O(n^d \log n)$
 $T(n) = O(n \log n)$