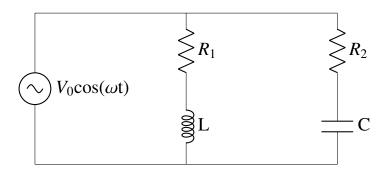
## 1

## GATE 2023 Assignment EE1205 Signals and Systems

## Kurre Vinay EE23BTECH11036

**Question:** In the circuit shown  $\omega = 100\pi \text{rads/s}$ , R1=R2=2.2 $\Omega$  and L=7mH. the capacitance C for which  $Y_{in}$  is purely real is \_\_\_\_ mF



(GATE IN 2023)

## **Solution:**

From Table I

variable	value	description	formulae
Yin	??	Admittance of circuit	$\frac{R_1 - Ls}{R_1^2 - (Ls)^2} + \frac{R_2 - \frac{1}{sC}}{R_2^2 - \left(\frac{1}{sC}\right)^2}$
$X_L$	$7s\Omega$	Inductive reactance	sL
$X_C$	$\frac{1}{sC}\Omega$	Capacitive reactance	1 sC
S	100πj	Laplace complex frequency	jω
ω	100πrads/s	Angular frequency	-
V	$V_0\cos(\omega t)$	voltage of source	-
$R_1, R_2$	2.2Ω	resistance of resistors	-
TABLE I			

TABLE: INPUT PARAMETERS

$$Y_{in} = \frac{R_1 - Ls}{R_1^2 - (Ls)^2} + \frac{R_2 - \frac{1}{sC}}{R_2^2 - \left(\frac{1}{sC}\right)^2}$$
(1)

$$Im(Y_{in}) = \frac{-Ls}{R_1^2 - (Ls)^2} + \frac{-\frac{1}{sC}}{R_2^2 - \left(\frac{1}{sC}\right)^2}$$
(2)

According to the question given,  $Y_{in}$  is purely real, so imaginary part should be equal to zero

Take the values from Table I

$$\frac{-7(100\pi)}{(2.2)^2 + (7(100\pi))^2} + \frac{\frac{1}{(100\pi)C}}{(2.2)^2 + \left(\frac{1}{C(100\pi)}\right)^2} = 0$$
(3)

$$\frac{-1}{4.4} + \frac{\frac{1}{(100\pi)C}}{(2.2)^2 + \left(\frac{1}{(100\pi)C}\right)^2} = 0$$

$$\frac{\frac{1}{(100\pi)C}}{(2.2)^2 + \left(\frac{1}{(100\pi)C}\right)^2} = \frac{1}{4.4}$$
(5)

$$\frac{\frac{1}{(100\pi)C}}{(2.2)^2 + \left(\frac{1}{(100\pi)C}\right)^2} = \frac{1}{4.4}$$
 (5)

$$(2.2)^2 - \frac{4.4}{(100\pi)C} + \left(\frac{1}{(100\pi)C}\right)^2 = 0 \tag{6}$$

$$\left(2.2 - \frac{1}{(100\pi)C}\right)^2 = 0\tag{7}$$

$$\frac{1}{(100\pi)C} = 2.2\tag{8}$$

$$C = \frac{700}{484} \text{mF} \tag{9}$$

$$C = 1.446281 \text{mF}$$
 (10)

The capacitance of capacitor C is 1.45mF

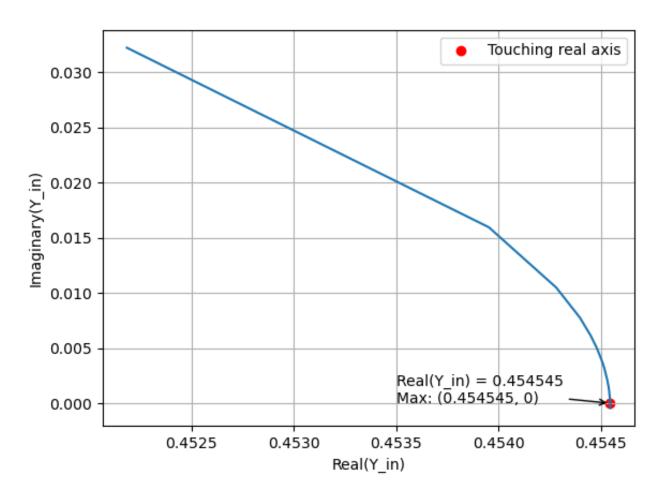


Fig. 1. the graph opf admittance  $(Y_{in})$  amplitude