1

Discrete Assignment EE1205 Signals and Systems

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Question 11.9.3.8: Find the sum to indicated number of term in each of the geometric progressions in $\sqrt{7}$, $\sqrt{21}$, $3\sqrt{7}$, n terms

Solution: Sum of the geometric progression of $\sqrt{7}$, $\sqrt{21}$, $3\sqrt{7}$, n terms is **Input Table:**

variable	value	description
x(0)	$\sqrt{7}$	first term of the geometric progession
r	$\sqrt{3}$	common ratio of the geometeric progression
x(n)	$\sqrt{7(3^n)}$	n^{th} term of the geometric progession
n		no of the term in the geometric progression
y(n+1)	$\frac{x(0)(r^{n+1}-1)}{r-1}$	Sum of the n+1 term of the geometric progression
U(z)	$\frac{1}{1-z^{-1}}$ $ z^{-1} < 1$	z-transformation of u(n)

Z-Transformation:

$$x(n) = x(0)r^{(n)}u(n) \tag{1}$$

$$X(z) = \sum_{n = -\infty}^{\infty} x(n)z^{-n}u(n)$$
 (2)

$$=\sum_{n=0}^{\infty}x(n)z^{-n}\tag{3}$$

$$= \sum_{n=0}^{\infty} x(0)r^n z^{-n}$$
 (4)

$$= x(0) \sum_{n=0}^{\infty} r^n z^{-n}$$
 (5)

$$= x(0)(z^{0}r^{0}U(z) + r^{1}z^{-1}U(z) + r^{2}z^{-2}U(z) + r^{3}z^{-3}U(z) + r^{4}z^{-4}U(z) + \dots$$
 (6)

$$= x(0)(1 + r^{1}z^{-1} + r^{2}z^{-2} + r^{3}z^{-3} + r^{4}z^{-4} + r^{5}z^{-5} + r^{6}z^{-6} + \dots)$$
(7)

$$X(Z) = x(0) \left(\frac{1}{1 - rz^{-1}} \right), \quad |rz^{-1}| < 1$$
 (8)

$$y(n) = x(n)u(n) \tag{9}$$

$$Y(z) = X(z)U(z) \tag{10}$$

$$= x(0) \left(\frac{1}{1 - rz^{-1}} \right) \left(\frac{1}{1 - z^{-1}} \right) \tag{11}$$

$$= \sqrt{7} \left(\frac{1}{1 - \sqrt{3}z^{-1}} \right) \left(\frac{1}{1 - z^{-1}} \right) \tag{12}$$

$$= \left(\frac{\sqrt{7}}{\sqrt{3}-1}\right) \left(\left(\frac{\sqrt{3}}{1-\sqrt{3}z^{-1}}\right) - \left(\frac{1}{1-z^{-1}}\right)\right) \tag{13}$$

$$y(n) = \frac{\sqrt{7}}{\sqrt{3} - 1} \left(\sqrt{3^{n+1}} - 1\right) u(n) \tag{14}$$

$$y(n) = \sqrt{7} \left(\frac{\sqrt{3^{n+1}} - 1}{\sqrt{3} - 1} \right) u(n)$$
 (15)

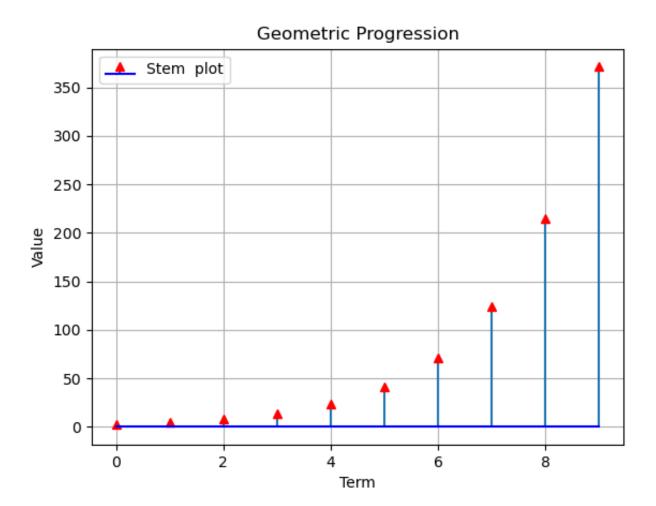


Fig. 0.