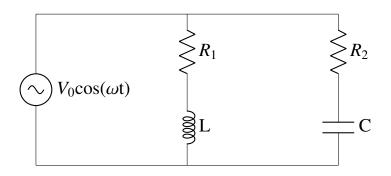
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GATE 2023 Assignment EE1205 Signals and Systems

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Question: In the circuit shown $\omega = 100\pi \text{rads/s}$, R1=R2=2.2 Ω and L=7mH. the capacitance C for which Y_{in} is purely real is ____ mF



(GATE IN 2023)

Solution:

formulae	
$\frac{R_2 - \frac{1}{sC}}{-\left(\frac{1}{sC}\right)^2}$	
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TABLE: INPUT PARAMETERS

According to the question given, Y_{in} is purely real, so imaginary part should be equal to zero

From Table I

$$Y_{in} = \frac{R_1 - Ls}{R_1^2 - (Ls)^2} + \frac{R_2 - \frac{1}{sC}}{R_2^2 - \left(\frac{1}{sC}\right)^2}$$
(1)

$$Y_{in}(\text{imaginary part}) = \frac{-Ls}{R_1^2 - (Ls)^2} + \frac{-\frac{1}{sC}}{R_2^2 - (\frac{1}{sC})^2}$$
 (2)

$$\frac{-L\omega}{R_1^2 + (L\omega)^2} + \frac{\frac{1}{\omega C}}{R_2^2 + \left(\frac{1}{C\omega}\right)^2} = 0$$
(3)

$$\frac{-7(100\pi)}{(2.2)^2 + (7(100\pi))^2} + \frac{\frac{1}{(100\pi)C}}{(2.2)^2 + \left(\frac{1}{C(100\pi)}\right)^2} = 0 \tag{4}$$

$$\frac{-1}{4.4} + \frac{\frac{1}{(100\pi)C}}{(2.2)^2 + \left(\frac{1}{(100\pi)C}\right)^2} = 0$$
 (5)

$$\frac{\frac{1}{(100\pi)C}}{(2.2)^2 + \left(\frac{1}{(100\pi)C}\right)^2} = \frac{1}{4.4}$$
 (6)

$$(2.2)^2 - \frac{4.4}{(100\pi)C} + \left(\frac{1}{(100\pi)C}\right)^2 = 0 \tag{7}$$

$$\left(2.2 - \frac{1}{(100\pi)C}\right)^2 = 0\tag{8}$$

$$\frac{1}{(100\pi)C} = 2.2\tag{9}$$

$$C = \frac{700}{484} \text{mF} \tag{10}$$

$$C = 1.446281 \text{mF}$$
 (11)

The capacitance of capacitor C is 1.45mF

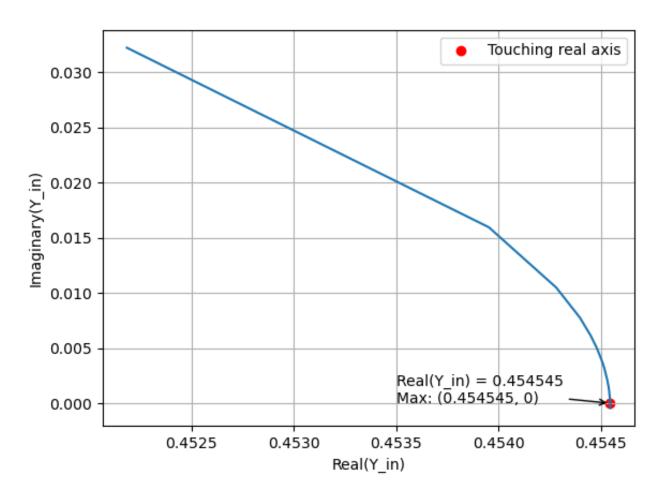


Fig. 1. the graph opf admittance (Y_{in}) amplitude