

From a given vertex in a weighted connected graph, find shortest paths to other vertices using **Dijkstra's algorithm**.

Handwrite the Algorithm

- Handwrite the Program

- Pasting of the printout of the Output or handwrite the Output

ALGORITHM: dijkstras($c[1 \dots n, 1 \dots n]$, src)

//To compute shortest distance from given source node to all nodes of a weighted undirected graph

//Input: An $n \times n$ cost matrix $c[1 \dots n, 1 \dots n]$ with source node src

//Output: The length $dist[j]$ of a shortest path from src to j

```
for  $j \leftarrow 1$  to  $n$  do
     $dist[j] \leftarrow c[src, j]$ 
end for
for  $j \leftarrow 1$  to  $n$  do
     $vis[j] \leftarrow 0$ 
end for
 $dist[src] \leftarrow 0$ 
 $vis[src] \leftarrow 1$ 
 $count \leftarrow 1$ 
while  $count \neq n$  do
     $min \leftarrow 9999$ 
    for  $j \leftarrow 1$  to  $n$  do
        if  $dist[j] < min$  and  $vis[j] \neq 1$ 
             $min \leftarrow dist[j]$ 
             $u \leftarrow j$ 
        end if
    end for
     $vis[u] \leftarrow 1$ 
     $count \leftarrow count + 1$ 
    for  $j \leftarrow 1$  to  $n$  do
        if  $min + c[u, j] < dist[j]$  and  $vis[j] \neq 1$ 
             $dist[j] \leftarrow min + c[u, j]$ 
        end if
    end for
end while
write 'shortest distance is'
for  $j \leftarrow 1$  to  $n$  do
    write  $src, j, dist[j]$ 
end for
```

Code:

```
#include <stdio.h>
```

```
#include <stdlib.h>
```

```
#define MAX_NODES 100
```

```
#define INF 9999
```

```
void dijkstra(int n, int src, int cost[MAX_NODES][MAX_NODES]);
```

```
int main() {
```

```
    int n;
```

```
    int cost[MAX_NODES][MAX_NODES];
```

```
    int src;
```

```
    printf("Enter the number of nodes: ");
```

```
    scanf("%d", &n);
```

```
    printf("Enter the cost adjacency matrix (use -1 for infinity):\n");
```

```
    for (int i = 0; i < n; i++) {
```

```
        for (int j = 0; j < n; j++) {
```

```
            scanf("%d", &cost[i][j]);
```

```
            if (cost[i][j] == -1 && i != j) {
```

```
                cost[i][j] = INF;
```

```
            }
```

```
        }
```

```
    }
```

```
    printf("Enter the source node: ");
```

```
    scanf("%d", &src);
```

```
    dijkstra(n, src, cost);
```

```
    return 0;
```

```
}
```

```
void dijkstra(int n, int src, int cost[MAX_NODES][MAX_NODES]) {
```

```
    int dist[MAX_NODES];
```

```
    int vis[MAX_NODES];
```

```
    for (int j = 0; j < n; j++) {
```

```
        dist[j] = cost[src][j];
```

```
        vis[j] = 0;
```

```
    }
```

```
    dist[src] = 0;
```

```
    vis[src] = 1;
```

```

int count = 1;
while (count != n) {
    int min = INF;
    int u = -1;
    for (int j = 0; j < n; j++) {
        if (!vis[j] && dist[j] < min) {
            min = dist[j];
            u = j;
        }
    }
    if (u == -1) break;
    vis[u] = 1;
    count++;
    for (int j = 0; j < n; j++) {
        if (!vis[j] && cost[u][j] != INF && dist[u] + cost[u][j] < dist[j]) {
            dist[j] = dist[u] + cost[u][j];
        }
    }
}
printf("Shortest distances from source node %d:\n", src);
for (int j = 0; j < n; j++) {
    if (dist[j] == INF) {
        printf("To %d: Infinity\n", j);
    } else {
        printf("To %d: %d\n", j, dist[j]);
    }
}
}

```

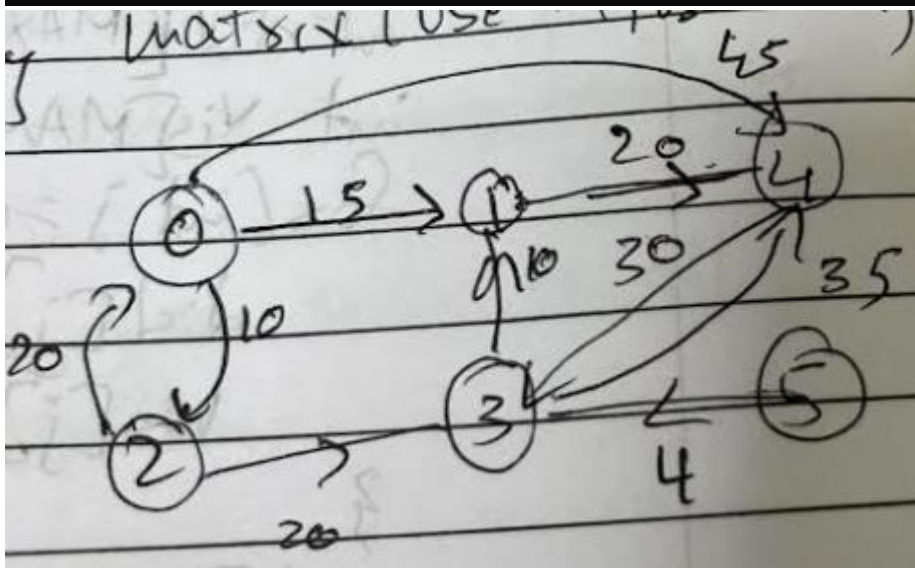
Output:

```

Enter the number of nodes: 6
Enter the cost adjacency matrix (use -1 for infinity):
0 15 10 -1 45 -1
-1 0 15 -1 20 -1
20 -1 0 20 -1 -1
-1 10 -1 0 35 -1
-1 -1 -1 30 0 -1
-1 -1 -1 4 -1 0
Enter the source node: 5
Shortest distances from source node 5:
To 0: 49
To 1: 14
To 2: 29
To 3: 4
To 4: 34
To 5: 0

Process returned 0 (0x0)   execution time : 8.517 s
Press any key to continue.
|

```



Find Minimum Cost Spanning Tree of a given undirected graph using **Kruskals algorithm**.

- Handwrite the Algorithm
- Handwrite the Program
- Pasting of the printout of the Output or handwrite the Output

ALGORITHM: `kruskals(c[1...n,1...n])`

//To compute the minimum spanning tree of a given weighted undirected graph using Kruskal's
// algorithm

//Input: An $n \times n$ cost matrix `c[1...n,1...n]`

//Output: minimum cost of spanning tree of given undirected graph

`ne` \square 0

```

mincost□0
for i□1 to n do
    parent[i]□0
end for
while ne!≡n-1 do
    min□9999
    for i□1 to n do
        for j□1 to n do
            if c[i,j]<min
                min□c[i,j]
                u□i
                a□i
                v□j
                b□j
            end if
        end for
    end for
    while parent[u]!≡0 do
        u□parent[u]
    end while
    while parent[v]!≡0 do
        v□parent[v]
    end while
    if u!≡ v
        write a,b,min
        parent[v]□u
        ne□ne+1
        mincost□mincost+min
    end if
    c[a,b]□9999
    c[b,a]□9999
end while
write mincost
return

```

Code:

```

#include <stdio.h>

#include <stdlib.h>

#define MAX 100

#define INF 9999

struct Edge {
    int u, v, weight;
};

int compare(const void *a, const void *b) {

```

```

    struct Edge *a1 = (struct Edge *)a;
    struct Edge *b1 = (struct Edge *)b;
    return a1->weight - b1->weight;
}

int find(int parent[], int i) {
    if (parent[i] == 0)
        return i;
    return find(parent, parent[i]);
}

void unionSets(int parent[], int u, int v) {
    parent[v] = u;
}

void kruskals(int cost_matrix[][MAX], int n) {
    struct Edge edges[MAX * MAX];
    int edge_count = 0;
    int parent[MAX] = {0};
    for (int i = 1; i <= n; i++) {
        for (int j = 1; j <= n; j++) {
            if (cost_matrix[i][j] != INF) {
                edges[edge_count++] = (struct Edge){i, j, cost_matrix[i][j]};
            }
        }
    }
    qsort(edges, edge_count, sizeof(edges[0]), compare);
    int mincost = 0;
    int ne = 0;
    printf("Edges in the Minimum Cost Spanning Tree:\n");
    for (int i = 0; i < edge_count; i++) {
        int u = find(parent, edges[i].u);
        int v = find(parent, edges[i].v);
    }
}

```

```

    if (u != v) {
        printf("%d - %d : %d\n", edges[i].u, edges[i].v, edges[i].weight);
        unionSets(parent, u, v);
        mincost += edges[i].weight;
        ne++;
    }
    if (ne == n - 1)
        break;
}
printf("Minimum Cost of Spanning Tree: %d\n", mincost);
}

int main() {
    int n;
    printf("Enter the number of vertices: ");
    scanf("%d", &n);
    int cost_matrix[MAX][MAX];
    printf("Enter the cost matrix (n x n):\n");
    for (int i = 1; i <= n; i++) {
        for (int j = 1; j <= n; j++) {
            scanf("%d", &cost_matrix[i][j]);
            if (cost_matrix[i][j] == 0 || cost_matrix[i][j] == -1)
                cost_matrix[i][j] = INF;
        }
    }
    kruskals(cost_matrix, n);
    return 0;
}

```

Output:

```

Enter the number of vertices: 6
Enter the cost matrix (n x n):
0 15 10 -1 45 -1
-1 0 15 -1 20 -1
20 -1 0 20 -1 -1
-1 10 -1 0 35 -1
-1 -1 -1 30 0 -1
-1 -1 -1 4 -1 0
Edges in the Minimum Cost Spanning Tree:
6 - 4 : 4
4 - 2 : 10
1 - 3 : 10
2 - 3 : 15
2 - 5 : 20
Minimum Cost of Spanning Tree: 59

Process returned 0 (0x0)   execution time : 15.980 s
Press any key to continue.
|

```

