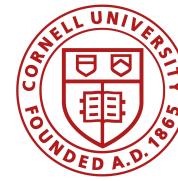


Pulsars and Pulsar Timing

Thankful Cromartie

Einstein Postdoctoral Fellow | Cornell University
Chair, NANOGrav Pulsar Timing Working Group

2022 VIPER Summer School | July 12, 2022



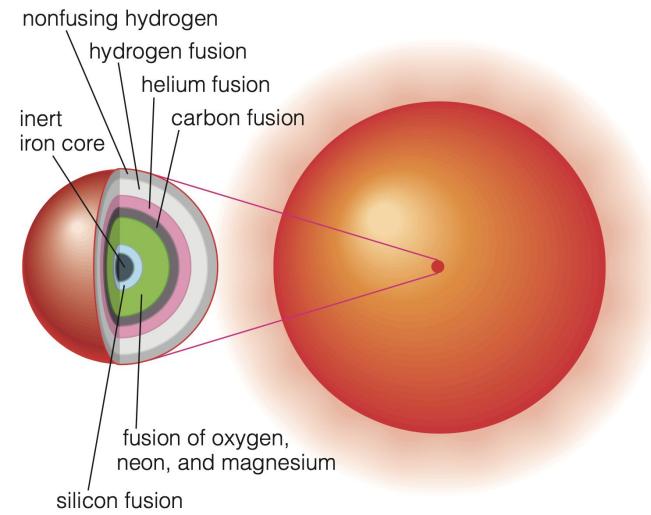
North American Nanohertz Observatory for Gravitational Waves
A National Science Foundation Physics Frontiers Center

Outline

- Neutron Stars
- Millisecond Pulsars
- The ISM
- Millisecond Pulsar Timing
- PTA Data Sets
- The Noise Budget
- NANOGrav's Timing Pipeline

Neutron Stars

- The fate of stars depends on their mass
 - High mass stars go through the process of fusing $H \rightarrow He \rightarrow$ heavier elements
 - Binding energy per nucleon highest for Iron
 - Core collapse when gravity wins
- < 8 solar masses: white dwarfs ($1.4 M_{\odot}$)
- > 8 solar masses: neutron stars (up to $\sim 3 M_{\odot}$)
- > 10 - 30 solar masses: black holes ($> 3 M_{\odot}$)

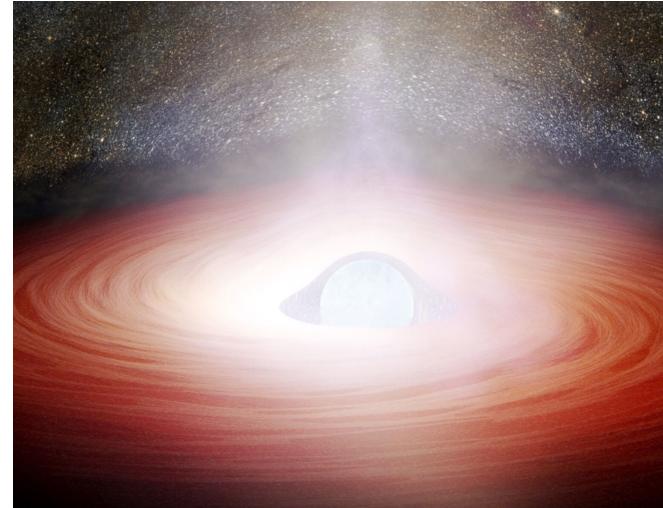


The Cosmic Perspective

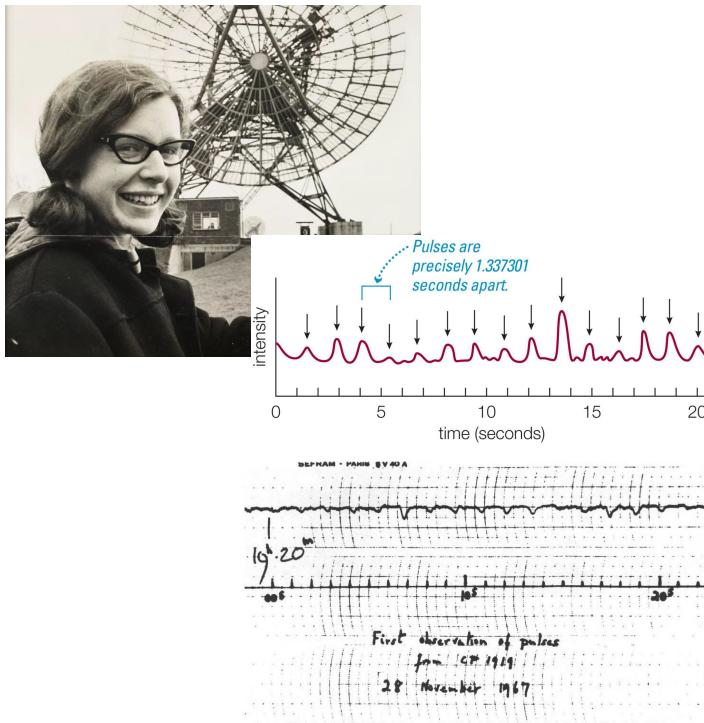
Neutron Stars

Massive stars can undergo supernovae and leave behind neutron stars:

- Balls of neutrons supported by neutron degeneracy pressure
- Density: a paperclip with a neutron star's density would weigh as much as Mount Everest
- Typical NS: $1.4 M_{\odot}$, $r \approx 10$ km



The Discovery of Neutron Stars (Pulsars)



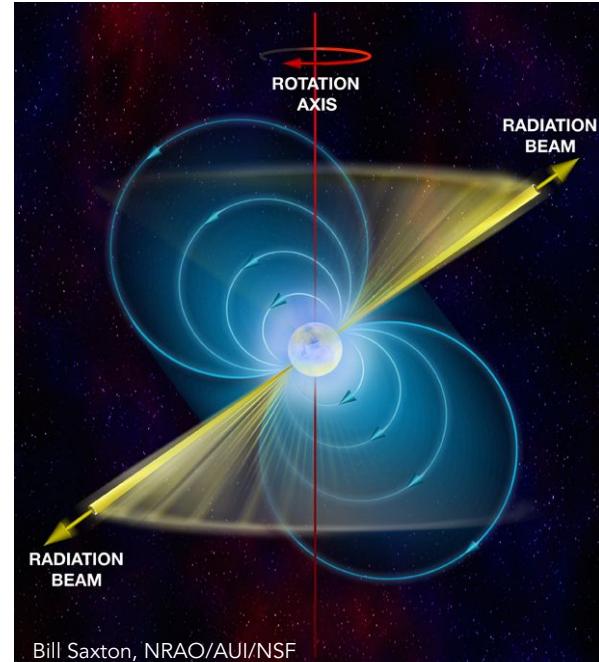
- Using a radio telescope in 1967, grad student Jocelyn Bell-Burnell noticed very regular pulses of radio emission coming from a single part of the sky
- Called "LGM" initially
- The pulses came from a spinning neutron star — a pulsar
- Process of iterating over theory and observations → notable: crab pulsar period increasing
- Bell-Burnell was snubbed by the Nobel committee in favor of her advisor and department head
 - Read her own account:
<http://www.bigar.org/vol1no1/burnell.htm>

What are Pulsars?

- Don't pulse (lighthouses)
- Stable pulse periods (some more than others)
- Initial info can be learned by imposing requirement that centrifugal acceleration at the equator doesn't exceed gravitational acceleration:
 - Angular velocity $\Omega \equiv 2\pi/P$

$$\Omega^2 R < \frac{GM}{R^2} \longrightarrow \rho > \frac{3\pi}{GP^2}$$

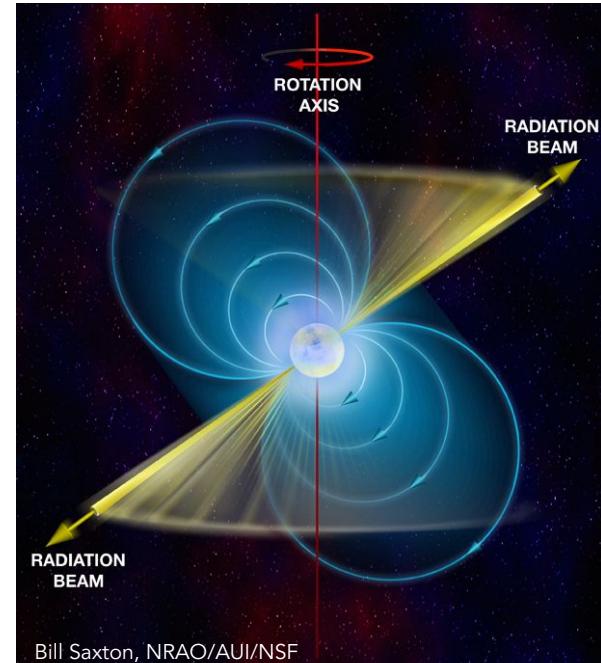
- Fastest < 1.4 ms \rightarrow density $> 10^{14}$ g cm $^{-3}$ = atomic nuclei



Bill Saxton, NRAO/AUI/NSF

What are Pulsars?

- Stars → approx. dipolar B fields
- Magnetic flux is conserved during collapse, so pulsars have B fields up to 10^{15} G (usually more like 10^{12} ; Earth = 0.5 G)
- Rotating magnetic dipole model
 - Misaligned rotation and magnetic axis = dipole radiation; extracts energy; slows down over time
 - Example: Crab pulsar's dipole radiation heats up its nebula, then re-radiates in wide spectrum
 - It's more complicated than this!

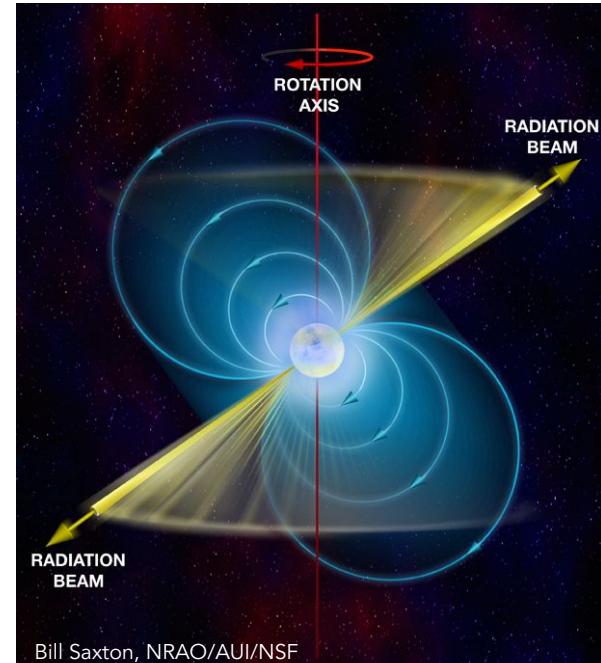


Bill Saxton, NRAO/AUI/NSF

What are Pulsars?

- Assuming dipole + measurement of spin-down, can calculate spin-down luminosity, B field strength, characteristic age
- Most pulsars $10^5 < \text{age} < 10^{10}$ yr (Galaxy)

$$\tau \equiv \frac{P}{2\dot{P}}$$

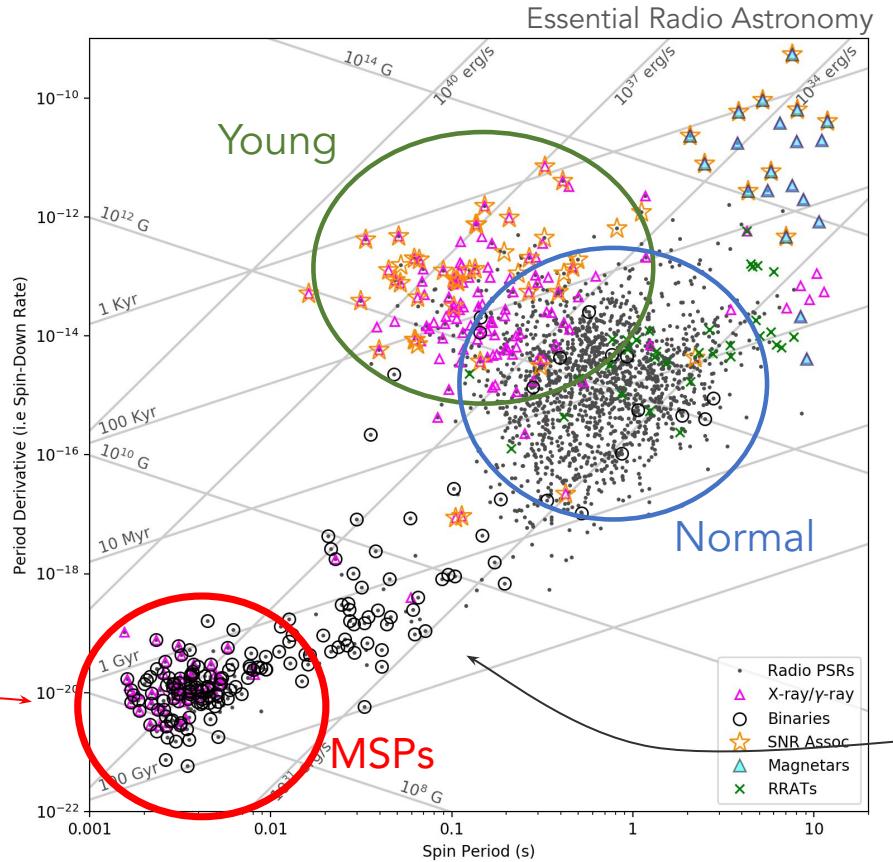


Bill Saxton, NRAO/AUI/NSF

What are Pulsars?

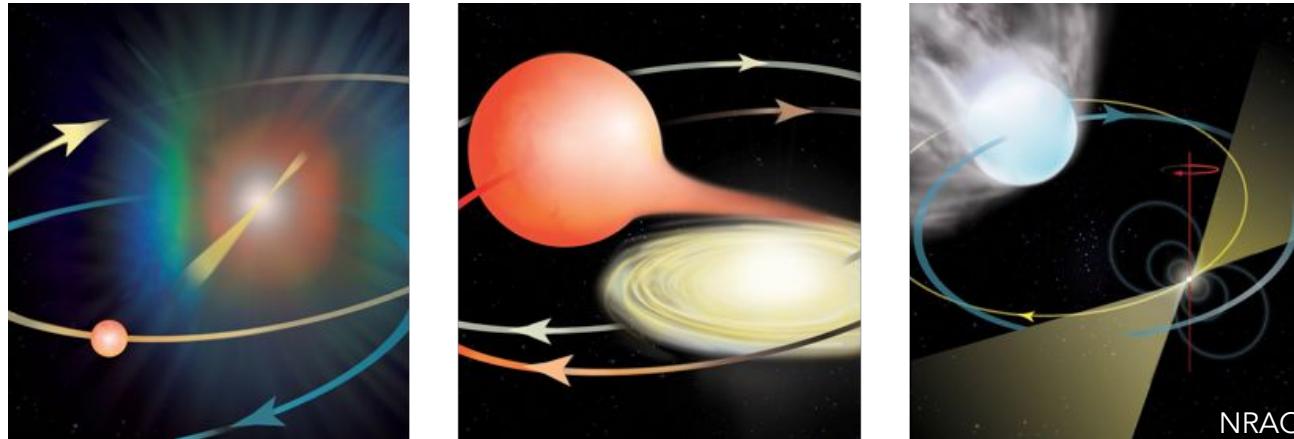
MSPs:
fully recycled,
low-e orbits,
stable, fast!

Low B



Double NS:
~17; mildly
recycled, high-e
orbits, good GR
tests

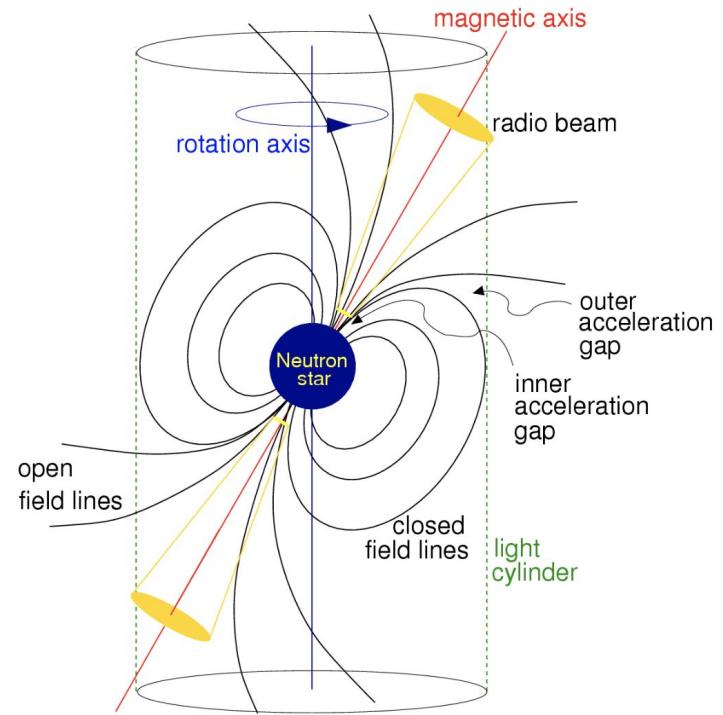
Millisecond Pulsar Recycling



- Low B-fields ($<10^{11}$ G); plasma shielding during accretion
- Spun up by stellar companion (almost always binaries) → recycling
- Not eccentric, very stable rotators

Pulsar Emission

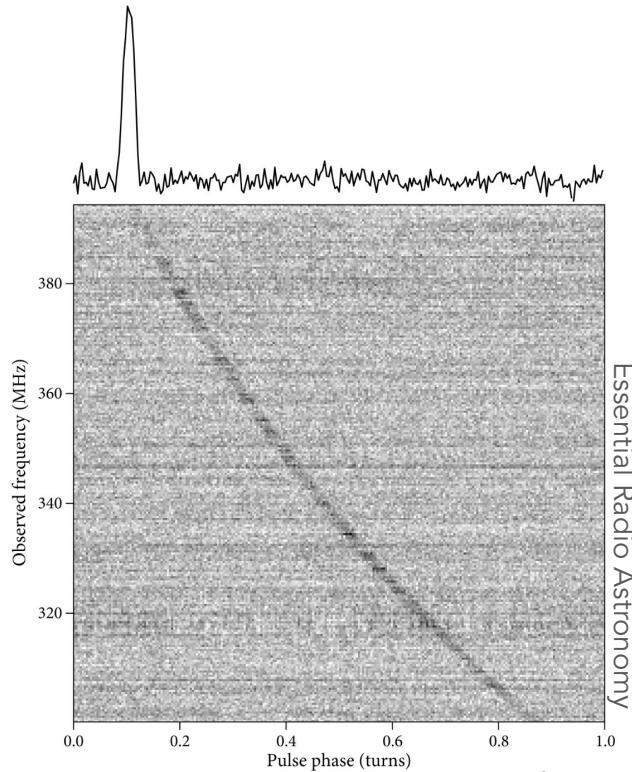
- B field $\rightarrow E$ field pulls charge from surface = magnetosphere
 - Co-rotates with pulsar
 - Light cylinder where plasma velocity approaches c
 - B field lines don't reconnect here
 - e^- emit curvature radiation as they travel along the open field lines
 - Photons produced in the process trigger electron/positron cascade, pairs produce more photons = radio emission



Lorimer & Kramer (2004)

The Interstellar Medium

- Cold, ionized ISM causes interesting and complicated delays
 - Inhomogeneous and turbulent
- Dispersion measure (DM; next slide)
- Diffractive and refractive scintillation = flux density changes
- Scattering → pulse broadening
 - Multi-path propagation; some rays take longer paths
 - Usually proportional to $\sim v^{-4}$



Dispersion Measure

$$\mu = \sqrt{1 - \left(\frac{v_p}{v}\right)^2}$$

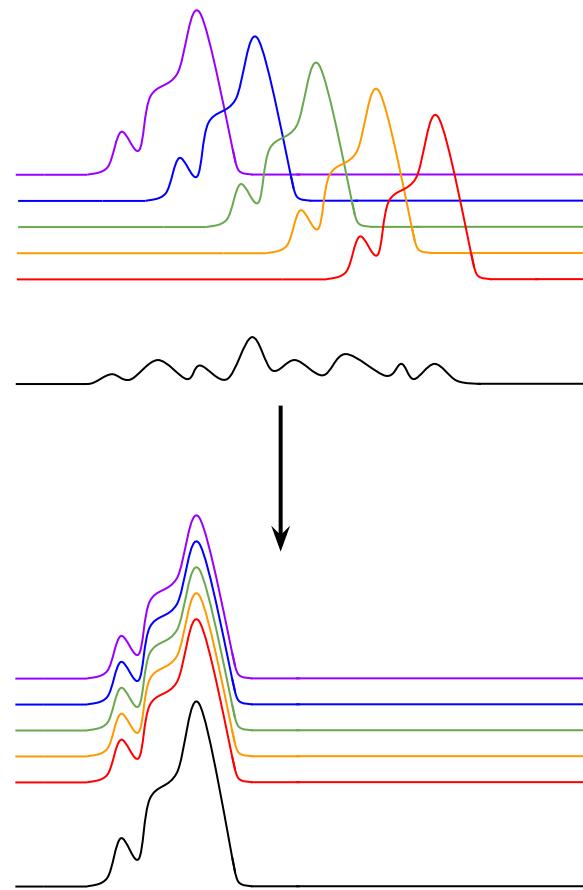
$$v_g \approx c \left(1 - \frac{v_p^2}{2v^2}\right)$$

$$t = \int_0^d v_g^{-1} dl - \frac{d}{c} = \frac{e^2}{2\pi m_e c} \frac{\int_0^d n_e dl}{v^2}$$

$$DM = \int_0^d n_e dl$$

$$t \propto DM v^{-2}$$

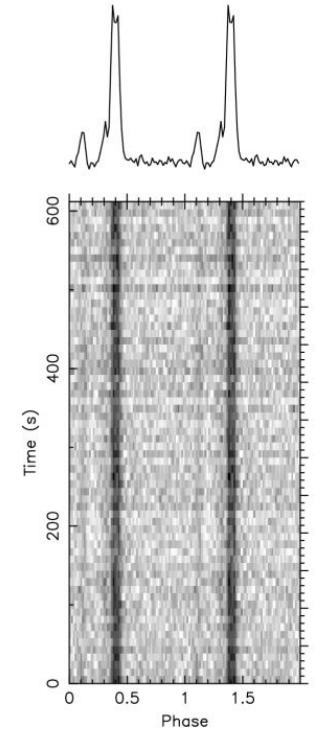
Dispersion measure → estimate distance



How do we Study Pulsars?



- Pretty weak! Need sensitivity
- They emit most at low frequencies (long wavelengths; they have steep spectra)
- Radio telescopes like the Green Bank telescope and the Arecibo telescope (plus FAST, CHIME, etc.)
- Usually observe from $< 1 \text{ GHz} \rightarrow \sim\text{few GHz}$
- High-frequencies, too (NICER, *Fermi-LAT*)
- Dr. Bell-Burnell's pulsar isn't typical; need to fold the data modulo the pulse period to bring out the signal



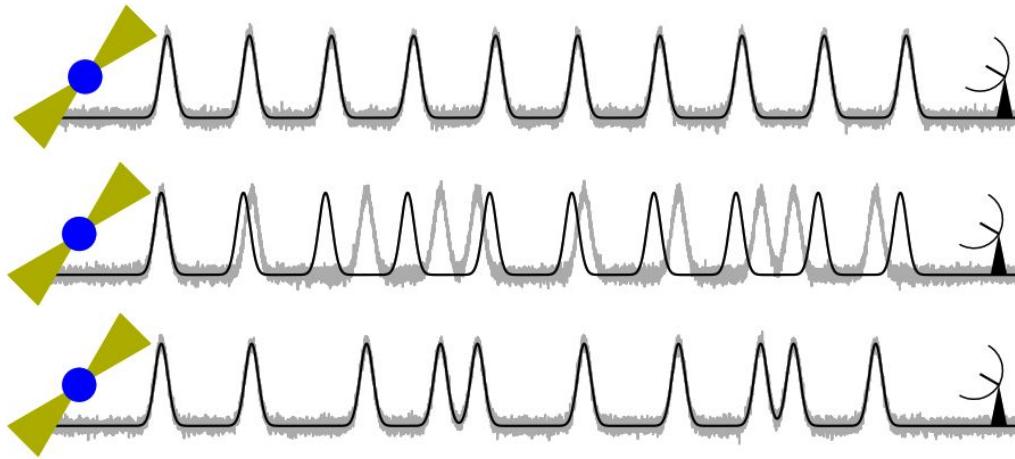
OK, but what are they good for?

- They're space clocks!
- Some of the most accurate measurements ever (comparable to atomic clocks)
- PSR J1737+0747: Period = 4.570136528819804 +/- 0.000000000000001 ms
- How? Pulsar timing!



Getty Images

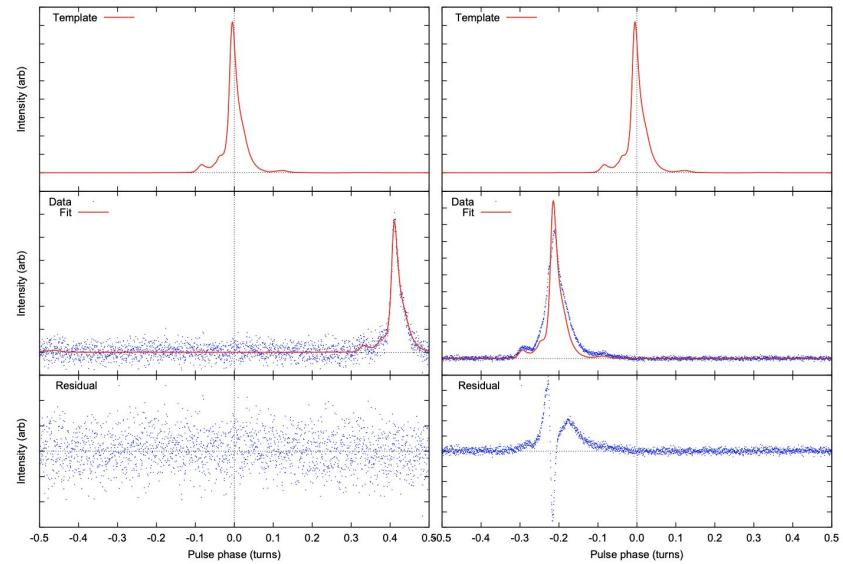
Pulsar Timing = modeling every rotation



- Two steps:
 - Extracting times of arrival (TOAs)
 - Fitting a timing model to the TOAs

Extracting TOAs

- Fold data from many pulses modulo the pulse period P
- Determine shift in rotational phase between the profile and a reference profile (template, usually many observations)
- Cross correlate template and data, usually in the Fourier domain, to find maximum
- The phase shift where correlation is maximized = difference between observed and model predicted pulse phases, averaged over the whole observation

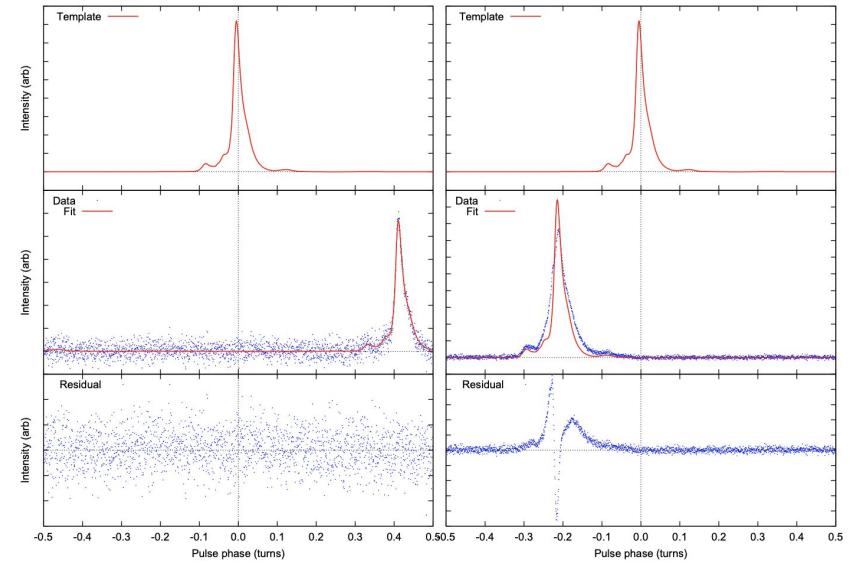


Lommen & Demorest

Left: profile from 1600 MHz GBT, Right:
profile from 750 MHz GBT

Extracting TOAs

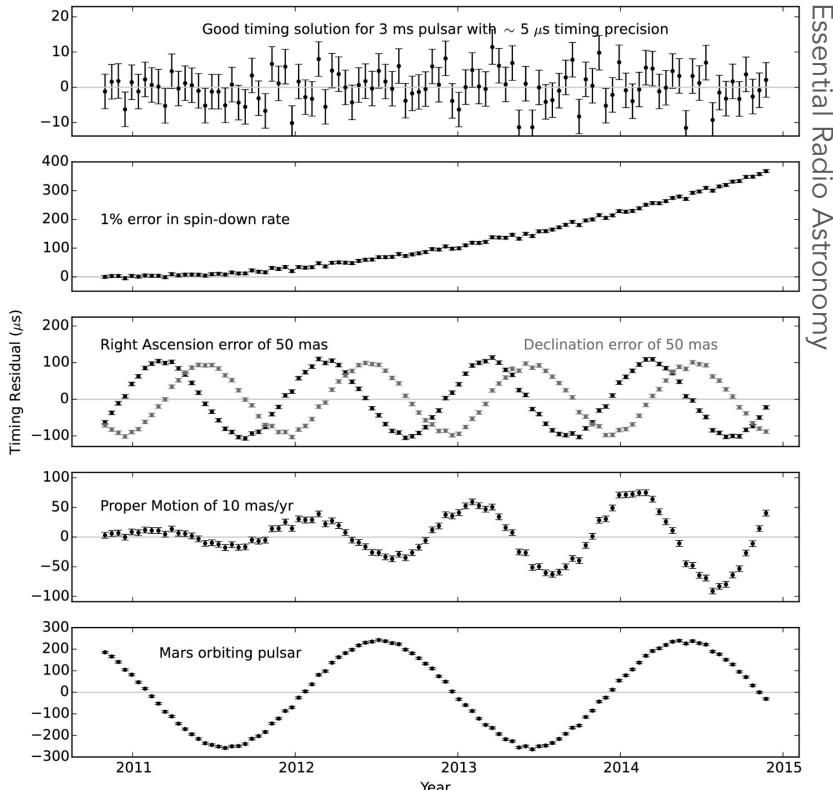
- Turn this into a TOA: subtract model-predicted phase at observation midpoint from measured phase shift, multiply by model predicted pulse period and add it to the reference time
- Time dependent phase of pulsar approximated with Taylor expansion (can measure frequency and frequency derivative):
$$\phi(t) = \phi_0 + f(t - t_0) + \frac{1}{2}\dot{f}(t - t_0)^2 + \dots$$
- Pulsar timing works because the rotational phase difference between each TOA must contain an integer number of rotations
- How well we can measure TOAs depends on S/N, sharpness of peak, etc.



Lommen & Demorest

Left: profile from 1600 MHz GBT, Right:
profile from 750 MHz GBT

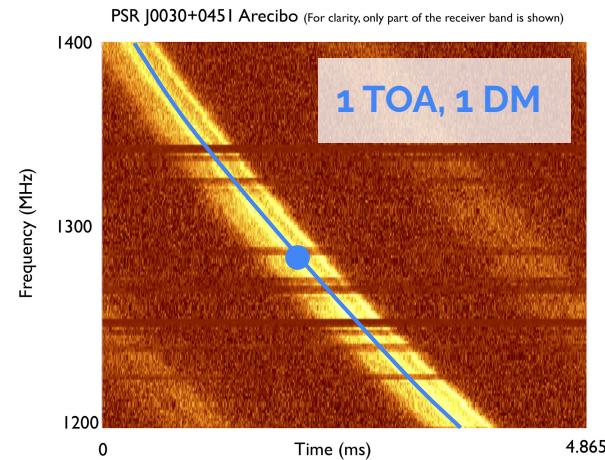
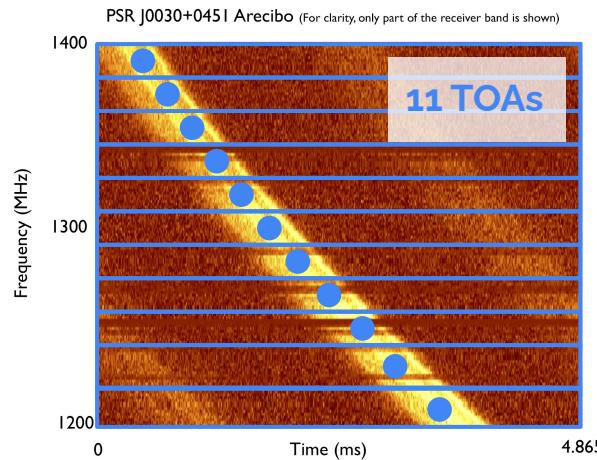
Fitting Timing Models



- Many factors dictate pulse arrival times
 - Most basic are pulse period, period derivative, pulsar position on sky (and Keplerian parameters if it's a binary)
 - DM, GR effects, etc. add more terms to the timing delays
- Difference between measured TOA and model = timing residual

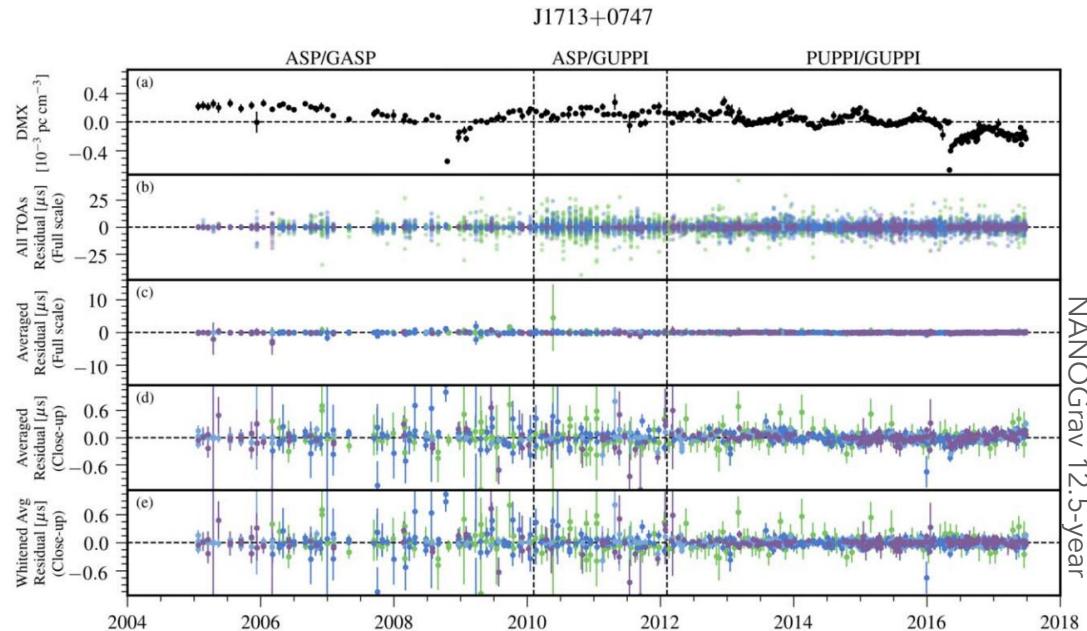
More Timing Details

- Timing models are often fit using chi-square minimization, but other techniques can be used (MCMC)
- Many timing models have hundreds of parameters (there are lots of different ways to describe DM, for example)
- There are multiple ways to extract TOAs: “narrowband” and “wideband” pulsar timing

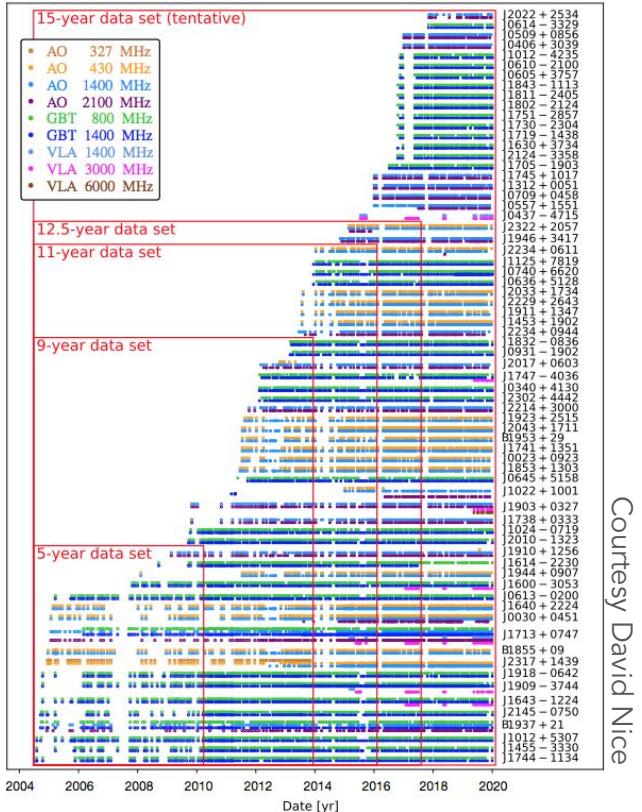


What is a PTA data set?

- Typical things to include:
 - *.par (parameter) files, i.e. best-fit values
 - *.tim (TOA) files
 - DM time series
 - For NG, wideband and narrowband par/tim
 - Versions compatible with different timing software

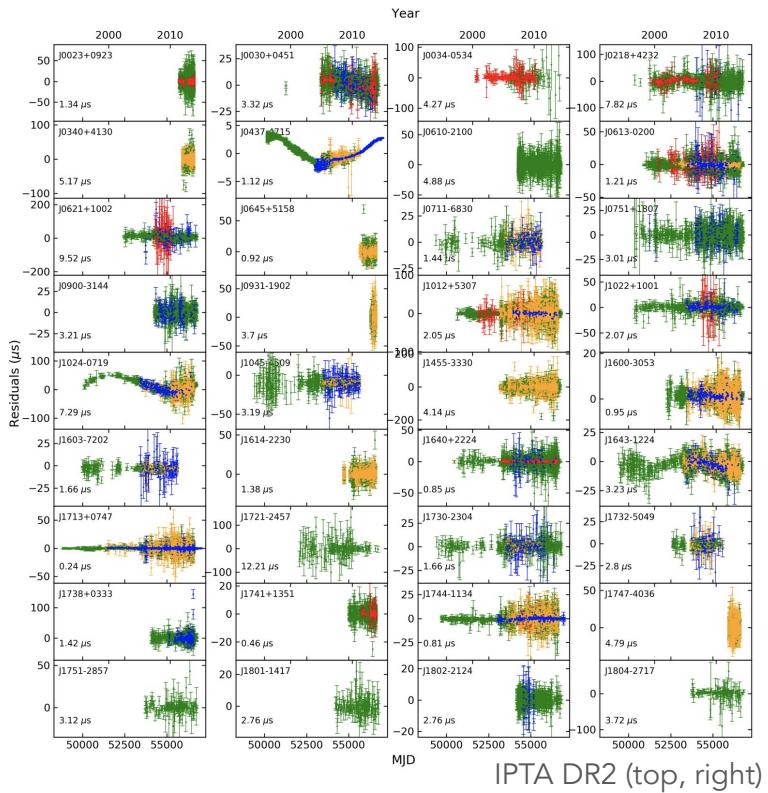


NANOGrav Data Sets

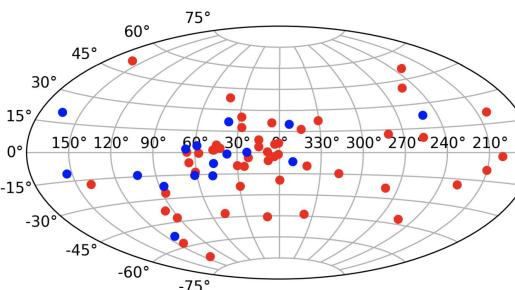


- 12.5-year data set (Alam et al. 2021 a, b)
 - First wideband data set
- 15-year data set (in progress)
 - $47 \rightarrow 68$ MSPs
 - VLA data, including J0437-4715
 - Completely overhauled timing pipeline
 - PINT ("PINT is not TEMPO3")
 - Luo et al. 2021
 - Still releasing TEMPO2 + PINT results, NB and WB data sets

IPTA Data Sets

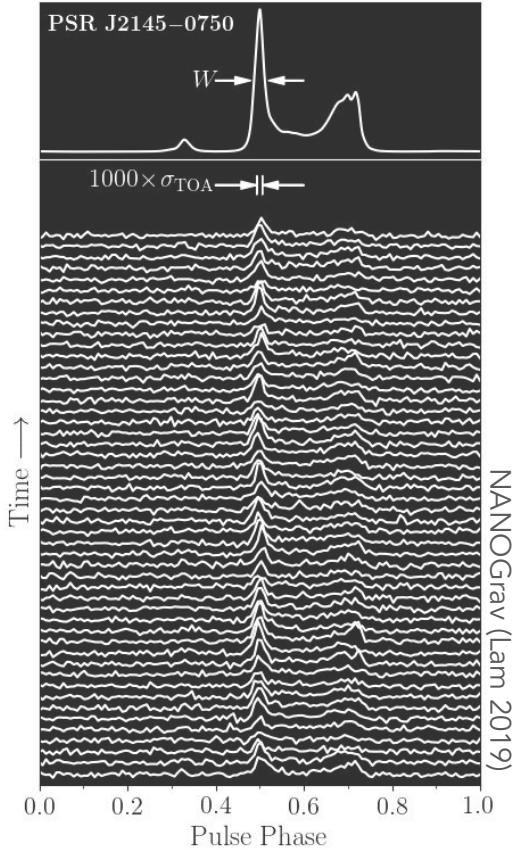


- IPTA = International Pulsar Timing Array
- Other PTAs (EPTA, PPTA, InPTA, MeerTime, CPTA, etc.)
- Combined data set = more sensitivity (in theory, but it's hard)
- IPTA DR2: EPTA DR1 (42 MSPs), PPTA DR1 + extended (20 MSPs), NANOGrav 9-year (37 MSPs)
 - All have their own strengths and weaknesses
 - 65 MSPs total (some overlap)



The “Noise Budget”

- PTAs need *great* timing precision, <1us
- White noise (dominant on short timescales):
 - Radiometer noise
 - Pulse jitter (shape changes between pulses)
- Red noise (dominant over long periods):
 - Achromatic red noise = spin / timing noise
 - Due to irregularities in pulsar rotation
 - Chromatic red noise
 - DM variations
- Deal with these with white and red noise parameters



The timing_analysis pipeline

- **toagen**: raw data → calibration, subbanding, excision → template fitting → TOAs
- **timing_analysis**:
 - **YAML configuration files** make it easy to adjust parameters, track outlier excision and DMX issues, and **log changes!**
 - Jupyter notebook framework for easy use and auto-runs
 - Let's see the PDF output...

```
source: J1022+1001
par-directory: results/
tim-directory: /nanograv/timing/releases/15y/toagen/releases/2021.08.25-9d8d617/
timing-model: J1022+1001_PINT_20220121.nb.par
compare-model: archive/J1022+1001_PINT_20220113.nb.par
toas:
- J1022+1001.430.PUPPI.15y.x.nb.tim
- J1022+1001.L-wide.PUPPI.15y.x.nb.tim

free-params: [ELONG, ELAT, PMELONG, PMELAT, PX, F0, F1, A1, PB, T0, E, OM, FD1, FD2,
free-dmx: Yes
toa-type: NB
fitter: DownhillGLSFitter
n-iterations: 20
ephem: DE440
...
ignore: # toa excision
mjd-start:
mjd-end: 59072.0
snr-cut: 8
bad-toa:
bad-range:
- [57984, 58447, PUPPI]
bad-file:
- [guppi_55625_J1022+1001_0003.15y.x.ff, isolated]
- [guppi_55672_J1022+1001_0005.15y.x.ff, isolated]
prob-outlier: 0.1
...
changelog:
- '2021-09-14 thankful.cromartie NOISE: switched to 20210914.Noise.nb.7d3eff0'
- '2021-09-14 thankful.cromartie REMOVE: AIDOT'
- '2021-09-15 thankful.cromartie NOISE: switched to 20210915.Noise.nb.3a02c6b'
- '2021-09-15 thankful.cromartie READY_FOR: v1.0'
- '2021-09-24 joe.swiggum NOTE: updated AO/GBO coords (pint v0.8.3) and refit'
- '2021-09-30 joe.swiggum NOTE: par file handed off to DWG for v1.0 is J1022+1001_PIT'
- '2021-12-10 joe.swiggum NOTE: we expect PMELAT to be poorly determined given ELAT
```

The timing_analysis pipeline

PSR J1713+0747 narrowband

Summary generated on 2022 Jan 27 (Thu) 20:06:11 GMT by Thankful Cromartie
Input par file: results/J1713+0747_PINT_20220127.nb.par
Input tim file directory: /nanograv/share/15yr/timing/intermediate/20210908.Outlier.
Input tim files:

- J1713+0747.nb_excise.tim

Span: 15.5 years (2005.1 – 2020.6)
Epochs (defined as observations within 6.5-day spans): 395
Wideband data: No
Fitter: DownhillGLSFitter

Timing model

This is the timing model as specified in the input par file, with no additional fitting.

```
# Created: 2022-01-27T20:06:29.234759
# PINT_version: 0.8.4
# User: joyvan
# Host: a5d33d8d9eff
# OS: Linux-3.10.0-862.14.4.el7.x86_64-x86_64-with-glibc2.31
PSR          J1713+0747
EPHEM         DE440
CLOCK         TT(BIPM2019)
UNITS         TDB
START        53393.5613838799041435
FINISH       59071.0046889241220602
CHI2         59007.003379638016
ELONG      256.668699131799997 1 0.0000000198426318595
ELAT        30.700358284037190 1 0.0000000346002920038
```

PDF output: quicker assessment of solutions, **harder to miss problems**, long-lived record of results and steps

Frozen parameters all zero?

Ignoring START, FINISH, CHI2, POSEPOCH, PEPOCH, DM, DMEPOCH, DMX, TZRMJD, TZRFQ, EFAC1, EQUAD1, EFAC2, EFAC3, EFAC4, EFAC5, EFAC6, EFAC7, EFAC8, EFAC9, EFAC10, EQUAD2, EQUAD3, EQUAD4, EQUAD5, EQUAD6, EQUAD7, EQUAD8, EQUAD9, EQUAD10, ECORR1, ECORR2, ECORR3, ECORR4, ECORR5, ECORR6, ECORR7, ECORR8, ECORR9, ECORR10, RNAMP, RNIDX
Yes.

par file fully fit?

par file initial χ^2 : 59007.00962619488
par file final χ^2 : 59007.00962619488
Decrease: 0.0

Fitting produces no major change, all is probably fine.
Largest parameter change during fit was JUMP5 by 0 sigma.

Reduced χ^2 close to 1.00?

Reduced χ^2 is 59007.009626/58976 = 1.000526 (false positive probability 0.463263)
False positive probability is believable

The timing_analysis pipeline

Excised TOAs by Frontend/Backend Combination

Rcvr_800_GUPPI: 8492 TOAs remain (371 cut; 8863 total).
Rcvr1_2_GUPPI: 22053 TOAs remain (1379 cut; 23432 total).
3GHz_YUPPI: 3470 TOAs remain (818 cut; 4288 total).
L-wide_ASP: 864 TOAs remain (670 cut; 1534 total).
Rcvr1_2_GASP: 1081 TOAs remain (548 cut; 1629 total).
Rcvr_800_GASP: 1012 TOAs remain (387 cut; 1399 total).
S-wide_PUPPI: 7440 TOAs remain (2643 cut; 10083 total).
430_PUPPI: 0 TOAs remain (45 cut; 45 total). **100.0% cut!**

Hard to miss when things go **wrong**

Error parameters agree with chains?

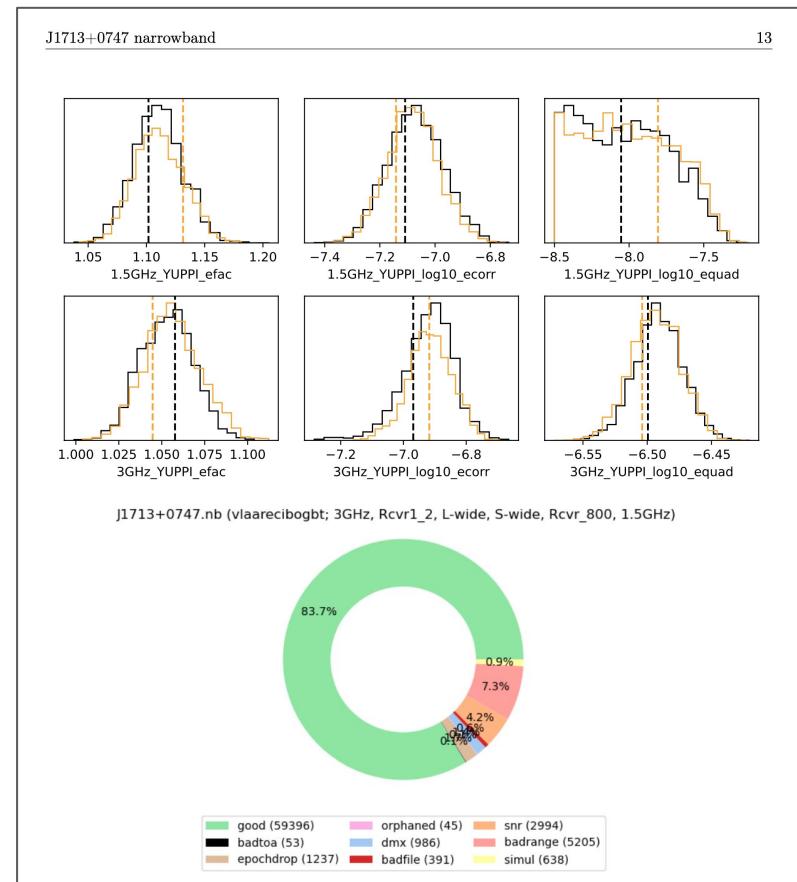
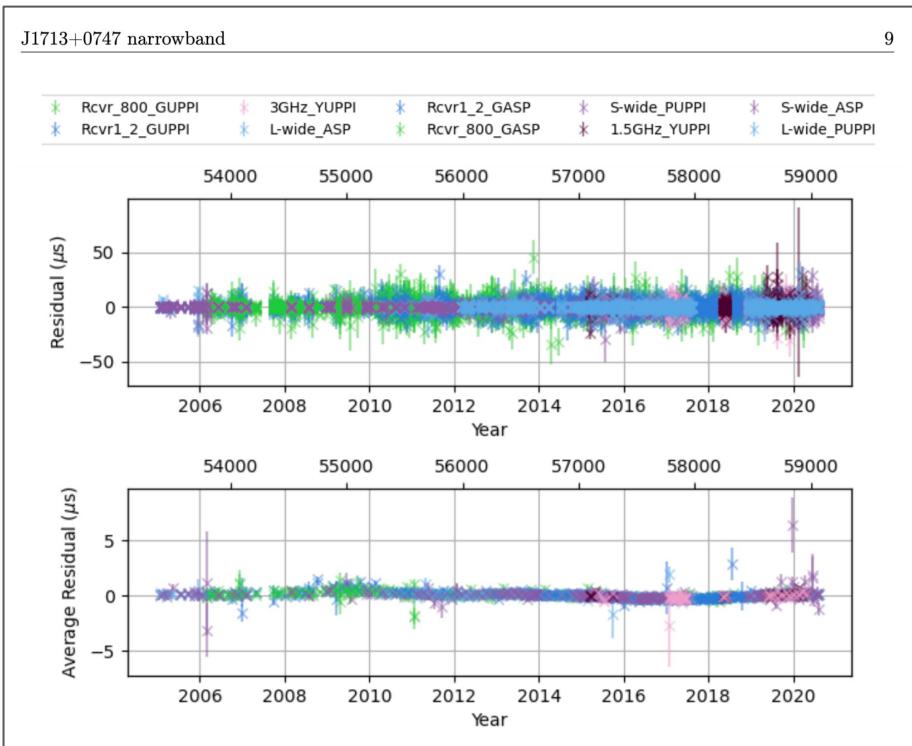
Par file created: 2022-01-27T18:37:59.908153
Par file modified/checked out of git: 2022-01-27T19:30:41.127
Noise chains created: 2021-09-30T13:03:56.000

Permanent documentation of software / data release version

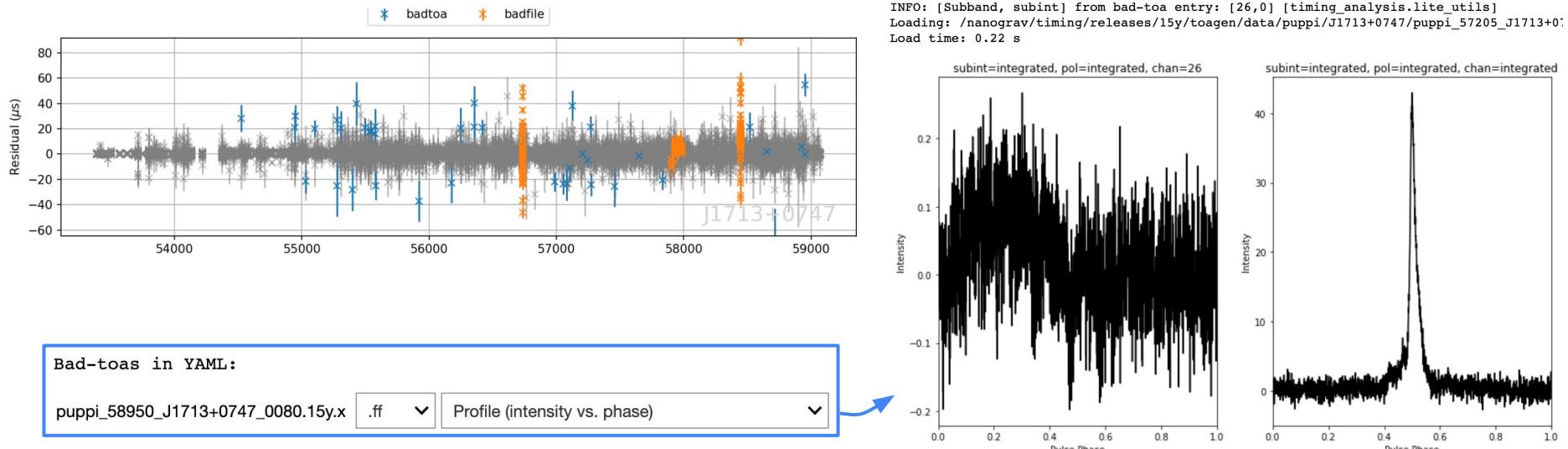
Software versions used in timing_analysis:

PINT: 0.8.4
astropy: 4.3.1
numpy: 1.21.0
python: 3.9.5 | packaged by conda-forge | (default, Jun 19 2021, 00:32:32) [GCC 9.3.0]
enterprise: 3.1.1.dev21+ga06d1f6

The timing_analysis pipeline



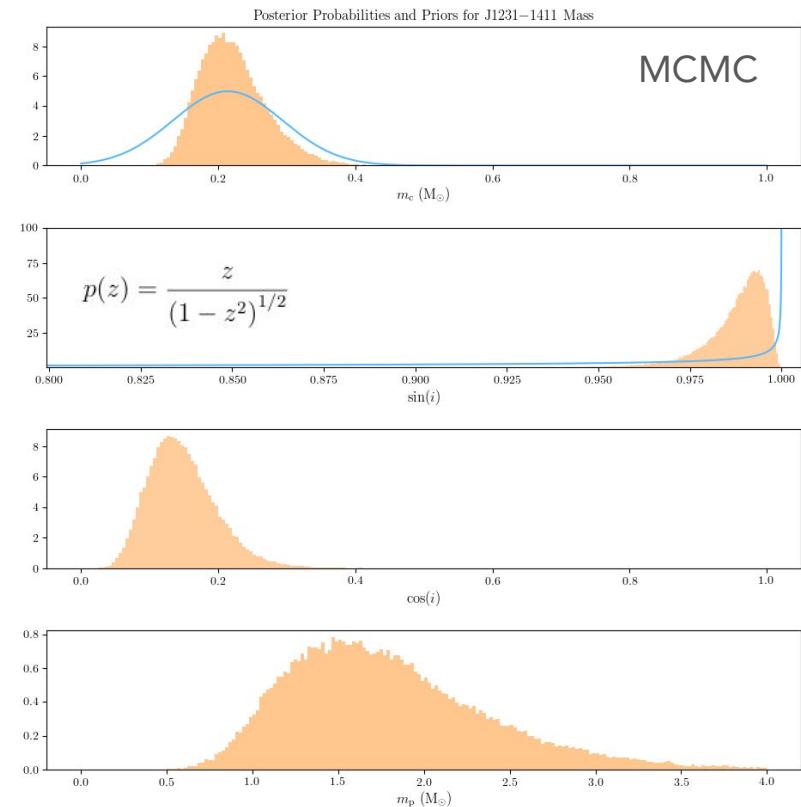
The timing_analysis pipeline



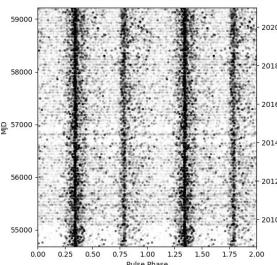
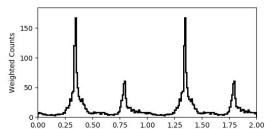
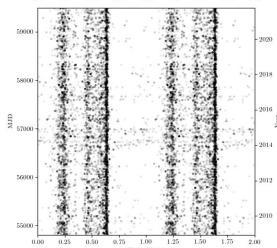
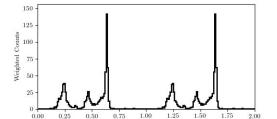
YAML is a record of manual excision (including reasons)

Advanced Timing Techniques

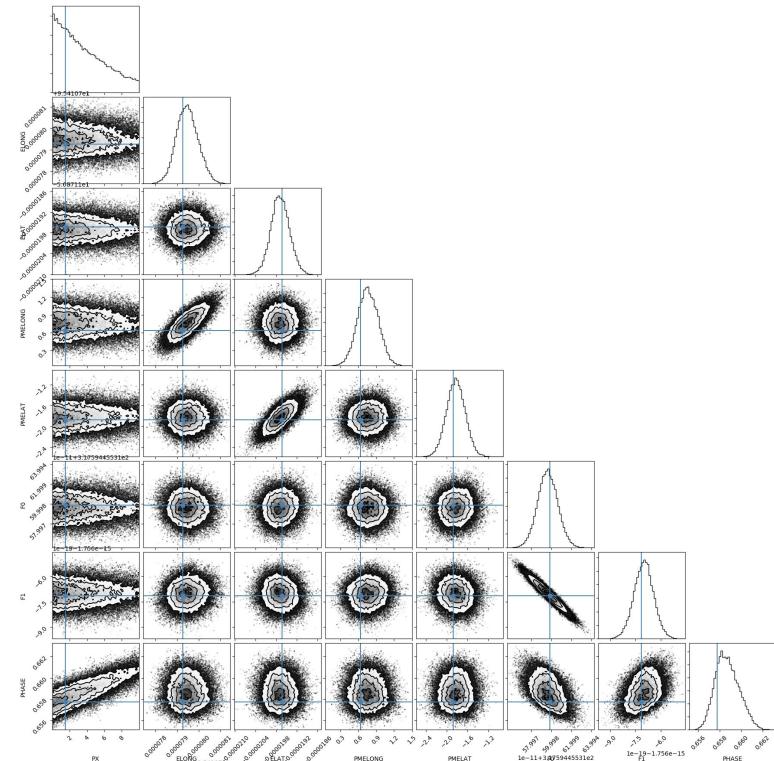
- Bayesian pulsar timing:
 - Uncertainty: parameters and correlations; model non-linear dependence
 - Priors: use physical information
 - Model comparison: compare models with different parameters
 - Nice summary in Vigeland & Vallisneri 2014
- Implemented in `PINT` as `MCMCFitter`
- For now, χ^2 gridding in `TEMPO (2)` / `PINT` helps; implementing in pipeline
- WB data set makes Bayesian timing feasible



High-Frequency Timing



- Detect as few as 1-2 photons per day
 - J1231: 4,627 photons over \sim 11 years \approx 1.1 photon/day for brightest Gamma-ray MSP
- Single-photon timing: Bayesian technique yields timing solutions similar to those in radio
- PINT event_optimize
- This is helpful for NANOGrav
 - New paper in Science about Gamma-ray PTAs!



Conclusions

- Pulsar timing = accounting for each rotation of a pulsar
- Because MSPs can be timed to high precision, they're powerful tools for PTAs and other applications (neutron star masses, probing the ISM, and more)
- PTA data sets consist of best-fit parameters and time-of-arrival measurements
- Noise matters! Short term, long term, intrinsic and extrinsic
- NANOGrav has been building a long-lived pipeline for timing all our MSPs
- Other kinds of timing exist, including advanced fitting techniques and high-frequency (X and Gamma-ray)



Ezreal hopes you have a great time for the next two weeks!