

March 2nd, 2018

Attention: Jia Hao Wu

We are a juice manufacturer that wants to improve how we import frozen concentrated orange juice (FCOJ) for making our products, particularly in the off-season when there is limited local supply in Australia. We currently ship into the ports of Brisbane, Melbourne and Adelaide. Each of these ports feed our local factories and we can predict the demands (barrels) and costs (\$/barrel) involved for each of the next eight quarters:

| Quarter | Brisbane | Melbourne | Adelaide | Cost |
|---------|----------|-----------|----------|-------|
| Q1 | 1400 | 1900 | 2500 | \$890 |
| Q2 | 1850 | 2700 | 2200 | \$972 |
| Q3 | 2950 | 2550 | 850 | \$978 |
| Q4 | 2100 | 1450 | 2300 | \$882 |
| Q5 | 1750 | 2900 | 2850 | \$865 |
| Q6 | 2300 | 3400 | 2150 | \$815 |
| Q7 | 3150 | 2500 | 1200 | \$826 |
| Q8 | 2900 | 1450 | 2300 | \$979 |

Each quarter we use a single ship for imports with a capacity of 10,000 barrels. We currently have 3200 barrels of frozen concentrated orange juice in Brisbane, 4000 barrels in Melbourne, and 3800 barrels in Adelaide. We can store any concentrate on hand at the end of a quarter for a cost of \$35 per barrel.

Please provide us with the optimal cost for delivery over the next eight quarters:

\$37339200

Communication 2

Thank you for your initial estimate. We noticed that your schedule will leave us with no frozen concentrate in storage at the end of the eight quarters. We feel it would be desirable to end up with at least 3000 barrels in storage in each port. Could you take this into account in your proposal?

Please provide us with the optimal cost for delivery over the next eight quarters:

\$46454850

Communication 3

Thank you for your revised estimate. We have realised that the storage amounts you have suggested actually exceed the capacities of our facilities in each port. We have a maximum storage capacity of 3700 barrels in Brisbane, 4300 barrels in Melbourne and 4500 barrels in Adelaide. Could you ensure that we do not exceed these capacities?

Please provide us with the optimal cost for delivery over the next eight quarters:

\$46491750

Communication 4

Thank you for your advice on how to minimise the cost of purchasing our frozen concentrated orange juice for the next eight quarters. We are now looking at our processing operations in Brisbane and would again appreciate your help.

In each quarter we will be using the FCOJ delivered to Brisbane to produce our signature range of Pure Fresh juices, made with fresh local fruit. Each barrel of concentrate can be reconstituted to make 1000 litres of orange juice. We can sell this directly as orange juice or blend it to make other juices, as shown in the following table:

| Regular Juices | | | | | | | |
|------------------------|--|--|--|--|--|--|--|
| Orange Juice | 100% Orange | | | | | | |
| Orange and Mango Juice | 90% Orange, 10% Mango | | | | | | |
| Breakfast Juice | 55% Apple, 28% Pineapple, 15% Orange, 2% Mango | | | | | | |
| Tropical Juice | 65% Apple, 30% Pineapple, 4% Orange, 1% Passionfruit | | | | | | |
| Gourmet Juices | | | | | | | |
| Guava Delight | 80% Apple, 10% Pineapple, 10% Guava | | | | | | |
| Orchard Medley | 50% Apple, 45% Orange, 5% Mango | | | | | | |
| Strawberry Surprise | 90% Apple, 8% Strawberry, 2% Guava | | | | | | |

Thanks to your previous work, the average cost of reconstituted orange juice is \$901 per thousand litres (kL). Taking into account purchasing and processing, the costs of the local fruits are as follows:

| Fruit | Cost (\$/kL) |
|--------------|--------------|
| Apple | 620 |
| Mango | 1300 |
| Pineapple | 800 |
| Passionfruit | 1500 |
| Guava | 710 |
| Strawberry | 1370 |

The amount of orange juice is limited by the demand we noted for our original shipping schedule into Brisbane. (We reconstitute it and will use it for other products as well, so you do not need to

restrict amounts to whole numbers of barrels.) We can obtain any amount of the local fruits at the above prices.

In each quarter we anticipate being able to sell at most the following amounts (kL) of each juice:

| Quarter | Q1 | Q2 | Q3 | Q4 | Q5 | Q6 | Q7 | Q8 |
|----------------------|------|-----|------|-----|------|-----|------|------|
| Orange Juice | 669 | 859 | 1340 | 955 | 787 | 933 | 1689 | 1404 |
| Orange & Mango Juice | 286 | 387 | 593 | 400 | 377 | 401 | 611 | 601 |
| Breakfast Juice | 466 | 746 | 1266 | 900 | 571 | 757 | 1121 | 1054 |
| Tropical Juice | 455 | 531 | 802 | 671 | 499 | 620 | 946 | 946 |
| Guava Delight | 316 | 462 | 508 | 375 | 306 | 464 | 509 | 417 |
| Orchard Medley | 1197 | 808 | 603 | 995 | 1111 | 760 | 632 | 800 |
| Strawberry Surprise | 677 | 714 | 548 | 323 | 622 | 786 | 489 | 407 |

We sell all juice produced for \$1.50 per litre. Please provide us with the optimal profit from producing our juice range over the next eight quarters:

\$28427394

Communication 5

Our transport division have advised us that their delivery trucks must always bring full loads of a single local fruit, equivalent to 10 kL of processed juice per truck. Could you take this into account in your cost calculations?

Please provide us with the revised optimal profit from producing our juice range over the next eight quarters:

\$28228655

Communication 6

Due to staffing difficulties in manufacturing our gourmet juices (Guava Delight, Orchard Medley, and Strawberry Surprise) we would like to only produce two of these juices each quarter. Could you revise your blending schedule accordingly?

Please provide us with the revised optimal profit from producing our juice range over the next eight quarters:

\$25491433

Communication 7

We have realised it is not desirable to have a gourmet juice out of production for more than one quarter in a row. Could you revise your blending schedule accordingly?

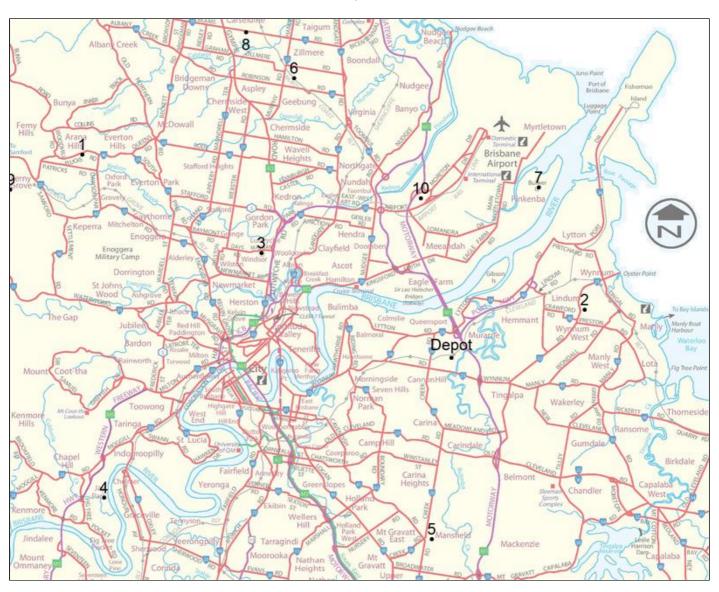
Please provide us with the revised optimal profit from producing our juice range over the next eight quarters:

\$25125359

Communication 8

Thank you for your help in planning our production schedule. Based on the excellent profits you have achieved for us, we are now looking at taking more direct control of our deliveries.

Below you will find a map showing the proposed location of our main depot for Brisbane and ten of the locations where we will need to deliver each day.



We have estimated the following travel costs (\$) between each pair of locations:

| | D | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|---|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| D | _ | 192 | 65 | 99 | 172 | 84 | 146 | 87 | 175 | 216 | 73 |
| 1 | 192 | _ | 241 | 94 | 157 | 238 | 103 | 210 | 94 | 37 | 156 |
| 2 | 65 | 241 | _ | 150 | 236 | 126 | 170 | 60 | 200 | 269 | 91 |
| 3 | 99 | 94 | 150 | _ | 133 | 152 | 81 | 130 | 101 | 119 | 77 |
| 4 | 172 | 157 | 236 | 133 | _ | 151 | 211 | 244 | 223 | 147 | 199 |
| 5 | 84 | 238 | 126 | 152 | 151 | | 220 | 168 | 247 | 251 | 156 |
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                                        130 110
   216
           269 119 147 251 140 242 130
       37
                                54 110 188
10
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       156
          91
                77
                   199 156
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Please provide us with the minimum cost for travelling from the depot to visit each of the locations and then return to the depot:

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