

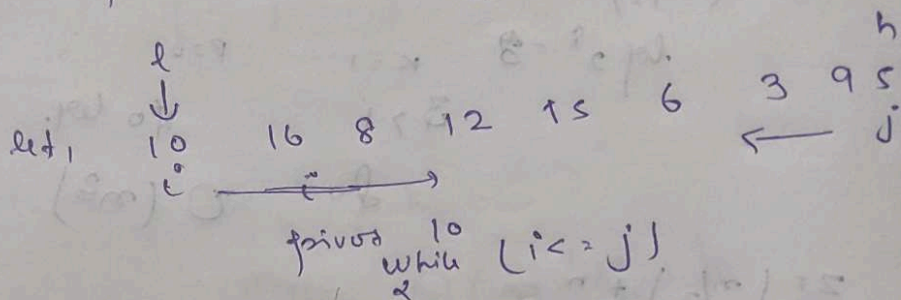
# Quick sort

Approach:-

Step 1: select our element  $\uparrow$

Step 2: On that element all right side has been smaller than that

Step 3:- Left side be greater than that element



~~check~~ Increment  $i$  until you find element is  $> 10$

$$16 > 10$$

so, 10 16 . . .

Decrement  $j$  until you find element smaller than 10

5  
 $j$   
the exchange then

10 5 8 12 15 6 3 9 16

$i \rightarrow$   $j \leftarrow$

Increment  $i$  — next greater elem is 12

decre  $j$  — next smaller elem is 3  
exchange

10 5 8 9 15 6 3 12 16  
 $i \quad j$

Continue

Now 15 > 10  
 $i$

& 3 < 10  
 $j$

Swap

10 5 8 9 3 6 15 12 16  
 $i \rightarrow j$

10 5 8 9 3 6 15 12 16  
 $j \quad i$

Stop

doesn't swap  $i$  &  $j$  bec  
 both  $i > j$   
 we found pos. of pivot

i.e.  $j$

6 5 8 9 3 10 15 12 16  
 fixed

Now, perform Quick Sort  
 Recursively.



partition (l, h)

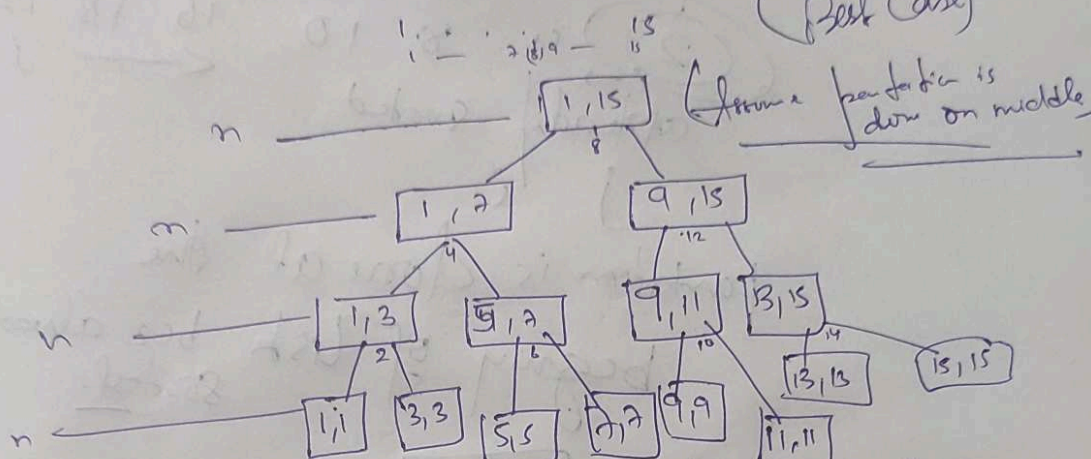
```
*  
    pivot = A[l];  
    i = l, j = h;  
    while (i < j)  
    {  
        do  
        {  
            i++;  
        } while (A[i] ≤ pivot);  
        do  
        {  
            j--;  
        } while (A[j] > pivot);  
        if (i < j)  
            swap (A[i], A[j]);  
        swap (A[l], A[j]);  
    }  
    return j;
```

Quick Sort (l, h)

```
* if (l < h) // at least two element  
{  
    j = partition (l, h);  
    Quick Sort (l, j);  
    Quick Sort (j+1, h);  
}
```

# Analysis of Quick sort $O(n \log n)$

(Best Case)



Here compare the element and exchange them.

So,  $n$  times

$n$  — partition (1, n)

$n \times n \times \dots$  (height of tree)

they all are divide by 2 again by 2

$n/2, n/2^2, \dots$

$n/2^k = 1$

$k = \log_2 n$

$O(n \times \log_2 n)$

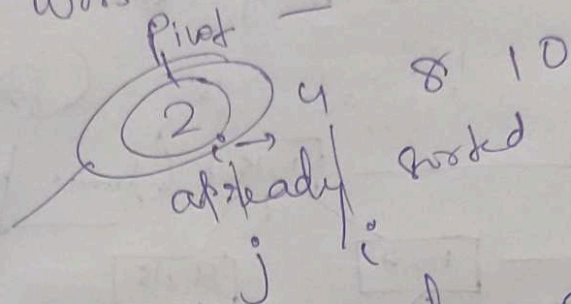
partition is done always on middle

Only when we know median should be tested — 1 2 3 4 5 6 7

by It is not possible always

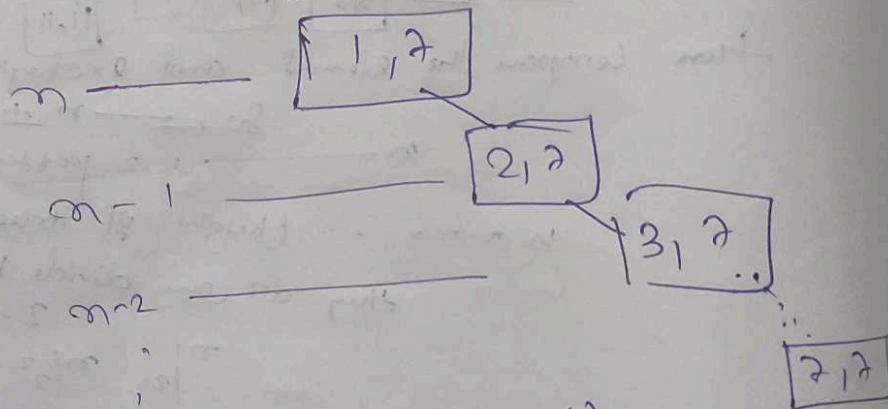


Worst case



16 18 12  
← j

partition is done at the  
beginning of list bc 2 already  
sorted



$$1 + 2 + 3 + \dots + n = \frac{n(n+1)}{2}$$

$$= O(n^2) \text{ (worst case)}$$

So, It is problem

So, for solving this

don't select 1st element as  
pivot

① Select the middle element  
as pivot

② Random element is pivot