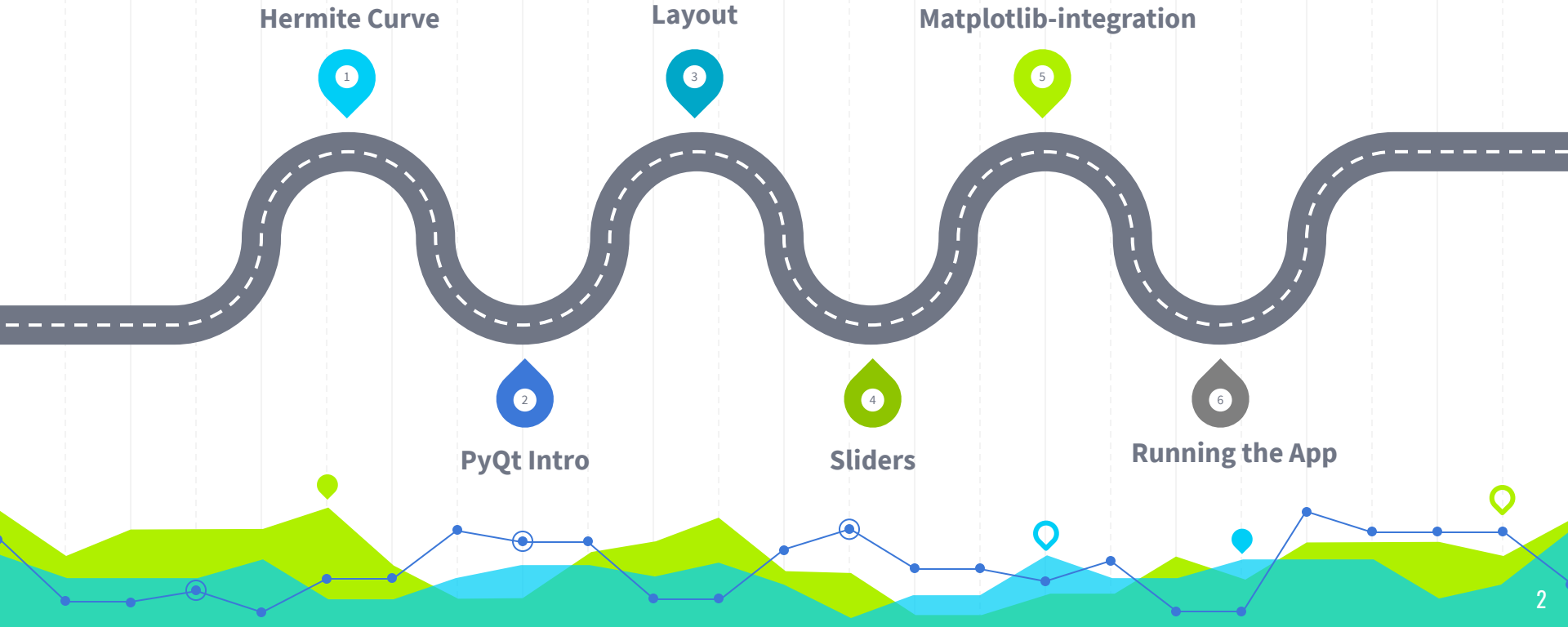


HERMITE CURVE

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ROADMAP



Introduction to Hermite Curve

A cubic Hermite spline or cubic Hermite interpolator is a spline where each piece is a third-degree polynomial specified in Hermite form, that is, by its values and first derivatives at the end points of the corresponding domain interval.

A Hermite Curve is made by fitting:

- The Endpoints (P1, P2)
- The 1st Derivative at the Endpoints (R1, R2)

The 2 forms of Hermite Curves are as follows:- Algebraic form and Matrix form

Algebraic form is given by :

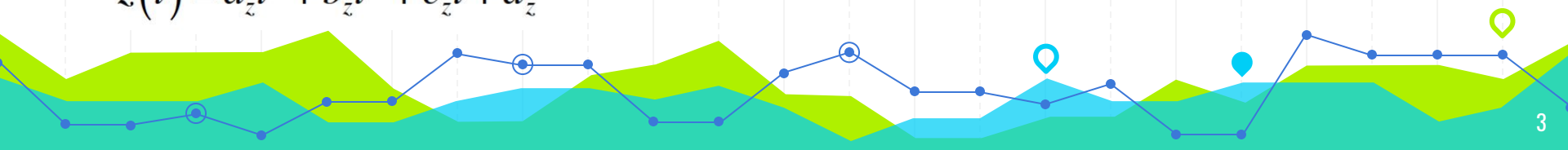
$$x(t) = a_x t^3 + b_x t^2 + c_x t + d_x$$

$$y(t) = a_y t^3 + b_y t^2 + c_y t + d_y$$

$$z(t) = a_z t^3 + b_z t^2 + c_z t + d_z$$

This algebraic form is reduced in vector form as $\mathbf{p}(t) = \mathbf{a}t^3 + \mathbf{b}t^2 + \mathbf{c}t + \mathbf{d}$

Where \mathbf{t} varies from 0 to 1.



MATRIX FORM

```
def update_plot(self):  
  
    p1 = self.s1.value()  
    p2 = self.s2.value()  
    t = np.loadtxt('data.csv', delimiter=',')  
    r1 = self.s3.value()  
    r2 = self.s4.value()  
  
    s = (2*(t**3) - 3*(t**2) + 1)*p1 + (-2*(t**3) + 3*(t**2))*p2 + (t**3 - 2*(t**2) + t)*r1 + (t**3 - t**2)*r2
```

- The $[a \ b \ c \ d]$ matrix formed is known as Hermite basis transformation matrix. Equation $\mathbf{p}(t) = at^3 + bt^2 + ct + d$ can be written in matrix form as: $\mathbf{p}(t) = [t^3 \ t^2 \ t \ 1] * [a \ b \ c \ d]^T$
- After applying end conditions that is the values of tangents and points are known we get the following equation for the Hermite Curve as:

$$H(t) = (2t^3 - 3t^2 + 1)P_1 + (-2t^3 + 3t^2)P_2 + (t^3 - 2t^2 + t)R_1 + (t^3 - t^2)R_4, \quad \text{where } t \text{ varies from } 0 \text{ to } 1.$$

- Input for t is taken from the 'data.csv' file.
- Values for the points P_1 , P_2 , R_1 & R_2 are assigned using `value()` function which gives the value of the slider.

PyQt5



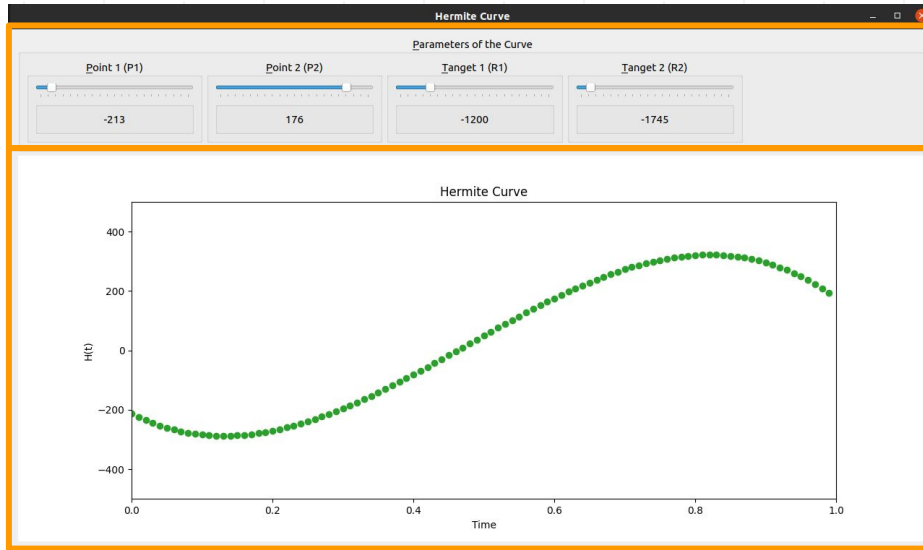
- PyQt5 is a library that can be used to create graphical user interfaces (GUI).
- In our project, we'll be using predefined classes and widgets available in PyQt5 to create the GUI for our program.

We've made the use of following widgets:

```
QGridLayout(), QGroupBox(), QLabel(),  
QSlider(), QPushButton(),  
QHBoxLayout(), QApplication(),  
QVBoxLayout(), QWidget() imported from  
QtWidgets, and Qt imported from  
Qt.core()
```

```
from PyQt5.QtWidgets import QGridLayout, QGroupBox, QLabel, QSlider, QPushButton, QHBoxLayout, QApplication, QVBoxLayout, QWidget  
from PyQt5.QtCore import Qt
```

Layout



```
def init_ui(self):  
    #visual box for the buttons and the graph  
    grid_box = QGridLayout()  
    grid_box.addWidget(self.create_grp_coeff())  
    self.canvas = FigureCanvas(plt.Figure(figsize = (15,6)))  
    grid_box.addWidget(self.canvas)  
    self.insert_plot()  
  
    self.setLayout(grid_box)  
    self.setWindowTitle("Hermite Curve")  
    self.show()
```

This layout is created using `QGridLayout()` widget. In Which two another widgets are added namely `create_grp_coeff()` and `canvas` to plot graph.

Code of slider for Point (P1) :

```
def grp_1(self):
    #slider 1 --->
    self.s1 = QSlider(Qt.Horizontal)
    self.s1.setMinimum(-250)
    self.s1.setMaximum(250)
    self.s1.setValue(0)
    self.s1.setTickInterval(25)
    self.s1.setTickPosition(QSlider.TicksBelow)
    self.s1.valueChanged.connect(self.update_label_1)

    self.label1 = QLabel('0', self)
    self.label1.setAlignment(Qt.AlignCenter | Qt.AlignVCenter)
    self.label1.setMinimumWidth(80)

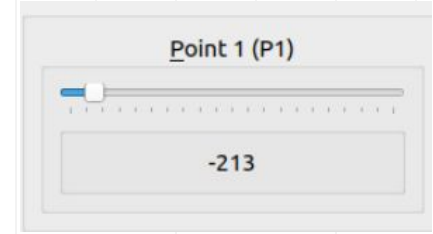
    self.s1.valueChanged.connect(self.update_plot)

    grp_box_1 = QGroupBox("&Point 1 (P1)")
    grp_box_1.setAlignment(Qt.AlignHCenter)
    h_box_1 = QVBoxLayout()
    h_box_1.addWidget(self.s1)

    grp_label_1 = QGroupBox()
    h_box_label_1 = QVBoxLayout()
    h_box_label_1.addWidget(self.label1)

    grp_label_1.setLayout(h_box_label_1)
    grp_box_1.setLayout(h_box_1)
    h_box_1.addWidget(grp_label_1)
    return grp_box_1
```

Sliders

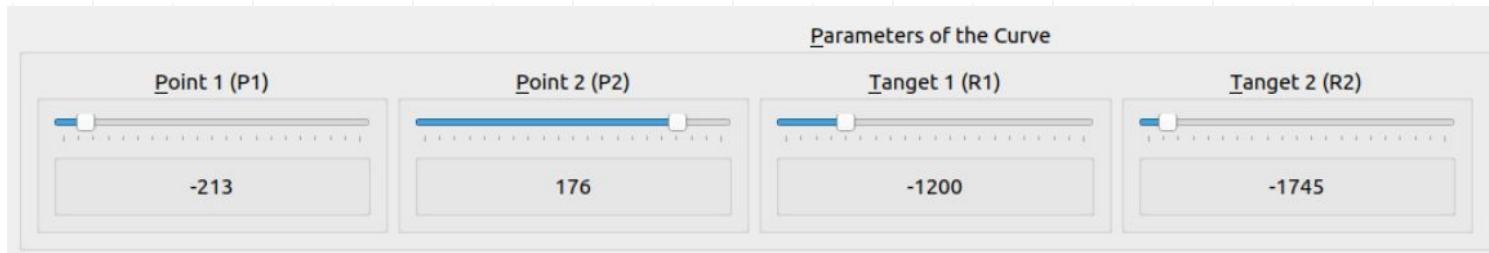


- Sliders are made using the using the Widget `QSlider` from the class `QWidgets`.
- Sliders are connected to the function `update_Label_(i)` function which defines the value of the slider with the help of the label attached to it.
- Label is made using the Widget `QLabel`.
- Also sliders are connected to the function `update_plot` which updates the plot when the slider is moved.
- Sliders are defined in a vertical box adding slider on the top of the label.
- Similarly all the sliders are defined and then added together in a horizontal box defined using `QHBoxLayout()`.

All Sliders together

```
def create_grp_coeff(self):
    group_box = QGroupBox("&Parameters of the Curve")
    group_box.setAlignment(Qt.AlignHCenter)
    H_box = QHBoxLayout()
    H_box.setAlignment(Qt.AlignCenter)
    H_box.addWidget(self.grp_1())
    H_box.addWidget(self.grp_2())
    H_box.addWidget(self.grp_3())
    H_box.addWidget(self.grp_4())
    H_box.addStretch()
    group_box.setLayout(H_box)
    return group_box
```

- Using `QGroupBox()` we define group_box layout to add a
- `H_box` defined using `QHBoxLayout()`
- In the `H_Box` we added all the slider widgets
- This Layout looks like this ↓



Matplotlib Integration

```
def init_ui(self):  
    #visual box for the buttons and the graph  
    grid_box = QGridLayout()  
    grid_box.addWidget(self.create_grp_coeff())  
    self.canvas = FigureCanvas(plt.Figure(figsize = (15,6)))  
    grid_box.addWidget(self.canvas)  
    self.insert_plot()  
  
    self.setLayout(grid_box)  
    self.setWindowTitle("Hermite Curve")  
    self.show()
```

```
def insert_plot(self):  
    self.ax = self.canvas.figure.subplots()  
    self.ax.set_xlim([0,1])  
    self.ax.set_ylim([-500,500])  
    self.ax.set_title("Hermite Curve")  
    self.ax.set_xlabel("Time")  
    self.ax.set_ylabel("H(t)")  
    self.graph = None
```

- Using FigureCanvas, canvas for Hermite is defined. Then widget is added in the grid_box defined using QGridLayout().
- insert_graph() function defines the basic properties of the graph such as xlim, ylim, title and labels for the axes.
- Self.graph is “None” initially but it plots the graph once the values of the parameters are changed through the sliders

Exception Handling:

```
try:
    p1 = int(p1)
except ValueError:
    p1 = 0

try:
    p2 = int(p2)
except ValueError:
    p2 = 0

try:
    r1 = int(r1)
except ValueError:
    r1 = 0

try:
    r2 = int(r2)
except ValueError:
    r2 = 0

if self.graph:
    self.graph.remove()

self.graph = self.ax.scatter(t,s)
self.canvas.draw()
```

Running Application

```
if __name__ == "__main__":  
    app = QApplication(sys.argv)  
    a_window = Window()  
    a_window.init_ui()  
    sys.exit(app.exec_())
```

- Using QApplication an app is declared and a_window object is defined
- Using init_ui() GUI for graph is displayed.
- App can be run by running the command in the terminal : `$ python3 app.py`
- Github Link : [Here](#)

Thank you!

