$C=< x^4+x^2+x+1>$, цикличен код с дължина 7, над F_2 $g(x)=x^4+x^2+x+1$, deg(g(x))=4=n-k, n=7, k=n-4=7-4=3,

С е [7, 3] цикличен код над F_2

$$h(x) = \frac{x^7 - 1}{g(x)} = \frac{x^7 - 1}{x^4 + x^2 + x + 1} = x^3 - x - 1 + \frac{2x^2 + 2x}{x^4 + x^2 + x + 1},$$

тъй като $2x^2 + 2x \equiv 0 \pmod{2}$, то следва, че $g(x) \mid x^7 - 1$ без остатък

в F_2 , $x^3-x-1\equiv x^3+x+1\ (mod\ 2)$, което е пораждащ полином на дулания код на $\mathcal C$

$$H = \begin{array}{c} 1110100 \\ H = 0111110 \\ 0010001 \end{array}$$

a)

 $H\ e\ 3x$ 7 матрица, тогава n-k=3, n=7, от тук, k=4. $H_3[7,4,3]_2$

b)

v е код, тогава и само тогава, когато $vH^T=0$.

Това са векторите

 $\{(0,\!0,\!0,\!0,\!0,\!0,\!0),(1,\!1,\!0,\!1,\!0,\!0),(0,\!1,\!0,\!0,\!1,\!0,\!0),(1,\!0,\!0,\!1,\!1,\!0,\!0),$

(1,1,0,0,0,1,0), (0,0,0,1,0,1,0), (1,0,0,0,1,1,0), (0,1,0,1,1,1,0),

(0,1,1,0,0,0,1), (1,0,1,1,0,0,1), (0,0,1,0,1,0,1), (1,1,1,1,1,0,1),

(1,0,1,0,0,1,1), (0,1,1,1,0,1,1), (1,1,1,0,1,1,1), (0,0,1,1,1,1,1)

16 на брой.

c)

$$G = \begin{matrix} 1000111 \\ 0100101 \\ 0010110 \\ 0001011 \end{matrix}$$

Намираме (0,1,0,1)G = (0,1,1,0,1,1,0), (1,0,1,0)G = (1,1,0,1,0,1,1)

- d) n k = 3, n = 7, тогава [7, 3, 4] линеен код.
- е) Умножаваме всички бинарни вектори с дължина 3 с матрицата Н и получаваме

$$\{(0,0,0,0,0,0,0),(1,1,0,1,0,0,1),(1,0,1,1,0,1,0),(0,1,1,0,0,1,1),(1,1,1,0,1,0,0),\\$$

$$(0,0,0,1,1,1,1),(0,1,1,0,1,1,0),(1,0,1,1,1,1,1,1)$$

8 на брой.