

VISVESVARAYA TECHNOLOGICAL UNIVERSITY
“JnanaSangama”, Belgaum -590014, Karnataka.



LAB REPORT
on
Artificial Intelligence (23CS5PCAIN)

Submitted by

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in partial fulfillment for the award of the degree of
BACHELOR OF ENGINEERING
in
COMPUTER SCIENCE AND ENGINEERING



B.M.S. COLLEGE OF ENGINEERING
(Autonomous Institution under VTU)
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**B.M.S. College of Engineering,
Bull Temple Road, Bangalore 560019**
(Affiliated To Visvesvaraya Technological University, Belgaum)
Department of Computer Science and Engineering



CERTIFICATE

This is to certify that the Lab work entitled “Artificial Intelligence (23CS5PCAIN)” carried out by **VIJAY J (1WA23CS040)**, who is bonafide student of **B.M.S. College of Engineering**. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements in respect of an Artificial Intelligence (23CS5PCAIN) work prescribed for the said degree.

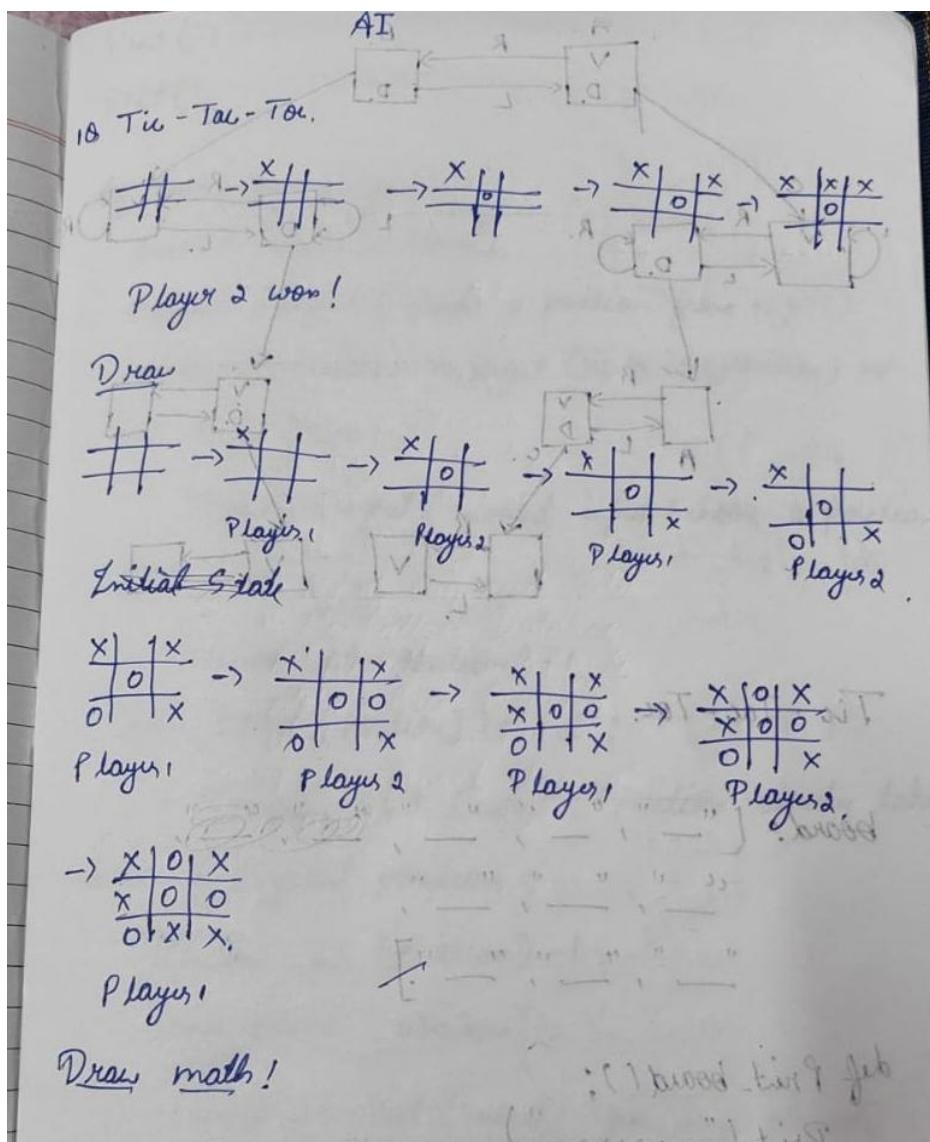
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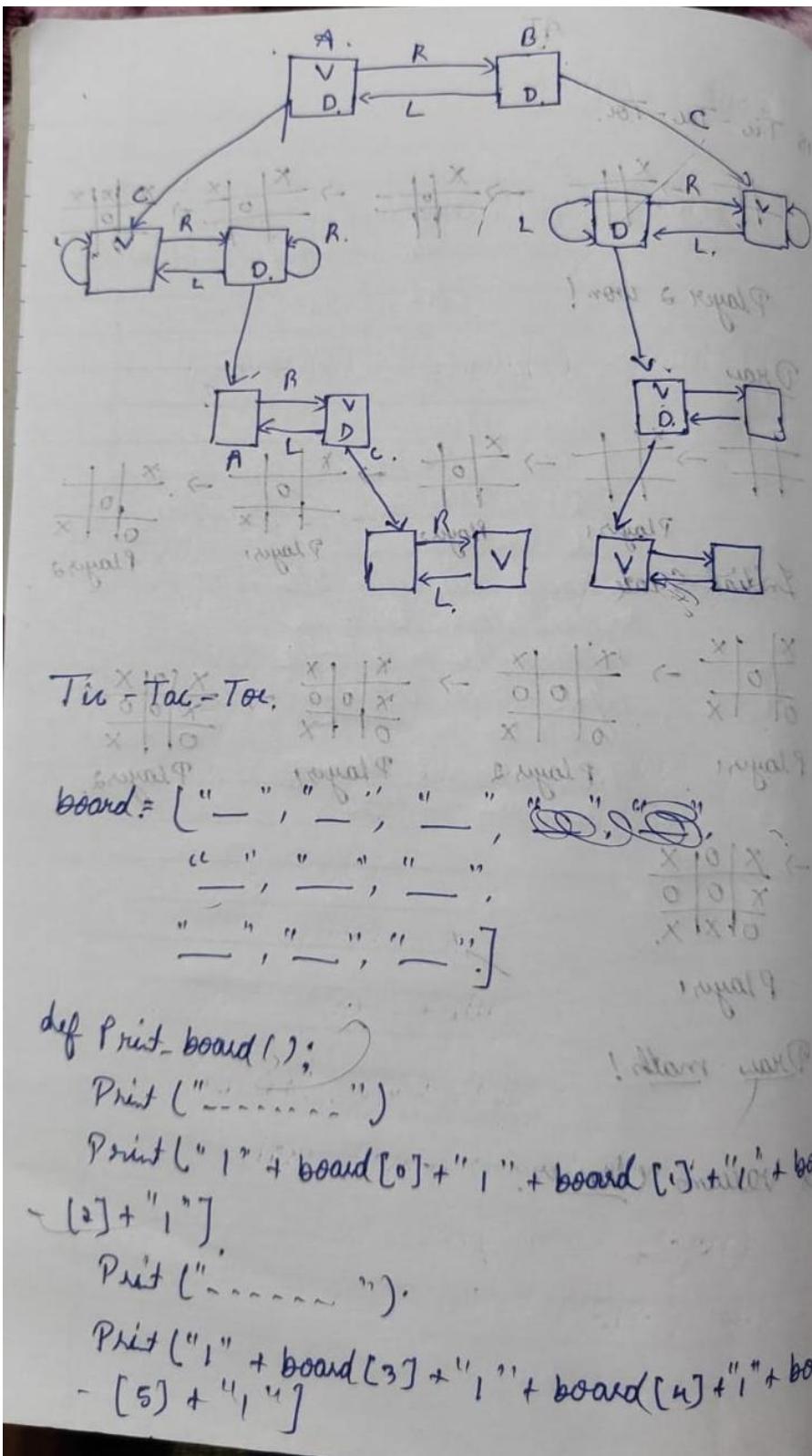
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Program 1 - Tic Tac toe and Vacum Cleaner

Algorithm



Code



```
Print("1" + board[6] + "1" + board[7] + "1" + board[8] + "\n")  
Print("-----\n" + "[0] board))
```

```
def take_turn(player):  
    board = [0] * 9
```

```
    Print(f"Player's turn")
```

```
    position = input("choose a position from 1-9: ")
```

```
- while not position.isdigit() or int(position) not  
- in range(1, 10):
```

```
    position = input("invalid input choose a position  
from 1-9: ")
```

```
    position = int(position) - 1
```

```
    while board[position] != " ":
```

```
        position = int(input("position already taken  
choose a different position: ")) - 1
```

```
    position = int(position) - 1
```

```
    while board[position] != " ":
```

```
        position = int(input("position already  
taken. choose a different position: ")) - 1
```

```
    board[position] = player
```

```
    Print(board)
```

```
    print("next = next - 1")
```

```
def check-win(player):  
    return ((board[0] == board[1] == board[2]) and  
           player) or
```

```
(board[3] == board[4] == board[5] == player)  
or (board[6] == board[7] == board[8] == player)
```

```
def check-tie():  
    return " " not in board
```

```
def play-game():  
    print("Welcome to Tic Tac Toe!")
```

```
print(board[0])  
current-player = 'X'  
game-over = False
```

```
while not game-over:  
    take-turn(current-player)  
    if check-win(current-player):  
        print(f"current-player wins!")  
        game-over = True
```

elif check_tie():

Print("It's a tie!")

game_over = True

: (current) mailing file

else:

: ("O" == [V] user, and "O" == [V] user) if current_player -
current_player = "O" if current_player -
= "X" else "X"

Play-game().

2/9/25

: (O) user-mail file

(O = V)

: (current) mailing file status

: ("G" == [V] user) if

: ("O" == [V] user)

("! mailed" "V" "need") time?

: ("OW" == [V] user) file

: (O == V) if

I = +V

I = -V : else

loop ("I mailed need WA") time?

: (mailed) mailing-mail

7/0

I mailed O need

I mailed I need

I mailed need WA

Vacuum Cleaner

rooms = ['0', '0']; /* int. o & i */
 def fullclean (rooms):
 if (rooms[0] == "ND" and rooms[1] == "ND"):
 return True
 else:
 return False.

def clean_rooms ():
 v=0;
 while not fullclean (rooms):
 if (rooms[v] == "D");
 rooms[v] = "ND"
 Print("Room", "v", "cleaned!")
 elif (rooms[v] == "ND"):
 if (v==0):
 v+=1
 else: v-=1
 Print ("All rooms cleaned!")

clean_rooms();

O/P

Room 0 cleaned!
 Room 1 cleaned!
 All rooms cleaned!

S
2/9/25

Code

```
import random
class TicTacToe:
```

```

def __init__(self):
    self.board = []
def create_board(self):
    for i in range(3):
        row = []
        for j in range(3):
            row.append('-')
        self.board.append(row)
def get_random_first_player(self):
    return random.randint(0, 1)
def fix_spot(self, row, col, player):
    self.board[row][col] = player
def is_player_win(self, player):
    win = None
    n = len(self.board)
    for i in range(n):
        win = True
        for j in range(n):
            if self.board[i][j] != player:
                win = False
                break
        if win:
            return win
    for i in range(n):
        win = True
        for j in range(n):
            if self.board[j][i] != player:
                win = False
                break
        if win:
            return win
    win = True
    for i in range(n):
        if self.board[i][i] != player:
            win = False
            break
    if win:
        return win
    win = True

```

```

for i in range(n):
    if self.board[i][n - 1 - i] != player:
        win = False
        break
    if win:
        return win
    return False
for row in self.board:
    for item in row:
        if item == '-':
            return False
    return True
def is_board_filled(self):
    for row in self.board:
        for item in row:
            if item == '-':
                return False
    return True
def swap_player_turn(self, player):
    return 'X' if player == 'O' else 'O'
def show_board(self):
    for row in self.board:
        for item in row:
            print(item, end=" ")
        print()
def start(self):
    self.create_board()
    player = 'X' if self.get_random_first_player() == 1 else 'O'
    while True:
        print(f"Player {player} turn")
        self.show_board()
        row, col = list(
            map(int, input("Enter row and column numbers to fix spot: ").split()))
        print()
        self.fix_spot(row - 1, col - 1, player)
        if self.is_player_win(player):
            print(f"Player {player} wins the game!")
            break
        if self.is_board_filled():

```

```
        print("Match Draw!")
        break
    player = self.swap_player_turn(player)
    print()
    self.show_board()
tic_tac_toe = TicTacToe()
tic_tac_toe.start()
```

Output Snapshot

```
Player O turn
- - -
- - -
- - -
Enter row and column numbers to fix spot: 0 3
Player X turn
- - -
- - -
- - 0
Enter row and column numbers to fix spot: 1 2
Player O turn
- X - - -
- - 0
Enter row and column numbers to fix spot: 3 0
Player X turn
- X -
- - -
- - 0
Enter row and column numbers to fix spot: 3 2
Player O turn
- X -
- - -
- X 0
Enter row and column numbers to fix spot: 2 1
Player X turn
- X -
0 - -
- X 0
Enter row and column numbers to fix spot: 2 2
Player X wins the game!
```

Program 2 - Vacuum Cleaner

Code

```
def vacuum_world():

    goal_state = {'A': '0', 'B': '0'}
    cost = 0

    location_input = input("Enter Location of Vacuum: ")
    status_input = input("Enter status of " + location_input+ " : ")
    status_input_complement = input("Enter status of other room : ")

    print("Initial Location Condition {A : " + str(status_input_complement) + ", B : " + str(status_input) + " }"
        if location_input == 'A':
            print("Vacuum is placed in Location A")
            if status_input == '1':
                print("Location A is Dirty.")
                goal_state['A'] = '0'
                cost += 1 #cost for suck
                print("Cost for CLEANING A " + str(cost))
                print("Location A has been Cleaned.")

                if status_input_complement == '1':
                    print("Location B is Dirty.")
                    print("Moving right to the Location B. ")
                    cost += 1
                    print("COST for moving RIGHT " + str(cost))
                    goal_state['B'] = '0'
                    cost += 1
                    print("COST for SUCK " + str(cost))
                    print("Location B has been Cleaned. ")
                else:
                    print("No action" + str(cost))
                    print("Location B is already clean.")

            if status_input == '0':
                print("Location A is already clean ")
                if status_input_complement == '1':
                    print("Location B is Dirty.")
                    print("Moving RIGHT to the Location B. ")
                    cost += 1
                    print("COST for moving RIGHT " + str(cost))
                    goal_state['B'] = '0'
                    cost += 1
```

```

print("Cost for SUCK" + str(cost))
print("Location B has been Cleaned. ")
else:
    print("No action " + str(cost))
    print(cost)
    print("Location B is already clean.")

else:
    print("Vacuum is placed in location B")
    if status_input == '1':
        print("Location B is Dirty.")
        goal_state['B'] = '0'
        cost += 1
        print("COST for CLEANING " + str(cost))

    print("Location B has been Cleaned.")

    if status_input_complement == '1':
        print("Location A is Dirty.")
        print("Moving LEFT to the Location A. ")
        cost += 1
        print("COST for moving LEFT " + str(cost))
        goal_state['A'] = '0'
        cost += 1
        print("COST for SUCK " + str(cost))
        print("Location A has been Cleaned.")

    else:
        print(cost)
        print("Location B is already clean.")

    if status_input_complement == '1':
        print("Location A is Dirty.")
        print("Moving LEFT to the Location A. ")
        cost += 1
        print("COST for moving LEFT " + str(cost))
        goal_state['A'] = '0'
        cost += 1
        print("Cost for SUCK " + str(cost))
        print("Location A has been Cleaned. ")

else:

```

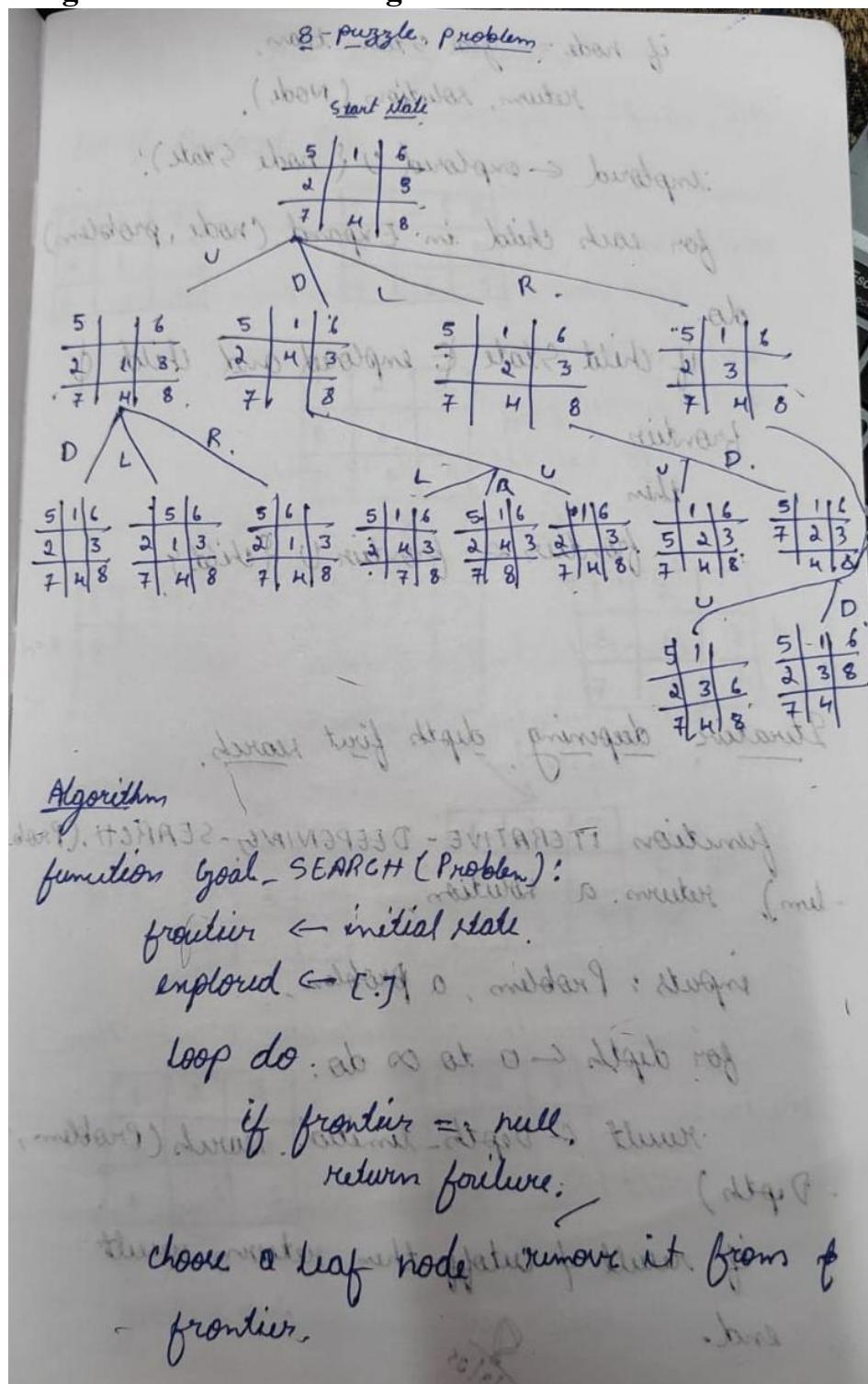
```
print("No action " + str(cost))
print("Location A is already clean.")

print("GOAL STATE: ")
print(goal_state)
print("Performance Measurement: " + str(cost))
vacuum_world()
```

Output Snapshot

```
Enter Location of Vacuum: A
Enter status of A : 0
Enter status of other room : 1
Initial Location Condition {A : 1, B : 0 }
Vacuum is placed in Location A
Location A is already clean
Location B is Dirty.
Moving RIGHT to the Location B.
COST for moving RIGHT 1
Cost for SUCK2
Location B has been Cleaned.
GOAL STATE:
{'A': '0', 'B': '0'}
Performance Measurement: 2
```

Program 3 - 8 Puzzle Using BFS



Algorithm :

if node == goal state then,
return, solutions (Node).

explored \leftarrow explored $\cup \{ \text{node state} \}$.

for each child in Expand (node, problem)

do.

if child state \notin explored and child
frontier
then
frontier \leftarrow frontier $\cup \{ \text{child} \}$

Iterative deepening, depth first search.

function ITERATIVE-DEEPENING-SEARCH (Prob-
lem) returns a solution
state, history \rightarrow history
inputs: Problem, a problem, frontier
for depth $\leftarrow 0$ to ∞ do. ab goal

result \leftarrow Depth-limited-search (Problem,
Depth)

if result \neq cutoff then return result

end.

Code

```
import sys
import numpy as np
class Node:
    def __init__(self, state, parent, action):
        self.state = state
        self.parent = parent
```

```

        self.action = action
class StackFrontier:
    def __init__(self):
        self.frontier = []
    def add(self, node):
        self.frontier.append(node)
    def contains_state(self, state):
        return any((node.state[0] == state[0]).all() for node in self.frontier)
    def empty(self):
        return len(self.frontier) == 0
    def remove(self):
        if self.empty():
            raise Exception("Empty Frontier")
        else:
            node = self.frontier[-1]
            self.frontier = self.frontier[:-1]
            return node
class QueueFrontier(StackFrontier):
    def remove(self):
        if self.empty():
            raise Exception("Empty Frontier")
        else:
            node = self.frontier[0]
            self.frontier = self.frontier[1:]
            return node
class Puzzle:
    def __init__(self, start, startIndex, goal, goalIndex):
        self.start = [start, startIndex]
        self.goal = [goal, goalIndex]
        self.solution = None

    def neighbors(self, state):
        mat, (row, col) = state

```

```

results = [] if row > 0:
    mat1 = np.copy(mat)
    mat1[row][col] = mat1[row - 1][col]
    mat1[row - 1][col] = 0
    results.append(('up', [mat1, (row - 1, col)]))

if col > 0:
    mat1 = np.copy(mat)
    mat1[row][col] = mat1[row][col - 1]
    mat1[row][col - 1] = 0
    results.append(('left', [mat1, (row, col - 1)]))

if row < 2:
    mat1 = np.copy(mat)
    mat1[row][col] = mat1[row + 1][col]
    mat1[row + 1][col] = 0
    results.append(('down', [mat1, (row + 1, col)]))

if col < 2:
    mat1 = np.copy(mat)
    mat1[row][col] = mat1[row][col + 1]
    mat1[row][col + 1] = 0
    results.append(('right', [mat1, (row, col + 1)]))

return results

def print(self):
    solution = self.solution if self.solution is not None else None

```

```

print("Start State:\n", self.start[0], "\n")
print("Goal State:\n", self.goal[0], "\n")
print("\nStates Explored: ", self.num_explored, "\n")
print("Solution:\n ")
for action, cell in zip(solution[0], solution[1]):
    print("action: ", action, "\n", cell[0], "\n")
print("Goal Reached!!")

def does_not_contain_state(self, state):
    for st in self.explored:
        if (st[0] == state[0]).all():
            return False
    return True

def solve(self):
    self.num_explored = 0
    start = Node(state=self.start, parent=None, action=None)

```

```

frontier = QueueFrontier()
frontier.add(start)
self.explored = []
while True:
    if frontier.empty():
        raise Exception("No solution")
    node = frontier.remove()
    self.num_explored += 1
    if (node.state[0] == self.goal[0]).all():
        actions = []
        cells = []
        while node.parent is not None:
            actions.append(node.action)
            cells.append(node.state)
            node = node.parent
        actions.reverse()
        cells.reverse()
        self.solution = (actions, cells)
        return
    self.explored.append(node.state)
    for action, state in self.neighbors(node.state):
        if not frontier.contains_state(state) and self.does_not_contain_state(state):
            child = Node(state=state, parent=node, action=action)
            frontier.add(child)
start = np.array([[1, 2, 3], [8, 0, 4], [7, 6, 5]])

```

```

goal = np.array([[2, 8, 1], [0, 4, 3], [7, 6, 5]])
startIndex = (1, 1)
goalIndex = (1, 0)
p = Puzzle(start, startIndex, goal, goalIndex)
p.solve() p.print()

```

Output Snapshot

```
Start State:  
[[1 2 3]  
[8 0 4]  
[7 6 5]]  
  
Goal State:  
[[2 8 1]  
[0 4 3]  
[7 6 5]]  
  
States Explored: 358  
  
Solution:  
  
action: up  
[[1 0 3]  
[8 2 4]  
[7 6 5]]  
  
action: left  
[[0 1 3]  
[8 2 4]  
[7 6 5]]  
  
action: down  
[[8 1 3]  
[0 2 4]  
[7 6 5]]  
  
action: right  
[[8 1 3]  
[2 0 4]  
[7 6 5]]  
  
action: right  
[[8 1 3]  
[2 4 0]  
[7 6 5]]
```

```
action: down  
[[8 1 3]  
[0 2 4]  
[7 6 5]]  
  
action: right  
[[8 1 3]  
[2 0 4]  
[7 6 5]]  
  
action: right  
[[8 1 3]  
[2 4 0]  
[7 6 5]]  
  
action: up  
[[8 1 0]  
[2 4 3]  
[7 6 5]]  
  
action: left  
[[8 0 1]  
[2 4 3]  
[7 6 5]]  
  
action: left  
[[0 8 1]  
[2 4 3]  
[7 6 5]]  
  
action: down  
[[2 8 1]  
[0 4 3]  
[7 6 5]]  
  
Goal Reached!!
```

Program 04 - 8 Puzzle Using A*

Algorithm

A* Algorithms on 8 puzzle

Algorithm

function A* (start, goal)

open-list \leftarrow priority queue ordered by
 $f(n) = g(n) + h(n)$

closed-list \leftarrow empty set

$g(\text{start}) \leftarrow 0$

$f(\text{start}) \leftarrow g(\text{start}) + h(\text{start})$

open-list.insert (start, f(start))

while open-list is not empty

 current \leftarrow node in open-list with lowest f value

 if current = goal:

 return path from start to goal

 add current to closed-list

 for each neighbour of current:

 if neighbour is closed-list:

 continue

 tentative-g $\leftarrow g(\text{current}) + \text{cost}(\text{current}, \text{neighbour})$

5	6	7
4		8
2	1	3

if neighbour not in open list or.

- tentative₋g < g(neighbour)

- g(neighbour) ← tentative₋g

+ (neighbour) ← g(neighbour) +

h(neighbour)

Parent(neighbour) ← current.

- if neighbour not in open list.

open-list.insert(neighbour, +(-

- neighbour))

return failure.

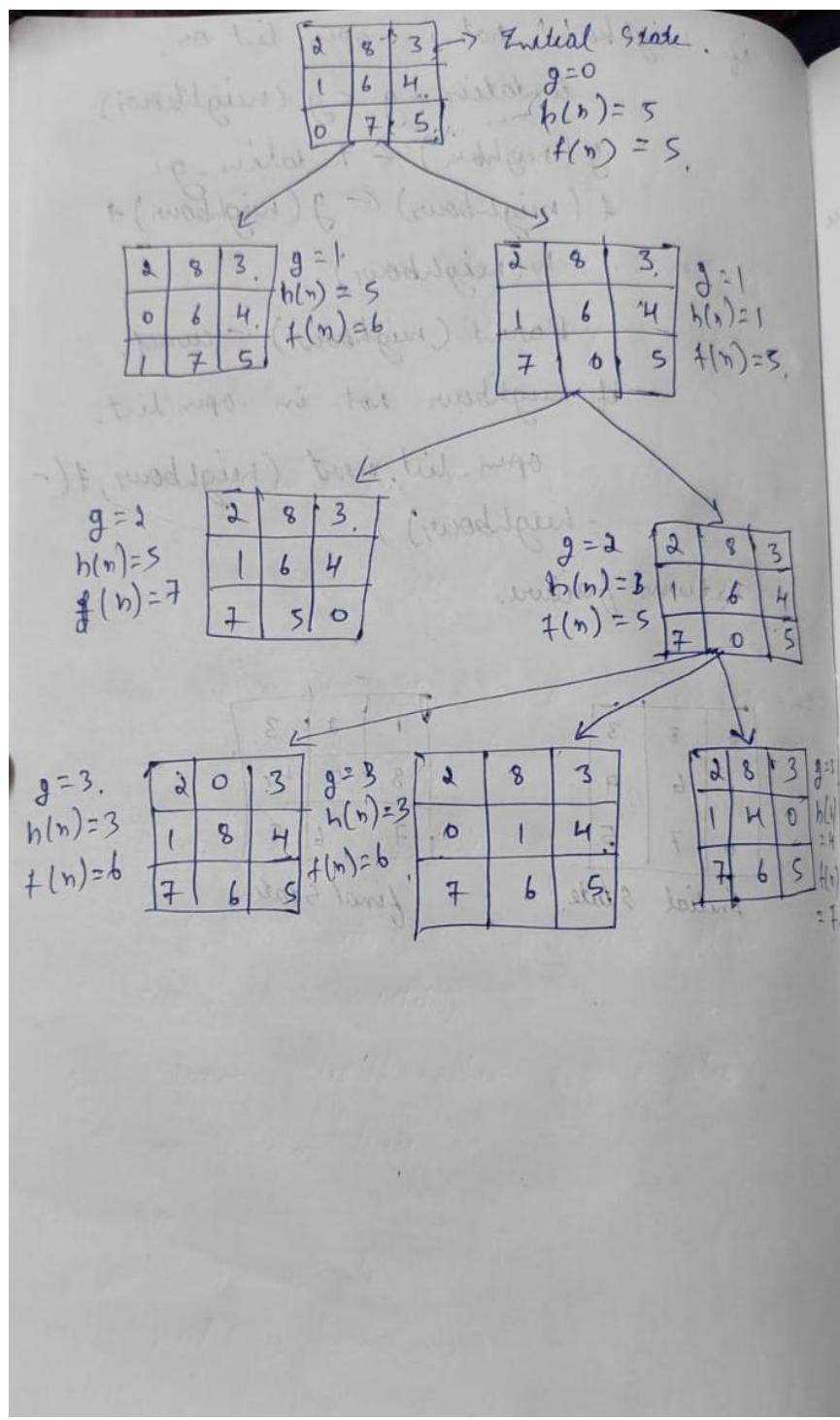
Ex:-

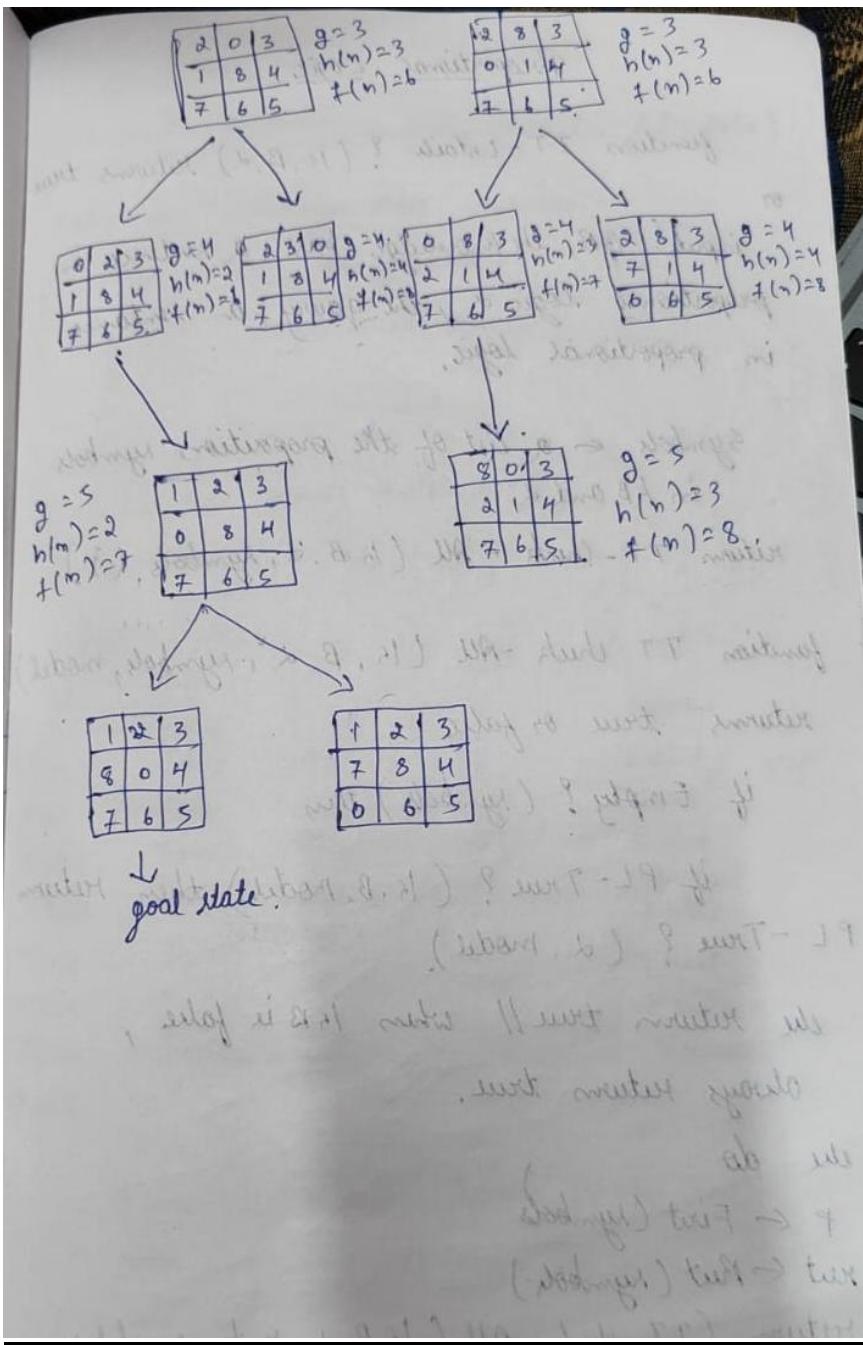
2	8	3
1	6	4
0	7	5

Initial state.

1	2	3
8	0	4
7	6	5

final state





Code

```
def print_b(src):
    state = src.copy()
    state[state.index(-1)] = ''
    print(
f"""
{state[0]} {state[1]} {state[2]}
{state[3]} {state[4]} {state[5]}
{state[6]} {state[7]} {state[8]}
""")
```

```

def h(state, target):
    count = 0
    i = 0
    for j in state:
        if state[i] != target[i]:
            count = count+1
    return count

def astar(state, target):
    states = [src]
    g = 0
    visited_states = []
    while len(states):
        print(f"Level: {g}")
        moves = []
        for state in states:
            visited_states.append(state)
            print_b(state)
            if state == target:
                print("Success")
                return
            moves += [move for move in possible_moves(
                state, visited_states) if move not in moves]
        costs = [g + h(move, target) for move in moves]
        states = [moves[i]
                  for i in range(len(moves)) if costs[i] == min(costs)]
        g += 1
    print("Fail")

def possible_moves(state, visited_state):

```

```

b = state.index(-1)
d = []
if b - 3 in range(9):
    d.append('u')
if b not in [0, 3, 6]:
    d.append('l')
if b not in [2, 5, 8]:
    d.append('r')
if b + 3 in range(9):
    d.append('d')
pos_moves = []
for m in d:
    pos_moves.append(gen(state, m, b))
return [move for move in pos_moves if move not in visited_state]
def gen(state, m, b):
    temp = state.copy()
    if m == 'u':
        temp[b - 3], temp[b] = temp[b], temp[b - 3]
    if m == 'l':
        temp[b - 1], temp[b] = temp[b], temp[b - 1]
    if m == 'r':
        temp[b + 1], temp[b] = temp[b], temp[b + 1]
    if m == 'd':
        temp[b + 3], temp[b] = temp[b], temp[b + 3]
    return temp
src = [1, 2, 3, -1, 4, 5, 6, 7, 8]
target = [1, 2, 3, 4, 5, 6, 7, 8, -1]
astar(src, target)

```

Output Snapshot

```

Enter the start state matrix

1 0 1 0
1 0 0 1
1 1 1 1
Enter the goal state matrix

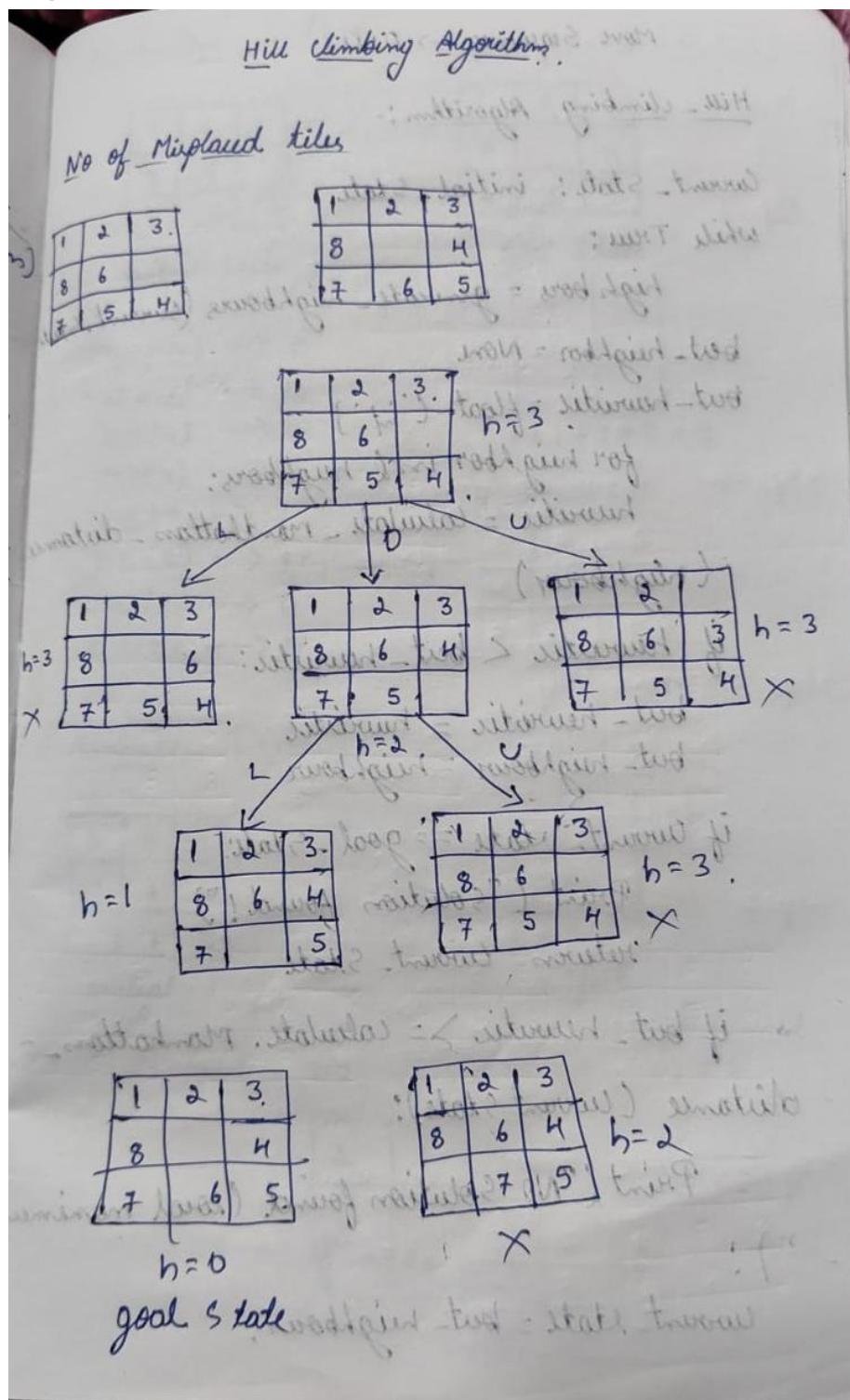
1 1 0 1
1 0 0 1
1 1 1 0
|
|
\^/

1 0 1 0
1 0 0 1
1 1 1 1

```

Program 05 – Hill Climbing

Algorithm



Move Sequence \rightarrow OLU with

Hill-climbing Algorithm :-

Current-State: initial-state,

while True:

 high_bors = generate_neighbours (current_state)

 best_neighbor = None

 but_heuristic = float ('inf')

 for neighbor in bors:

 heuristic = calculate_manhattan_distance

 (neighbors)

8	6	1
3	2	5
4	7	0

8	6	1
3	2	5
4	7	0

 if heuristic < best_heuristic:

 best_heuristic = heuristic

 best_neighbor = neighbor

 if current_state == goal_state:

 Print ("solution found!")

 return current_state

 if best_heuristic >= calculate_manhattan_

 distance (current_state):

8	6	1
3	2	5
4	7	0

 Print ("No solution found (local minimum)")

-")!

 current_state = best_neighbor

Manhattan Distance: (x_1, y_1) to (x_2, y_2)

1	2	3
8	6	
7	5	4

1	2	3
8		4
7	6	5

Initial State

Goal State

$$MD(1) \rightarrow 0$$

$$MD(2) \rightarrow 0$$

$$MD(3) \rightarrow 0$$

$$MD(4) \rightarrow 1$$

$$MD(5) \rightarrow 1$$

$$MD(6) \rightarrow 1$$

$$MD(7) \rightarrow 0$$

$$MD(8) \rightarrow 0$$

$$0 + 0 + 1 + 1 + 1 + 0 + 0$$

$$= 3, \text{ no swap } 6-\text{gate}$$

8	3	6
H		1
2	5	F.

Manhattan Distance

2	8	3
1	6	4
7	5	

initial state

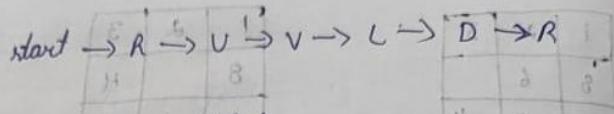
1	2	3
8		4
7	6	5

Goal state

$$h = 1 + 1 + 0 + 0 + 0 + 0 + 1 + 1 + 2 = 6$$

2	8	3
1	6	4
7	5	

Blank at (3, 1) can move right $h=5$ but ~~not~~



Step - 1 : move right

state 2 loop

2	8	3
1		4
7		5

$$0+0+1+1+1+0+0$$

$h=5$, state 2 initial

0 $\leftarrow (1)_{DM}$

0 $\leftarrow (6)_{DM}$

0 $\leftarrow (2)_{DM}$

1 $\leftarrow (H)_{DM}$

1 $\leftarrow (2)_{DM}$

1 $\leftarrow (3)_{DM}$

0 $\leftarrow (F)_{DM}$

0 $\leftarrow (8)_{DM}$

Step - 2 move up

2	8	3
1		H
7	6	5

$$h=4$$

initial middle

5	3	8
N	3	1
2	4	

final state

Step 3: move up.

2	8	3
1		H
7	6	5

$$h=3,$$

1	2	3
1		4
7	6	5

$$h=3,$$

Step 4: move left.

1	2	3
8		4
7	6	5

$$h=3,$$

$$d = 8 + 1 + 1 + 1 = d$$

$$d = 8 + 1 + 1 + 1 = d$$

Step 5: Move down.

1	2	3
8		4
7	6	5

$$h=2,$$

step 6 move right

1	2	3
8		4
7	6	5

$h = 0$

Manhattan distance Algorithm.

1. start with initial state
2. calculate the Manhattan distance of the current state
3. while the current state is not goal.
 - a. generate all valid neighbouring state by sliding the blank tile up/down/left/right.
 - b. calculate the Manhattan distance for each neighbour.
 - c. choose the neighbor with lowest Manhattan distance
4. if the Manhattan dist is zero goal state is reached.

Code

```
from random import randint
N = 8
def configureRandomly(board, state):
    for i in range(N):
        state[i] = randint(0, 100000) % N;
        board[state[i]][i] = 1;
def printBoard(board):
    for i in range(N):
        print(*board[i])
def printState(state):
    print(*state)
def compareStates(state1, state2):
    for i in range(N):
        if (state1[i] != state2[i]):
```

```

        return False;
    return True;
def fill(board, value):
    for i in range(N):
        for j in range(N):
            board[i][j] = value;
def calculateObjective( board, state):
    for i in range(N):
        row = state[i]
        col = i - 1;
        while (col >= 0 and board[row][col] != 1) :
            col -= 1
        if (col >= 0 and board[row][col] == 1) :
            attacking += 1;
        row = state[i]
        col = i + 1;
        while (col < N and board[row][col] != 1):
            col += 1;
        if (col < N and board[row][col] == 1) :
            attacking += 1;
        row = state[i] - 1
        col = i - 1;
        while (col >= 0 and row >= 0 and board[row][col] != 1) :
            col-= 1;
            row-= 1;

        if (col >= 0 and row >= 0 and board[row][col] == 1) :
            attacking+= 1;

# Diagonally to the right down
# (row and col simultaneously
# increase)
row = state[i] + 1
col = i + 1;
while (col < N and row < N and board[row][col] != 1) :
    col+= 1;
    row+= 1;

if (col < N and row < N and board[row][col] == 1) :
    attacking += 1;

```

```

row = state[i] + 1
col = i - 1;
while (col >= 0 and row < N and board[row][col] != 1) :
    col -= 1;
    row += 1;
if (col >= 0 and row < N and board[row][col] == 1) :
    attacking += 1;
row = state[i] - 1
col = i + 1;
while (col < N and row >= 0 and board[row][col] != 1) :
    col += 1;
    row -= 1;
if (col < N and row >= 0 and board[row][col] == 1) :
    attacking += 1;
return int(attacking / 2);
def generateBoard( board, state):
    fill(board, 0);
    for i in range(N):
        board[state[i]][i] = 1;
def copyState( state1, state2):

    for i in range(N):
        state1[i] = state2[i];

def getNeighbour(board, state):
    opBoard = [[0 for _ in range(N)] for _ in range(N)]
    opState = [0 for _ in range(N)]

    copyState(opState, state);
    generateBoard(opBoard, opState);
    opObjective = calculateObjective(opBoard, opState);
    NeighbourBoard = [[0 for _ in range(N)] for _ in range(N)]

    NeighbourState = [0 for _ in range(N)]
    copyState(NeighbourState, state);
    generateBoard(NeighbourBoard, NeighbourState);
    for i in range(N):
        for j in range(N):
            if (j != state[i]) :
                NeighbourState[i] = j;

```

```

        NeighbourBoard[NeighbourState[i]][i] = 1;
        NeighbourBoard[state[i]][i] = 0;
        temp = calculateObjective( NeighbourBoard, NeighbourState)
        if (temp <= opObjective) :
            opObjective = temp;
            copyState(opState, NeighbourState);
            generateBoard(opBoard, opState);
            NeighbourBoard[NeighbourState[i]][i] = 0;
            NeighbourState[i] = state[i];
            NeighbourBoard[state[i]][i] = 1;
        copyState(state, opState);
        fill(board, 0);
        generateBoard(board, state);

def hillClimbing(board, state):
    neighbourBoard = [[0 for _ in range(N)] for _ in range(N)]
    neighbourState = [0 for _ in range(N)]
    copyState(neighbourState, state);
    generateBoard(neighbourBoard, neighbourState);

    while True:
        copyState(state, neighbourState);
        generateBoard(board, state);
        # Getting the optimal neighbour
        getNeighbour(neighbourBoard, neighbourState);
        if (compareStates(state, neighbourState)) :

            printBoard(board);
            break;

        elif (calculateObjective(board, state) == calculateObjective(
neighbourBoard,neighbourState)):
            # Random neighbour
            neighbourState[randint(0, 100000) % N] = randint(0, 100000) % N;
            generateBoard(neighbourBoard, neighbourState);

# Driver code
state = [0] * N
board = [[0 for _ in range(N)] for _ in range(N)]
configureRandomly(board, state);

```

```
hillClimbing(board, state);
```

OUTPUT

```
Step 0: Initial state
. . . Q
. Q .
. . Q .
Q . .

Cost = 2

Step 1: Move to better neighbour
. . . Q
Q . .
. . Q .
. Q . .

Cost = 1

Step 2: Move to better neighbour
. . Q .
Q . .
. . . Q
. Q . .

Cost = 0

Step 3: Reached local minimum
Final state:
. . Q .
Q . .
. . . Q
. Q . .

Final cost = 0
```

Program-07 Knowledge-Base

ALGORITHM :

Propositional Logic

function TT-~~exists~~? (k, B, Δ) returns true or

inputs:- k, B , the knowledge base, a sentence in propositional logic & Δ , the query, a sentence in propositional logic.

Symbols \leftarrow a list of the proposition symbols in k, B and Δ

return TT-~~check~~-All (k, B, Δ , symbols, {})

function TT check -All (k, B, Δ , symbols, model)

returns true or false

if Empty? (symbols) then

if PL-True? (k, B , model) then return

PL-True? (Δ , model).

we return true // when k, B is false,

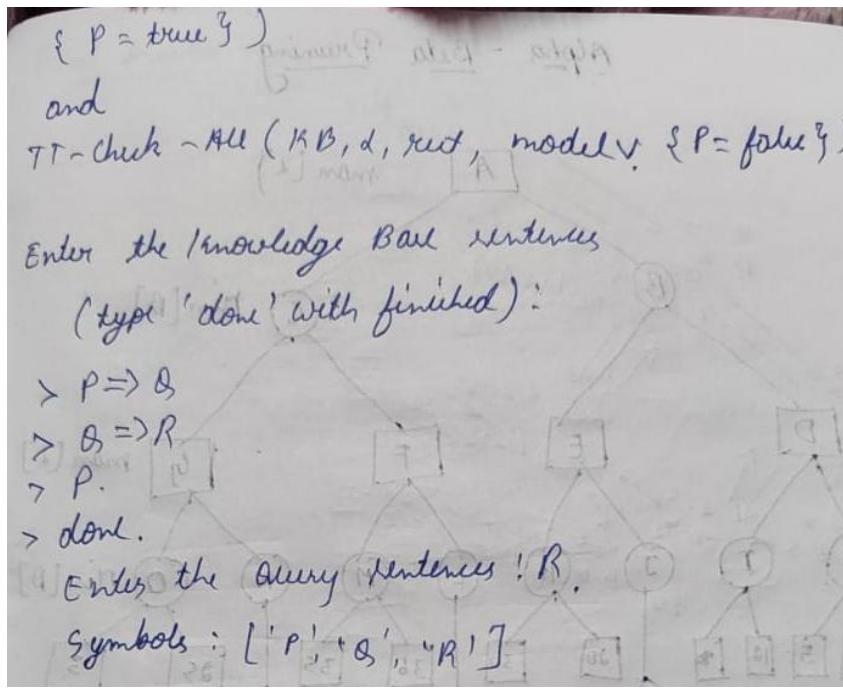
always return true.

we do

$p \leftarrow$ First (symbols)

ret \leftarrow Ret (symbols)

return (TT-~~check~~-All (k, B, Δ , ret, model))



Code

```

combinations=[(True,True, True),(True,True, False),(True, False, True),(True, False, False),(False, True, True),(False, True, False),(False, False, True),(False, False, False)]
variable={'p':0,'q':1,'r':2}

```

```
kb=""
```

```
q=""
```

```
priority={'~":"3,'~":"1,'~":"2}
```

```
def input_rules()
```

```
    global kb, q
```

```
    kb = (input("Enter rule: "))
```

```
    q = input("Enter the Query: ")
```

```
def entailment():
```

```
    global kb, q
```

```
    print("*10+"Truth Table Reference"+*10)
```

```
    print('kb','alpha')
```

```
    print('*'*10)
```

```
    for comb in combinations:
```

```
        s = evaluatePostfix(toPostfix(kb), comb)
```

```
        f = evaluatePostfix(toPostfix(q), comb)
```

```
        print(s, f)
```

```
        print('*'*10)
```

```
        if s and not f:
```

```
            return False
```

```
    return True
```

```
def isOperand(c):
```

```
    return c.isalpha() and c != 'v'
```

```

def isLeftParanthesis(c):
    return c == '('

def isRightParanthesis(c):
    return c == ')'

def isEmpty(stack):
    return len(stack) == 0

def peek(stack):
    return stack[-1]

def hasLessOrEqualPriority(c1, c2):
    try:
        return priority[c1] <= priority[c2]
    except KeyError:
        return False

def toPostfix(infix):
    stack = []
    postfix = ""
    for c in infix:
        if isOperand(c):
            postfix += c
        else:
            if isLeftParanthesis(c):
                stack.append(c)
            elif isRightParanthesis(c):
                operator = stack.pop()
                while not isLeftParanthesis(operator):
                    postfix += operator
                    operator = stack.pop()
            else:
                while (not isEmpty(stack)) and hasLessOrEqualPriority(c, peek(stack)):
                    postfix += stack.pop()
                stack.append(c)
    while (not isEmpty(stack)):
        postfix += stack.pop()

    return postfix

def evaluatePostfix(exp, comb):
    stack = []
    for i in exp:

```

```

if isOperand(i):
    stack.append(comb[variable[i]])
elif i == '~':
    val1 = stack.pop()
    stack.append(not val1)
else:
    val1 = stack.pop()
    val2 = stack.pop()
    stack.append(_eval(i, val2, val1))
return stack.pop()
def _eval(i, val1, val2):
    if i == '^':
        return val2 and val1
    return val2 or val1
#Test 1
input_rules()
ans = entailment()
if ans:

print("Knowledge Base entails query") else:
    print("Knowledge Base does not entail query")
#Test 2
input_rules()
ans = entailment()

```

```

if ans:
    print("Knowledge Base entails query")
else:
    print("Knowledge Base does not entail query")

```

OUTPUT:

```
Enter rule: (~qv~pvr)^(~q^p)^q
Enter the Query: r
Truth Table Reference
kb alpha
*****
False True
-----
False False
-----
Knowledge Base entails query
```

Program-08 Unification in first order logic

Algorithm :

Unification in FOL

Algorithm: unify(ϕ_1, ϕ_2)

Step 1: If ϕ_1 or ϕ_2 is a variable or constant, then
a) if ϕ_1 or ϕ_2 are identical, then Return NIL.
b) Else if ϕ_1 is available,
 a. then if ϕ_1 occurs in ϕ_2 , then Return Failure.
 b. Else return $\{\phi_2/\phi_1\}$.
c) Else if ϕ_2 is a variable,
 a. if ϕ_2 occurs in ϕ_1 , then return Failure.
 b. Else return $\{\phi_1/\phi_2\}$.
d) Else return Failure.

Step 2: If the initial predicate symbols in ϕ_1, ϕ_2 are not same, then return Failure.

Step 3: If ϕ_1, ϕ_2 have a different number of arguments, then return failure.

Step n: Set substitution set(SUB) to NIL.

Step s: For i=1 to the number of elements in ϕ_1 ,
 a) Call unify function with the ith element of ϕ_1 and ith element of ϕ_2 and Put the
 result into S.
 b) If S=failure then Return Failure.

c) if $S \neq \text{NIN}$ then do

a) apply S to the remainder of both b ,

and

b) $\text{subst} = \text{append}(S, \text{subst})$.

Step 6: Return subst

Code

```
import re
def getAttributes(expression):
    expression = expression.split("(")[1:]
    expression = ".join(expression)
    expression = expression.split(")")[:-1]
    expression = ")".join(expression)
    attributes = expression.split(',')
    return attributes

def getInitialPredicate(expression):
    return expression.split("(")[0]

def isConstant(char):
    return char.isupper() and len(char) == 1

def isVariable(char):
    return char.islower() and len(char) == 1

def replaceAttributes(exp, old, new):

    attributes = getAttributes(exp)
    predicate = getInitialPredicate(exp)
    for index, val in enumerate(attributes):
        if val == old:
            attributes[index] = new
    return predicate + "(" + ",".join(attributes) + ")"

def apply(exp, substitutions):
    for substitution in substitutions:
        new, old = substitution
        exp = replaceAttributes(exp, old, new)
    return exp

def checkOccurs(var, exp):
    if exp.find(var) == -1:
        return False
    return True

def getFirstPart(expression):
```

```

attributes = getAttributes(expression)
return attributes[0]
def getRemainingPart(expression):
    predicate = getInitialPredicate(expression)
    attributes = getAttributes(expression)
    newExpression = predicate + "(" + ",".join(attributes[1:]) + ")"
    return newExpression
def unify(exp1, exp2):
    if exp1 == exp2:
        return []
    if isConstant(exp1) and isConstant(exp2):
        if exp1 != exp2:
            print(f'{exp1} and {exp2} are constants. Cannot be unified')
            return []
    if isConstant(exp1):
        return [(exp1, exp2)]
    if isConstant(exp2):
        return [(exp2, exp1)]
    if isVariable(exp1):
        return [(exp2, exp1)] if not checkOccurs(exp1, exp2) else [] if isVariable(exp2):
        return [(exp1, exp2)] if not checkOccurs(exp2, exp1) else []
    if getInitialPredicate(exp1) != getInitialPredicate(exp2):
        print("Cannot be unified as the predicates do not match!")
        return []
    attributeCount1 = len(getAttributes(exp1))
    attributeCount2 = len(getAttributes(exp2))
    if attributeCount1 != attributeCount2:
        print(f'Length of attributes {attributeCount1} and {attributeCount2} do not match. Cannot
be unified')
        return []
    head1 = getFirstPart(exp1)
    head2 = getFirstPart(exp2)
    initialSubstitution = unify(head1, head2)
    if not initialSubstitution:
        return []

```

```

if attributeCount1 == 1:
    return initialSubstitution

tail1 = getRemainingPart(exp1)
tail2 = getRemainingPart(exp2)

if initialSubstitution != []:
    tail1 = apply(tail1, initialSubstitution)
    tail2 = apply(tail2, initialSubstitution)

remainingSubstitution = unify(tail1, tail2)
if not remainingSubstitution:
    return []
else:
    return initialSubstitution + remainingSubstitution

if __name__ == "__main__":
    print("Enter the first expression")
    e1 = input()

    print("Enter the second expression")
    e2 = input()
    substitutions = unify(e1, e2)
    print("The substitutions are:")
    print([' / '.join(substitution) for substitution in substitutions])

```

Output Snapshot

Enter the first expression

king(x)

Enter the second expression

king(john)

The substitutions are:

['john / x']

Program-9 Forward Reasoning

ALGORITHM :

First order logic: Forward chaining

Example:

As per the law, it is a crime for an American to sell weapons to hostile nations. Country A, an enemy of America, has some missiles and all the missiles were sold to it by Robert, who is an American citizen.

Prove that "Robert is a criminal."

Representations in FOL

- It is a crime for an American to sell weapons to hostile nations.

Let's say P , q and r are variables
American (P) \wedge weapon (q) \wedge sells (P, q, r) \wedge
Hostile (r) \Rightarrow criminal (P)

- Country A has some missiles

$\exists x \text{ owns}(A, x) \wedge \text{missile}(x)$

- Existential instantiation, introducing a new constant T_1 , "owns (A, T_1)".
 $\text{missile}(T_1)$

- All missiles were sold to country A by Robert
 $\forall x \text{ missile}(x) \wedge \text{own}(A, x) \Rightarrow \text{sells}(\text{Robert}, x)$

- Missiles are weapons

$\text{missile}(x) \Rightarrow \text{weapon}(x)$

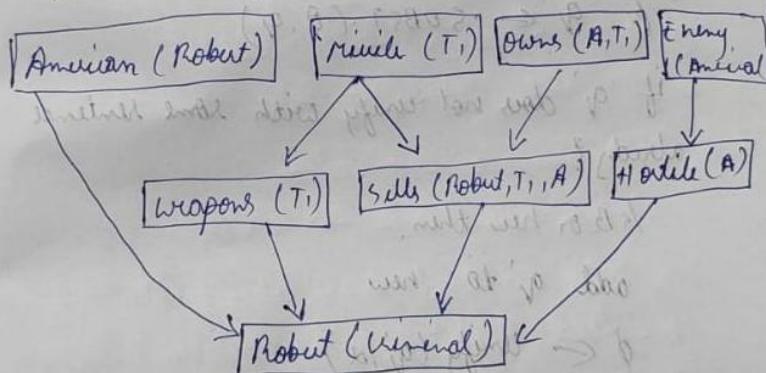
• Enemy of America is known as hostile
 $\text{the Enemy } (\alpha, \text{America}) \Rightarrow \text{Hostile } (\alpha)$

• Robert is an American & uses lethal weapon
 $\text{American } (\text{Robert}) \quad \& \quad \text{LethalWeapon } (\text{Robert})$

• the country A is an Enemy of America.
 $\text{Enemy } (A, \text{America})$

To Prove:
 $\text{Robert is a Criminal}$
 $\text{Criminal } (\text{Robert})$

Forward chaining:



Forward Reasoning Algorithm:

function $\text{FOL-FC-AS}(\text{KB}, d)$
 returns a substitution or false.

inputs: KB , the knowledge base.

α , the query

$\text{American } (P) \wedge \text{Weapon } (Q)$

$\vdash \text{Sells } (P, Q, R) \wedge \text{Hostile } (R)$

$\Rightarrow \text{Criminal } (P)$

local variables : new, the new sentences inferred
 - id on each iteration
 repeat until new is empty

$$\text{new} \leftarrow \{\}$$

 for each rule in KB do

$$(P, \lambda, \dots, \Delta P_n \Rightarrow q) \leftarrow \text{Standardize-Variable}$$

 for each θ such that $\text{Subst}(\theta, P, \lambda, \dots, \Delta P_n) =$

$$\text{Subst}(\theta, P^*, \lambda, \dots, \Delta P'_n)$$

 for some P^*, \dots, P'_n in KB

$$t \quad q' \leftarrow \text{SUBST}(\theta, q)$$

 if q' does not unify with some sentence
 already?
 if in KB or new then
 add q' to new

$$\phi \leftarrow \text{Unify}(q', \alpha)$$

 if ϕ is not fail then return ϕ
 add new to KB
 returns false, if no substitution is found

Code

```

import re
def isVariable(x):
  return len(x) == 1 and x.islower() and x.isalpha()

```

```

def getAttributes(string):
  expr = '([^\n]+)'
  matches = re.findall(expr, string)
  return matches

```

```

def getPredicates(string):
    expr = '([a-zA-Z]+)\([^\&]+\)'
    return re.findall(expr, string)

class Fact:

    def __init__(self, expression):
        self.expression = expression
        predicate, params = self.splitExpression(expression)
        self.predicate = predicate
        self.params = params
        self.result = any(self.getConstants())

    def splitExpression(self, expression):
        predicate = getPredicates(expression)[0]
        params = getAttributes(expression)[0].strip(')').split(',')
        return [predicate, params]

    def getResult(self):
        return self.result

    def getConstants(self):
        return [None if isVariable(c) else c for c in self.params]

    def getVariables(self):
        return [v if isVariable(v) else None for v in self.params]

    def substitute(self, constants):
        c = constants.copy()
        f = f'{self.predicate}({",".join([constants.pop(0) if isVariable(p) else p for p in self.params])})'
        return Fact(f)

class Implication:

    def __init__(self, expression):
        self.expression = expression
        l = expression.split('=>')
        self.lhs = [Fact(f) for f in l[0].split('&')]
        self.rhs = Fact(l[1])

    def evaluate(self, facts):
        constants = {}
        new_lhs = []
        for fact in facts:
            for p in fact.params:
                if isVariable(p):
                    constants[p] = fact.result
                else:
                    new_lhs.append(Fact(fact))
        self.lhs = new_lhs

```

```

for val in self.lhs:
    if val.predicate == fact.predicate:
        for i, v in enumerate(val.getVariables()):
            if v:
                constants[v] = fact.getConstants()[i]
        new_lhs.append(fact)
    predicate, attributes = getPredicates(self.rhs.expression)[0],
    str(getAttributes(self.rhs.expression)[0])
for key in constants:
    if constants[key]:
        attributes = attributes.replace(key, constants[key])

expr = f'{predicate} {attributes}'
return Fact(expr) if len(new_lhs) and all([f.getResult() for f in new_lhs]) else None

```

class KB:

```

def __init__(self):
    self.facts = set()
    self.implications = set()

def tell(self, e):
    if '=>' in e:
        self.implications.add(Implication(e))
    else:
        self.facts.add(Fact(e))
for i in self.implications:
    res = i.evaluate(self.facts)
    if res:
        self.facts.add(res)

def ask(self, e):
    facts = set([f.expression for f in self.facts])
    i = 1
    print(f'Querying {e}:')
    for f in facts:
        if Fact(f).predicate == Fact(e).predicate:
            print(f'\t{i}. {f}')
            i += 1

def display(self):
    print("All facts: ")
    for i, f in enumerate(set([f.expression for f in self.facts])):

```

```
print(f'\t{i+1}. {f}')
```

```
def main():
    kb = KB()
    print("Enter the number of FOL expressions present in KB:")
    n = int(input())
    print("Enter the expressions:")
    for i in range(n):
        fact = input()
        kb.tell(fact)
    print("Enter the query:")
    query = input()
    kb.ask(query)
    kb.display()

main()
```

Output Snapshot

Querying criminal(x):

1. criminal(West)

All facts:

1. american(West)
2. sells(West,M1,Nono)
3. owns(Nono,M1)
4. missile(M1)
5. enemy(Nono,America)
6. weapon(M1)
7. hostile(Nono)
8. criminal(West)

Querying evil(x):

1. evil(John)

Program-10 KnowledgeBase - Resolution

Algorithm :

Resolutions in FQL

Steps for proving in Resolution.

Premise, ... Premises

(all expressed in FQL)

1. Convert all series to CNF
2. Negative conclusion S and convert result to CNF
3. Add Negated conclusion S to the premise class

4. Repeat until contradiction or no progress is made:

- a. Select 2 clauses (call them parent clauses)
- b. Resolve them together, performing all required unifications
- c. If Resolved is the empty clause, a contradiction has been found (i.e.) S follows from the premises.
- d. If not add Resolved to the premises

Example:

- a. John likes all kinds of food
- b. Apple and vegetables are food
- c. Anything anyone eats and not killed is food
- d. Anil eats peanuts and still alive.
- e. Harry eats peanuts and still that Anil eats

- b. Anyone who is alive implies not killed.
 g. Anyone who is not killed & implies alive.

Prove by resolution that:

h. John likes peanuts

Step 1: Representations in FOL:

- $\forall x: \text{food}(x) \rightarrow \text{Likes}(\text{John}, x)$
- $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetable})$
- $\forall x \forall y: \text{eats}(x, y) \rightarrow \neg \text{killed}(x) \rightarrow \text{food}(y)$
- $\text{eats}(\text{Anil}, \text{peanuts}) \wedge \text{alive}(\text{Anil})$
- $\forall x: \text{eats}(\text{Anil}, x) \rightarrow \text{eats}(\text{Harry}, x)$
- $\forall x: \neg \text{killed}(x) \rightarrow \text{alive}(x)$
- $\forall x: \text{alive}(x) \rightarrow \neg \text{killed}(x)$
- $\neg \text{Likes}(\text{John}, \text{peanuts})$

Step 2: Eliminate implication

$\alpha \Rightarrow \beta$ with $\rightarrow \alpha \vee \beta$.

- $\forall x \rightarrow \text{food}(x) \vee \text{Likes}(\text{John}, x)$
- $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetable})$
- $\forall x \forall y \rightarrow [\text{eats}(x, y) \rightarrow \neg \text{killed}(x)] \vee \text{food}(y)$
- $\text{eats}(\text{Anil}, \text{peanuts}) \wedge \text{alive}(\text{Anil})$
- $\forall x \neg \text{eats}(\text{Anil}, x) \vee \text{eats}(\text{Harry}, x)$
- $\forall x \neg \text{alive}(x) \vee \neg \text{killed}(x)$
- $\forall x \neg \text{alive}(x) \vee \neg \neg \text{killed}(x)$

h. likes (John, peanuts)

step 3: move negation inwards and write

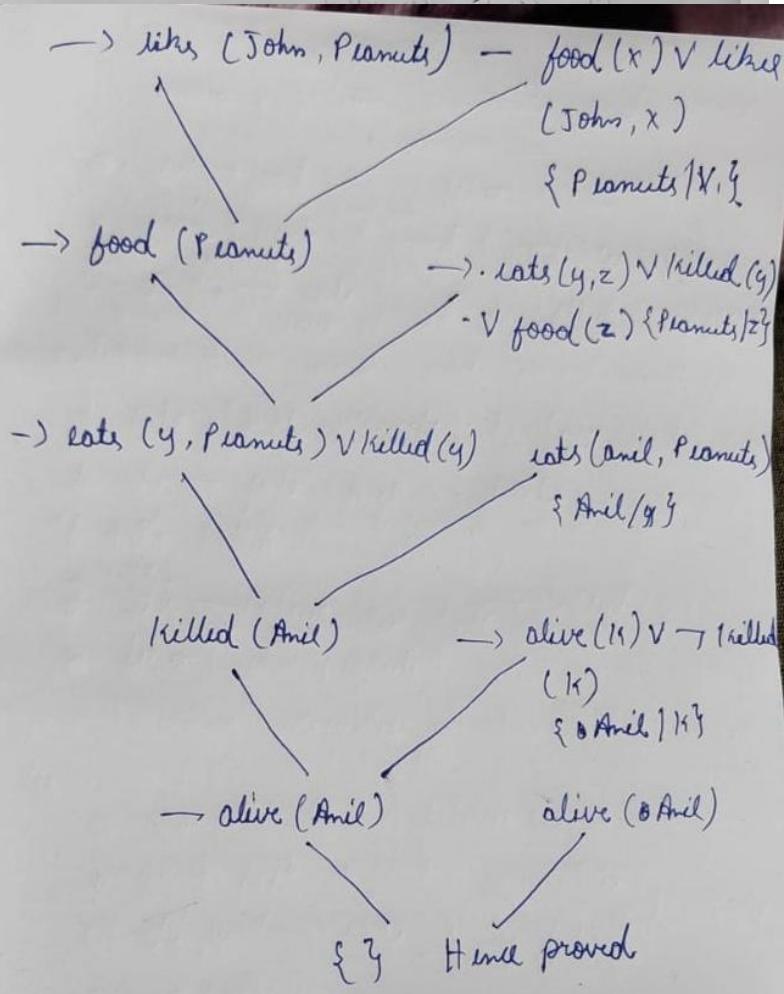
- a. $\forall x \rightarrow \text{food}(x) \vee \text{likes}(\text{John}, x)$
- b. $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetables})$
- c. $\forall x \forall y \rightarrow \text{eats}(x, y) \vee \text{killed}(x) \vee \text{food}$
 $- (y)$
- d. eats (Anil, peanuts) \wedge alive (Anil)
- e. $\forall x \rightarrow \text{eats}(\text{Anil}, x) \vee \text{eats}(\text{Harry}, x)$
- f. $\forall x \text{killed}(x) \vee \text{alive}(x)$
- g. $\forall x \rightarrow \text{alive}(x) \vee \text{killed}(x)$
- h. likes (John, peanuts)

step 4: Rename variables or standardize variables

- a. $\forall x \rightarrow \text{food}(x) \vee \text{likes}(\text{John}, x)$
- b. $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetables})$
- c. $\forall y \forall z \rightarrow \text{eats}(y, z) \vee \text{killed}(y) \vee$
 $\text{food}(z)$
- d. eats (Anil, Peanuts) \wedge alive (Anil)
- e. $\forall w \rightarrow \text{eats}(\text{Anil}, w) \vee \text{eats}(\text{Harry}, w)$
- f. $\forall g \neg \text{killed}(g) \rightarrow \text{alive}(g)$
- g. $\forall h \rightarrow \text{alive}(h) \vee \text{killed}(h)$
- h. likes (John, Peanuts)

Step 5: Drop animal.

- a. \rightarrow food (x) \vee likes (John, x)
- b. food (Apple)
- c. food (vegetable)
- d. \rightarrow eats (y, z) \vee killed (y) \vee food (z)
- e. eats (Anil, Peanuts)
- f. alive (Anil)
- g. \rightarrow eats (Anil, w) \vee eats (Harry, w)
- h. killed (g) \vee alive (g)
- i. \rightarrow alive (k) \vee \rightarrow killed (k)
- j. likes (John, Peanuts)



Code

```
def disjunctify(clauses):
    disjuncts = []
    for clause in clauses:
        disjuncts.append(tuple(clause.split('v')))

    return disjuncts

def getResolvent(ci, cj, di, dj):
    resolvent = list(ci) + list(cj)
    resolvent.remove(di)
    resolvent.remove(dj)
    return tuple(resolvent)

def resolve(ci, cj):
    for di in ci:
        for dj in cj:
            if di == '~' + dj or dj == '~' + di:
                return getResolvent(ci, cj, di, dj)

def checkResolution(clauses, query):
    clauses += [query if query.startswith('~') else '~' + query]
    proposition = '^'.join(['(' + clause + ')' for clause in clauses])
    print(f'Trying to prove {proposition} by contradiction. ')

    clauses = disjunctify(clauses)
    resolved = False
    new = set()

    while not resolved:
        n = len(clauses)

        pairs = [(clauses[i], clauses[j]) for i in range(n) for j in range(i + 1, n)]
        for (ci, cj) in pairs:
            resolvent = resolve(ci, cj)
            if not resolvent:
                resolved = True
                break
            new = new.union(set(resolvents))
            if new.issubset(set(clauses)):
                break
        for clause in new:
```

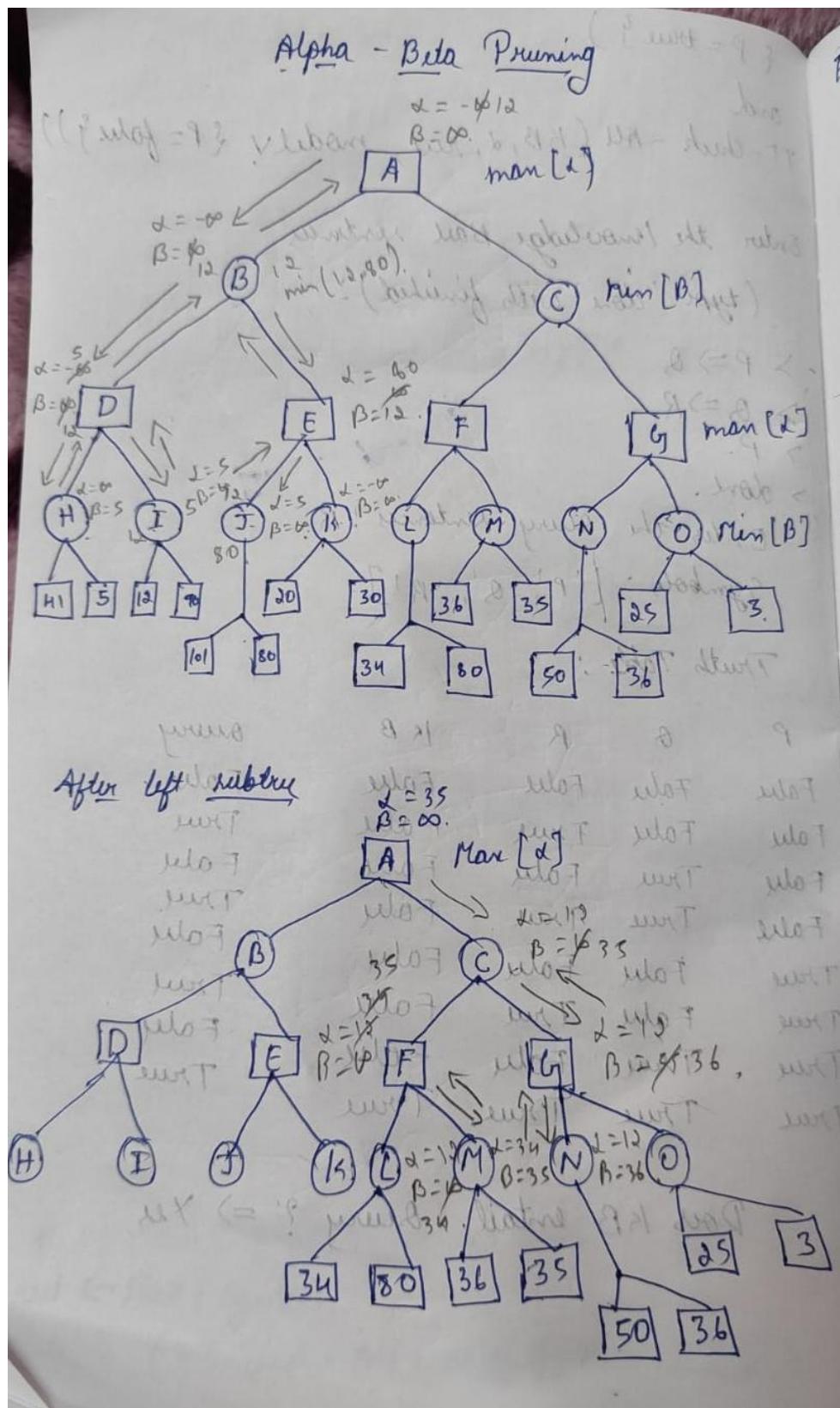
```
if clause not in clauses:  
    clauses.append(clause)  
  
if resolved:  
    print('Knowledge Base entails the query, proved by resolution')  
else:  
    print("Knowledge Base doesn't entail the query, no empty set produced after resolution")  
clauses = input('Enter the clauses ').split()  
query = input('Enter the query: ')  
checkResolution(clauses, query)
```

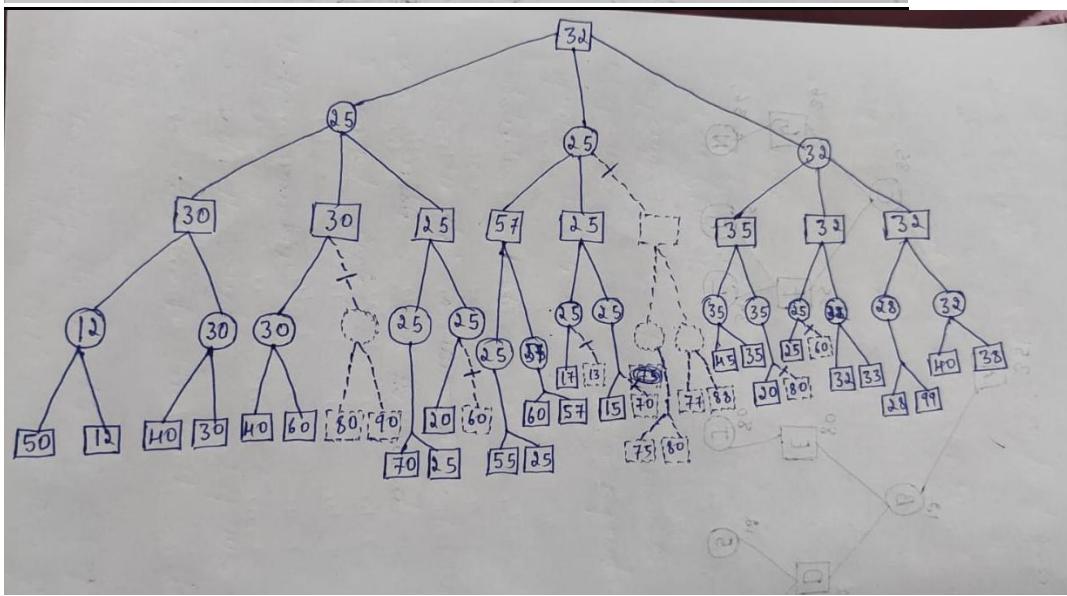
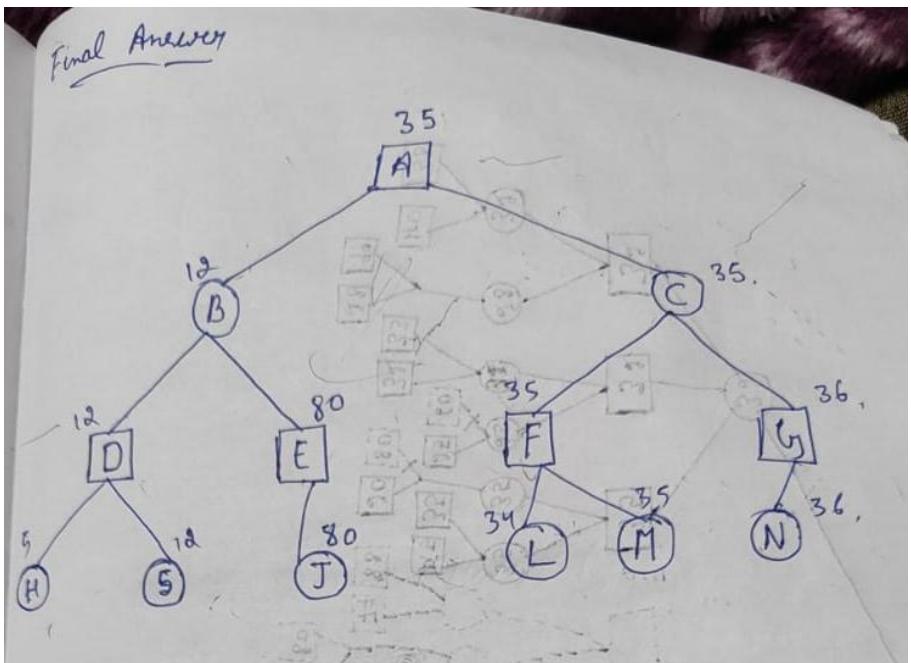
Output Snapshot

```
Enter the clauses (~qv~pvr)^(~q^p)^q  
Enter the query: r  
Trying to prove ((~qv~pvr)^(~q^p)^q)^(~r) by contradiction....  
Knowledge Base entails the query, proved by resolution
```

Program-11

Alpha Beta Pruning Algorithm :





Code

```

import math
# Alpha-Beta Pruning Functions
def alpha_beta_search(state):
    """ Alpha-Beta Search to get the optimal action """
    value = max_value(state, -math.inf, math.inf)
    print("Optimal Value:", value)
    return value

def max_value(state, alpha, beta):
    """ Function to calculate the MAX value node """
    if terminal_test(state): # If leaf node, return utility value
        return utility(state)
    v = -math.inf
    for child in state["children"]:
        # Iterate through child nodes
        v = max(v, alpha_beta_search(child))
        if v >= beta:
            break
    return v
  
```

```

v = max(v, min_value(child, alpha, beta))
if v >= beta:
    return v # Beta cutoff
    alpha = max(alpha, v)
return v

def min_value(state, alpha, beta):
    """ Function to calculate the MIN value node """
    if terminal_test(state): # If leaf node, return utility value
        return utility(state)
    v = math.inf
    for child in state["children"]:
        # Iterate through child nodes
        v = min(v, max_value(child, alpha, beta))
        if v <= alpha:
            return v # Alpha cutoff
            beta = min(beta, v)
    return v

# Utility Functions
def terminal_test(state):
    """ Check if the node is a leaf node """
    return "value" in state # Leaf node if it contains 'value'

def utility(state):
    """ Return the utility value of a leaf node """
    return state["value"]

# Build the Binary Tree Based on Leaf Nodes
def build_tree(values):
    """ Recursively build a binary tree from a list of leaf node values """
    if len(values) == 1: # Single value -> Leaf node
        return {"value": values[0]}
    mid = len(values) // 2
    left_subtree = build_tree(values[:mid])
    right_subtree = build_tree(values[mid:])
    return {"children": [left_subtree, right_subtree]}

# Main Program
if __name__ == "__main__":
    leaf_nodes = [10, 9, 14, 18, 5, 4, 50, 3]
    tree = build_tree(leaf_nodes) # Build the binary tree
    print("Alpha-Beta Pruning Search:")
    alpha_beta_search(tree)

```

Output

Alpha-Beta Pruning Search:
Optimal Value: 10

