

VISVESVARAYA TECHNOLOGICAL UNIVERSITY

“JnanaSangama”, Belgaum -590014, Karnataka.



LAB REPORT on

Artificial Intelligence (23CS5PCAIN)

Submitted by

VIJAY J(1WA23CS040)

in partial fulfillment for the award of the degree of
BACHELOR OF ENGINEERING
in
COMPUTER SCIENCE AND ENGINEERING



B.M.S. COLLEGE OF ENGINEERING

(Autonomous Institution under VTU)

BENGALURU-560019

Aug-2025 to Jan-2026

B.M.S. College of Engineering,
Bull Temple Road, Bangalore 560019
(Affiliated To Visvesvaraya Technological University, Belgaum)
Department of Computer Science and Engineering



CERTIFICATE

This is to certify that the Lab work entitled “Artificial Intelligence (23CS5PCAIN)” carried out by **VIJAY J (1WA23CS040)**, who is bonafide student of **B.M.S. College of Engineering**. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements in respect of an Artificial Intelligence (23CS5PCAIN) work prescribed for the said degree.

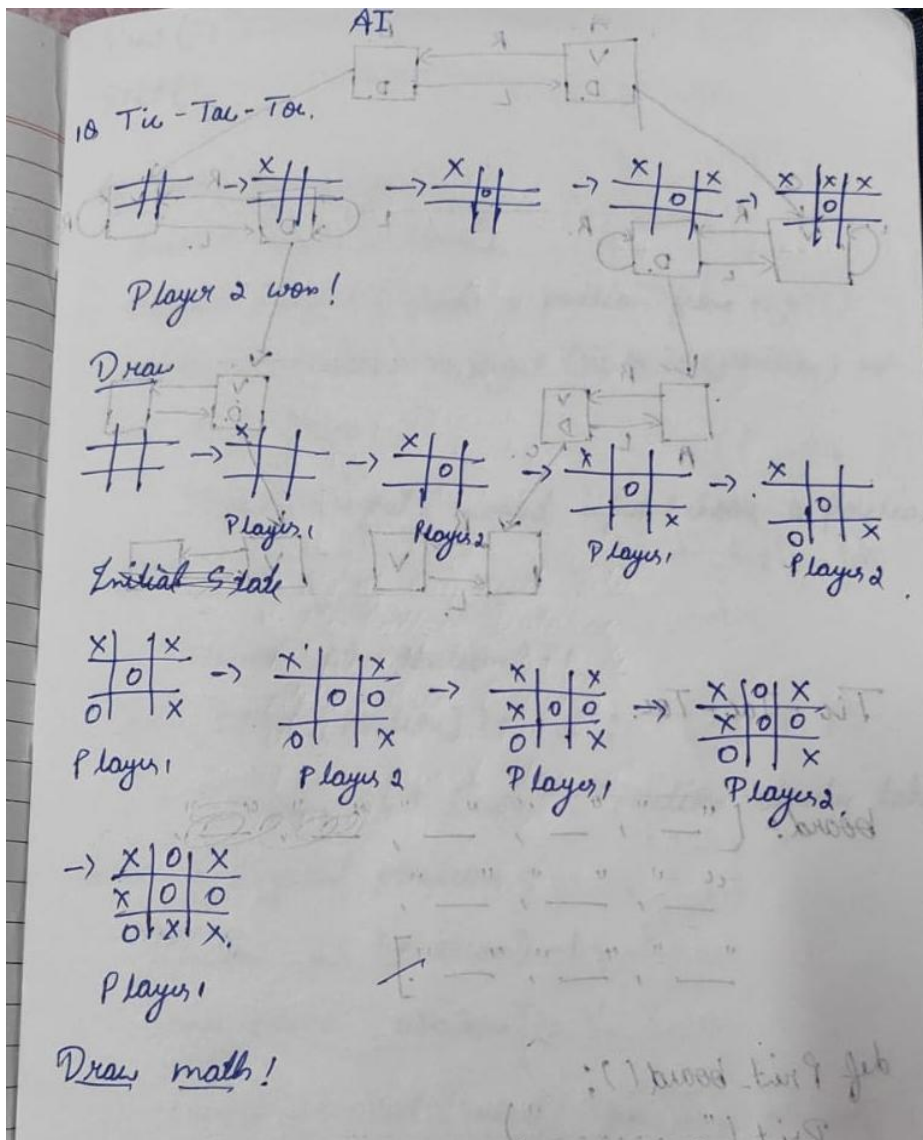
Lab faculty : SINDHOOR N Assistant Professor Department of CSE, BMSCE	Dr. Kavitha Sooda Professor & HOD Department of CSE, BMSCE
---	--

Index

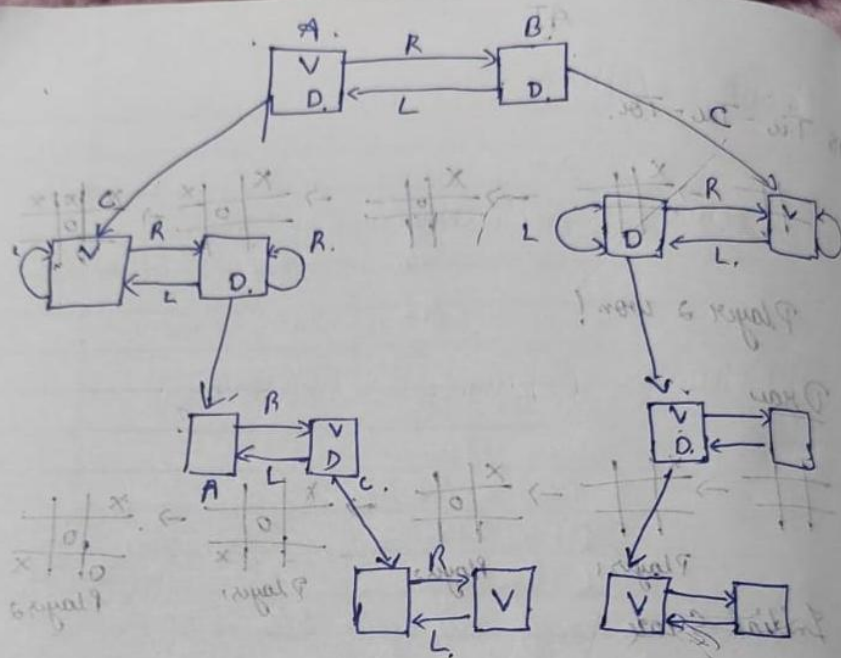
Sl. No.	Date	Experiment Title	Page No.
1.	19-8-2025	Implement Tic –Tac –Toe Game Implement vacuum cleaner agent	1-11
2.	2-9-2025	Implement 8 puzzle problems using Depth First Search (DFS) Implement Iterative deepening search algorithm	12-17
3.	16-9-2025	Implement A* search algorithm	18-23
4.	9-9-2025	Implement Hill Climbing search algorithm to solve N-Queens problem	24-28
5.	14-10-2025	Create a knowledge base using propositional logic and show that the given query entails the knowledge base or not.	29-32
6.	13-11-2025	Implement unification in first order logic	33-37
7.	13-11-2025	Create a knowledge base consisting of first order logic statements and prove the given query using forward reasoning.	38-44
8.	13-11-2025	Create a knowledge base consisting of first order logic statements and prove the given query using Resolution	45-50
9.	11-11-2025	Implement Alpha-Beta Pruning.	51-55

Program 1 - Tic Tac toe and Vacum Cleaner

Algorithm



Code



Tic - Tac - Toe

board = ["-", "-", "-", "~~0~~", "~~0~~"]
 ["-", "-", "-", "~~0~~", "~~0~~"]
 ["-", "-", "-", "~~0~~", "~~0~~"]

def Print_board():

Print("-----")

Print("1" + board[0] + "1" + board[1] + "1" + board[2] + "1")

- [2] + "1"]

Print("-----")

Print("1" + board[3] + "1" + board[4] + "1" + board[5] + "1")

- [5] + "1"]

```

Print("1" + board[0] + "1" + board[3] + "1" + board[6] + "1")
Print("2" + board[1] + "2" + board[4] + "2" + board[7] + "2")
Print("3" + board[2] + "3" + board[5] + "3" + board[8] + "3")

def take_turn(player):
    Print(f"{player}'s turn")
    Position = input("choose a position from 1-9:")
    while not Position.isdigit() or int(Position) not
    in range(1, 10):
        Position = input("invalid input (choose a position
        from 1-9: ")
    Position = int(Position) - 1
    while board[Position] != "_":
        Position = int(input("position already taken
        choose a different position: "))
    Position = int(Position) - 1
    while board[Position] != "_":
        Position = int(input("position already
        taken (choose a different position: ") - 1
    board[Position] = player
    Print(board())

```



```
def check-win(player):
```

```
    return ((board[0] == board[1] == board[2]
```

```
    == player) or
```

```
    (board[3] == board[4] == board[5] ==
```

```
    player) or
```

```
    (board[6] == board[7] == board[8] ==
```

```
    player)).
```

```
def check-tie():
```

```
    return "_" not in board.
```

```
def play-game():
```

```
    print("Welcome to Tic Tac Toe!")
```

```
    print
```

```
    print-board()
```

```
    current-player = "X"
```

```
    game-over = False
```

```
    while not game-over:
```

```
        take-turn(current-player)
```

```
        if check-win(current-player):
```

```
            print(f"current-player wins!")
```

```
            game-over = True.
```

elif check tie():

Print ("its a tie!")

game-over = True

else:
current-player = "O" if current-player == "X" else "X"

Play-game()

8/29/25

Print ("Room", "V", "max")

if ("O" == [v] room):

if (v == 0):

v += 1

else: v -= 1

loop ("! Room clean!")

clean-room()

Room 0 clean!

Room 1 clean!

Vacuum Cleaner

```
rooms = ["0", "0"];
```

```
def fullclean(rooms):
```

```
    if (rooms[0] == "ND" and rooms[1] == "ND"):
```

```
        return True
```

```
    else:
```

```
        return False.
```

```
def clean_rooms():
```

```
    v = 0;
```

```
    while not fullclean(rooms):
```

```
        if (rooms[v] == "0"):
```

```
            rooms[v] = "ND"
```

```
            Print("Room", "v", "cleaned!")
```

```
        elif (rooms[v] == "ND"):
```

```
            if (v == 0):
```

```
                v += 1
```

```
            else: v -= 1
```

```
            Print("All rooms cleaned!")
```

```
clean_rooms()
```

O/P

Room 0 cleaned!

Room 1 cleaned!

All rooms cleaned!

2/9/25

Code

```
import random  
class TicTacToe:
```

```

def __init__(self):
    self.board = []
    def create_board(self):
        for i in range(3):
            row = []
            for j in range(3):
                row.append('-')
            self.board.append(row)
    def get_random_first_player(self):
        return random.randint(0, 1)
    def fix_spot(self, row, col, player):
        self.board[row][col] = player
    def is_player_win(self, player):
        win = None
        n = len(self.board)
        for i in range(n):
            win = True
            for j in range(n):
                if self.board[i][j] != player:
                    win = False
                    break
            if win:
                return win
        for i in range(n):
            win = True
            for j in range(n):
                if self.board[j][i] != player:
                    win = False
                    break
            if win:
                return win
        win = True
        for i in range(n):
            if self.board[i][i] != player:
                win = False
                break
        if win:
            return win
        win = True

```

```

for i in range(n):
    if self.board[i][n - 1 - i] != player:
        win = False
        break
if win:
    return win
return False
for row in self.board:
    for item in row:
        if item == '-':
            return False
return True
def is_board_filled(self):
    for row in self.board:
        for item in row:
            if item == '-':
                return False
    return True
def swap_player_turn(self, player):
    return 'X' if player == 'O' else 'O'
def show_board(self):
    for row in self.board:
        for item in row:
            print(item, end=" ")
        print()
def start(self):
    self.create_board()
    player = 'X' if self.get_random_first_player() == 1 else 'O'
    while True:
        print(f'Player {player} turn')
        self.show_board()
        row, col = list(
            map(int, input("Enter row and column numbers to fix spot: ").split()))
        print()
        self.fix_spot(row - 1, col - 1, player)
        if self.is_player_win(player):
            print(f'Player {player} wins the game!')
            break
        if self.is_board_filled():

```

```

        print("Match Draw!")
        break
    player = self.swap_player_turn(player)
    print()
    self.show_board()
tic_tac_toe = TicTacToe()
tic_tac_toe.start()

```

Output Snapshot

```

Player 0 turn
- - -
- - -
- - -
Enter row and column numbers to fix spot: 0 3
Player X turn
- - -
- - -
- - 0
Enter row and column numbers to fix spot: 1 2
Player 0 turn
- X - - -
- - 0
Enter row and column numbers to fix spot: 3 0
Player X turn
- X -
- - -
- - 0
Enter row and column numbers to fix spot: 3 2
Player 0 turn
- X -
- - -
- X 0
Enter row and column numbers to fix spot: 2 1
Player X turn
- X -
0 - -
- X 0
Enter row and column numbers to fix spot: 2 2
Player X wins the game!

```

Program 2 - Vacuum Cleaner

Code

```
def vacuum_world():

    goal_state = {'A': '0', 'B': '0'}
    cost = 0

    location_input = input("Enter Location of Vacuum: ")
    status_input = input("Enter status of " + location_input + " : ")
    status_input_complement = input("Enter status of other room : ")

    print("Initial Location Condition {A : " + str(status_input_complement) + ", B : " + str(status_input) + " }")
    if location_input == 'A':
        print("Vacuum is placed in Location A")
        if status_input == '1':
            print("Location A is Dirty.")
            goal_state['A'] = '0'
            cost += 1 #cost for suck
            print("Cost for CLEANING A " + str(cost))
            print("Location A has been Cleaned.")

            if status_input_complement == '1':
                print("Location B is Dirty.")
                print("Moving right to the Location B. ")
                cost += 1
                print("COST for moving RIGHT " + str(cost))
                goal_state['B'] = '0'
                cost += 1
                print("COST for SUCK " + str(cost))
                print("Location B has been Cleaned. ")
            else:
                print("No action" + str(cost))
                print("Location B is already clean.")

        if status_input == '0':
            print("Location A is already clean ")
            if status_input_complement == '1':
                print("Location B is Dirty.")
                print("Moving RIGHT to the Location B. ")
                cost += 1
                print("COST for moving RIGHT " + str(cost))
                goal_state['B'] = '0'
                cost += 1
```

```

        print("Cost for SUCK" + str(cost))
        print("Location B has been Cleaned. ")
    else:
        print("No action " + str(cost))
        print(cost)
        print("Location B is already clean.")

else:
    print("Vacuum is placed in location B")
    if status_input == '1':
        print("Location B is Dirty.")
        goal_state['B'] = '0'
        cost += 1
        print("COST for CLEANING " + str(cost))

    print("Location B has been Cleaned.")

    if status_input_complement == '1':
        print("Location A is Dirty.")
        print("Moving LEFT to the Location A. ")
        cost += 1
        print("COST for moving LEFT " + str(cost))
        goal_state['A'] = '0'
        cost += 1
        print("COST for SUCK " + str(cost))
        print("Location A has been Cleaned.")

    else:
        print(cost)
        print("Location B is already clean.")

    if status_input_complement == '1':
        print("Location A is Dirty.")
        print("Moving LEFT to the Location A. ")
        cost += 1
        print("COST for moving LEFT " + str(cost))
        goal_state['A'] = '0'
        cost += 1
        print("Cost for SUCK " + str(cost))
        print("Location A has been Cleaned. ")
    else:

```



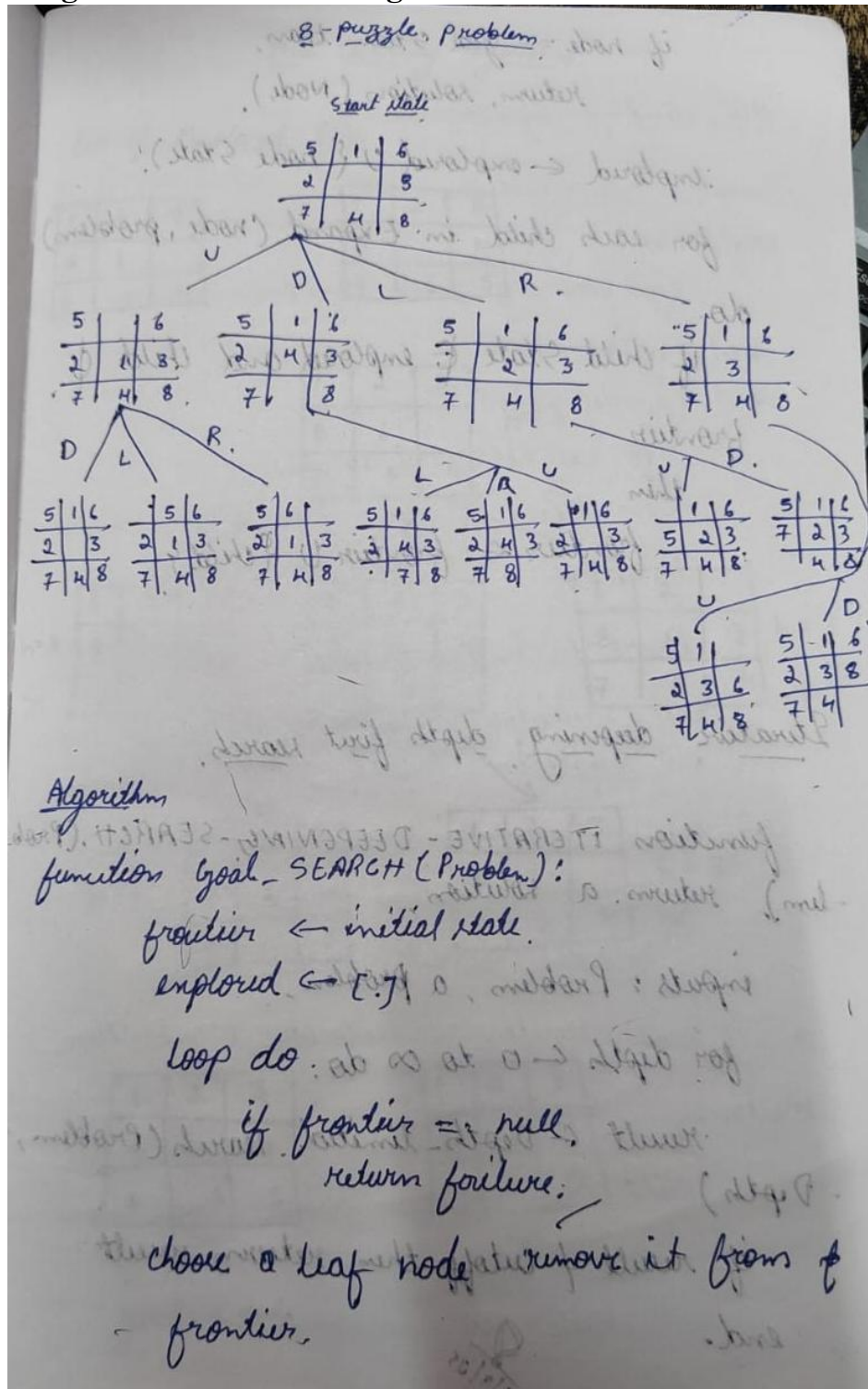
```
print("No action " + str(cost))
print("Location A is already clean.")
```

```
print("GOAL STATE: ")
print(goal_state)
print("Performance Measurement: " + str(cost))
vacuum_world()
```

Output Snapshot

```
Enter Location of Vacuum: A
Enter status of A : 0
Enter status of other room : 1
Initial Location Condition {A : 1, B : 0 }
Vacuum is placed in Location A
Location A is already clean
Location B is Dirty.
Moving RIGHT to the Location B.
COST for moving RIGHT 1
Cost for SUCK2
Location B has been Cleaned.
GOAL STATE:
{'A': '0', 'B': '0'}
Performance Measurement: 2
|
```

Program 3 - 8 Puzzle Using BFS



Algorithm :

if node == goal state then,
 return, solution (Node).
 explored \leftarrow explored \cup { node state }.
 for each child in Expand (node, problem)
 do
 if child state \notin explored and child \notin
 frontier
 then
 frontier \leftarrow frontier \cup { child }
Iterative deepening depth first search.
 function ITERATIVE-DEEPENING-SEARCH (Prob-
 lem) return, a solution
 inputs: Problem, a problem
 for depth $\leftarrow 0$ to ∞ do
 result \leftarrow Depth-limited search (Problem,
 Depth)
 if result \neq cutoff then return result
 end.

Code

```

import sys
import numpy as np
class Node:
    def __init__(self, state, parent, action):
        self.state = state
        self.parent = parent
  
```

```

        self.action = action
class StackFrontier:
    def __init__(self):
        self.frontier = []
    def add(self, node):
        self.frontier.append(node)
    def contains_state(self, state):
        return any((node.state[0] == state[0]).all() for node in self.frontier)
    def empty(self):
        return len(self.frontier) == 0
    def remove(self):
        if self.empty():
            raise Exception("Empty Frontier")
        else:
            node = self.frontier[-1]
            self.frontier = self.frontier[:-1]
            return node
class QueueFrontier(StackFrontier):
    def remove(self):
        if self.empty():
            raise Exception("Empty Frontier")
        else:
            node = self.frontier[0]
            self.frontier = self.frontier[1:]
            return node
class Puzzle:
    def __init__(self, start, startIndex, goal, goalIndex):
        self.start = [start, startIndex]
        self.goal = [goal, goalIndex]
        self.solution = None

    def neighbors(self, state):
        mat, (row, col) = state

```

```

results = []
if row > 0:
    mat1 = np.copy(mat)
    mat1[row][col] = mat1[row - 1][col]
    mat1[row - 1][col] = 0
    results.append(('up', [mat1, (row - 1, col)]))
if col > 0:
    mat1 = np.copy(mat)
    mat1[row][col] = mat1[row][col - 1]
    mat1[row][col - 1] = 0
    results.append(('left', [mat1, (row, col - 1)]))
if row < 2:
    mat1 = np.copy(mat)
    mat1[row][col] = mat1[row + 1][col]
    mat1[row + 1][col] = 0
    results.append(('down', [mat1, (row + 1, col)]))
if col < 2:
    mat1 = np.copy(mat)
    mat1[row][col] = mat1[row][col + 1]
    mat1[row][col + 1] = 0
    results.append(('right', [mat1, (row, col + 1)]))
return results

def print(self):
    solution = self.solution if self.solution is not None else None

    print("Start State:\n", self.start[0], "\n")
    print("Goal State:\n", self.goal[0], "\n")
    print("\nStates Explored: ", self.num_explored, "\n")
    print("Solution:\n ")
    for action, cell in zip(solution[0], solution[1]):
        print("action: ", action, "\n", cell[0], "\n")
    print("Goal Reached!!")

def does_not_contain_state(self, state):
    for st in self.explored:
        if (st[0] == state[0]).all():
            return False
    return True

def solve(self):
    self.num_explored = 0
    start = Node(state=self.start, parent=None, action=None)

```

```

frontier = QueueFrontier()
frontier.add(start)
self.explored = []
while True:
    if frontier.empty():
        raise Exception("No solution")
    node = frontier.remove()
    self.num_explored += 1
    if (node.state[0] == self.goal[0]).all():
        actions = []
        cells = []
        while node.parent is not None:
            actions.append(node.action)
            cells.append(node.state)
            node = node.parent
        actions.reverse()
        cells.reverse()
        self.solution = (actions, cells)
        return
    self.explored.append(node.state)
    for action, state in self.neighbors(node.state):
        if not frontier.contains_state(state) and self.does_not_contain_state(state):
            child = Node(state=state, parent=node, action=action)
            frontier.add(child)

start = np.array([[1, 2, 3], [8, 0, 4], [7, 6, 5]])

goal = np.array([[2, 8, 1], [0, 4, 3], [7, 6, 5]])
startIndex = (1, 1)
goalIndex = (1, 0)
p = Puzzle(start, startIndex, goal, goalIndex)
p.solve() p.print()

```


Output Snapshot

```
Start State:
[[1 2 3]
 [8 0 4]
 [7 6 5]]

Goal State:
[[2 8 1]
 [0 4 3]
 [7 6 5]]

States Explored: 358

Solution:

action: up
[[1 0 3]
 [8 2 4]
 [7 6 5]]

action: left
[[0 1 3]
 [8 2 4]
 [7 6 5]]

action: down
[[8 1 3]
 [0 2 4]
 [7 6 5]]

action: right
[[8 1 3]
 [2 0 4]
 [7 6 5]]

action: right
[[8 1 3]
 [2 4 0]
 [7 6 5]]

action: down
[[8 1 3]
 [0 2 4]
 [7 6 5]]

action: right
[[8 1 3]
 [2 0 4]
 [7 6 5]]

action: right
[[8 1 3]
 [2 4 0]
 [7 6 5]]

action: down
[[8 1 3]
 [0 2 4]
 [7 6 5]]

action: right
[[8 1 3]
 [2 0 4]
 [7 6 5]]

action: up
[[8 1 0]
 [2 4 3]
 [7 6 5]]

action: left
[[8 0 1]
 [2 4 3]
 [7 6 5]]

action: left
[[0 8 1]
 [2 4 3]
 [7 6 5]]

action: down
[[2 8 1]
 [0 4 3]
 [7 6 5]]

Goal Reached!!
```

Program 04 - 8 Puzzle Using A*

Algorithm

A* Algorithm on 8 puzzle

Algorithm

function $A^*(start, goal)$

 open-list \leftarrow priority queue ordered by
 $f(n) = g(n) + h(n)$

 closed-list \leftarrow empty set

$g(start) \leftarrow 0$

$f(start) \leftarrow g(start) + h(start)$

 open-list.insert($start, f(start)$)

 while open-list is not empty

 current \leftarrow node in open-list with
 lowest f value,

 if current = goal:

 return path from start to goal

 add current to closed-list

 for each neighbour of current:

 if neighbour is closed-list:

 continue

 tentative-g $\leftarrow g(current) + cost($
 current, neighbour)

5	6	1
4		8
2	3	7

if neighbour not in open-list or,

tentative $\rightarrow g < g(\text{neighbour})$

$g(\text{neighbour}) \leftarrow \text{tentative } g$

$f(\text{neighbour}) \leftarrow g(\text{neighbour}) +$

$h(\text{neighbour})$

$\text{Parent}(\text{neighbour}) \leftarrow \text{current}$

if neighbour not in open-list,

open-list.insert(neighbour, $f(-$

$-\text{neighbour})$)

return failure.

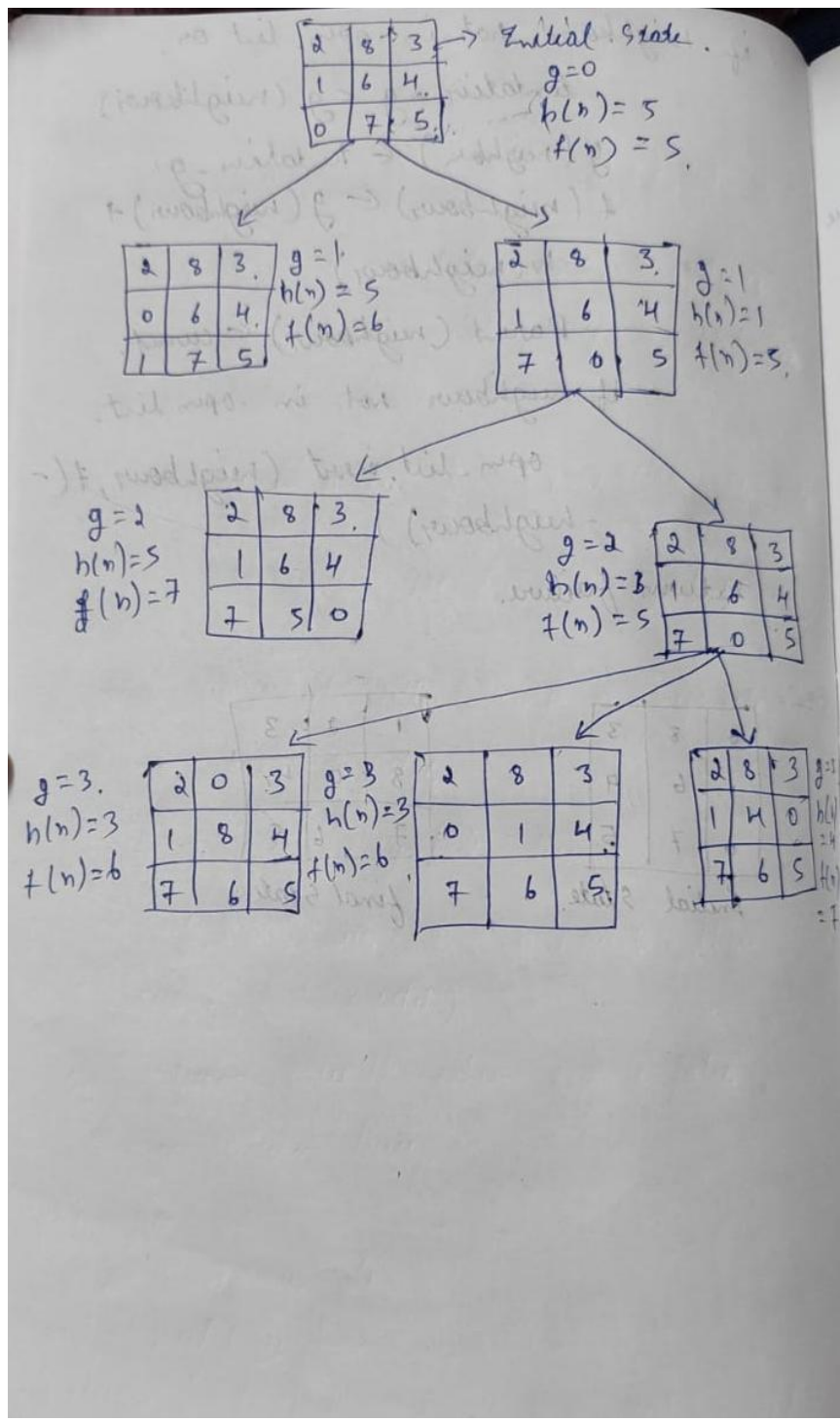
Ex:-

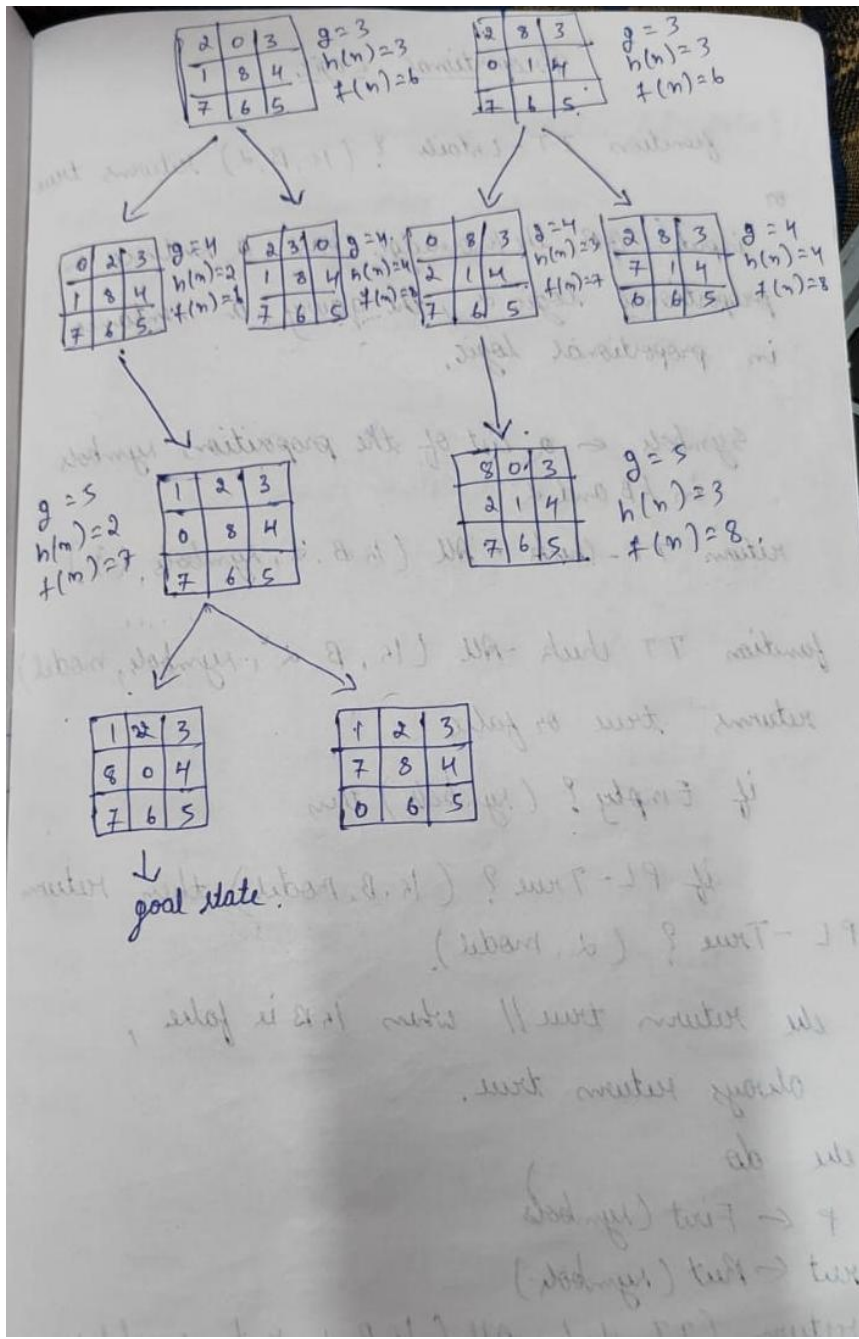
2	8	3
1	6	4
0	7	5

Initial state

1	2	3
8	0	4
7	6	5

final state





Code

```
def print_b(src):
    state = src.copy()
    state[state.index(-1)] = ''
    print(
        f"""
        {state[0]} {state[1]} {state[2]}
        {state[3]} {state[4]} {state[5]}
        {state[6]} {state[7]} {state[8]}
        """)
    )
```

```

def h(state, target):
    count = 0
    i = 0
    for j in state:
        if state[i] != target[i]:
            count = count+1
    return count

def astar(state, target):
    states = [src]
    g = 0
    visited_states = []
    while len(states):
        print(f'Level: {g}')
        moves = []
        for state in states:
            visited_states.append(state)
            print_b(state)
            if state == target:
                print("Success")
                return
            moves += [move for move in possible_moves(
                state, visited_states) if move not in moves]
        costs = [g + h(move, target) for move in moves]
        states = [moves[i]
                    for i in range(len(moves)) if costs[i] == min(costs)]
        g += 1
    print("Fail")

def possible_moves(state, visited_state):

```



```

b = state.index(-1)
d = []
if b - 3 in range(9):
    d.append('u')
if b not in [0, 3, 6]:
    d.append('l')
if b not in [2, 5, 8]:
    d.append('r')
if b + 3 in range(9):
    d.append('d')
pos_moves = []
for m in d:
    pos_moves.append(gen(state, m, b))
return [move for move in pos_moves if move not in visited_state]
def gen(state, m, b):
    temp = state.copy()
    if m == 'u':
        temp[b - 3], temp[b] = temp[b], temp[b - 3]
    if m == 'l':
        temp[b - 1], temp[b] = temp[b], temp[b - 1]
    if m == 'r':
        temp[b + 1], temp[b] = temp[b], temp[b + 1]
    if m == 'd':
        temp[b + 3], temp[b] = temp[b], temp[b + 3]
    return temp
src = [1, 2, 3, -1, 4, 5, 6, 7, 8]
target = [1, 2, 3, 4, 5, 6, 7, 8, -1]
astar(src, target)

```

Output Snapshot

```

Enter the start state matrix

1 0 1 0
1 0 0 1
1 1 1 1
Enter the goal state matrix

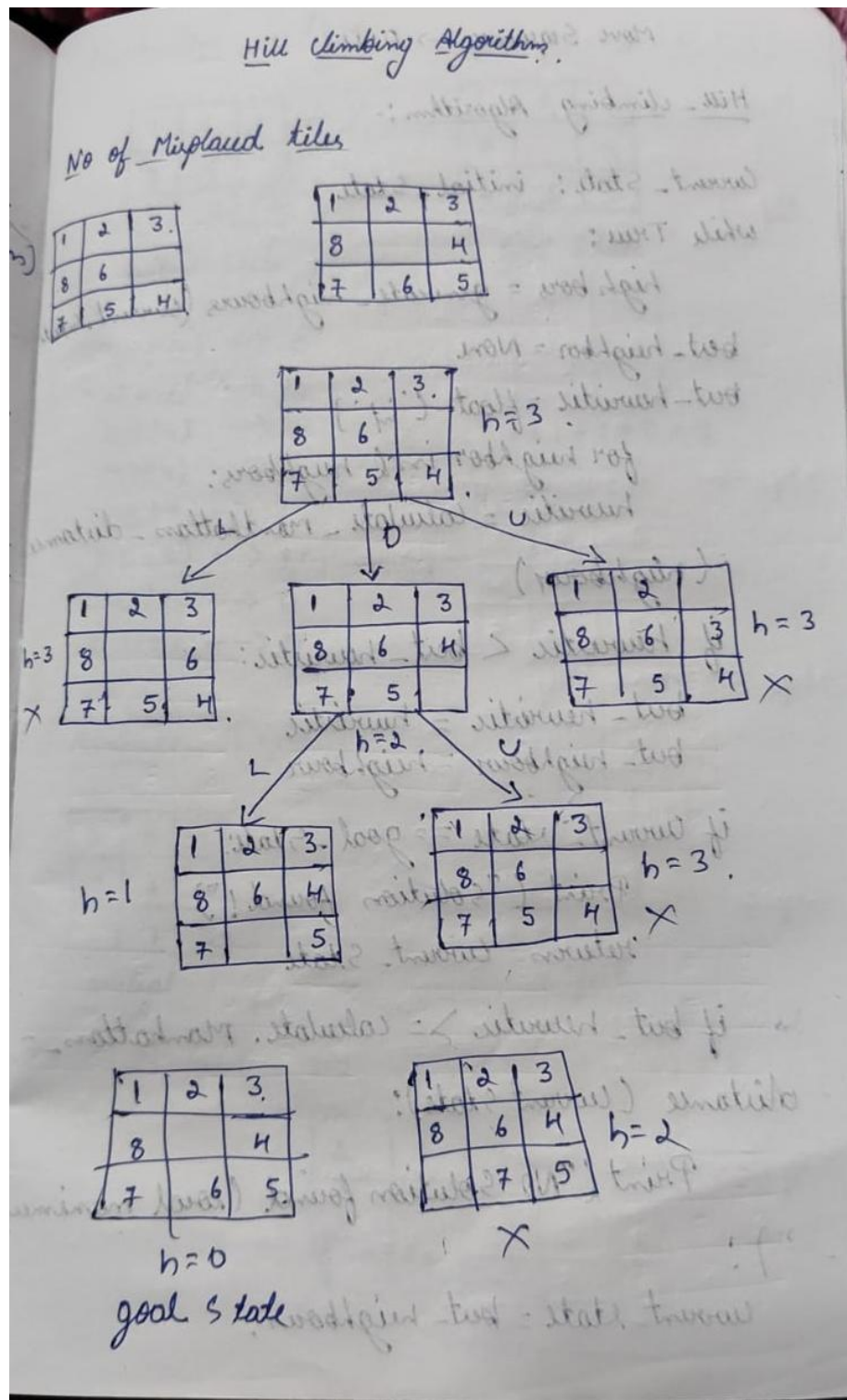
1 1 0 1
1 0 0 1
1 1 1 0
|
|
\'/

1 0 1 0
1 0 0 1
1 1 1 1

```

Program 05 – Hill Climbing

Algorithm



Move Sequence \rightarrow DLU with

Hill-climbing Algorithm:-

Current-State: initial-state

while True:

highbores = generate-neighbours (Current-State)

best-neighbor = None

best-heuristic = float('inf')

for neighbor in highbores:

heuristic = calculate-manhattan-distance

=(neighbor)

if heuristic < best-heuristic:

best-heuristic = heuristic

best-neighbor = neighbor

if Current-State == goal-State:

Print ("Solution found!")

return Current-State

if best-heuristic >= calculate-manhattan-

distance (Current State):

Print ("No Solution found (local maximum)

-"):

Current-State = best-neighbor

Manhattan Distance

1	2	3
8	6	
7	5	4

Initial State

1	2	3
8		4
7	6	5

Goal State

$$MD(1) \rightarrow 0$$

$$MD(2) \rightarrow 0$$

$$MD(3) \rightarrow 0$$

$$MD(4) \rightarrow 1$$

$$MD(5) \rightarrow 1$$

$$MD(6) \rightarrow 1$$

$$MD(7) \rightarrow 0$$

$$MD(8) \rightarrow 0$$

$$0 + 0 + 1 + 1 + 1 + 0 + 0$$

$$= 3$$

iii) Manhattan Distance

2	8	3
1	6	4
	7	5

initial state

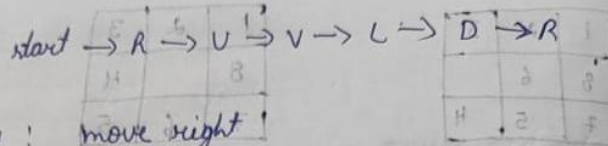
1	2	3
8		4
7	6	5

Goal state

$$h = 1 + 1 + 0 + 0 + 0 + 1 + 1 + 2 = 6$$

2	8	3
1	6	4
	7	5

Blank at (3,1) can move right $h=5$ but...



step-1: move right

state loop

2	8	3
1	6	4
7		5

$0+0+1+1+1+0+0$

step-2 move up

2	8	3
1		4
7	6	5

$h=4$

step 3: move up

2		3
4	8	4
7	6	5

$h=3$

step 4: move left

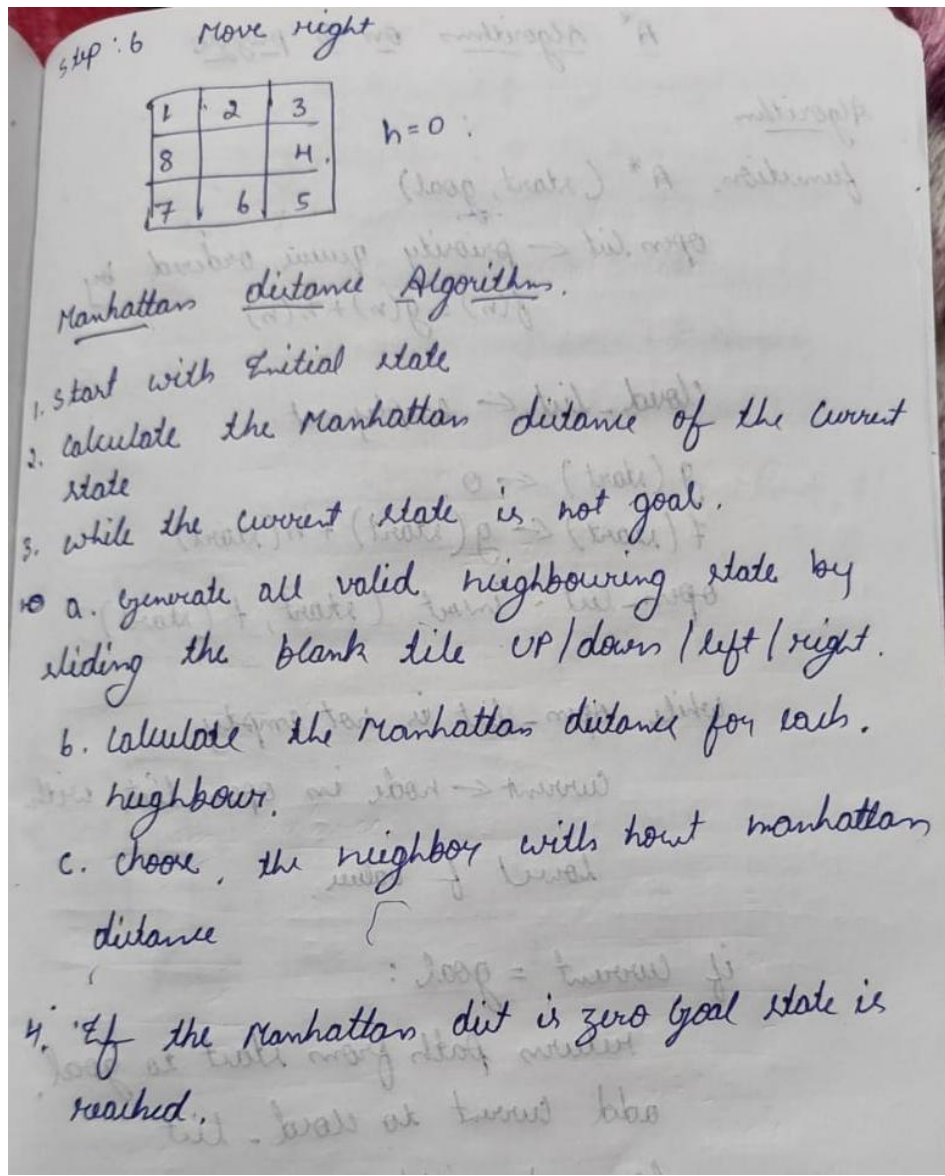
1	2	3
1		4
7	6	5

$h=3$

step 5: Move down

1	2	3
	8	4
7	6	5

$h=2$



Code

```
from random import randint
N = 8
def configureRandomly(board, state):
    for i in range(N):
        state[i] = randint(0, 100000) % N;
        board[state[i]][i] = 1;
def printBoard(board):
    for i in range(N):
        print(*board[i])
def printState( state):
    print(*state)
def compareStates(state1, state2):
    for i in range(N):
        if (state1[i] != state2[i]):
```

```

        return False;
    return True;
def fill(board, value):
    for i in range(N):
        for j in range(N):
            board[i][j] = value;
def calculateObjective( board, state):
    for i in range(N):
        row = state[i]
        col = i - 1;
        while (col >= 0 and board[row][col] != 1) :
            col -= 1
        if (col >= 0 and board[row][col] == 1) :
            attacking += 1;
        row = state[i]
        col = i + 1;
        while (col < N and board[row][col] != 1):
            col += 1;
        if (col < N and board[row][col] == 1) :
            attacking += 1;
        row = state[i] - 1
        col = i - 1;
        while (col >= 0 and row >= 0 and board[row][col] != 1) :
            col-= 1;
            row-= 1;

        if (col >= 0 and row >= 0 and board[row][col] == 1) :
            attacking+= 1;

    # Diagonally to the right down
    # (row and col simultaneously
    # increase)
    row = state[i] + 1
    col = i + 1;
    while (col < N and row < N and board[row][col] != 1) :
        col+= 1;
        row+= 1;

    if (col < N and row < N and board[row][col] == 1) :
        attacking += 1;

```

```

        row = state[i] + 1
        col = i - 1;
        while (col >= 0 and row < N and board[row][col] != 1) :
            col -= 1;
            row += 1;
        if (col >= 0 and row < N and board[row][col] == 1) :
            attacking += 1;
        row = state[i] - 1
        col = i + 1;
        while (col < N and row >= 0 and board[row][col] != 1) :
            col += 1;
            row -= 1;
        if (col < N and row >= 0 and board[row][col] == 1) :
            attacking += 1;
    return int(attacking / 2);
def generateBoard( board, state):
    fill(board, 0);
    for i in range(N):
        board[state[i]][i] = 1;
def copyState( state1, state2):

    for i in range(N):
        state1[i] = state2[i];

def getNeighbour(board, state):
    opBoard = [[0 for _ in range(N)] for _ in range(N)]
    opState = [0 for _ in range(N)]

    copyState(opState, state);
    generateBoard(opBoard, opState);
    opObjective = calculateObjective(opBoard, opState);
    NeighbourBoard = [[0 for _ in range(N)] for _ in range(N)]

    NeighbourState = [0 for _ in range(N)]
    copyState(NeighbourState, state);
    generateBoard(NeighbourBoard, NeighbourState);
    for i in range(N):
        for j in range(N):
            if (j != state[i]) :
                NeighbourState[i] = j;

```



```

        NeighbourBoard[NeighbourState[i]][i] = 1;
        NeighbourBoard[state[i]][i] = 0;
        temp = calculateObjective( NeighbourBoard, NeighbourState)
        if (temp <= opObjective) :
            opObjective = temp;
            copyState(opState, NeighbourState);
            generateBoard(opBoard, opState);
        NeighbourBoard[NeighbourState[i]][i] = 0;
        NeighbourState[i] = state[i];
        NeighbourBoard[state[i]][i] = 1;

    copyState(state, opState);
    fill(board, 0);
    generateBoard(board, state);

def hillClimbing(board, state):
    neighbourBoard = [[0 for _ in range(N)] for _ in range(N)]
    neighbourState = [0 for _ in range(N)]
    copyState(neighbourState, state);
    generateBoard(neighbourBoard, neighbourState);

    while True:
        copyState(state, neighbourState);
        generateBoard(board, state);
        # Getting the optimal neighbour
        getNeighbour(neighbourBoard, neighbourState);
        if (compareStates(state, neighbourState)) :

            printBoard(board);
            break;

        elif (calculateObjective(board, state) == calculateObjective(
neighbourBoard,neighbourState)):
            # Random neighbour
            neighbourState[randint(0, 100000) % N] = randint(0, 100000) % N;
            generateBoard(neighbourBoard, neighbourState);

# Driver code
state = [0] * N
board = [[0 for _ in range(N)] for _ in range(N)]
configureRandomly(board, state);

```

hillClimbing(board, state);

OUTPUT

```
Step 0: Initial state
. . . Q
. Q . .
. . Q .
Q . . .

Cost = 2

Step 1: Move to better neighbour
. . . Q
Q . . .
. . Q .
. Q . .

Cost = 1

Step 2: Move to better neighbour
. . Q .
Q . . .
. . . Q
. Q . .

Cost = 0

Step 3: Reached local minimum
Final state:
. . Q .
Q . . .
. . . Q
. Q . .

Final cost = 0
```

Program-07 Knowledge-Base

ALGORITHM :

Proportional Logic

function TT-entails ? (K, B, α) returns true

or

inputs: - K, B , the knowledge base, a sentence in proportional logic
 α , the query, a sentence in proportional logic.

Symbols \leftarrow a list of the proposition symbols in K, B and α

return TT-Check - All (K, B, α , Symbols, { })

function TT check - All (K, B, α , Symbols, model)

returns true or false

if Empty ? (Symbols) then

if PL-True ? (K, B , model) then return

PL-True ? (α , model).

else return true // when K, B is false,

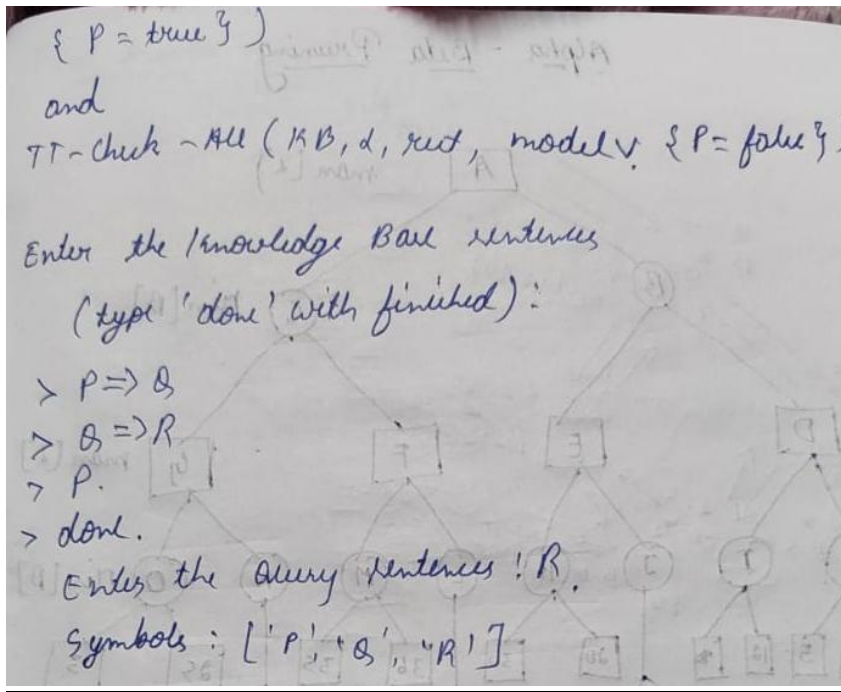
always return true.

else do

$p \leftarrow \text{First}(\text{Symbols})$

$\text{rest} \leftarrow \text{Rest}(\text{Symbols})$

return (TT-check - All (K, B, α , rest, model) \wedge



Code

```

combinations=[(True,True, True),(True,True,False),(True,False,True),(True,False,
False),(False,True, True),(False,True, False),(False, False,True),(False,False, False)]
variable={'p':0,'q':1, 'r':2}
kb=""
q=""
priority={'~':3,'v':1,'^':2}
def input_rules()

    global kb, q
    kb = (input("Enter rule: "))
    q = input("Enter the Query: ")
def entailment():
    global kb, q
    print("*10+"Truth Table Reference"+"*10)
    print('kb','alpha')
    print('*10)
    for comb in combinations:
        s = evaluatePostfix(toPostfix(kb), comb)
        f = evaluatePostfix(toPostfix(q), comb)
        print(s, f)
        print('-'*10)
        if s and not f:
            return False
    return True
def isOperand(c):
    return c.isalpha() and c!='v'

```

```

def isLeftParanthesis(c):
    return c == '('

def isRightParanthesis(c):
    return c == ')'

def isEmpty(stack):
    return len(stack) == 0

def peek(stack):
    return stack[-1]

def hasLessOrEqualPriority(c1, c2):
    try:
        return priority[c1] <= priority[c2]
    except KeyError:
        return False

def toPostfix(infix):
    stack = []
    postfix = ""
    for c in infix:
        if isOperand(c):
            postfix += c
        else:
            if isLeftParanthesis(c):
                stack.append(c)
            elif isRightParanthesis(c):
                operator = stack.pop()
                while not isLeftParanthesis(operator):
                    postfix += operator
                    operator = stack.pop()
            else:
                while (not isEmpty(stack)) and hasLessOrEqualPriority(c, peek(stack)):
                    postfix += stack.pop()
                stack.append(c)
    while (not isEmpty(stack)):
        postfix += stack.pop()

    return postfix

def evaluatePostfix(exp, comb):
    stack = []
    for i in exp:

```

```

    if isOperand(i):
        stack.append(comb[variable[i]])
    elif i == '~':
        val1 = stack.pop()
        stack.append(not val1)
    else:
        val1 = stack.pop()
        val2 = stack.pop()
        stack.append(_eval(i,val2,val1))
    return stack.pop()
def _eval(i, val1, val2):
    if i == '^':
        return val2 and val1
    return val2 or val1
#Test 1
input_rules()
ans = entailment()
if ans:
print("Knowledge Base entails query") else:
    print("Knowledge Base does not entail query")
#Test 2
input_rules()
ans = entailment()

if ans:
    print("Knowledge Base entails query")
else:
    print("Knowledge Base does not entail query")

```

OUTPUT:

```

Enter rule: ( $\sim q \vee \sim p \vee r$ ) $^{\wedge}(\sim q \wedge p) \wedge q$ 
Enter the Query: r
Truth Table Reference
kb alpha
*****
False True
-----
False False
-----
False True
-----
False False
-----
False True
-----
False False
-----
False True
-----
False False
-----
Knowledge Base entails query

```

Program-08 Unification in first order logic

Algorithm :

Unification in FOL

Algorithm: $\text{Unify}(\phi_1, \phi_2)$

Step 1: If ϕ_1 or ϕ_2 is a variable or constant, then

- a) If ϕ_1 or ϕ_2 are identical, then Return NIL.
- b) Else if ϕ_1 is available,
 - a. then if ϕ_1 occurs in ϕ_2 , then Return Failure.
 - b. Else return $\{(\phi_2, \phi_1)\}$
- c) Else if ϕ_2 is a variable,
 - a. if ϕ_2 occurs in ϕ_1 , then return Failure
 - b. Else return $\{(\phi_1, \phi_2)\}$
- d) Else return Failure.

Step 2: If the initial predicate symbol in ϕ_1 & ϕ_2 are not same, then return Failure.

Step 3: If ϕ_1 & ϕ_2 have a different number of arguments, then return failure.

Step 4: Set substitution $\text{set}(\text{SUB})$ to NIL.

Step 5: for $i=1$ to the number of elements in ϕ_1 ,

- a) call unify function with the i th element of ϕ_1 and i th element of ϕ_2 and put the result into S .
- b) if $S = \text{failure}$ then Return Failure

c) if $S \neq \text{NIL}$ then do

a) apply S to the remainder of both v_1
and v_2

b) $\text{subst} = \text{append}(S, \text{subst})$

Step 6: Return subst

Code

```
import re

def getAttributes(expression):
    expression = expression.split("(")[1:]
    expression = "(" + ".join(expression)
    expression = expression.split(")")[:-1]
    expression = ")" + ".join(expression)
    attributes = expression.split(',')
    return attributes

def getInitialPredicate(expression):
    return expression.split("(")[0]

def isConstant(char):
    return char.isupper() and len(char) == 1

def isVariable(char):
    return char.islower() and len(char) == 1

def replaceAttributes(exp, old, new):

    attributes = getAttributes(exp)
    predicate = getInitialPredicate(exp)
    for index, val in enumerate(attributes):
        if val == old:
            attributes[index] = new
    return predicate + "(" + ", ".join(attributes) + ")"

def apply(exp, substitutions):
    for substitution in substitutions:
        new, old = substitution
        exp = replaceAttributes(exp, old, new)
    return exp

def checkOccurs(var, exp):
    if exp.find(var) == -1:
        return False
    return True

def getFirstPart(expression):
```

```

    attributes = getAttributes(expression)
    return attributes[0]
def getRemainingPart(expression):
    predicate = getInitialPredicate(expression)
    attributes = getAttributes(expression)
    newExpression = predicate + "(" + ",".join(attributes[1:]) + ")"
    return newExpression
def unify(exp1, exp2):
    if exp1 == exp2:
        return []
    if isConstant(exp1) and isConstant(exp2):
        if exp1 != exp2:
            print(f' {exp1} and {exp2} are constants. Cannot be unified')
            return []

    if isConstant(exp1):
        return [(exp1, exp2)]

    if isConstant(exp2):
        return [(exp2, exp1)]

    if isVariable(exp1):
        return [(exp2, exp1)] if not checkOccurs(exp1, exp2) else []
    if isVariable(exp2):
        return [(exp1, exp2)] if not checkOccurs(exp2, exp1) else []

    if getInitialPredicate(exp1) != getInitialPredicate(exp2):
        print("Cannot be unified as the predicates do not match!")
        return []

    attributeCount1 = len(getAttributes(exp1))
    attributeCount2 = len(getAttributes(exp2))
    if attributeCount1 != attributeCount2:
        print(f'Length of attributes {attributeCount1} and {attributeCount2} do not match. Cannot
be unified')
        return []

    head1 = getFirstPart(exp1)
    head2 = getFirstPart(exp2)
    initialSubstitution = unify(head1, head2)
    if not initialSubstitution:
        return []

```

```

if attributeCount1 == 1:
    return initialSubstitution

tail1 = getRemainingPart(exp1)
tail2 = getRemainingPart(exp2)

if initialSubstitution != []:
    tail1 = apply(tail1, initialSubstitution)
    tail2 = apply(tail2, initialSubstitution)

remainingSubstitution = unify(tail1, tail2)
if not remainingSubstitution:
    return []

return initialSubstitution + remainingSubstitution

if __name__ == "__main__":
    print("Enter the first expression")
    e1 = input()

    print("Enter the second expression")
    e2 = input()
    substitutions = unify(e1, e2)
    print("The substitutions are:")
    print([' / '.join(substitution) for substitution in substitutions])

```

Output Snapshot

Enter the first expression

king(x)

Enter the second expression

king(john)

The substitutions are:

['john / x']

Program-9 Forward Reasoning

ALGORITHM:

First order logic: Forward Chaining

Example:

As per the law, it is a crime for an American to sell weapons to hostile nations. Country A, an enemy of America, has some missiles and all the missiles were sold to it by Robert, who is an American citizen.

Prove that "Robert is a criminal."

Representation in FOL

- It is a crime for an American to sell weapons to hostile Nations.

Let's say P, q and r are variables

American (P) \wedge weapon (q) \wedge sells (P, q, r) \wedge

Hostile (r) \Rightarrow criminal (P)

- Country A has some missiles

$\exists x$ owns (A, x) \wedge missile (x)

- Existential instantiation, introducing a new constant T , "owns (A, T) missile (T)".

- All missiles were sold to Country A by Robert

$\forall x$ missile (x) \wedge owns (A, x) \Rightarrow sells (Robert, x)

- Missiles are weapons

missile (x) \Rightarrow weapon (x)

• Enemy of America is known as hostile
 $\text{the Enemy}(x, \text{America}) \Rightarrow \text{Hostile}(x)$

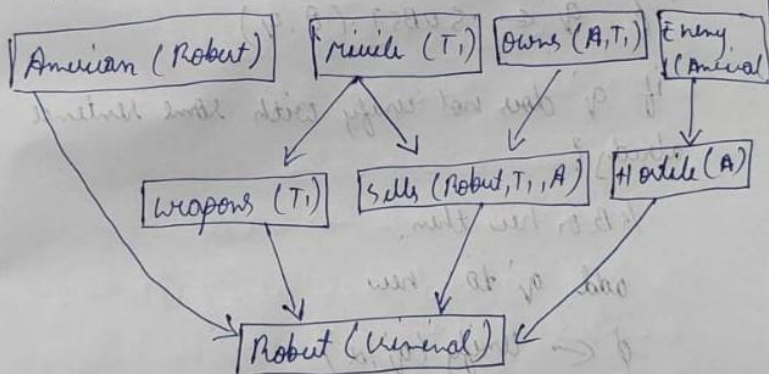
• Robot is an American
 $\text{American}(\text{Robot})$

• the country A, an Enemy of America.
 $\text{Enemy}(A, \text{America})$

To Prove:

Robot is a criminal
 $\text{Criminal}(\text{Robot})$

Forward chaining:



Forward Reasoning Algorithm:

function FOL-FC-ASK(KB, d)

returns a substitution or false

inputs: KB , the knowledge base.

α , the query

$\text{American}(p) \wedge \text{Weapon}(a)$
 \wedge
 $\text{Sells}(p, a, s) \wedge \text{Hostile}(a)$
 $\Rightarrow \text{Criminal}(p)$

local variables : new, the new sentences inferred
- id on each iteration

repeat until new is empty

$new \leftarrow \{\}$

for each rule in KB do

$(P_1, \lambda, \dots, \lambda P_n \Rightarrow Q) \leftarrow \text{standardize-variable}(\text{rule})$

for each θ such that $\text{Subst}(\theta, P_1, \lambda, \dots, \lambda P_n) = \text{Subst}(\theta, P^*, \lambda, \dots, \lambda P'_n)$

for some P^*, \dots, P'_n in KB

$Q' \leftarrow \text{SUBST}(\theta, Q)$

if Q' does not unify with some sentence

already?

KB or new then

add Q' to new

$\phi \leftarrow \text{Unify}(Q', \alpha)$

if ϕ is not fail then return ϕ

add new to KB

return false

Code

import re

def isVariable(x):

return len(x) == 1 and x.islower() and x.isalpha()

def getAttributes(string):

expr = '([^\s]+)'

matches = re.findall(expr, string)

return matches


```

def getPredicates(string):
    expr = '([a-z~+])\([^&]+\)'
    return re.findall(expr, string)

class Fact:

    def __init__(self, expression):
        self.expression = expression
        predicate, params = self.splitExpression(expression)
        self.predicate = predicate
        self.params = params
        self.result = any(self.getConstants())

    def splitExpression(self, expression):
        predicate = getPredicates(expression)[0]
        params = getAttributes(expression)[0].strip('(').split(',')
        return [predicate, params]

    def getResult(self):
        return self.result

    def getConstants(self):
        return [None if isVariable(c) else c for c in self.params]

    def getVariables(self):
        return [v if isVariable(v) else None for v in self.params]

    def substitute(self, constants):
        c = constants.copy()
        f = f"{self.predicate}({','.join([constants.pop(0) if isVariable(p) else p for p in self.params])})"
        return Fact(f)

class Implication:

    def __init__(self, expression):
        self.expression = expression
        l = expression.split('=>')
        self.lhs = [Fact(f) for f in l[0].split('&')]
        self.rhs = Fact(l[1])

    def evaluate(self, facts):
        constants = {}
        new_lhs = []
        for fact in facts:

```

```

    for val in self.lhs:
        if val.predicate == fact.predicate:
            for i, v in enumerate(val.getVariables()):
                if v:
                    constants[v] = fact.getConstants()[i]
            new_lhs.append(fact)
        predicate, attributes = getPredicates(self.rhs.expression)[0],
str(getAttributes(self.rhs.expression)[0])
    for key in constants:
        if constants[key]:
            attributes = attributes.replace(key, constants[key])

    expr = f'{predicate} {attributes}'
    return Fact(expr) if len(new_lhs) and all([f.getResult() for f in new_lhs]) else None

```

class KB:

```

    def __init__(self):
        self.facts = set()
        self.implications = set()

    def tell(self, e):
        if '=>' in e:
            self.implications.add(Implication(e))
        else:
            self.facts.add(Fact(e))
        for i in self.implications:
            res = i.evaluate(self.facts)
            if res:
                self.facts.add(res)

    def ask(self, e):
        facts = set([f.expression for f in self.facts])
        i = 1
        print(f'Querying {e}:')
        for f in facts:
            if Fact(f).predicate == Fact(e).predicate:
                print(f'\t{i}. {f}')
            i += 1

    def display(self):
        print("All facts: ")
        for i, f in enumerate(set([f.expression for f in self.facts])):

```

```
        print(f'\t{i+1}. {f}')

def main():
    kb = KB()
    print("Enter the number of FOL expressions present in KB:")
    n = int(input())
    print("Enter the expressions:")
    for i in range(n):
        fact = input()
    kb.tell(fact)
    print("Enter the query:")
    query = input()
    kb.ask(query)
    kb.display()

main()
```

Output Snapshot

Querying criminal(x):

1. criminal(West)

All facts:

1. american(West)
2. sells(West,M1,Nono)
3. owns(Nono,M1)
4. missile(M1)
5. enemy(Nono,America)
6. weapon(M1)
7. hostile(Nono)
8. criminal(West)

Querying evil(x):

1. evil(John)

Program-10 KnowledgeBase - Resolution

Algorithm :

Resolution in FOL
Steps for proving in Resolution.

Premise, ... Premises

(all expressed in FOL)

1. Convert all series to CNF

2. Negative conclusion S and convert result to

3. Add ^{CNF} Negative conclusion S to the premise clause

4. Repeat until contradiction or no progress is made:

a. Select 2 clauses (call them parent clauses)

b. Resolve them together, performing all required unifications

c. If Result is the empty clause, a contradiction has been found (i.e.) S follows from the premises.

d. If not, add Result to the premises

Example:

a. John likes all kinds of food

b. Apple and vegetables are food

c. Anything anyone eats and not killed is food

d. Anil eats peanuts and still alive.

e. Harry eats peanuts and still that Anil eats

f. Anyone who is alive implies not killed.

g. Anyone who is not killed \wedge implies alive.

Prove by resolution that:

h. John likes peanuts

Step 1: Representation in FOL:

a. $\forall x: \text{food}(x) \rightarrow \text{likes}(\text{John}, x)$

b. $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetables})$

c. $\forall x \forall y: \text{eats}(x, y) \rightarrow \neg \text{killed}(x) \rightarrow \text{food}(y)$

d. $\text{eats}(\text{Anil}, \text{peanuts}) \wedge \text{alive}(\text{Anil})$

e. $\forall x: \text{eats}(\text{Anil}, x) \rightarrow \text{eats}(\text{Harry}, x)$

f. $\forall x: \neg \text{killed}(x) \rightarrow \text{alive}(x)$

g. $\forall x: \text{alive}(x) \rightarrow \neg \text{killed}(x)$

h. $\text{likes}(\text{John}, \text{peanuts})$

Step 2: Eliminate implication

$A \Rightarrow B$ with \rightarrow as $\neg A \vee B$

a. $\forall x \rightarrow \text{food}(x) \vee \text{likes}(\text{John}, x)$

b. $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetables})$

c. $\forall x \forall y \rightarrow [\text{eats}(x, y) \wedge \neg \text{killed}(x)] \vee \text{food}(y)$

d. $\text{eats}(\text{Anil}, \text{peanuts}) \wedge \text{alive}(\text{Anil})$

e. $\forall x \neg \text{eats}(\text{Anil}, x) \vee \text{eats}(\text{Harry}, x)$

f. $\forall x \neg \text{alive}(x) \vee \neg \text{killed}(x)$

g. $\forall x \neg \text{alive}(x) \vee \neg \text{killed}(x)$

h. likes (John, peanuts)

step 3: move negation inwards and write

a. $\forall x \rightarrow \text{food}(x) \vee \text{likes}(\text{John}, x)$

b. $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetables})$

c. $\forall x \forall y \rightarrow \text{eats}(x, y) \vee \neg \text{killed}(x) \vee \text{food}$

- (y)

d. $\text{eats}(\text{Ariel}, \text{peanuts}) \wedge \text{alive}(\text{Ariel})$

e. $\forall x \rightarrow \text{eats}(\text{Ariel}, x) \vee \text{eats}(\text{Harry}, x)$

f. $\forall x \text{ killed}(x) \vee \text{alive}(x)$

g. $\forall x \rightarrow \text{alive}(x) \vee \neg \text{killed}(x)$

h. likes (John, peanuts)

step 4: Rename variables or standardize variables

a. $\forall x \rightarrow \text{food}(x) \vee \text{likes}(\text{John}, x)$

b. $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetables})$

c. $\forall y \forall z \rightarrow \text{eats}(y, z) \vee \neg \text{killed}(y) \vee \text{food}(z)$

d. $\text{eats}(\text{Ariel}, \text{Peanuts}) \wedge \text{alive}(\text{Ariel})$

e. $\forall w \rightarrow \text{eats}(\text{Ariel}, w) \vee \text{eats}(\text{Harry}, w)$

f. $\forall g \rightarrow \text{killed}(g) \rightarrow \vee \text{alive}(g)$

g. $\forall k \rightarrow \text{alive}(k) \vee \neg \text{killed}$

h. likes (John, peanuts)

Step 5: Drop universal.

a. $\rightarrow \text{food}(x) \vee \text{likes}(\text{John}, x)$

b. $\text{food}(\text{Apple})$

c. $\text{food}(\text{vegetable})$

d. $\rightarrow \text{eats}(y, z) \vee \text{killed}(y) \vee \text{food}(z)$

e. $\text{eats}(\text{Anil}, \text{Peanuts})$

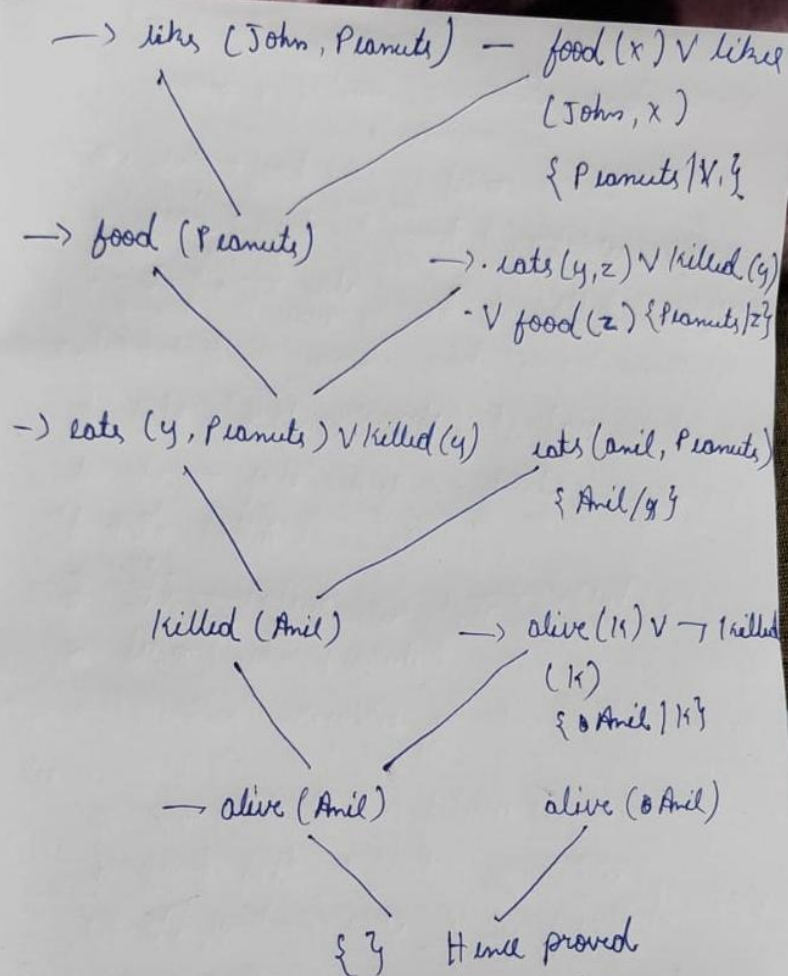
f. $\neg \text{alive}(\text{Anil})$

g. $\rightarrow \text{eats}(\text{Anil}, w) \vee \text{eats}(\text{Harry}, w)$

h. $\text{killed}(g) \vee \text{alive}(g)$

i. $\rightarrow \text{alive}(x) \vee \neg \text{killed}(x)$

j. $\text{likes}(\text{John}, \text{Peanuts})$



Code

```
def disjunctify(clauses):
    disjuncts = []
    for clause in clauses:
        disjuncts.append(tuple(clause.split('v')))
    return disjuncts

def getResolvent(ci, cj, di, dj):
    resolvent = list(ci) + list(cj)
    resolvent.remove(di)
    resolvent.remove(dj)
    return tuple(resolvent)

def resolve(ci, cj):
    for di in ci:
        for dj in cj:
            if di == '~' + dj or dj == '~' + di:
                return getResolvent(ci, cj, di, dj)

def checkResolution(clauses, query):
    clauses += [query if query.startswith('~') else '~' + query]
    proposition = '^'.join(['(' + clause + ')'] for clause in clauses)
    print(f'Trying to prove {proposition} by contradiction. ')

    clauses = disjunctify(clauses)
    resolved = False
    new = set()

    while not resolved:
        n = len(clauses)

        pairs = [(clauses[i], clauses[j]) for i in range(n) for j in range(i + 1, n)]
        for (ci, cj) in pairs:
            resolvent = resolve(ci, cj)
            if not resolvent:
                resolved = True
                break
            new = new.union(set(resolvent))
        if new.issubset(set(clauses)):
            break
        for clause in new:
```

if clause not in clauses:

```
clauses.append(clause)
```

if resolved:

```
print('Knowledge Base entails the query, proved by resolution')
```

else:

```
print("Knowledge Base doesn't entail the query, no empty set produced after resolution") clauses
```

```
= input('Enter the clauses ').split()
```

```
query = input('Enter the query: ')
```

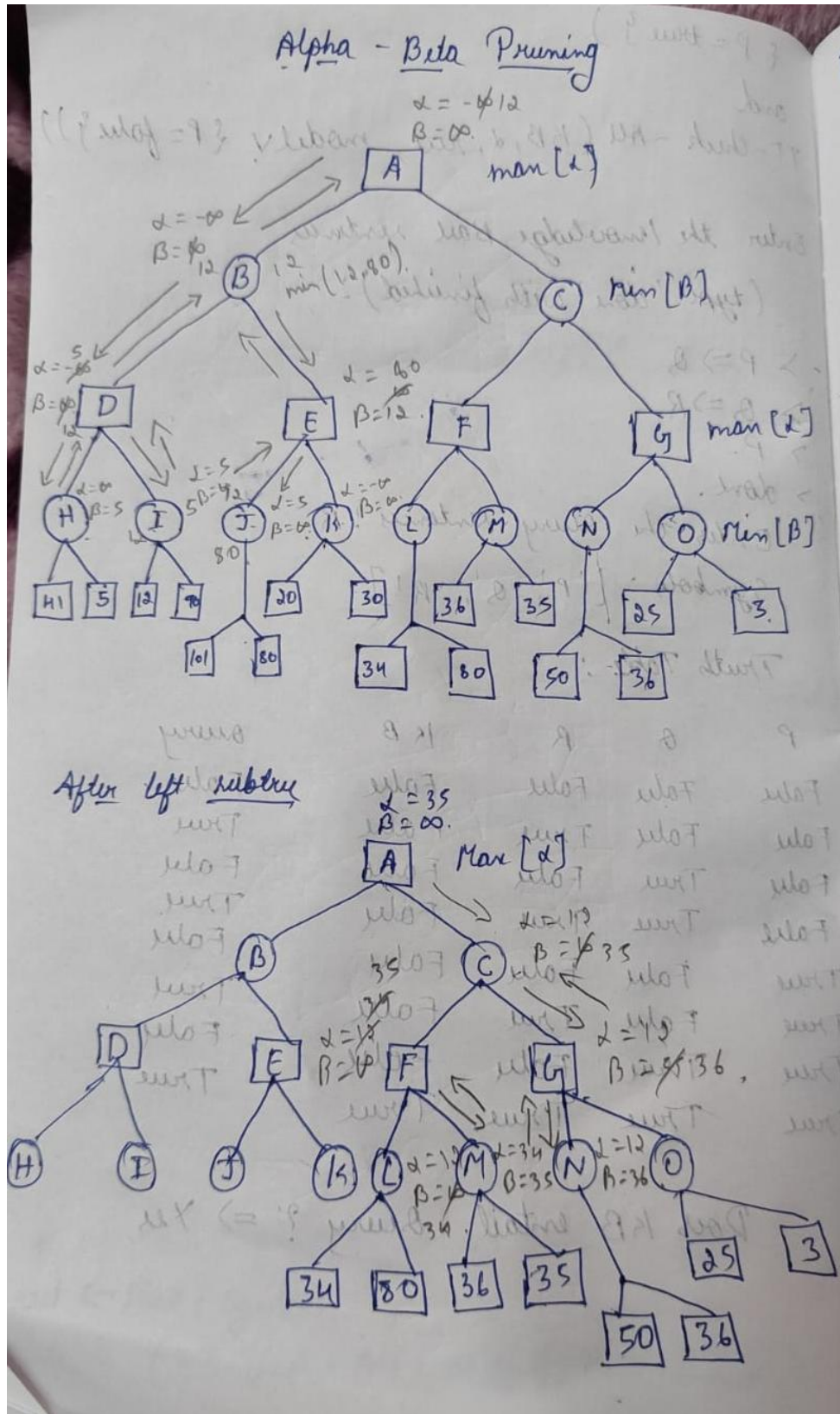
```
checkResolution(clauses, query)
```

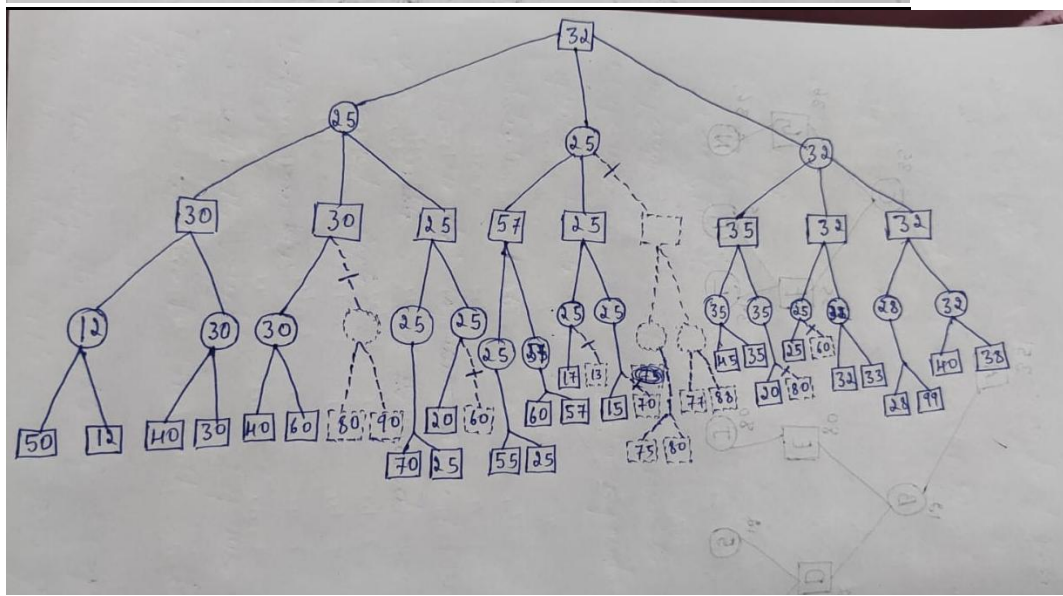
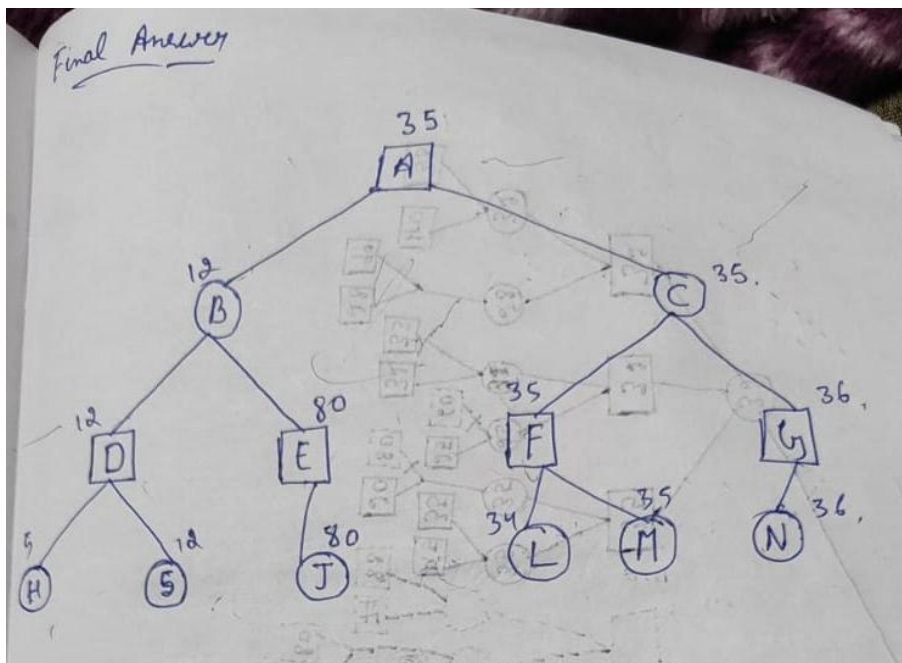
Output Snapshot

```
Enter the clauses (~qv~pvr)^(~q^p)^q
Enter the query: r
Trying to prove ((~qv~pvr)^(~q^p)^q)^(~r) by contradiction....
Knowledge Base entails the query, proved by resolution
```

Program-11

Alpha Beta Pruning Algorithm :





Code

```

import math
# Alpha-Beta Pruning Functions
def alpha_beta_search(state):
    """ Alpha-Beta Search to get the optimal action """
    value = max_value(state, -math.inf, math.inf)
    print("Optimal Value:", value)
    return value

def max_value(state, alpha, beta):
    """ Function to calculate the MAX value node """
    if terminal_test(state): # If leaf node, return utility value
        return utility(state)
    v = -math.inf
    for child in state["children"]: # Iterate through child nodes

```

```

        v = max(v, min_value(child, alpha, beta))
    if v >= beta:
        return v # Beta cutoff
    alpha = max(alpha, v)
return v

def min_value(state, alpha, beta):
    """ Function to calculate the MIN value node """
    if terminal_test(state): # If leaf node, return utility value
        return utility(state)
    v = math.inf
    for child in state["children"]: # Iterate through child nodes
        v = min(v, max_value(child, alpha, beta))
    if v <= alpha:
        return v # Alpha cutoff
    beta = min(beta, v)
return v

# Utility Functions
def terminal_test(state):
    """ Check if the node is a leaf node """
    return "value" in state # Leaf node if it contains 'value'

def utility(state):
    """ Return the utility value of a leaf node """
    return state["value"]

# Build the Binary Tree Based on Leaf Nodes
def build_tree(values):
    """ Recursively build a binary tree from a list of leaf node values """
    if len(values) == 1: # Single value -> Leaf node
        return {"value": values[0]}
    mid = len(values) // 2
    left_subtree = build_tree(values[:mid])
    right_subtree = build_tree(values[mid:])
    return {"children": [left_subtree, right_subtree]}

# Main Program
if __name__ == "__main__":
    leaf_nodes = [10, 9, 14, 18, 5, 4, 50, 3]
    tree = build_tree(leaf_nodes) # Build the binary tree
    print("Alpha-Beta Pruning Search:")
    alpha_beta_search(tree)

```

Output

```

Alpha-Beta Pruning Search:
Optimal Value: 10

```

