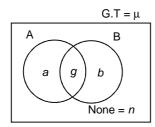
### CHAPTER – 7

# VENN DIAGRAMS

# Venn Diagrams involving two variables:



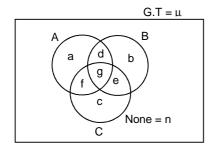
In the above diagram, A and B represent two different sets and the various regions can be referred to as given below.

A = a + g; B = b + gOnly A = a; Only B = bExactly one set = a + bA and B = g; Only A and B = gExactly two sets = g

At least one set = Exactly one + Exactly two = a + b + g = T

Grand Total  $(G.T = \mu) = a + b + g + n = T + n$  A + B = a + b + 2g = T + gA or B = a + b + g = TDoes not belongs to A = b + nDoes not belongs to B = a + n

#### Venn Diagram with three variables:



Here A, B and C are three different sets and the various regions can be referred to as given below.

 $A = a + d + g + f ; Only A = a \\ B = b + d + g + e ; Only B = b \\ C = c + f + g + e ; Only C = c \\ Exactly one set = a + b + c ; \\ A and B = d + g ; B and also$ 

A and B = d + g; B and also C = e + g; C as well as A = f + g;

Only A and B = d; A and B but not C = d; Only B and C = e; B and C but not A = e; Only C and A = f; C and A but not B = f; Exactly two sets = d + e + f;

A, B and C = All the three = Only A, B and C = g; Exactly three sets = g; None among A, B and C = n;

At least one set = Exactly one + Exactly two + Exactly three = a + b + c + d + e + f + g =  $\mu$  - n At least two sets = Exactly two + Exactly three = d + e + f + g

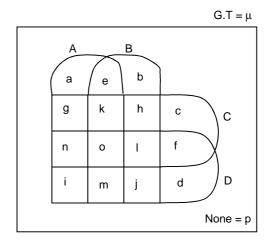
At least three sets = Exactly three = g At most one sets = Exactly one + None = a + b + c + nAt most two sets = Exactly two + Exactly one + None = d + e + f + a + b + c + n = u - q

At most three sets = Exactly three + Exactly two + Exactly one + None =  $q + d + e + f + a + b + c + n = \mu$ 

 $\begin{array}{l} A+B+C=a+b+c+2(d+e+f)+3g\\ = Exactly \ one+2(Exactly \ two)+3(Exactly \ three)\\ = (Exactly \ one+Exactly \ two+Exactly \ three)\\ + Exactly \ two+2 (Exactly \ three)\\ = At \ least \ one+Exactly \ two+2(Exactly \ three)\\ + Exactly \ three\\ + Exactly \ three\\ = At \ least \ one+At \ least \ two+At \ least \ three \end{array}$ 

Does not belong to A = b + e + c + nA or B or C = a + b + c + d + e + f + g = At least one. A or B = a + b + d + e + f + gA or B but not C = a + d + bNeither A nor B = c + n(A and B) or C = d + c + f + g + eA and (B or C) = d + g + f

### Venn diagram involving four variables:



Here, A, B, C and D are four different sets and the various regions can be referred to as given below.

 $\begin{array}{lll} A = a + e + g + k + n + o + i + m; & Only \ A = a \\ B = b + e + h + k + l + o + j + m; & Only \ B = b \\ C = c + f + h + l + k + o + g + n; & Only \ C = c \\ D = d + f + j + l + m + o + i + n; & Only \ D = d \end{array}$ 

Exactly one set = a + b + c + d

 $\begin{array}{lll} A \text{ and } B=e+k+o+m & ; & \text{Only A and B}=e \ ; \\ A \text{ and C}=g+k+o+n & ; & \text{Only A and C}=g \ ; \end{array}$ 

 $\begin{array}{lll} A \text{ and } D=n+o+i+m & ; & \text{Only A and D}=i \ ; \\ B \text{ and C}=k+h+o+l & ; & \text{Only B and C}=h \ ; \\ B \text{ and D}=m+j+o+l & ; & \text{Only B and D}=j \ ; \\ C \text{ and D}=n+o+l+f & ; & \text{Only C and D}=f \ ; \\ Exactly \text{ two sets}=e+f+g+h+i+j \end{array}$ 

Exactly three sets = k + l + m + nA, B, C and D = All the four = Exactly four set = o; None among A, B, C and D = p

#### **Important Note:**

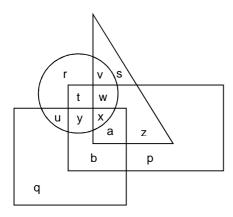
Note the following for a n-set Venn Diagram:

Name of the region	Number of regions	
(pocket of intersection	(pockets of intersections	For a 5-set
of the sets)	of the sets)	situation
Exactly 1, X	<sup>n</sup> C <sub>1</sub>	5
Exactly 2, Y	${}^{n}C_2$	10
Exactly 3, Z	${}^{n}C_3$	10
Exactly 4, A	<sup>n</sup> C <sub>4</sub>	5
Exactly 5, B	$^{ m n}$ C $_{ m 5}$	1
None, N	${}^{\mathrm{n}}C_{\mathrm{0}}$	1
Total Number		
of regions	2 <sup>n</sup>	32

### Exercise - 7(a)

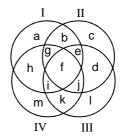
**Directions for questions 1 to 5:** These questions are based on the following diagram.

In the following diagram, the Circle represents all the people who like MAAZA, the Square represents all the people who like Thumbs up, the Triangle represents all the people who like Marinda and the Rectangle represents all the people who like Coca-Cola.



- 1. Which of the following represents the people who like coca-cola and Thumbs up?
  - (A) r
- (B) u
- (C) b
- (D) q
- 2. Which of the following represents the people who like Marinda but not Thumbs up?
  - (A) v, s, w, x
- (B) v, s, z, a
- (C) v, w, x, a
- (D) None of these
- 3. Which of the following represents the people who like Maaza and Thumbs up?
  - (A) u, t, w
- (B) v, w, x
- (C) b, a, x
- (D) u, y, x
- 4. Which of the following represents the people who like both Maaza and Marinda but not any of other two?
  - (A) y
- (B) v
- (C) u
- (D) None of these
- 5. Which of the following represents the people who like Marinda, Maaza, Coca-cola but not Thumbs up?
  - (A) b
- (B) r
- (C) s
- (D) w

**Directions for questions 6 to 10:** These questions are based on the following diagram.



In the above diagram,

Circle I represents the athletes who participated in Swimming.

Circle II represents the athletes who participated in Running.

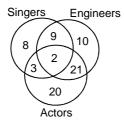
Circle III represents the athletes who participated in Javelin throw.

Circle IV represents the athletes who participated in Long jump.

- **6.** Which of the following represents the athletes who participated neither in Running nor in Long jump?
  - (A) j, k
- (B) c, d
- (C) a, I
- (D) k,
- 7. Which of the following represents the athletes who participated in Running and Swimming?
  - (A) a, h, b, g, e, f
- (B) a, b, c
- (C) g, e, f
- (D) b, g, e, f
- 8. Which of the following represents the athletes who participated in all the four events?
  - (A) g
- (B) i
- (C) i
- (D) f
- **9.** Which of the following represents the athletes who participated in exactly three of the four events?
  - (A) h, b, k, d
- (B) g, e, i, j
- (C) a, c, d, k
- (D) f, j, k, i
- 10. Which of the following represents the athletes who participated in Swimming and Javelin throw but not in Running?
  - (A) j
- (B) g
- (C) k
- (D) i

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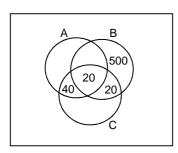
Directions for questions 11 to 15: These questions are based on the following Venn diagram.



- 11. How many Engineers are also Singers?
  - (A) 15

- 12. How many Actors are not Engineers?
  - (A) 24
- (B) 23
- (C) 15
- (D) 18
- 13. How many Singers are Actors but not Engineers?
  - (A) 8
- (B) 3
- (C) 9
- (D) 21
- 14. How many Engineers are either Singers or Actors but not both?
  - (A) 25
- (B) 28
- (C) 35
- (D) 30
- 15. How many Singers are Actors as well as Engineers?
  - (A) 21
- (B) 9
- (C) 3
- (D) 2

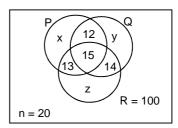
Directions for questions 16 to 20: The following Venn diagram represents the 1200 employees of a company. Each of the employees is a member of at least one of three clubs - A, B and C. Using the given data, answer the questions that follow.



Total member of club A = 420Total member of club B = 590Total member of club C = 340

- 16. How many employees are member of club C only? (A) 250 (B) 240 (C) 180 (D) 260
- 17. How many employees are member of both club A and club B?
  - (A) 50
- (B) 80
- (C) 70
- 18. How many employees are not member of club B? (A) 340 (B) 610 (C) 630 (D) 290
- 19. How many employees are member of club A or club C? (A) 850 (B) 700 (C) 975 (D) 675
- 20. How many employees are member of exactly two clubs?
  - (A) 110
- (B) 130
- (C) 98
- (D) 78

Directions for questions 21 to 25: These questions are based on the following Venn diagram.



P represents the number of students who have voter ID card. Q represents the number of students who have Passport. R represents the number of students who have PAN card. n represents the number of students who do not have any of the three ID proofs i.e. Voter ID card, Passport and PAN card.

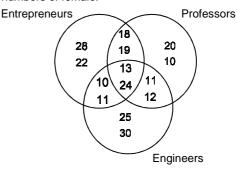
- 21. If the number of students who have Voter ID card is same as that of those who have Passport which in turn is PAN card, then how many students have at least one of the three ID proofs?
  - (A) 260
- (B) 279
- (C) 250
- 22. If the number of students who have voter ID card is half of the number of students who have PAN card then, how many students have only voter ID card?
  - (C) 15
- (B) 20
- (D) Cannot be determined
- 23. How many students have neither voter ID card nor Passport?
  - (A) 64
- (B) 50
- (C) 78
- (D) 72
- **24.** If  $\frac{x}{y} = \frac{2}{1}$  and  $\frac{y}{z} = \frac{1}{2}$  then how many students have

only voter ID card?

- (A) 60
- (B) 58
- (C) 29
- (D) 18
- **25.** If x = y = z then how many students do not have PAN card?
  - (A) 120
- (B) 138
- (C) 160
- (D) None of these

Directions for questions 26 to 30: These questions are based on the following Venn diagram.

In this diagram there are two numbers in each segment, one atop the other. The number at the top represents the number of male and the number at the bottom represents the numbers of female.



- 26. How many female Entrepreneurs are Professors also?
  - (A) 20
- (B) 23
- (C) 47

27.	How many Professors are neither Entrepreneurs nor Engineers?	29.	How mai (A) 51	ny female (B)	es are not l 48 (C	Engineer C) 58	s? (D) 60	
	(A) 20 (B) 28 (C) 30 (D) 38	30.	How mar	ny Profes	sors are al	so Entre	preneurs a	s well
28.	How many male Professors are not Entrepreneurs? (A) 29 (B) 31 (C) 49 (D) 58		as Engin (A) 37	eers? (B)	40 (0	C) 48	(D) 51	
	Exercis	e-7	(b)					
	rections for questions 1 to 5: These questions are sed on the following information.	The f	ollowing t	able sho	ws the rem	aining da	ata.	
	a class of 150 students, 45 take History, 65 take ography and 10 take both History and Geography.		Male	Doyle	Christie	Both	Total	
1.	How many students take only Geography? (A) 45 (B) 10 (C) 55 (D) 65		Female Total	40	70		100	
2.	How many take only History?		ner it is kn					_
3.	(A) 65 (B) 35 (C) 10 (D) 45  How many do not take either History or Geography?	(B) -	The ratio o	of males	s read both to females read books	is 1 : 1.		
-	(A) 10 (B) 35 (C) 100 (D) 140	(-)-			ead books			
4.	How many students take at least one subject? (A) 10 (B) 90 (C) 50 (D) 100		(A) 10 How manv	(B) 1	2 (C) s read book	37 s by only	(D) 45 v Christie?	
5.	How many students do not take any of the two subjects?	(	(A) 70	(B) 1	0 (C)	33	(D) 23	
	(A) 90 (B) 10 (C) 50 (D) 100		A) 25	(B) 4	read book 0 (C)	35	(D) 15	
	rections for questions 6 to 10: These questions are sed on the following information.	a	uthors?		ts do not		-	h the
In a survey conducted among 200 mobile phone using families, it was found that 140 use Panasonic, 120 use Nokia and 143 use Siemens. 95 use both Panasonic and Nokia, 85 use both Nokia and Siemens and 93 use both			(A) 12 How many	B) 2 males r	/ (C) ead books	37 by Doyle	(D) 63 e?	
			(A) 27 (B) 67 (C) 12 (D) 15  Directions for questions 16 to 20: These questions are					
	nasonic and Siemens. 70 families use mobile phones of the three companies.				information		e questior	is are
6.	How many families use mobilephones of only Siemens?	Vanil	la, Strawk	erry and	e creams of I Chocolate	are ser	ved. Amor	ng the
	(A) 50 (B) 35 (C) 70 (D) 143	gues	ts have e	aten Stra	ave eaten awberry ice ice cream	cream	and 170 g	uests
7.	How many families use mobilephones of both Panasonic and Nokia but not Siemens?  (A) 25 (B) 57 (C) 165 (D) 95	Vanil	la and St	rawberry	ice cream erry ice c	s. 60 gu	ests have	eaten
8.	How many families use mobilephones of exactly one	eater	n all the th	ree flavo	colate ice ured ice cre			
٠.	Company? (A) 63 (B) 67 (C) 70 (D) 200		aten any i How many		n. have attend	ded the r	artv?	
9.	How many families use neither Panasonic nor	(	(A) 250	(B) 2	80 (C)	400	(D) 380	
	Siemens? (A) 40 (B) 120 (C) 110 (D) 10	t	wo flavou	rs?	nave eaten			t least
10.	How many families use none of the mobilephones? (A) 10 (B) 70		(A) 190 How many	B) 1 guests l	00 (C) nave eaten	150 the ice c	(D) 180 reams of V	′anilla
	(C) 0 (D) Cannot be determined		and Straw (A) 20	berry flav (B) 3	vours only? 0 (C)	40	(D) 10	
dat	rections for questions 11 to 15: Study the following a and the table to answer the questions that follow.	(			have eate m but not \$ 0 (C)			
wh	survey was conducted among 100 students in a class or read detective novels written by Conan Doyle or	20.	Tow man	` ,	s have no		( )	a ice
	atha Christie or both. Due to some recording error in the nputer most of the figures were missing.		cream? (A) 170	(B) 1	50 (C)	250	(D) 280	
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Directions for questions 21 to 25: These questions are based on the following information.

In a locality, three magazines are read, namely India Today, Sports Star and Business India. 45 people read only one magazine, 20 read exactly two magazines and 5 read all the three. There is no one who does not read any of the three magazines.

- 21. How many people are there in the locality? (A) 65 (B) 70 (C) 50 (D) 90
- 22. How many people read at least two magazines? (C) 50 (B) 20 (A) 25
- 23. If the ratio of people who read India Today is to those who read Sports Star is to those who read Business India is 2:3:4 and 18 people read India Today, then how many read Sports Star?
  - (A) 28
- (B) 31
- (C) 27
- (D) 54
- 24. If 10 people stop reading India Today and start reading Business India, then what is the maximum number of people who read exactly two magazines?
  - (A) 20 (C) 25
- (B) 30 (D) 55
- 25. What percentage of the people who read at least one
  - (A) 25%
  - magazine read exactly two magazines? (B) 20%
  - (C)  $28^4/_7\%$
- (D) None of these

Directions for questions 26 to 30: These questions are based on the following information.

In a music centre 'Sangeet Mahal' there were cassettes belonging to the various types of music. It was found that 125 cassettes were of Pop Music, 135 cassettes were of classical Music and 95 cassettes were of Light Music. 60 cassettes had a mixture of at least two of the music types and 10 cassettes had a mixture of all the three. Every cassette in the music centre contained at least one of the above mentioned types of music.

- 26. How many cassettes were of exactly one type of music? (A) 60 (B) 70 (C) 225 (D) 200
- 27. How many cassettes were of exactly two types of music? (D) 90 (A) 60 (B) 50 (C) 100
- 28. How many cassettes had music of at least one type? (A) 285 (B) 225 (C) 90 (D) 205
- 29. If the number of cassettes of only Pop Music is equal to that of only Light Music, which is twice of the number of cassettes of only Classical Music type, then how many cassettes of only Classical Music were there? (A) 225 (B) 75 (C) 90 (D) 45
- 30. If the number of cassettes of only Pop Music is equal to 75 and the number of cassettes of both Pop and Classical but not Light is equal to the number of cassettes of both Pop and Light but not Classical, then how many cassettes are there in the Music Centre which are both Classical and Light but not Pop?
  - (A) 0 (B) 20 (C) 50 .

### Exercise - 7(c)

Directions for questions 1 to 3: These questions are based on the following information.

In a class of 100 students, 50 students passed in Mathematics and 70 passed in English. 5 students failed in both Mathematics and English.

- How many students passed in both the subjects? (A) 25 (B) 50 (C) 70 (D) 5
- How many students passed in exactly one of the two subjects?
  - (A) 5
- (B) 15
- (C) 95
- (D) 70
- 3. How many students failed in at least one subject? (A) 95 (B) 50 (C) 75 (D) 70

Directions for questions 4 to 6: These questions are based on the following information.

In a class, 30% of the students gave their names to participate in the NSS and 75% to participate in the NCC. Three students participate in neither of these two and six students wanted to participate in both.

- How many students are there in the class? (A) 100 (B) 75 (C) 60
- 5. What percentage of students wants to participate in only one programme - either NSS or NCC? (A) 85% (B) 90% (D) 20% (C) 75%
- How many students want to participate in at least one programme?
  - (A) 97
- (B) 87
- (C) 147

Directions for questions 7 to 9: These questions are based on the following information.

In a locality 60% people read the newspaper Times of India and 35% people read only the newspaper The Hindu. 10% people read both the newspapers and 240 people do not read any of the two newspapers.

- How many people are there in that locality? (A) 4800 (B) 2400 (C) 2000 (D) 4000
- How many people read only Times of India? (A) 2880 (B) 2000 (C) 2400 (D) 2800
- How many people read at most one of the two newspapers? (A) 4200 (B) 4400 (C) 4560 (D) 4320

Directions for questions 10 to 12: These questions are based on the following information.

In an institute, 150 students are members of "Club A", 140 students are the members of "Club B" and 165 students are the members of the "Club C". 25 students are the members of both the Clubs A and B. 35 students are the members of both the Clubs B and C and 30 students are the members of clubs A and C. 15 students are the members of all the three Clubs. Each student is a member of at least one of the Clubs.

- 10. How many students are not the members of Club C? (C) 210 (D) 310 (A) 215 (B) 200
- 11. How many students are the members of both the Clubs A and B but not C? (A) 10 (B) 20 (C) 15 (D) 30

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12.	How ma Club C? (A) 310			of Club A or (D) 285	17.	How many (A) 64	people d (B) 10		read BT? (C) 92	(D) 108
	ections f	or questions 13	18.	do not read		vho re	ead BW, ho	w many people		
based on the following information.						(A) 102	(B) 46		(C) 84	(D) 59
A survey was conducted among 600 bicycle owners. It was found that 200 people had Hero Ranger, 250 people had BSA SLR and 300 people had Atlas MTB					19.	How many (A) 64	people re (B) 10		least two m (C) 100	nagazines? (D) 129
bicy the	cles with 3 brands	them. Seventy of bicycles. Ea mentioned above		How many (A) 100	(B) 12	0	(C) 105	(D) 109		
13.	How ma (A) 70	ny people had al (B) 40		nds? (D) 110	<b>Directions for questions 21 to 23:</b> These questions are based on the following information.					
14.		ners had only BS en how many pe m?			Out of a group of 315 students who went to Mumbai, 125 visited Essel World, 140 visited Lumbini Garden and 160 visited Film Nagar. Twenty Five of them visited all the three places while 200 visited exactly one of the three					
	(A) 54	(B) 72	(C) 98	(D) 106						ed exactly 2 out
15.		ople had only BS y Atlas MTB and (B) 20	Hero Ranger w		of th		ces, is fi	ve tim	es as many	y as those who
16.	` '	ny owners have	` '	( )	21.	How many (A) 200	students (B) 18		not more the (C) 250	nan one place? (D) 215
	(A) 70	(B) 200	(C) 490	(D) 250	22.					at least one of
		for questions 17 e following inform		questions are				studer		d Film Nagar is aly Essel World? (D) 75
A group of people who read the three magazines – Business world (BW), Business Today (BT) and Business Standards (BS) is surveyed. 49% of the people read BW, 49% of the students read BT and 52% of the people read BS. 10% of the people read all the three. 26% read both BW and BS, 14% read only BS and BT. 15% read only BT. 20 people read only BW and BT.  **Directions for questions 24 to 27: These questions are based on the following information.**  Directions for questions 24 to 27: These questions are based on the following information.  The following table represents the survey result which is conducted in five companies to find out the number of Engin and the number of employees who are from Delhi.							only one of the d Film Nagar			
BW BT. <b>Dir</b> e	20 people ctions for following	e read only BW  or questions 24 g table represent	and BT. Ito 27: These of the survey res	questions are base		the followin	g informa	ation.	` ,	, ,
BW BT. <b>Dir</b> e	20 people ctions for following	e read only BW  or questions 24 g table represent	and BT.  I to 27: These of the survey reserved who are from	questions are base	ucted	the followin	g information in graph of the second of the	ation. find o	` ,	er of Engineers
BW BT. <b>Dir</b> e	20 people ctions for following	or questions 24 g table representations of employees Company	and BT. Ito 27: These of the survey res	questions are base sult which is condu Delhi. Employees	ucted	the followin	g information in graph of the second of the	ation. find o	ut the numb	er of Engineers
BW BT. <b>Dir</b> e	20 people ctions for following	or questions 24 g table represent ber of employees  Company Name  Company A  Company B	and BT.  to 27: These of the survey resist who are from Engineer 125 320	questions are base sult which is conducted Delhi.  Employees from Delhi  70  300	ucted	the following in five comparison for the five comparis	g information in graph of the second of the	ation. find o	otal numbe employees 200 400	er of Engineers
BW BT. <b>Dir</b> e	20 people ctions for following	or questions 24 g table represent ber of employees  Company Name  Company A  Company B  Company C	and BT.  Ito 27: These of the survey resists who are from Engineer 125 320 130	questions are base sult which is conducted below.  Employees from Delhi  70  300  170	ucted	the following in five comparison	g information in graph of the second of the	ation. find o	otal numbe employees 200 400 190	er of Engineers
BW BT. <b>Dir</b> e	20 people ctions for following	or questions 24 g table represent ber of employees  Company Name  Company A  Company B  Company C  Company D	and BT.  Ito 27: These of the survey resists who are from  Engineer  125  320  130  220	questions are base sult which is conducted below.  Employees from Delhi 70 300 170 140	ucted	Employees of the following in five comparison of the following in	g information in graph of the second of the	ation. find o	otal numbe employees 200 400 190 250	er of Engineers
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- 29. If the number of students who passed in Science is more than the number of students who are passed in English, then what is the maximum possible number of students, who passed in English as well as in Maths? (D) 25
  - (A) 15 (B) 27 (C) 14
- then how many students passed in exactly one subject?
  - (A) 101 (B) 139
- (C) 140

30. If the number of students passed in English is 68,

#### (D) 150

#### Exercise - 7(d)

Directions for questions 1 to 3: These questions are based on the following table.

Ago Croup		Num	Total including					
Age Group	BW		ВТ		Both		non-readers	
	Male	Female	Male	Female	Male	Female	Male	Female
< 15 years	145	65	155	65	50	30	260	115
15 - 34 years	175	125	105	85	40	50	265	190
≥ 35 years	115	135	120	100	35	45	215	195

- 1. How many males in 15 34 years age group do not read any of the 2 magazines?
  - (A) 15
- (B) 45
- (C) 75
- (D) 25
- 2. Approximately, what percentage of the BT readers, are above 15 years of age?
  - (A) 75%
- (B) 45%
- (C) 65%
- (D) 80%
- 3. What percentage of females, who read neither BT nor BW, are below 15 years of age?
  - (A) 30%
- (B) 60%
- (C) 40%
- (D) 20%

Directions for questions 4 to 7: These questions are based on the following information.

All the 1000 students at a summer camp are engaged in at least two of the activities - Painting, Swimming, Dancing, Singing or Karate. It is further known that the number of students engaged in every combination of exactly two activities is three times the number of students who are engaged in every combination of exactly three activities. Also, the number of students engaged in all the five activities is a third of that engaged in exactly four activities. The number of students engaged in every combination of exactly four activities is the same.

- If the number of students engaged in all the five activities is 100, then the number of students engaged in only painting and karate is
  - (A) 150
- (B) 45
- (C) 450
- (D) Cannot be determined
- 5. If the number of students engaged in exactly three activities is 1.5 times the number of students engaged in all the five activities, then which of the following is true?
  - (A) The number of students engaged in only swimming, dancing and painting is 15.
  - The number of students engaged in all the five activities is 100.
  - (C) Both (A) and (B)
  - (D) Neither (A) nor (B)
- If the number of students enrolled in painting, swimming, dancing, singing and karate are 750, 800, 400, 900 and 600 respectively, then which of the following is definitely false?
  - (A) The number of students engaged in only painting, dancing, singing and karate is 90.

- (B) The number of students engaged in exactly two activities is 300.
- (C) The number of students engaged in exactly three activities is lesser than that engaged in only dancing, singing, swimming and karate.
- (D) The number of students engaged in all the five activities is 150.
- 7. In the previous question, if the number of students engaged in painting is not known then which of the following can be that value?
  - (A) 270
- (B) 90
- (C) 360
- (D) 120

Directions for questions 8 to 10: These questions are based on the following data.

Out of a group of 245 pilgrims, 105 visited Badrinath, 95 visited Kedarnath and 95 visited Somnath. Fifteen of them visited all three shrines, while 190 visited exactly one of the three shrines. The number of pilgrims who visited exactly two out of the three shrines is three times as many as those who have not visited any one of the three shrines.

- 8. If the number of pilgrims who have visited at least one of the two shrines Kedarnath and Somnath is 165, then how many pilgrims visited only Kedarnath and Somnath?
  - (A) 20
- (B) 30
- (C) 10
- (D) 15
- If 180 pilgrims visited at least one of the two shrines Kedarnath or Badrinath, then how many pilgrims visited only Somnath?
  - (A) 55
- (B) 40
- (C) 35
- (D) 60
- 10. If there is nobody who visited only Badrinath and Somnath, then how many people visited only Kedarnath?
  - (A) 90
- (B) 80
- (C) 70
- (D) 50

Directions for questions 11 to 14: These questions are based on the following information.

Each of the students, who are residents of Kalpana Chawla Bhawan, likes at least one among the four different brands of cool-drinks - Coca-cola, Thums-Up, Limca and Sprite. 65 students like Thums-Up and Cocacola. 77 students like Sprite and Thums-Up. 73 students like Coca-cola and Limca. 76 students like Limca and Thums-Up. 74 students like Sprite and Coca-cola. There are 67 students who like exactly one brand. The number of students who like only Limca, Thums-Up and Coca-cola is same as the number of students who like only Sprite, Thums-Up and Coca-cola. The number of students who like Sprite, Limca and Thums-Up but not Coca-cola is same as the number of students who like Sprite, Limca and Coca-cola but not Thums-up. The number of students, who like only Coca-cola and Sprite is 14. The number of students who like only Sprite and Limca and only Thums-Up and Coca-cola are 10 and 15 respectively. The sum of the number of students who like Thums-Up, the number of students who like Coca-cola, the number of students who like Sprite and the number of students who like Limca is 557.

11.	How many students like both Sprite and Limca but no
	all the four?

(A) 60

(B) 50

(C) 55

(D) 44

12. What is the total number of students?

(A) 247

(B) 250

(C) 235

(D) 252

**13.** How many students like only Coca-cola and Limca? (A) 16 (B) 17 (C) 13 (D) 15

**14.** If 25 students like only Thums-Up or only Sprite, then how many like Coca-cola or Limca?

(A) 42

(B) 208

(C) 152

(D) 210

*Directions for questions 15 to 17:* These questions are based on the following data.

In a college library, four different business newspapers – Economic Times, Business Standard, Business Line and Financial Express – are available. All students visit the library regularly but 20% of them do not read any business newspaper.

The four newspapers given in the above order are read by 230, 180, 180 and 220 students respectively. The number of students reading exactly 2 newspapers for any two newspapers is 20. There are 30 students who read all the four newspapers but there is nobody who reads exactly three out of the four newspapers.

**15.** How many students do not read any newspaper at all? (A) 75 (B) 100 (C) 225 (D) 150

16. What percentage of the people reading Business Standard also read at least one other newspaper? (A) 35% (B) 55% (C) 50% (D) 65%

17. If all the students in the college including those who do not read any newspaper read at least one newspaper, (out of the four newspapers above) which he is not reading at present, then what is the least number of students reading all the four newspapers?

(A) 60 (B) 25 (C) 15 (D) 30

*Directions for questions 18 to 21:* These questions are based on the following data.

A survey of 300 respondents showed that 135 of them read Business India, 125 read Business Today and 115 read Business World. Further, 42 of the respondents

read Business India and Business Today, 48 read Business Today and Business World, 43 read Business India and Business World and 30 of the respondents read all the three magazines.

**18.** How many respondents read Business India or Business World?

(A) 199

(B) 272

(C) 207

(D) 175

19. If seven of the respondents who were previously reading only Business India now start reading a second magazine also and five of the respondents who were previously reading only Business India now stop even that, then how many respondents read Business India now?

(A) 75

(B) 132

(C) 142

(D) 130

20. If 15 respondents who were reading Business India stop reading Business India and start reading Business Today, then what is the maximum number of respondents who will now be reading only Business India?

(A) 120

(B) 65

(C) 78

(D) 93

21. If 16 of the respondents, who were reading Business Today, stop reading Business Today and instead start reading Business World, then what is the maximum number of respondents who will now be reading Business India and Business World?

(A) 59

(B) 55

(C) 75

(D) 63

*Directions for questions 22 to 24:* These questions are based on the following data.

In a colony, a survey was conducted regarding the ownership of three different types of vehicles – car, scooter and bicycle.

- The number of residents owning all three vehicles is the same as those owning none.
- The number of residents owning any two out of the three vehicles is the same as those owning any other two which in turn is the same as those owning none of the three.
- The number of residents owning scooters alone is the same as those owning cars alone and each in turn is twice those owning bicycles alone.
- Half the number of residents who own a bicycle also own at least one of the other two vehicles.

**22.** If the number of residents who own only bicycles is 150, then what is the total number of residents in the colony?

(A) 500

(B) 1000

(C) 750

(D) 1250

**23.** If 15 residents do not own any of the three vehicles, then how many residents are there in the colony?

(A) 100

(B) 200

(C) 500

(D) 300

**24.** What percentage of the residents own a scooter or a car but not a bicycle?

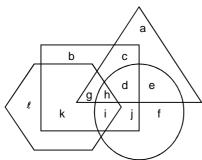
(A) 65%

(B) 55%

(C) 75%

(D) 45%

Directions for questions 25 to 27: These questions are based on the following diagram.



The circle represents the people who are Hindus. The triangle represents the people who are members of

The quadrilateral represents the people, who are Actors. The hexagon represents the people, whose mother tongue is Hindi.

25. Which of the following represents the people who are Hindus, club members, actors and whose mother tongue is Hindi?

(A) i

(B) h

(C) j

(D) d

26. Which of the following represents the people who are not Hindus but are members of a club and actors?

(A) g, c

(B) c, a

(C) g, k

(D) c, q, a

27. Which of the following represents the people, who are Hindu but are not the members of a club, are not actors and whose mother tongue is not Hindi?

(B) a

(C) f

Directions for questions 28 to 30: These questions are based on the following data.

A survey was conducted among 300 Room air conditioner owners. It was found that 125 people had Carrier Aircon, 145 people had Voltas and 90 people had Fedders Lloyd air conditioners with them. Thirty two of them had exactly two out of the three brands of air conditioners and each person owns atleast one of the three brands.

28. If six owners had only Voltas and Fedders Lloyd air conditioners with them, then how many have only Carrier Aircon with them?

(A) 125

(B) 65

(C) 45

(D) 85

29. If 110 owners had only Voltas air conditioners, then how many have only Carrier Aircon and Fedders Lloyd with them?

(A) 11

(B) 17

(C) 8

(D) 23

30. If ten of the owners having only Carrier Aircon now buy Voltas also, and 5 of the owners who had only Voltas and Fedders Lloyd now buy Carrier Aircon also, then how many have at least two out of the three brands of air conditioners?

(A) 19

(B) 61

(C) 56

(D) 73

### Key

## Exercise - 7(a)

						. ,					
1. 2. 3. 4. 5.	C D D B D	6. 7. 8. 9.	C D D B D	11. 12. 13. 14. 15.	C B B D	16. 17. 18. 19. 20.	D C B A	21. 22. 23. 24. 25.	D A C B D	26. 27. 28. 29. 30.	D C B A
	Exercise - 7(b)										
1. 2. 3. 4. 5.	C B D C	6. 7. 8. 9.	B A B D C	11. 12. 13. 14. 15.	B C D A	16. 17. 18. 19. 20.	D B B C	21. 22. 23. 24. 25.	B A C A C	26. 27. 28. 29. 30.	C B A D
					Exercise – 7	(c)					
1. 2. 3. 4. 5.	A D C C A	6. 7. 8. 9.	D A C D A	11. 12. 13. 14. 15.	A D B D	16. 17. 18. 19. 20.	C B B C A	21. 22. 23. 24. 25.	D A C C D	26. 27. 28. 29. 30.	A B A D A
					Exercise – 7	(d)					
1. 2. 3. 4. 5.	D C A B C	6. 7. 8. 9.	C A C A D	11. 12. 13. 14. 15.	A D C D	16. 17. 18. 19. 20.	C D C D	21. 22. 23. 24. 25.	B B D A B	26. 27. 28. 29. 30.	A C D A C