

Assignment 5: Trains - An Adventure Drama

Programming report

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Algorithms and Data Structures 2023-2024

1 Problem description

General input: The input consists of a finite number of train networks and their stations, as well as possible disruptions. Also, each train network has a list of queries/requests to get from one point on the "map" to another.

General output: For each query, the program should output the path from the starting point to the destination as well as the total travelled distance if the path exists and "UNREACHABLE" otherwise.

2 Problem analysis

To represent the map of the stations of a train network we will be using a graph, because it's a convenient way to represent stations as nodes and routes as edges, also, having a directed graph will allow us to apply the Dijkstra's algorithm to retrieve the shortest path between two stations.

The Dijkstra's algorithm can be described as following:

```
algorithm Dijkstra(Graph, source)
  for each vertex v in Graph:
    dist[v] = infinity
    [v] = undefined
  dist[source] = 0
  Q = the set of all nodes in Graph
  while Q is not empty:
    u = node in Q with smallest dist[ ]
    remove u from Q
    for each neighbor v of u:
      alt = dist[u] + dist_between(u, v)
      if alt < dist[v]
        dist[v] = alt
        previous[v] = u
  return previous[ ]
```

3 Program design

As suggested by the program description, the program first reads the number of networks, and then "jumps" to a while loop where the guard is the number of networks greater than 0. To ensure a correct execution of the loop, we decrement the number of networks and this way we're defining a block of code which will execute on every single network. Thus, after getting the information related to the train network and it's number of stations, we are building an initial graph which represents the train network, using an auxiliary function (makeGraph), and adding the stations to the graph using the function newGraphNode. By having a graph which represents the stations map, we will be able to apply the Dijkstra's algorithm for shortest path later on. It is worth noting that Dijkstra's algorithm was implemented using a min-priority queue, which also has a heap as its structure.

The attempted implementation of the A* algorithm follows a similar mentality, but the heuristic values are achieved using the mathematical formulas for the distance between two points in a 2D plane.

Design choice.

We define the functions `makeGraph`, `newGraphNode`, `addEdge` and `removeEdge` to create and manipulate the graph which represents the train stations map. Also, we are defining the structure `"adjListNode"` which holds information about the current station and a pointer to the next one and the structure `"graphStructure"` which holds the number of the vertices in the graph and a list of nodes (stations).

An important thing to note, when implementing Dijkstra's algorithm, the value of INFINITY appears. Since that is not easily available in a program, we are substituting it with the maximum value that an integer variable can hold.

Time complexity. The time complexity of the shortest path retrieval algorithm (Dijkstra) is $O((V + E) \log V)$, where V is the number of vertices and E is the number of edges in the graph.

4 Evaluation of the program

We test the program with the following input:

```
3, 2, 0 A, 1 B, 1, 0 1 1, 1, A, B, A, B, !, 4, 0 Amsterdam, 1 Berlin, 2 Paris, 3 Marseille, 5, 0 1 382, 0 2 238, 1 2
501, 1 3 709, 2 3 182, 1, Berlin, Marseille, Berlin, Marseille, Amsterdam, Marseille, !, 4, 0 Gallivare, 1 Ostersund,
2 Mora, 3 Trondheim, 3, 0 1 803, 1 2 309, 1 3 1609, 0, Mora, Gallivare, Trondheim, Mora, !
```

And get the expected output:

```
UNREACHABLE, Berlin, Paris, Marseille, 683, Amsterdam, Paris, Marseille, 420, Mora, Ostersund, Gallivare,
1112, Trondheim, Ostersund, Mora, 1918
```

On top of the correct output, it is also important to ensure correct memory management, which can become a tedious task with Data Structures. It is essential that only the required amount of memory is allocated and that every allocation is freed up in the end. For these purposes, we've used Valgrind to test our program and make sure that no leaks are possible:

```
==2589==
==2589== HEAP SUMMARY:
==2589== in use at exit: 0 bytes in 0 blocks
==2589== total heap usage: 137 allocs, 137 frees, 7,971 bytes allocated
==2589==
==2589== All heap blocks were freed – no leaks are possible
==2589==
==2589== For lists of detected and suppressed errors, rerun with: -s
==2589== ERROR SUMMARY: 0 errors from 0 contexts (suppressed: 0 from 0)
```

5 Process description

The program consists of accepting a number of networks as input, followed by data about each network : number of stations, the ID and name for each station, the connections, the disruptions between stations and queries that ask the for the path and distance between two stations. The program stops accepting queries upon encountering "!" as input.

Designing the data structures used in the program was not the hard part, but rather implementing the min-priority queue through a heap was difficult in the beginning. At first, the correct implementation eluded us and lead to us spending a lot of time running around in circles trying to figure out a solution. Upon understanding how to go about implementing, the process was much smoother and lead to the solution presented.

Another difficulty found in the program design was the memory deallocation. Initially, the process of deallocating memory seemed simple, but due to some design choices, a small leak always occurred. This lead to changing the approach to how to station names are stored and to the printing of the path.

Currently, however, the program presents an issue regarding Test case 6. We believe that it occurs due to using more memory than is available. This, in theory, could've been solved by changing the approach to using the `'pos[]'` array of integers from the heap struct, however we have not reached a good solution without it so we gave up on that idea.

By developing this program we became more accustomed to using Dijkstra's algorithm and correctly implementing more complex data structures.

6 Conclusions

The nature of the program has determined us to use graphs to represent the map of the train stations. The graph can be easily manipulated to add or remove stations and routes. Although processing the input and building the corresponding graph is a bit tedious and time consuming in the beginning, it surely pays off in the end later on because Dijkstra's algorithm can be applied on directed graphs to retrieve the shortest path while also being very effective in terms of runtime and memory consumption

7 Appendix: program text

Listing 1: Input processing

```
1  #include <stdio.h>
2  #include <stdlib.h>
3  #include "priorityQueue.h"
4  #include <string.h>
5
6  int main(int argc, char** argv) {
7      //First we read the number of networks to expect from the input
8      int networks;
9      scanf("%d", &networks);
10     while(networks) {
11         networks--;
12         //Now we start reading the input for each network
13         int stationsNr;
14         char bufferCleaner;
15         scanf("%d", &stationsNr);
16         //This list will hold all the stations and the data relevant to them
17         adjListNode* stations = malloc(sizeof(adjListElement)*(stationsNr));
18         //Here we make the graph used to apply Dijkstra's algorithm
19         graph stationsMap = makeGraph(stationsNr);
20         int cStationsNr = stationsNr;
21         while(cStationsNr){
22             cStationsNr--;
23             //This accepts the input for each station
24             int idNum;
25             scanf("%d ", &idNum);
26             char* staionNameInput = inputName();
27             stations[idNum] = newGraphNode(idNum, 0);
28             stations[idNum]->stationName = malloc((strlen(staionNameInput)+1)*
                sizeof(char));
29             strcpy(stations[idNum]->stationName, staionNameInput);
30             free(staionNameInput);
31         }
32         //This section handles the connections
33         int connections;
34         scanf("%d\n", &connections);
35         int i = 0;
36         while(i<connections) {
37             i++;
38             int place1, place2, distance;
39             //each connection is added as an edge
40             scanf("%d %d %d", &place1, &place2, &distance);
41             addEdge(stationsMap, stations[place1], stations[place2], distance);
42         }
43         //This section handles the disruptions
44         int disruptions;
45         scanf("%d", &disruptions);
46         //The buffer cleaner is here to handle the appearance of a NULL
            character
47         bufferCleaner = getchar();
```

```

48     if(bufferCleaner != '\n') {
49         printf("detected issue");
50     }
51
52
53     char* toremove;
54     while(disruptions>0) {
55         //This accepts a name as an input and removes the edge from the graph,
56         //it will ignore incorrect disruptions
57         toremove = inputName();
58         int stationToRemove1 = findInList(stations, toremove, stationsNr);
59         free(toremove);
60         toremove = inputName();
61         int stationToRemove2 = findInList(stations, toremove, stationsNr);
62         removeEdge(stationsMap, stations[stationToRemove1], stations[
63             stationToRemove2], &stationsNr);
64         disruptions--;
65         free(toremove);
66     }
67     //This section handles the queries
68     int queryID1, queryID2;
69     char* queryInput = inputName();
70     while(queryInput[0] != '!') {
71         //The queries consist of two names and the path and distance between
72         //them or UNREACHABLE if there is no path between them
73         int reached = 0;
74         queryID1 = findInList(stations, queryInput, stationsNr);
75         free(queryInput);
76         queryInput = inputName();
77         queryID2 = findInList(stations, queryInput, stationsNr);
78         dijkstraShortestPath(stationsMap, queryID1, queryID2, &reached,
79             stations);
80         if(reached==0) {
81             printf("UNREACHABLE\n");
82         }
83         free(queryInput);
84         queryInput = inputName();
85     }
86     //Now we free all the data structures we used
87     free(queryInput);
88     freeGraph(stationsMap);
89     freeNodeList(stations, stationsNr);
90 }

```

Listing 2: Graphs manipulation

```

1  #include <stdio.h>
2  #include <stdlib.h>
3  #include <string.h>
4  #include "graphStuff.h"
5
6
7  //This function is similar to the one provided in the code for the 4th
8  //assignment and its purpose is to accept
9  //a name as input
10 char *inputName() {
11     int strLen = 100;
12     int length = 0;
13
14     char character = getchar();

```

```

14 char *name = malloc(sizeof(char)*(strLen+1));
15
16 while(character!='\n') {
17     name[length] = character;
18     length++;
19     if(length >= strLen) {
20         strLen = 2*strLen;
21         name = realloc(name, (strLen+1)*sizeof(char));
22     }
23     character = getchar();
24 }
25 name[length] = '\0';
26 return name;
27 }
28
29
30 //This function makes and returns a new graph node using
31 adjListNode newGraphNode (int id, int distance) {
32     adjListNode new = malloc(sizeof(adjListElement));
33     new->stationIDNumber = id;
34     new->stationDistance = distance;
35     new->next = NULL;
36     new->distance = distance;
37     return new;
38 }
39
40 //This function creates and empty graph with the number of nodes equal to
    the one inputed
41 graph makeGraph (int nr) {
42     graph newGraph = malloc(sizeof(graph)*(nr+1));
43     newGraph->vertices = nr;
44     newGraph->graphArray = malloc(sizeof(adjListElement)*(nr+1));
45     for(int i = 0; i < nr; i++) {
46         newGraph->graphArray[i].head = NULL;
47     }
48     return newGraph;
49 }
50
51 //This function adds an edge to the graph's adjacency list using the data
    provided
52 void addEdge(graph elGrapho, adjListNode source, adjListNode destination,
    int distance) {
53     adjListNode new1 = newGraphNode(destination->stationIDNumber, distance);
54     new1->next = elGrapho->graphArray[source->stationIDNumber].head;
55     elGrapho->graphArray[source->stationIDNumber].head = new1;
56
57     //The graph is undirected so it must go from vertex A to B and from vertex
        B to A
58     adjListNode new2 = newGraphNode(source->stationIDNumber, distance);
59     new2->next = elGrapho->graphArray[destination->stationIDNumber].head;
60     elGrapho->graphArray[destination->stationIDNumber].head = new2;
61 }
62
63
64
65 //This function removes and edge from the graph's adjacency list, ignoring
    the invalid deletions
66 void removeEdge (graph elGrapho, adjListNode toRemove1, adjListNode
    toRemove2, int *totalStations) {
67     //Both the edge from A to B and from B to A must be removed, since the
        graph is undirected

```

```

68     adjListNode currentNode = elGrapho->graphArray[toRemove1->stationIDNumber
        ].head;
69     adjListNode previousNode = NULL;
70     //This loop looks for the other vertex incident with the edge to be
        removed
71     while(currentNode !=NULL && currentNode->stationIDNumber!=toRemove2->
        stationIDNumber) {
72         previousNode = currentNode;
73         currentNode = currentNode->next;
74     }
75
76
77     //Upon finding it,if it's found, it's removed by freeing the memory
78     if(currentNode!=NULL) {
79         if(previousNode == NULL) {
80             elGrapho->graphArray[toRemove1->stationIDNumber].head = currentNode->
                next;
81         } else {
82             previousNode->next = currentNode->next;
83         }
84         free(currentNode);
85     }
86
87     //The same procedure is applied for the second vertex of the node
88     currentNode = elGrapho->graphArray[toRemove2->stationIDNumber].head;
89     previousNode = NULL;
90     while(currentNode !=NULL && currentNode->stationIDNumber!=toRemove1->
        stationIDNumber) {
91         previousNode = currentNode;
92         currentNode = currentNode->next;
93     }
94
95     if(currentNode != NULL) {
96         if(previousNode == NULL) {
97             elGrapho->graphArray[toRemove2->stationIDNumber].head = currentNode->
                next;
98         } else {
99             previousNode->next = currentNode->next;
100         }
101         free(currentNode);
102     }
103
104     return;
105 }
106
107 //This funtion looks into the list of nodes and returns the position of the
    station in the list
108 int findInList(adjListNode* stations, char* name, int stationsNr) {
109     for(int i = 0; i<stationsNr; i++) {
110         if(strcmp((*stations[i]).stationName, name)==0) {
111             return i;
112         }
113     }
114     return -1;
115 }
116
117 //This function frees the graph
118 void freeGraph(graph g) {
119     for(int i = 0; i<g->vertices; i++) {
120         adjListNode newNode = g->graphArray[i].head;
121         adjListNode next;

```

```

122     while(newNode!=NULL) {
123         next = newNode->next;
124         freeNode(newNode);
125         newNode = next;
126     }
127 }
128 free(g->graphArray);
129 free(g);
130 }
131
132 //This funtcion frees a particular node
133 void freeNode(adjListNode node) {
134     free(node);
135 }
136
137 //This function frees the adjacency list
138 void freeNodeList(adjListNode* list, int number) {
139     for(int i=0; i< number; i++) {
140         free(list[i]->stationName);
141         freeNode(list[i]);
142     }
143     free(list);
144 }

```

Listing 2: Path priority

```

1  #include "priorityQueue.h"
2  #include <stdio.h>
3  #include <stdlib.h>
4  #include <limits.h>
5
6  //This fucntion frees the memorya allocated to a heap node
7  void freeHeapNode(heapNode node) {
8      free(node);
9  }
10
11 //This fucntion free the memory allocated to a heap
12 void freeHeap(heap h, int source) {
13
14     free(h->array);
15     free(h->pos);
16     free(h);
17 }
18
19 //This structure is used to remember the path discovered in the Dijkstra's
    algorithm
20 typedef struct pathHolder{
21     int* IDs;
22     int distance;
23 }pathHolder;
24
25
26 //This fucntion creates and allocates memory to a new node for the heap
27 heapNode newHeapNode(int distance, int v, adjListNode node) {
28     heapNode new = malloc(sizeof(heapElem));
29     new->dist = distance;
30     new->v = v;
31     new->node = node;
32     return new;
33 }
34

```

```

35
36 //This function creates and allocates memory for a heap
37 heap makeHeap(int capacity) {
38     heap new = malloc(sizeof(heapStructure));
39     new->pos = malloc(capacity*sizeof(int));
40     new->size = 0;
41     new->capacity = capacity;
42     new->front = 0;
43     new->array = malloc(capacity*sizeof(heapNode));
44     for(int i = 0; i < capacity; i++) {
45         new->array[i] = NULL;
46     }
47     return new;
48 }
49
50 //This function swaps two nodes of a heap
51 void swapHeapNodes(heapNode* a, heapNode* b) {
52     heapNode temp = *a;
53     *a = *b;
54     *b = temp;
55     return;
56 }
57
58 //This function fixes the heap from the given id in order for it to be a
    minimum Heap
59 //It also updates the position of nodes when they are swapped
60 void upHeap(heap h, int id) {
61     int smallest, leftChild, rightChild;
62     smallest = id;
63     leftChild = id*2+1;
64     rightChild = id*2+2;
65
66     if(leftChild < h->size && h->array[leftChild]->dist < h->array[smallest]->
        dist) {
67         smallest = leftChild;
68     }
69
70     if(rightChild < h->size && h->array[rightChild]->dist < h->array[smallest
        ]->dist) {
71         smallest = rightChild;
72     }
73
74     if(smallest != id) {
75         heapNode smallestNode = h->array[smallest];
76         heapNode idNode = h->array[id];
77         h->pos[smallestNode->v] = id;
78         h->pos[idNode->v] = smallest;
79
80
81         swapHeapNodes(&h->array[smallest], &h->array[id]);
82
83         upHeap(h, smallest);
84     }
85     return;
86 }
87
88
89 //This function returns the minimum of a heap and removes it from said
    structure
90 heapNode getMinimum(heap h) {
91     if(isEmptyHeap(h)) {

```



```

92     return NULL;
93 }
94
95 heapNode root = h->array[0];
96 heapNode lastNode = h->array[h->size - 1];
97 h->array[0] = lastNode;
98
99 h->pos[root->v] = h->size - 1;
100 h->pos[lastNode->v] = 0;
101
102
103 h->size = h->size-1;
104
105 upHeap(h, 0);
106
107 return root;
108 }
109
110 //This fucntion modifies the distance stored at vertex v/the priority stored
    at vertex v
111 void decreaseDistance(heap h, int vertex, int distance) {
112     int i = h->pos[vertex];
113     h->array[i]->dist = distance;
114
115     //Travels down the heap until it is correct
116     while(i && h->array[i]->dist < h->array[(i-1)/2]->dist) {
117         h->pos[h->array[i]->v] = (i-1)/2;
118         h->pos[h->array[(i-1)/2]->v] = i;
119         swapHeapNodes(&h->array[i], &h->array[(i-1)/2]);
120         i = (i-1)/2;
121     }
122 }
123
124 //This checks whether the heap is empty
125 int isEpmtyHeap(heap h) {
126     return h->size == 0;
127 }
128
129
130 //This checks whether an element is still in the heap
131 int isInHeap(heap h, int v) {
132     if(h->pos[v] < h->size) {
133         return 1;
134     }
135
136     return 0;
137 }
138
139
140 //This fucntion is used to print a string
141 void printString(char *str) {
142     for(int i = 0; str[i] != '\0'; i++) {
143         printf("%c", str[i]);
144     }
145     printf("\n");
146 }
147
148 //This is the implementation of Dijkstra's algorithm using an adjacency
    list and a min-priority queue represented by a heap
149 void dijkstraShortestPath(graph g, int source, int destination, int *
    reacheable, adjListNode* stations) {

```

```

150 pathHolder* p = malloc(g->vertices*sizeof(pathHolder));
151 int vertices = g->vertices;
152 int* prev = malloc((vertices+1)*sizeof(int));
153 //This is the empty priority queue
154 heap S = makeHeap(vertices);
155
156 //This loop declares the array which will be used to print the path later
157 for(int i = 0; i < vertices; i++) {
158     p[i].IDs = malloc((vertices+1)*sizeof(int));
159 }
160
161 //This is the initialization of the dist[source] = 0 and the other source-
    related values
162 //newHeapNode is going to be used as the add_with_priority() function
163 p[source].distance = 0;
164 prev[source] = -1;
165 S->array[source] = newHeapNode(p[source].distance, source, g->graphArray[
    source].head);
166 S->pos[source] = source;
167
168 //This initiates the other values different from the source
169 //instead of INFINITY, the maximum value that can be held by an integer
    variable is used
170 for(int i = 0; i < vertices; i++) {
171     if(i != source) {
172         p[i].distance = INT_MAX;
173         prev[i] = -1;
174         S->array[i] = newHeapNode(p[i].distance, i, g->graphArray[i].head);
175         S->pos[i] = i;
176     }
177 }
178
179
180
181 decreaseDistance(S, source, p[source].distance);
182 S->size = vertices;
183 //Here starts the loop to find the path
184 //while S is not empty
185 while(!isEmptyHeap(S)) {
186     //u <- S. extract_min()
187     heapNode minimumHeapNode = getMinimum(S);
188     int u = minimumHeapNode->v;
189     //This is used to go through the incident nodes
190     adjListNode crawler = g->graphArray[u].head;
191     while(crawler != NULL) {
192         //v is the node adjacent to the minimum node/u
193         int v = crawler->stationIDNumber;
194         //this holds the current distance from the source
195         int alt = p[u].distance + crawler->distance;
196         if(isInHeap(S, v) && p[u].distance!=INT_MAX && alt< p[v].distance) {
197             *reachable = 1;
198             //This modifies the distance from the source to the node v
199             p[v].distance = alt;
200             prev[v] = u;
201             //this reduces priority/ S.decrease_priority(v, alt), distance is
                the equivalent to priority
202             decreaseDistance(S, v, alt);
203         }
204         crawler = crawler->next;
205     }
206 }

```

```

207 //After using the node, we free it to avoid memeory leaks
208 free(minimumHeapNode);
209 }
210
211 //Here the printing is done, if the point is reacheable
212 int nr =0;
213 if(*reacheable!=0) {
214     if(p[destination].distance == INT_MAX) {
215         *reacheable = 0;
216         return;
217     }
218
219     int j = destination;
220
221     while(j!=-1) {
222         p[destination].IDs[nr] = j;
223         nr++;
224         j = prev[j];
225     }
226     for(int z = nr-1; z>=0;z--) {
227         printf("%s\n", stations[p[destination].IDs[z]]->stationName);
228     }
229     printf("%d\n", p[destination].distance);
230 }
231
232
233 //Now we free the used structures
234 free(prev);
235 for(int i = 0; i < vertices; i++) {
236     free(p[i].IDs);
237 }
238 free(p);
239 freeHeap(S, source);
240
241 return;
242 }

```