

Međusobno isključivanje

read/write promenljive

Algoritam sa ceduljicama (Bakery Algorithm)

Ovaj algoritam je sličan sa
read-modify-write algoritmom

Postoji red čekanja:

Proces na početku (glavi) reda je
u kritičnoj sekciji

Nov proces se ubacuje na kraj (rep)

Skica algoritma

Ulaz:

$t = \text{tail};$

$\text{tail} = \text{tail} + 1;$

Wait until $t == \text{head};$

Kritična sekcija

Izlaz:

$\text{head} = \text{head} + 1;$

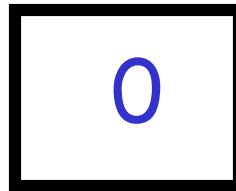
(*tail* i *head* su deljene promenljive,
t je lokalna promenljiva)

Problem: ovaj deo koda se ne
ponaša korektno

Ulaz:

```
t = tail;           //read tail  
tail = tail + 1;    //write tail
```

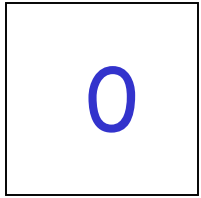
Dobar scenario



tail

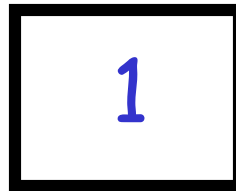
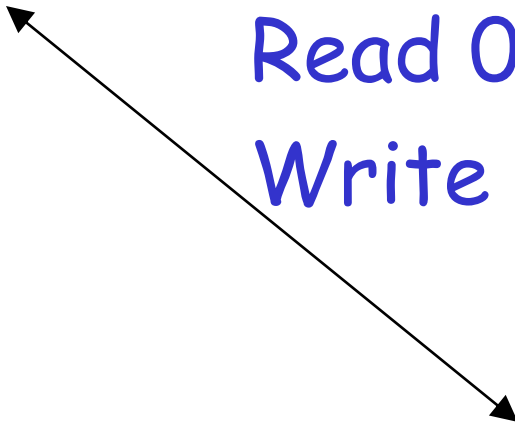
Dobar scenario

($t=0$)



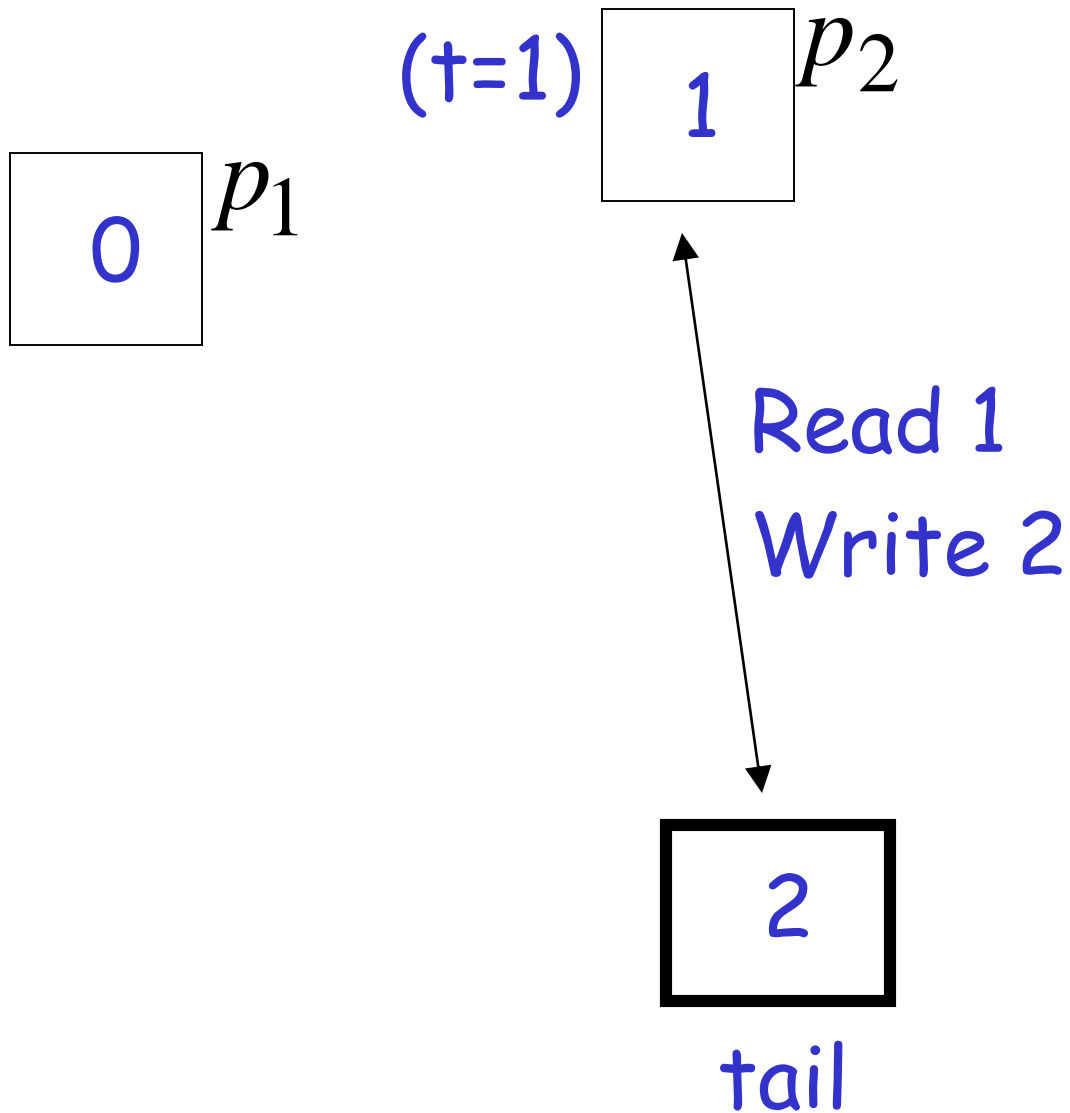
p_1

Read 0
Write 1

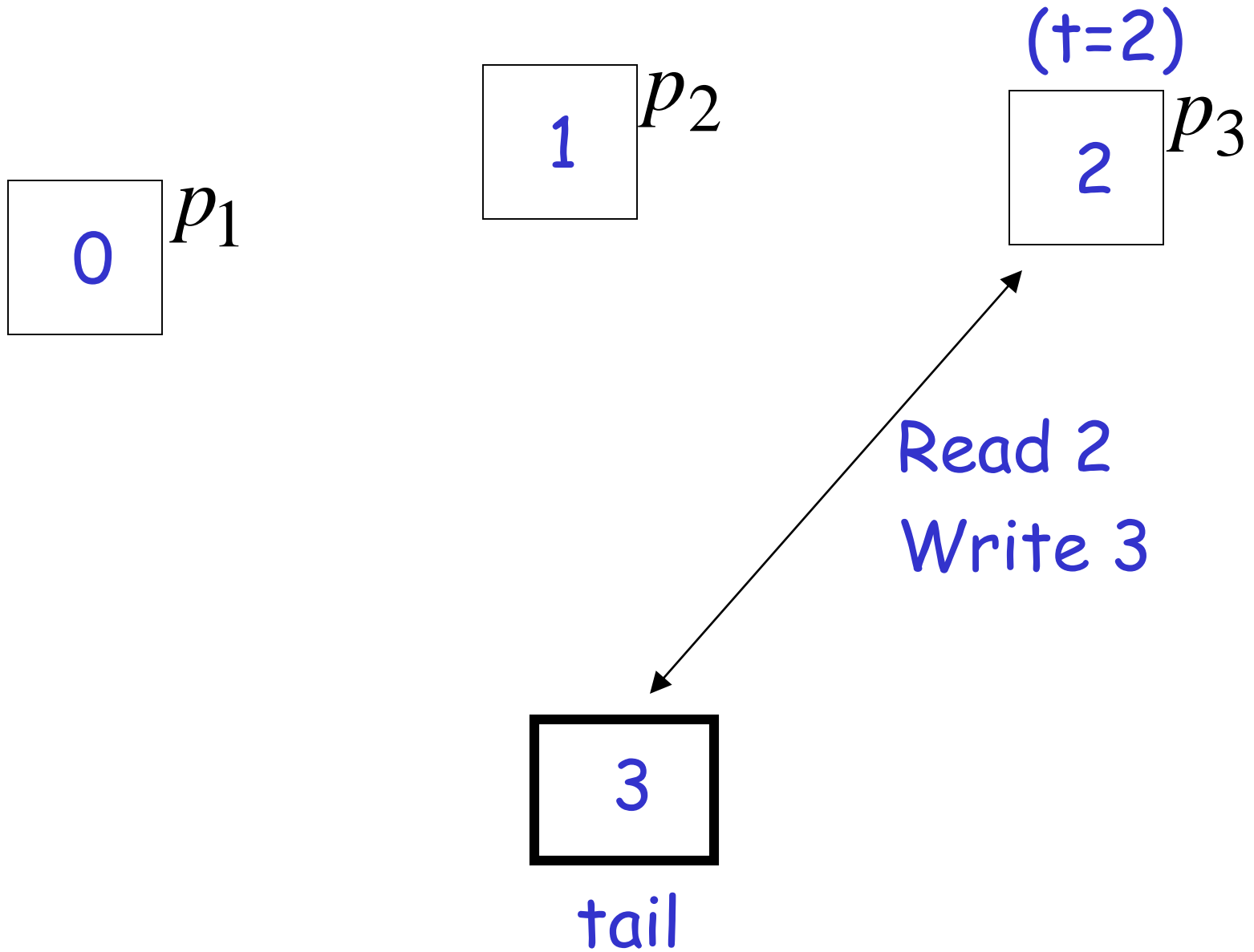


tail

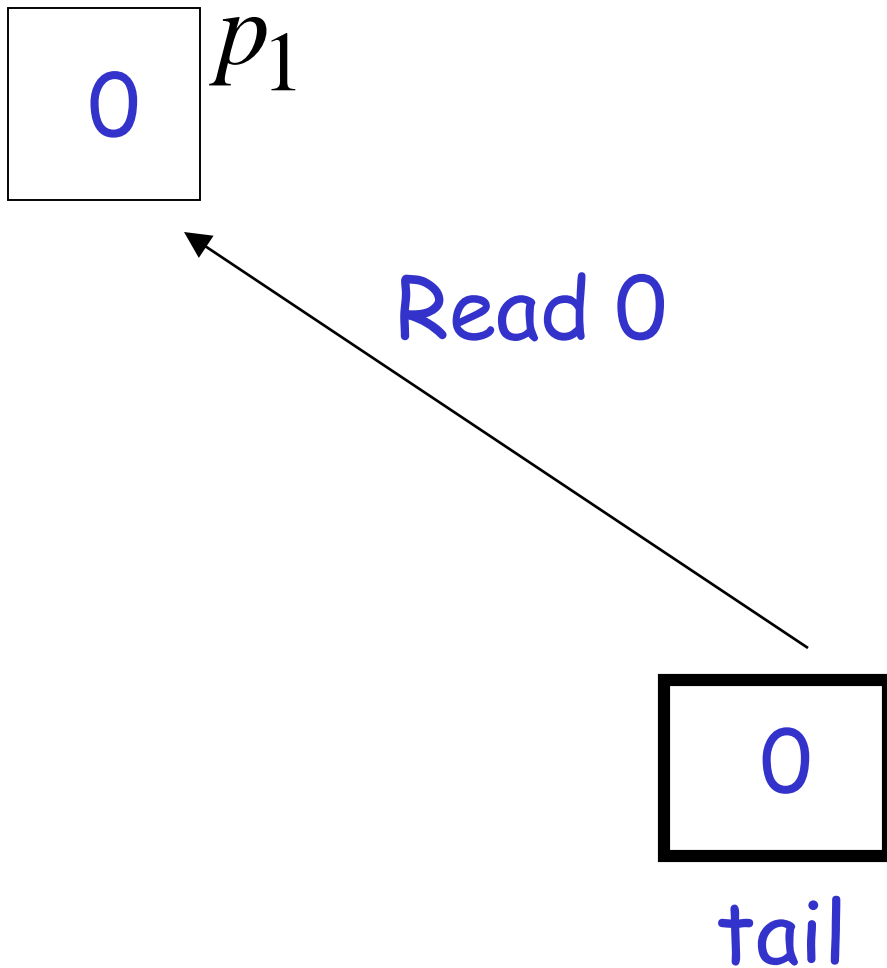
Dobar scenario



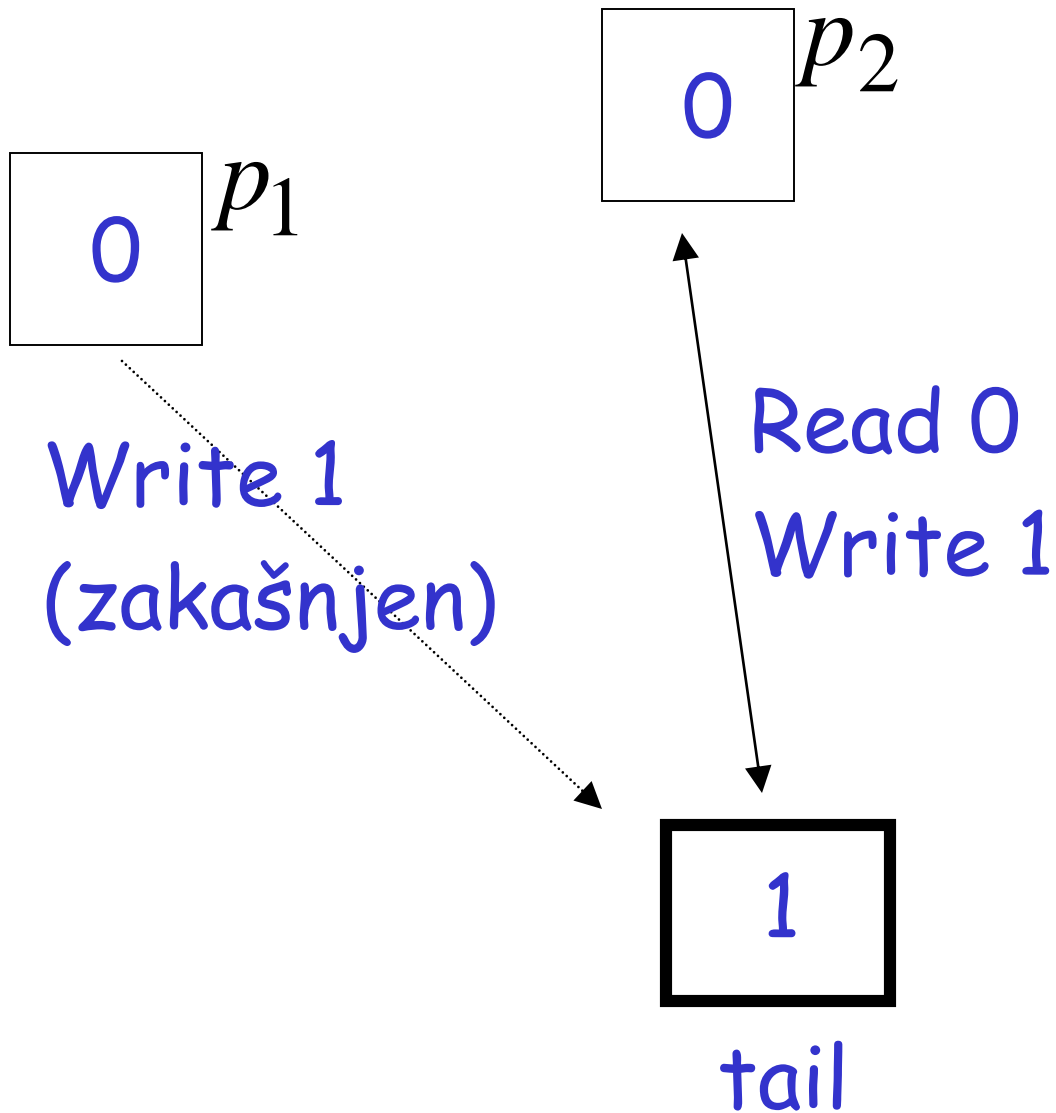
Dobar scenario



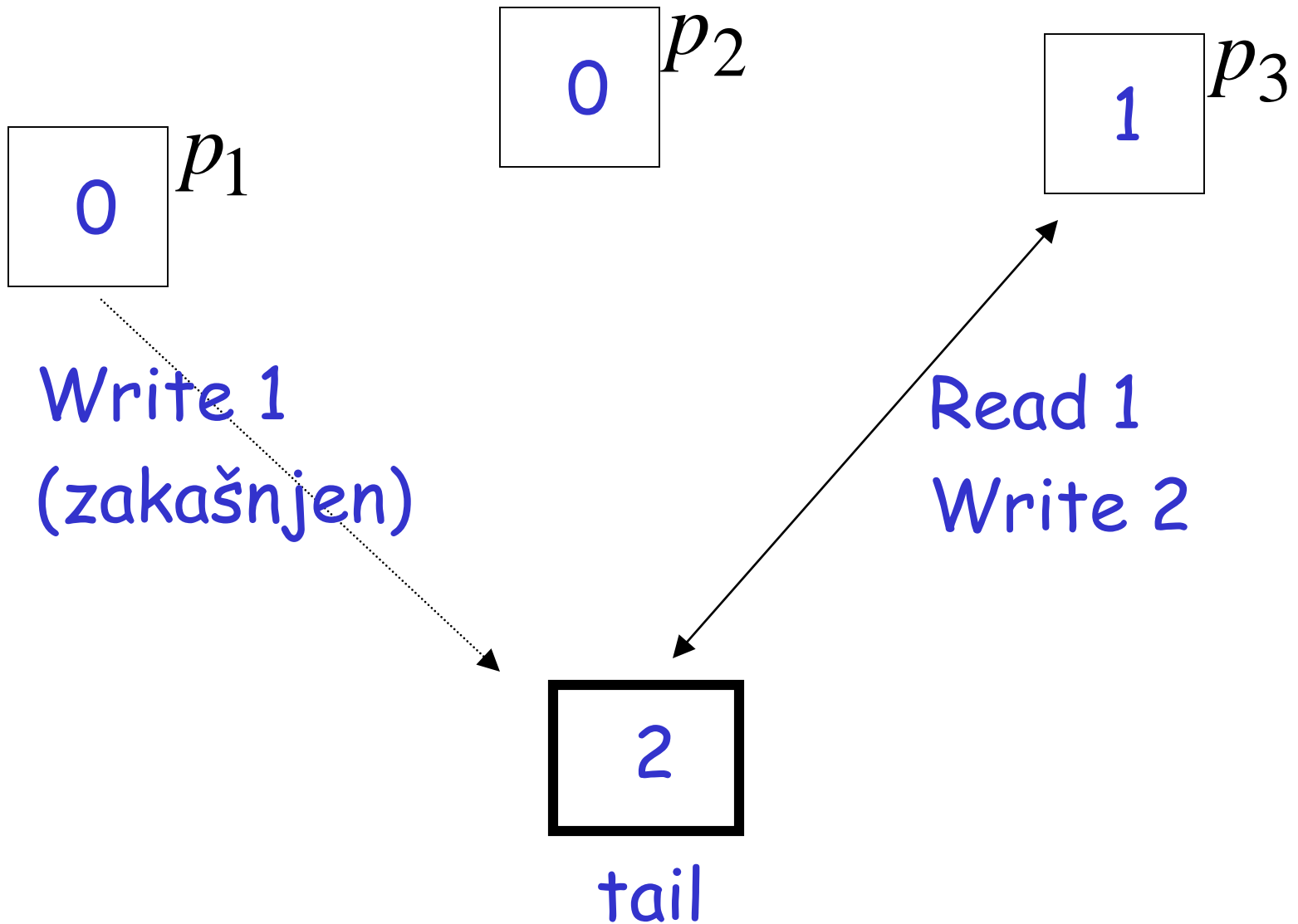
Loš scenario



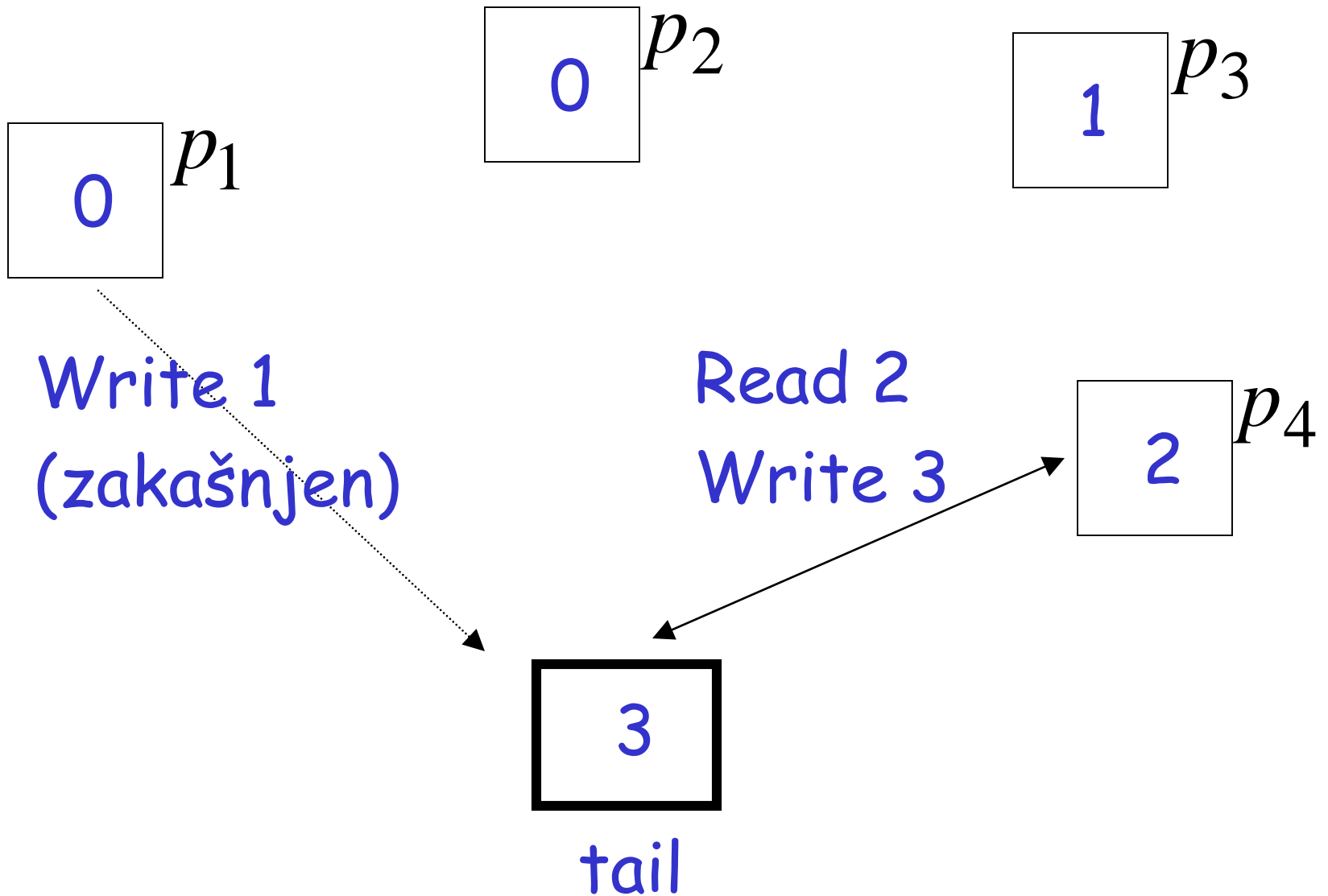
Loš scenario



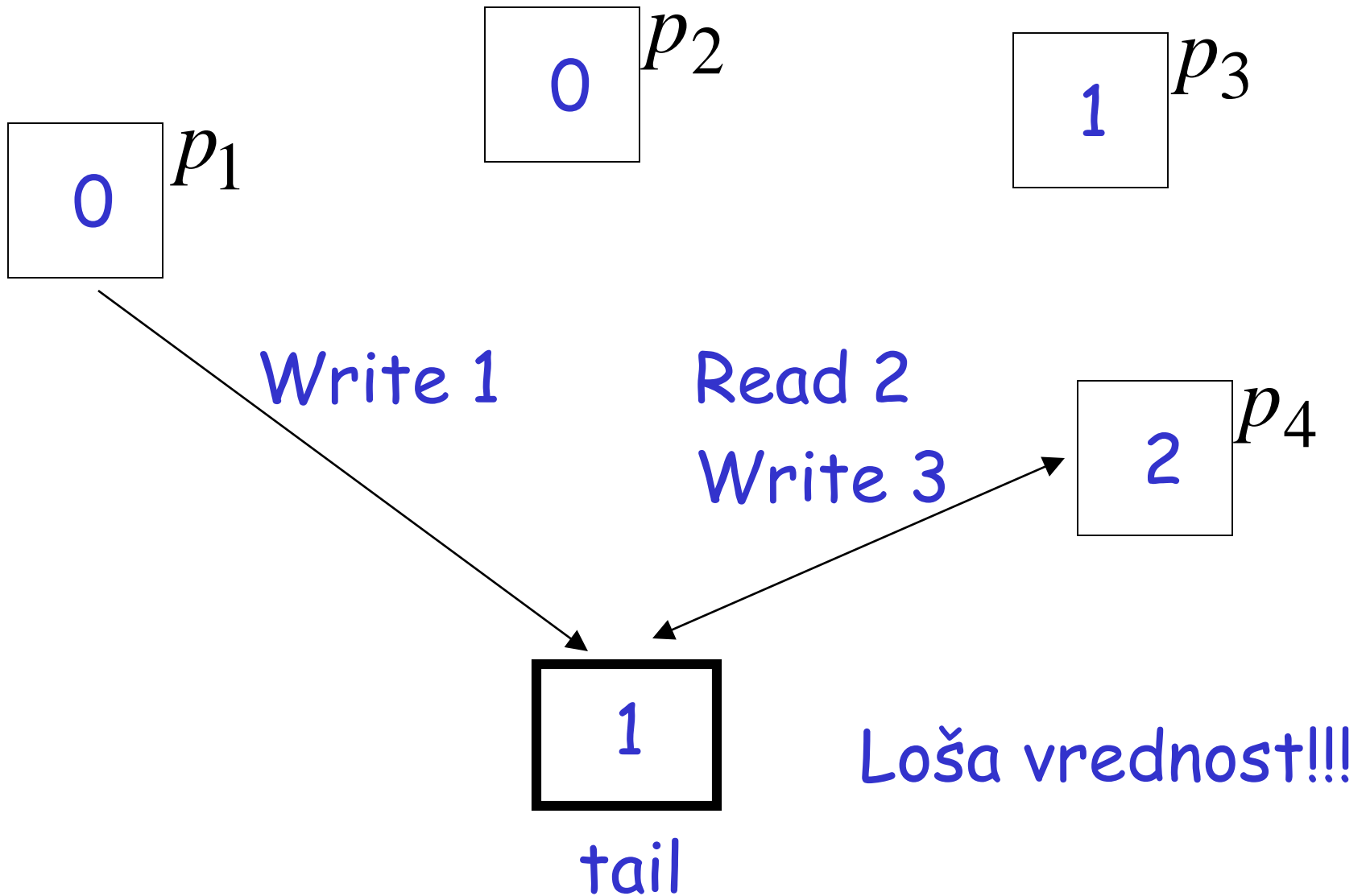
Loš scenario



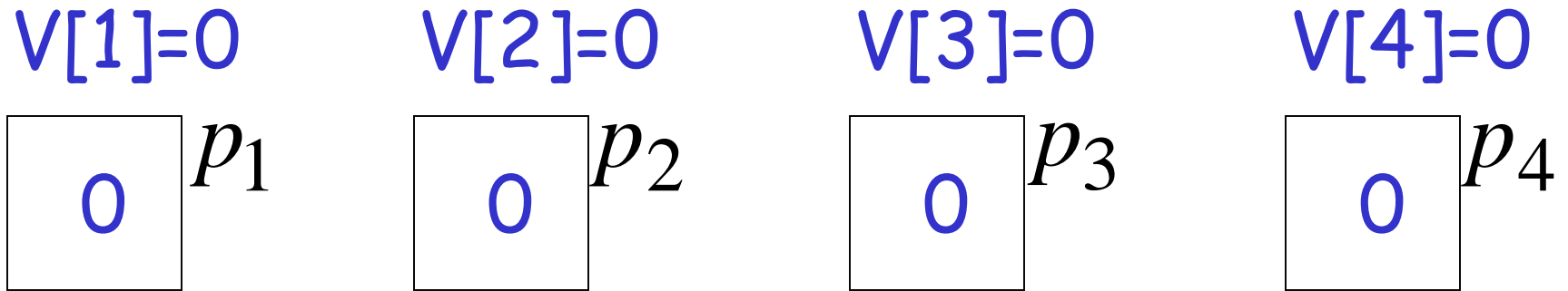
Loš scenario



Loš scenario



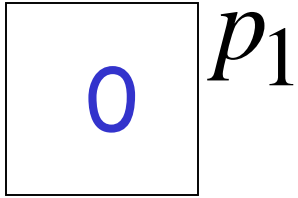
Rešenje: distribuirano brojanje



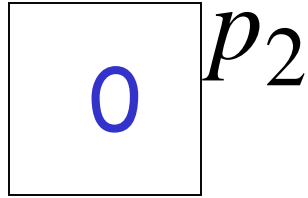
Treba nam niz deljenih promenljivih
 $v[1], v[2], \dots, v[n]$

Proces p_i ima vrednost $v[i]$

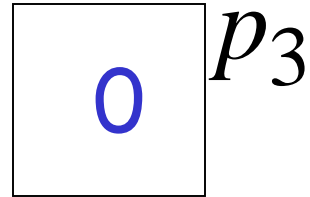
$V[1]=0$



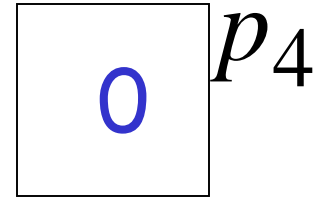
$V[2]=0$



$V[3]=0$



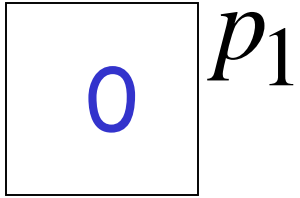
$V[4]=0$



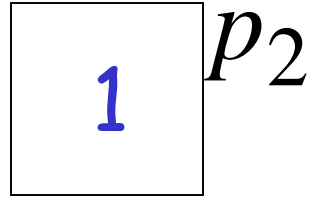
U ulaznom kodu, proces
čita vrednosti svih drugih procesa.

Nova vrednost je maximum + 1

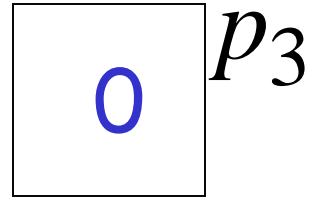
$V[1]=0$



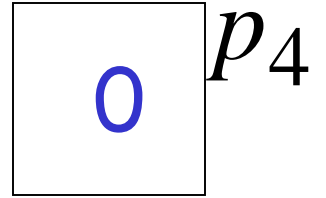
$V[2]=1$



$V[3]=0$



$V[4]=0$



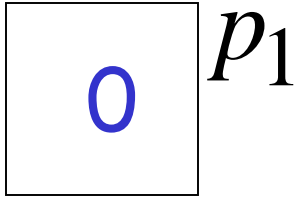
ulaz



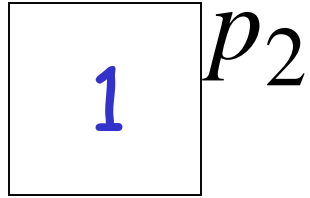
$Max = 0;$

$Max + 1 = 1;$

$V[1]=0$

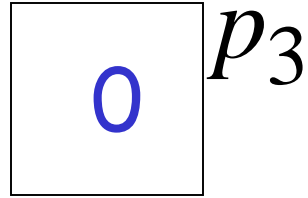


$V[2]=1$

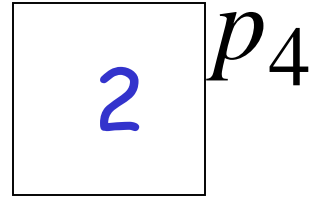


ulaz

$V[3]=0$



$V[4]=2$



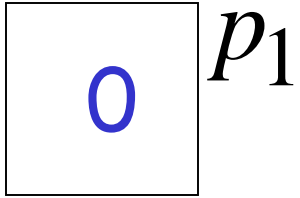
ulaz



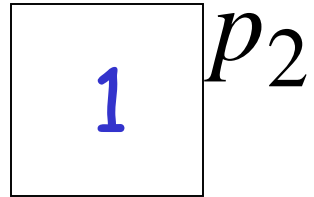
$Max = 1;$

$Max + 1 = 2;$

$V[1]=0$

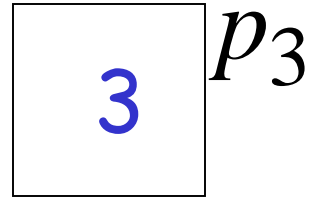


$V[2]=1$



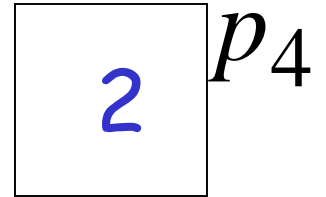
ulaz

$V[3]=3$

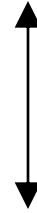


ulaz

$V[4]=2$

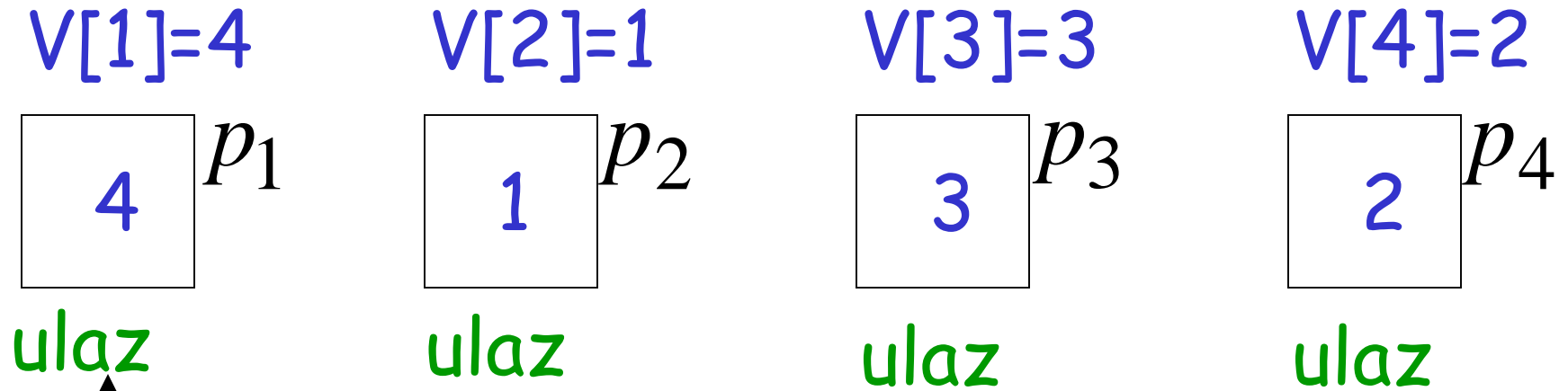


ulaz



$Max = 2;$

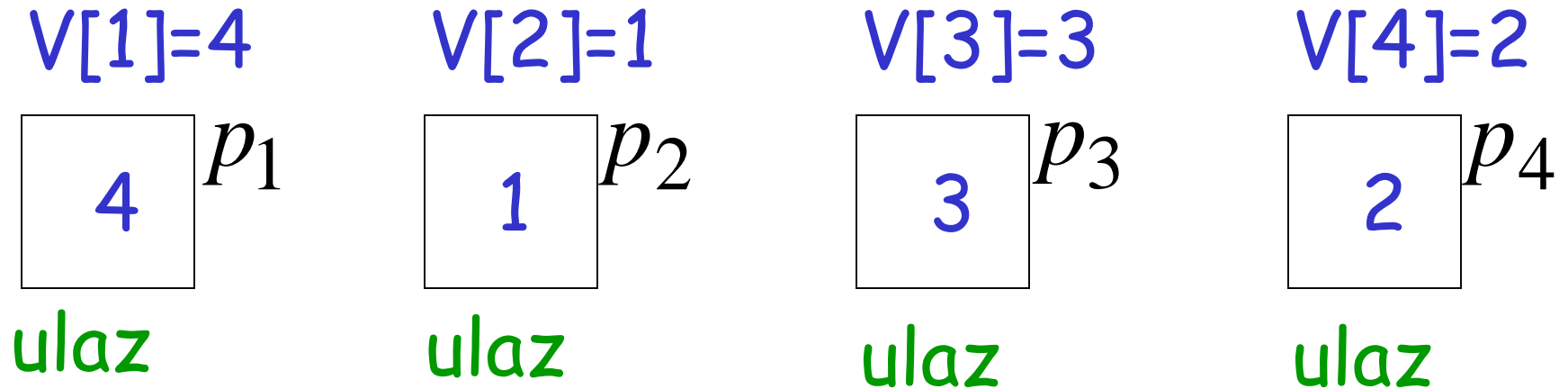
$Max + 1 = 3;$



$\text{Max} = 3;$

$\text{Max} + 1 = 4;$

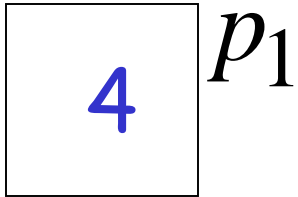
Svaki proces dobija jedinstvenu vrednost
(jedinstvena pozicija u distribuiranom redu)



Zatim procesi porede svoje vrednosti sa svim drugim vrednostima.

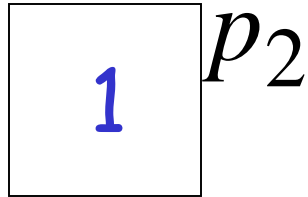
Najmanja vrednost ulazi u kritičnu sekciju
(različita od 0)

$V[1]=4$



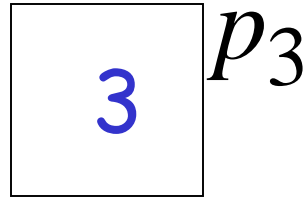
ulaz

$V[2]=1$



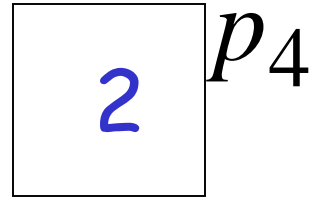
kritična
sekcija

$V[3]=3$



ulaz

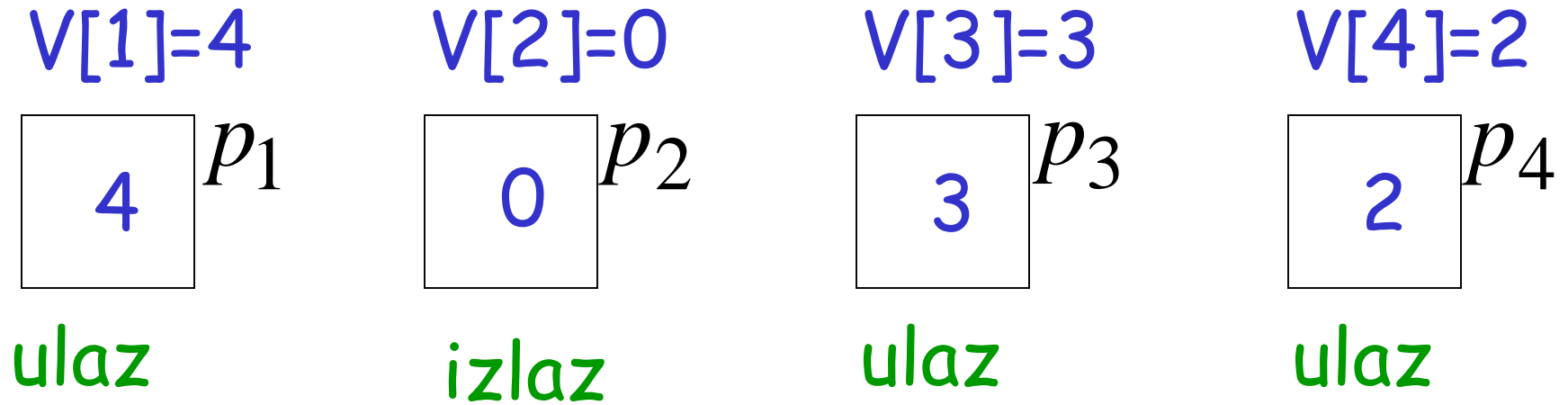
$V[4]=2$



ulaz

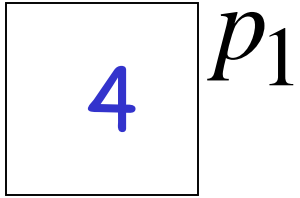
p_2 čita sve vrednosti

p_2 shvata da ima najmanju vrednost



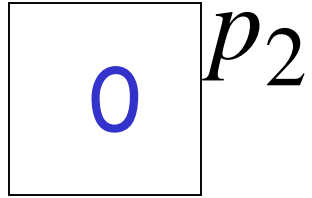
p_2 postavlja svoju prom na 0

$V[1]=4$

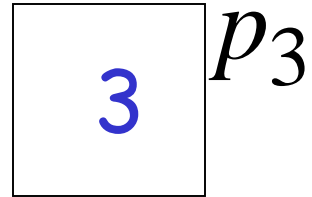


ulaz

$V[2]=0$

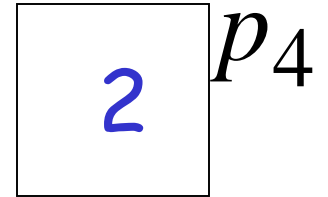


$V[3]=3$



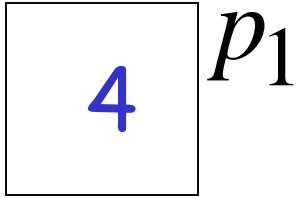
ulaz

$V[4]=2$



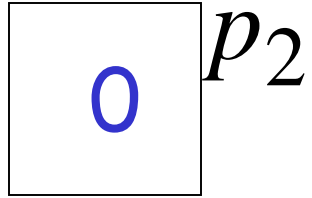
kritična
sekcija

$V[1]=4$

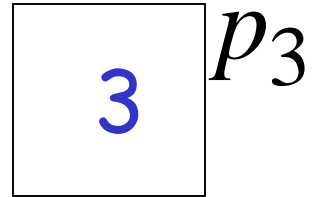


ulaz

$V[2]=0$

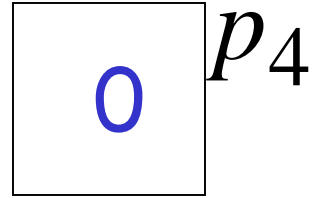


$V[3]=3$



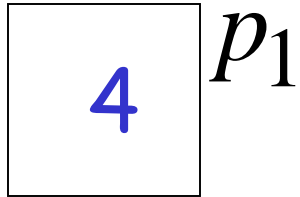
ulaz

$V[4]=0$



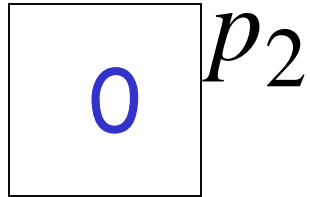
izlaz

$V[1]=4$

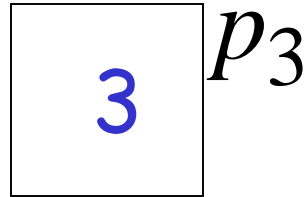


ulaz

$V[2]=0$

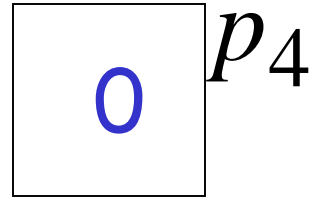


$V[3]=3$



Kritična
sekcija

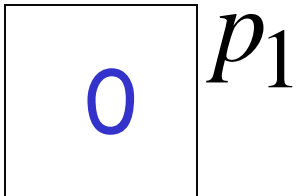
$V[4]=0$



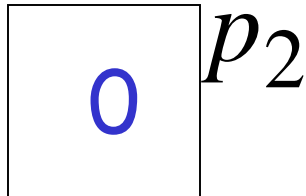
I tako dalje.....

Problem: Kada dva procesa uđu
u istom trenutku,
oni mogu da izaberu istu vred.

$V[1]=0$

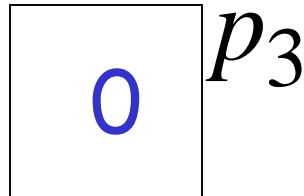


$V[2]=0$

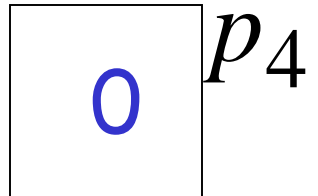


ulaz

$V[3]=0$



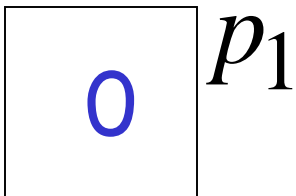
$V[4]=0$



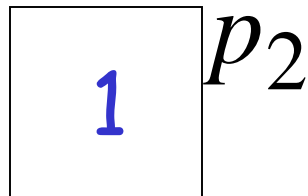
ulaz

Max vrednosti koje oni pročitaju su iste

$V[1]=0$

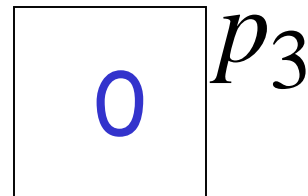


$V[2]=1$

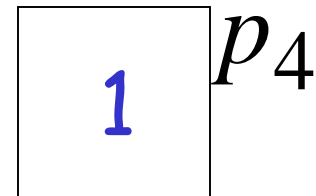


ulaz

$V[3]=0$



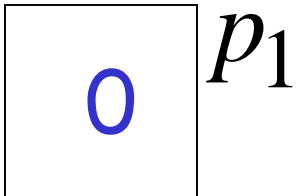
$V[4]=1$



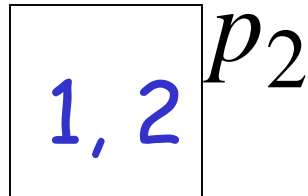
ulaz

Rešenje: koristiti ID za razbijanje simetrije
(najmanji ID pobeđuje)

$V[1]=0$

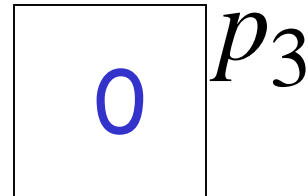


$V[2]=1$

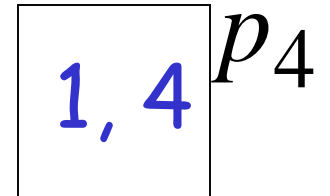


kritična
sekcija

$V[3]=0$

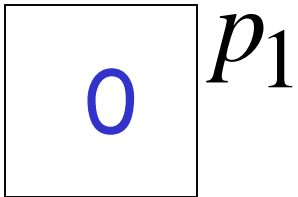


$V[4]=1$

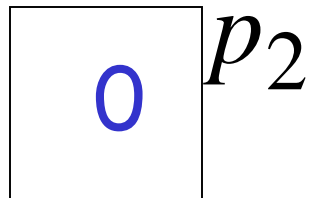


ulaz

$V[1]=0$

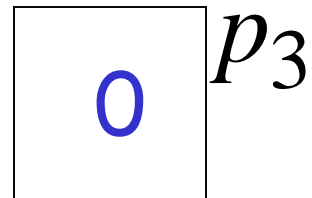


$V[2]=0$

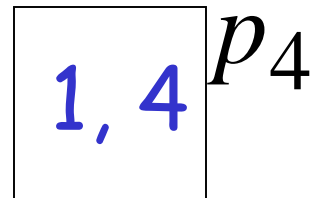


izlaz

$V[3]=0$



$V[4]=1$



ulaz

Ceo algoritam sa ceduljicama

Proces i: $V[i] = 0$; choosing[i] = false;

Ulaz: choosing[i] = true;
 $V[i] = \max(V[1], V[2], \dots, V[n]) + 1$;
choosing[i] = false;
for (k = 1; k <= n; k++)
 Wait until choosing[k] == false;
 Wait until $V[k] == 0$ or
 $(V[k], k) > (V[i], i)$

Kritična sekcija

Izlaz: $V[i] = 0$;

Prednosti algoritma sa ceduljicama:

- Koristi Read/Write promenljive
- Zadovoljava uslov da nema trajnog zaključavanja

Nedostaci:

- Koristi n deljenih prom. za n procesa
(u stvari, ne postoji rešenje sa manje prom.)
- Vrednosti mogu da rastu neograničeno
(voleli bi da nađemo neki algoritam
sa ograničenim vrednostima)

Međusobno isključivanje za 2 procesa

proces visokog priori.

proces niskog priori.

Ulaz:

```
Want[0] = 1;  
Wait until want[1]== 0;
```

Kritična sekcija

Izlaz:

```
Want[0] = 0;
```

```
1: Want[1] = 0;  
   Wait until want[0] ==0;  
   Want[1] = 1;  
   if (want[0] == 1) goto 1;
```

Kritična sekcija

```
Want[1] = 0;
```

Dobro: Koristi samo ograničene vred. prom.
Problem: Proces niskog prio. može se traj.zak.

Algoritam istog prioriteta

Proces 0

Proces 1

Ulaz:

```
1: Want[0] = 0;  
Wait until (want[1]== 0  
           or Priority == 0);  
Want[0] = 1;  
if priority == 1 then  
    if Want[1] == 1 then  
        goto Line 1  
Else wait until Want[1]==0;  
Critical section
```

```
1: Want[1] = 0;  
Wait until (want[0]== 0  
           or Priority == 1);  
Want[1] = 1;  
if priority == 0 then  
    if Want[0] == 1 then  
        goto Line 1  
Else wait until Want[0]==0;  
Critical section
```

Izlaz:

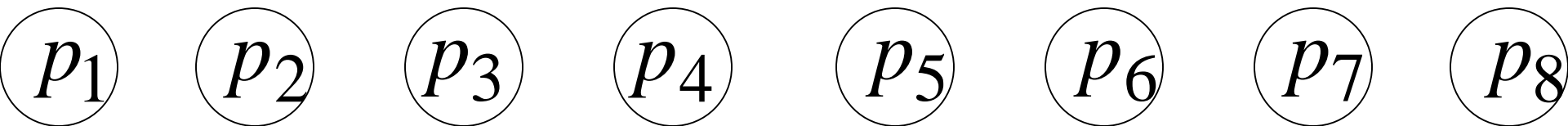
```
Priority = 1;  
Want[0] = 0;
```

```
Priority = 0;  
Want[1] = 0;
```

Dobro: Koristi ograničene vred. prom.
Nema trajnog zaključ. (lockout)

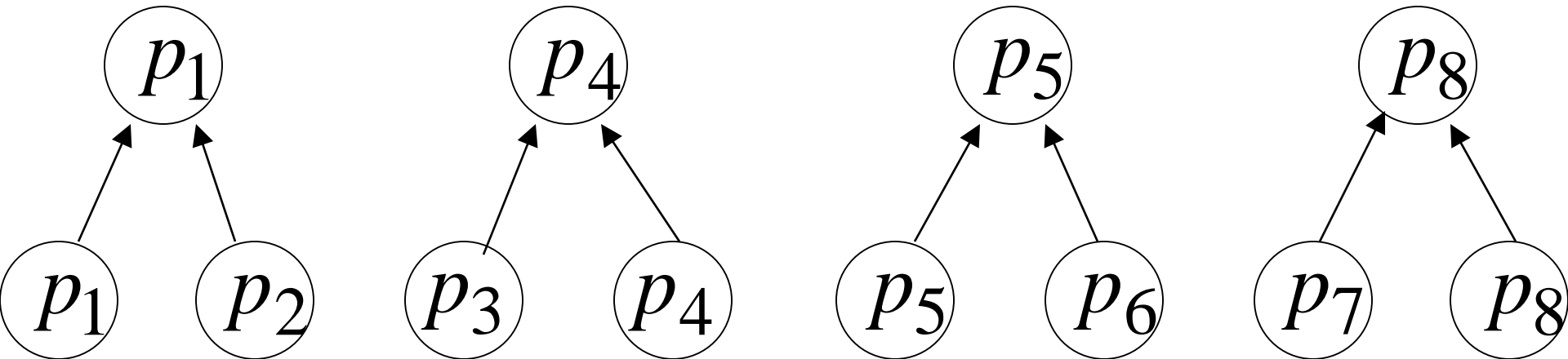
Algoritam sa turnirom (Tournament)

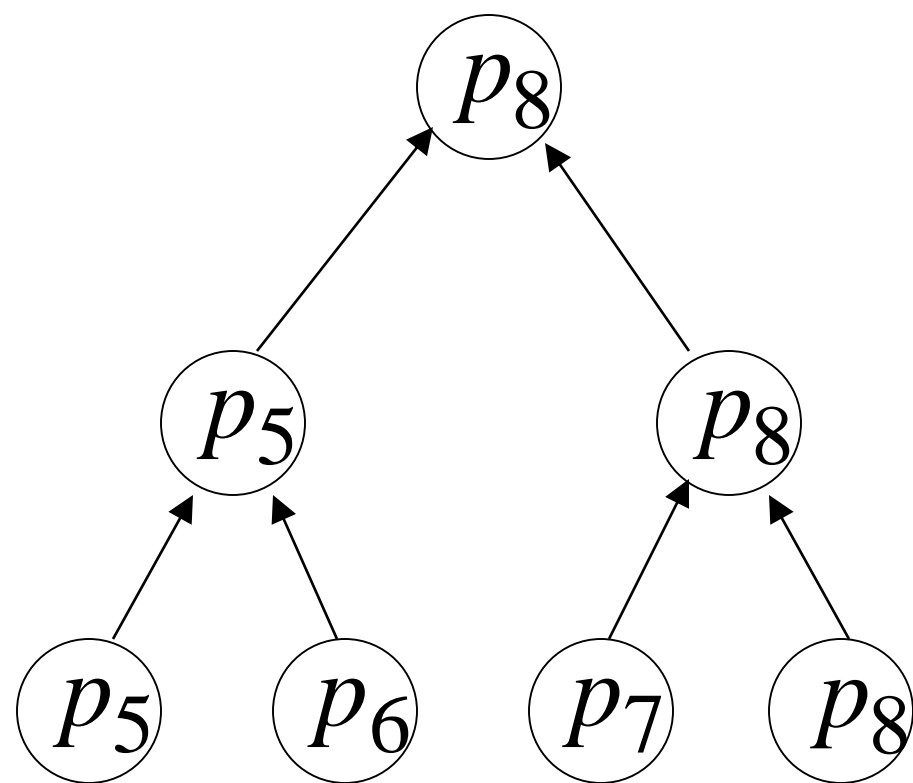
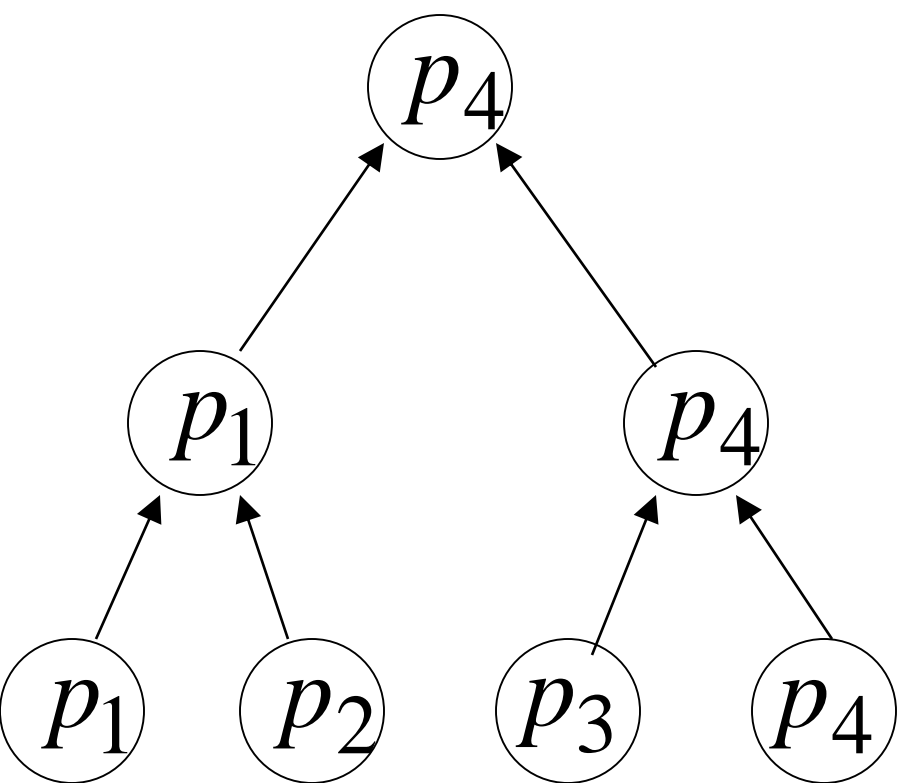
Možemo realizovati algoritam turnira za međusobno isključivanje, koristeći algorit. jednakog prioriteta po parovima



Međusobno isključivanje za parove procesa

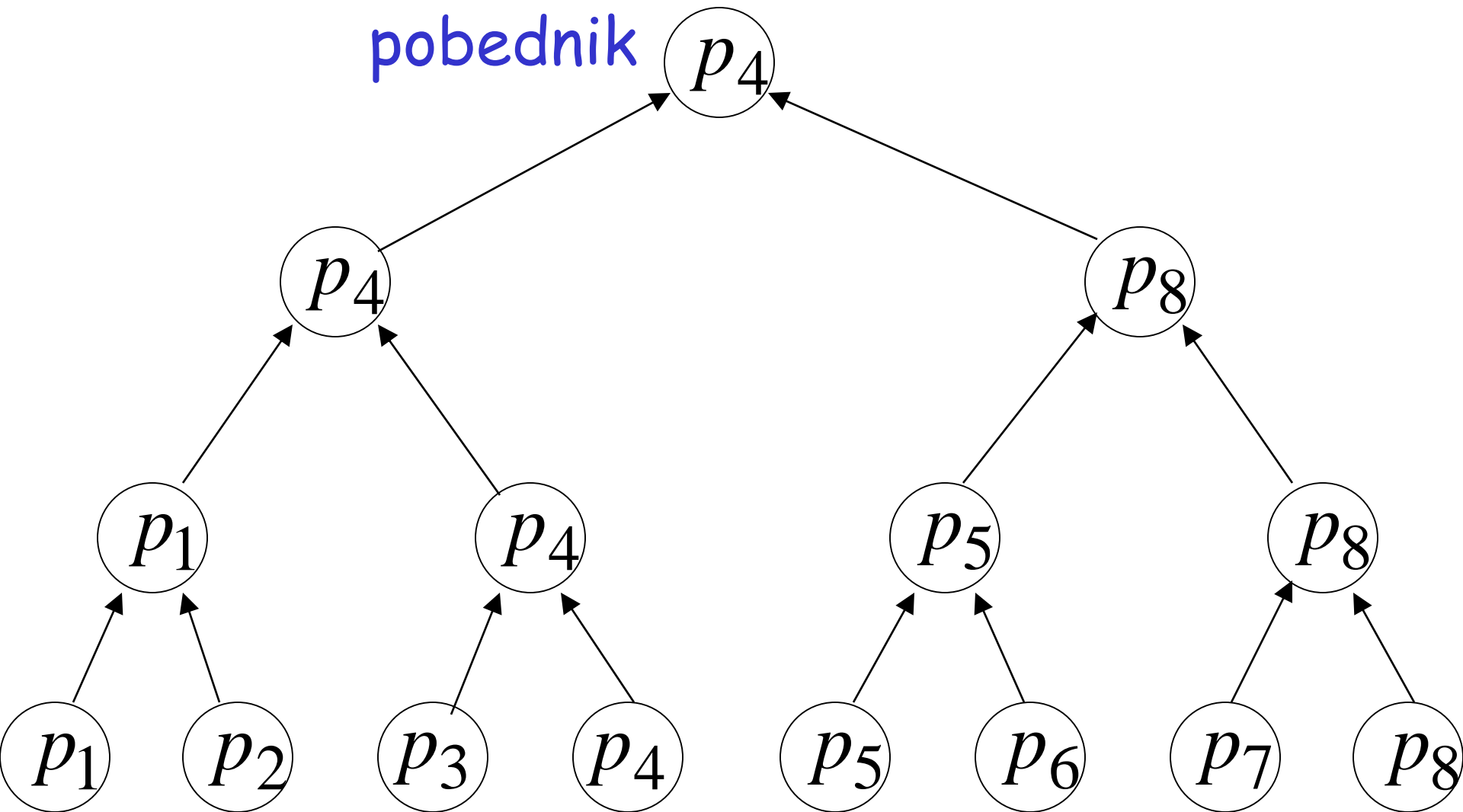
pobednik





Kritična sekcija

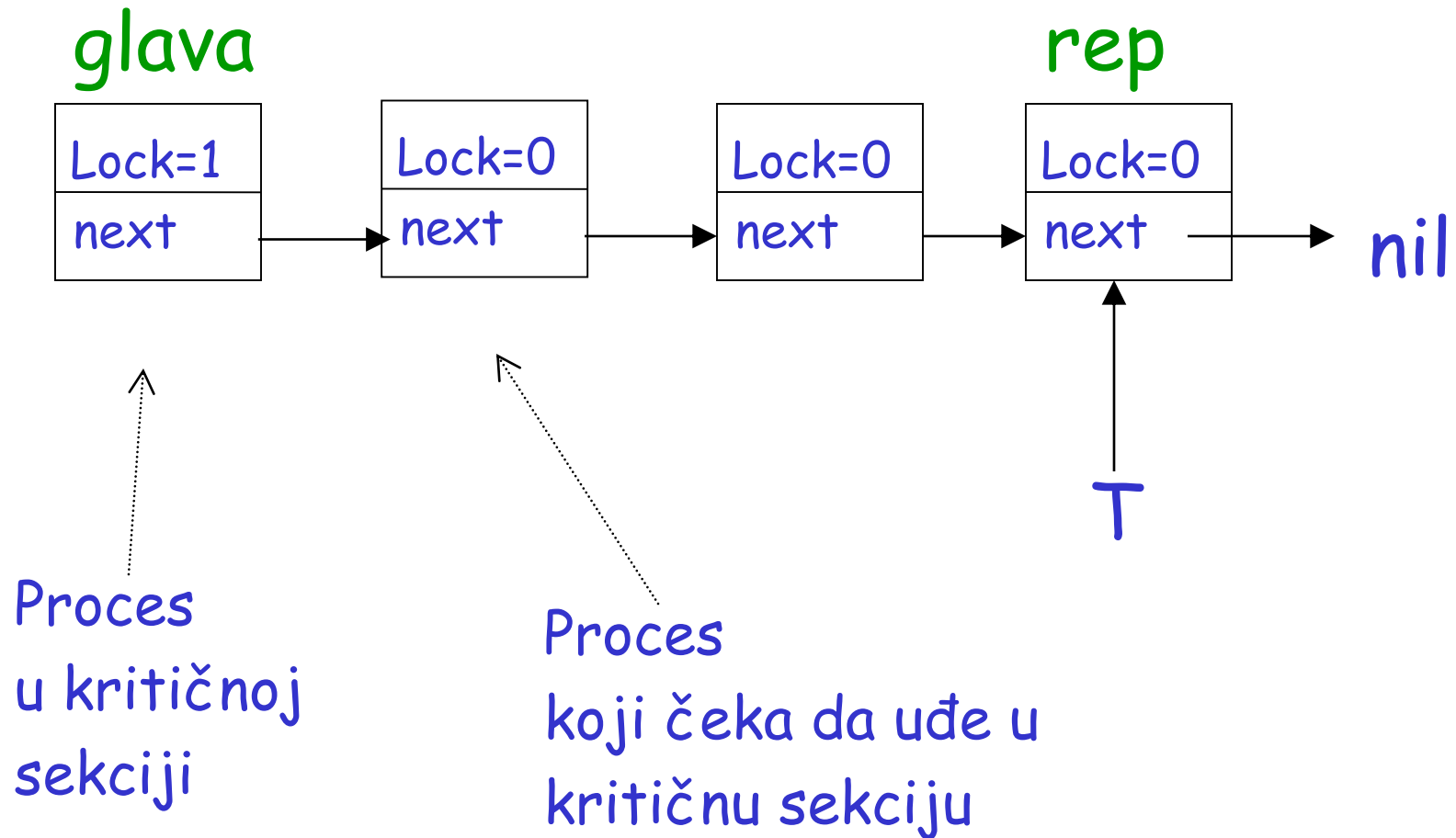
pobednik



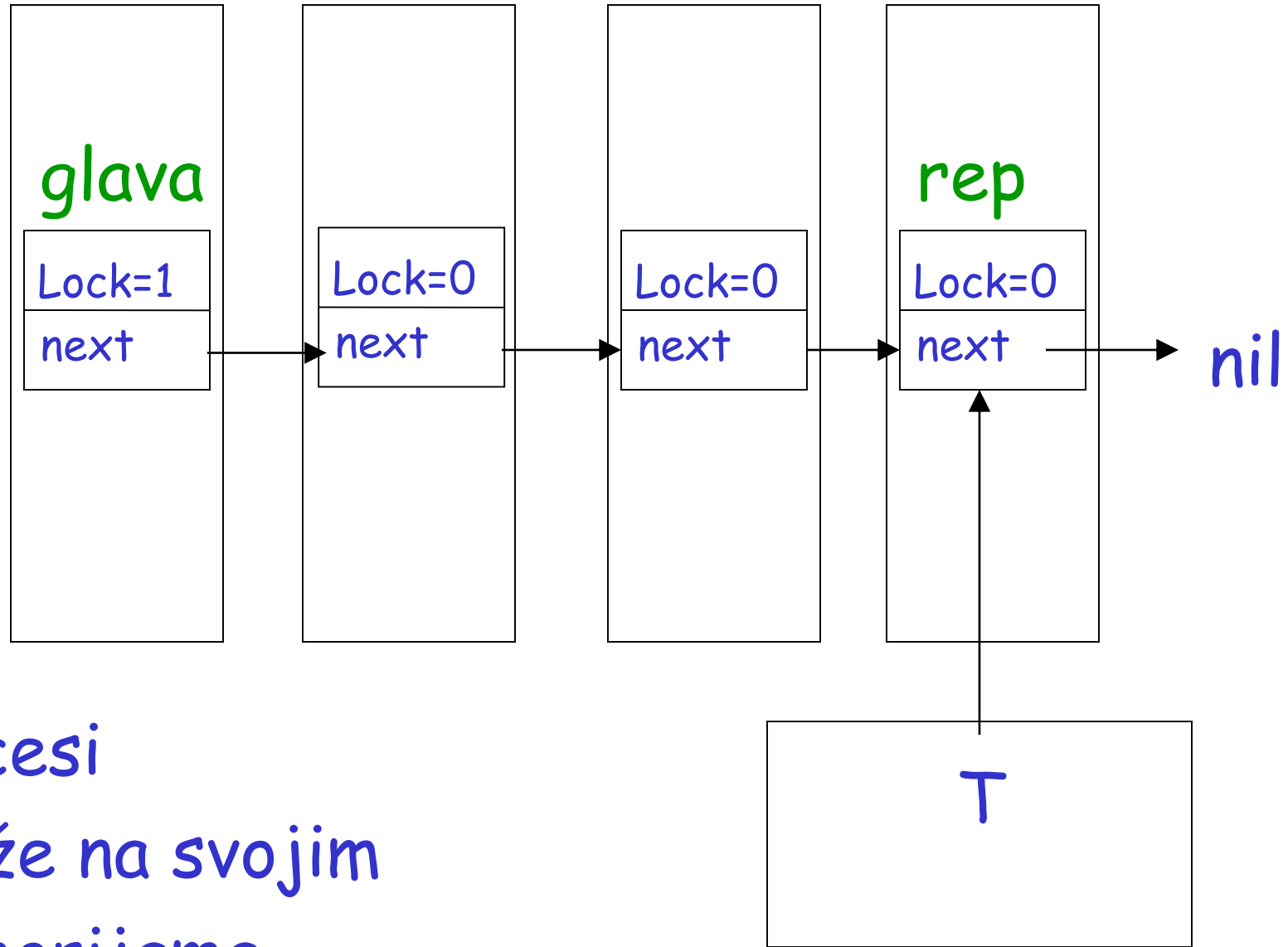
Prednosti algoritma sa turnirom

- $O(n)$ promenljivih
- Ograničene vred. promenljivih
- Nema trajnog zaključavanja
(pošto za međuso. isključivanje
para nema trajnog zaključavanja)

MCS algoritam međusobnog isključivanja

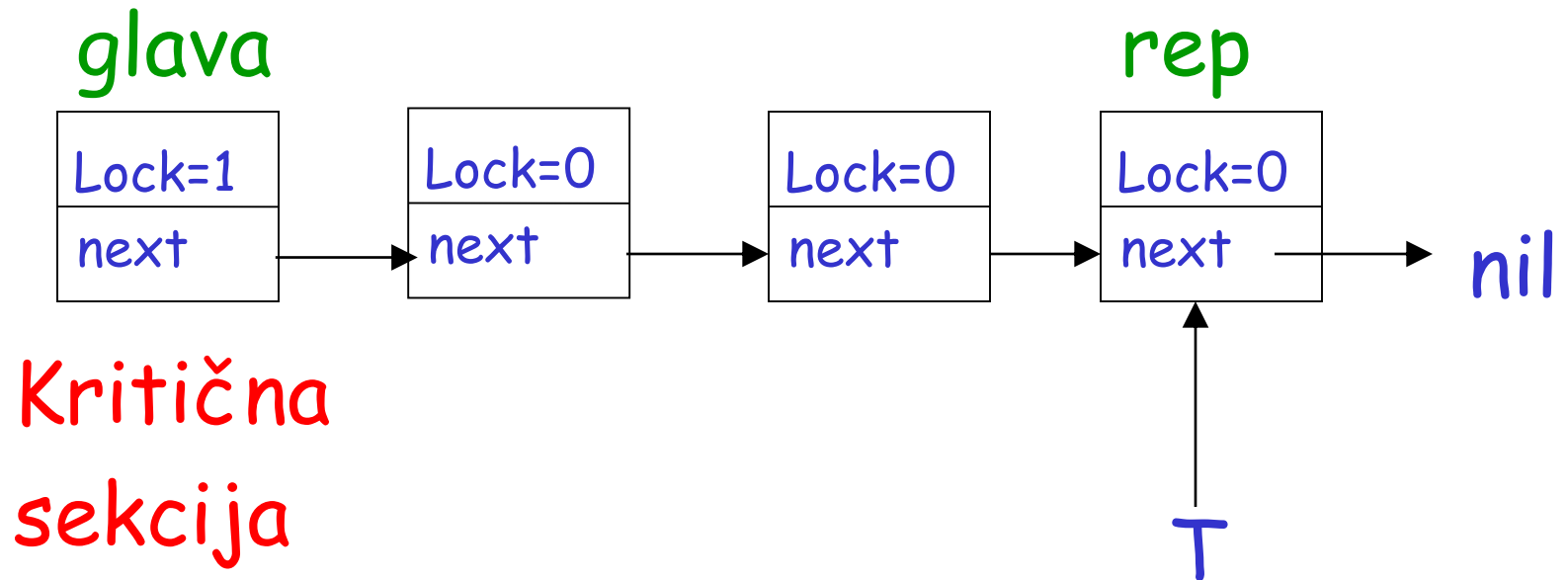


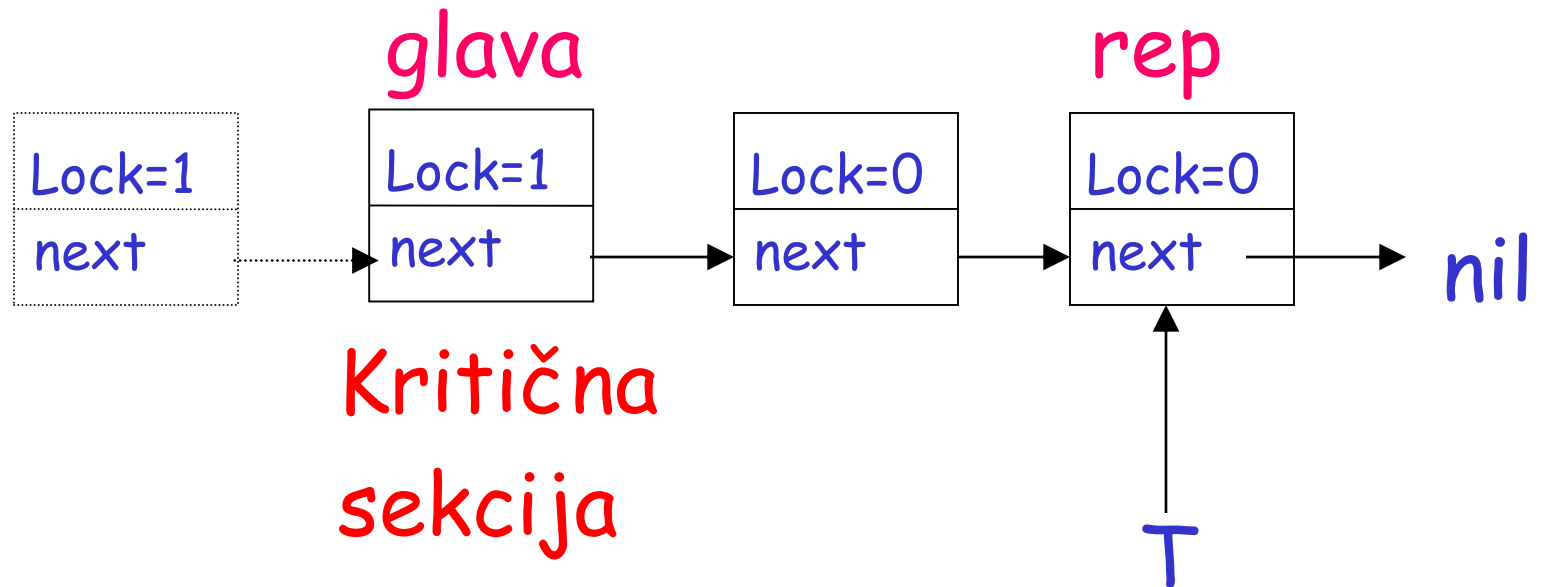
Lokalne memorije (npr. keš)

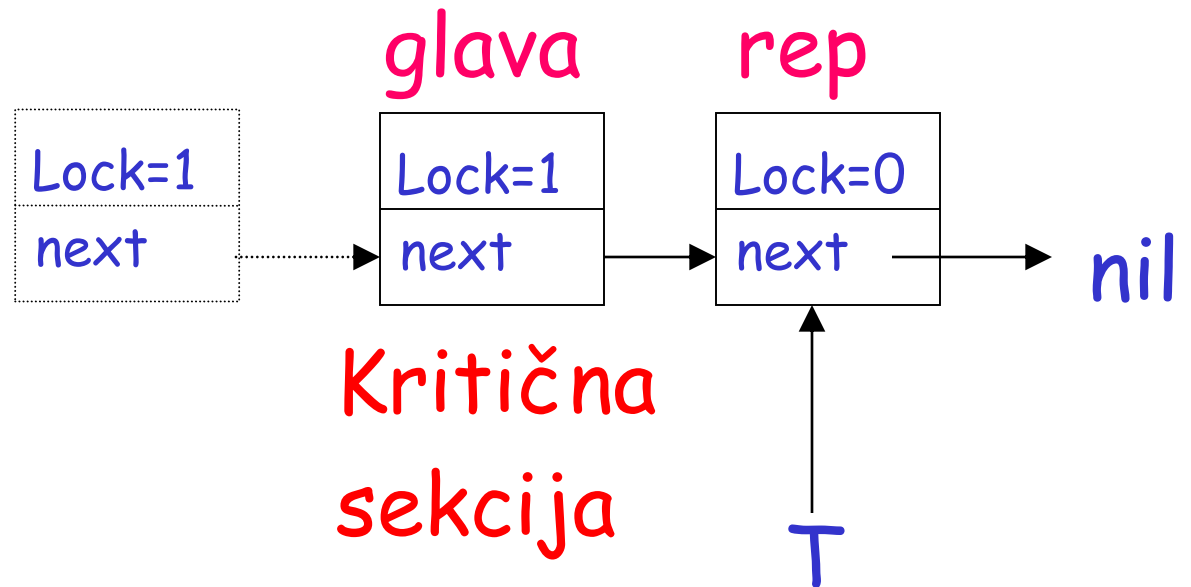


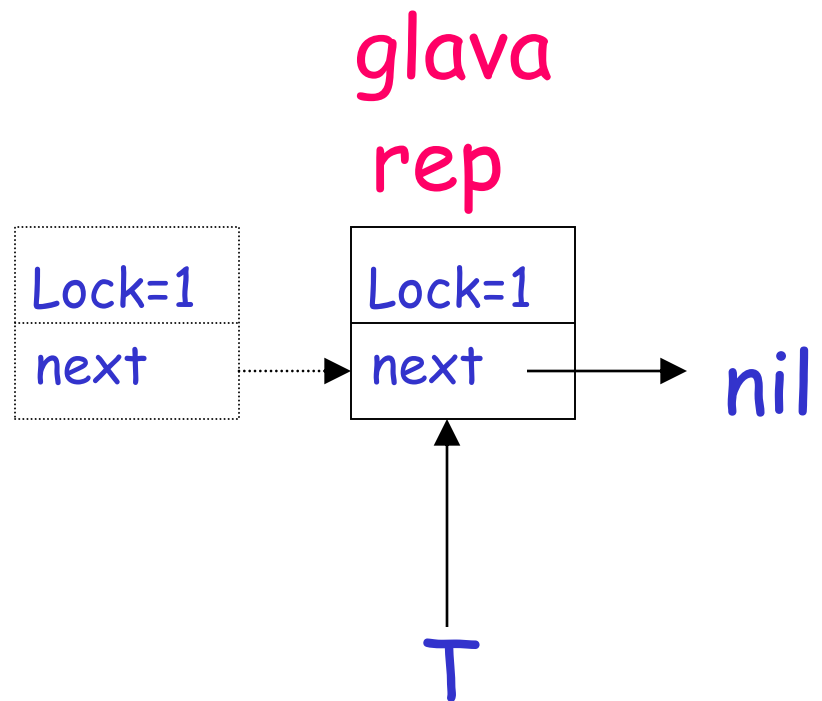
Procesi
Kruže na svojim
memorijama

Globalna deljena mem.









Kritična
sekcija

nil
↑
T

Ulazni kod za procesor i:

Qi = pokaz. na nov queue node; // Qi, *Qi je u lokalnoj mem.

Qi->Lock = 0;

Qi->Next = nil;

Ti = Swap(T, Qi); //Ti je u lokalnoj mem.

If Ti \neq nil then

 Ti -> next = Qi;

else

 Qi->Lock = 1; //on je na glavi reda

Wait until Qi->lock = 1;

Atomska operacija

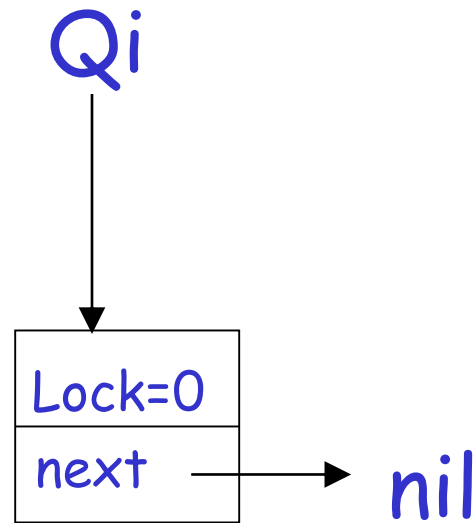
Swap(T, Qi)

{ x = T; //čitaj T

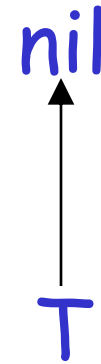
 T = Qi; // zameni T i Qi

 return x; // vrati staru vred. od T

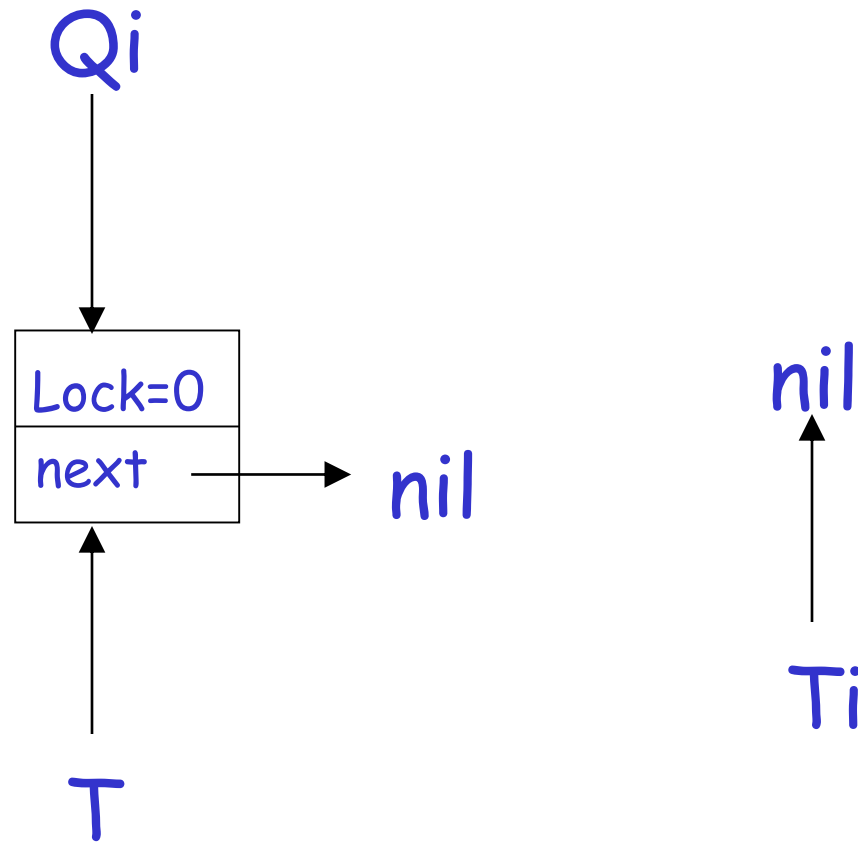
}



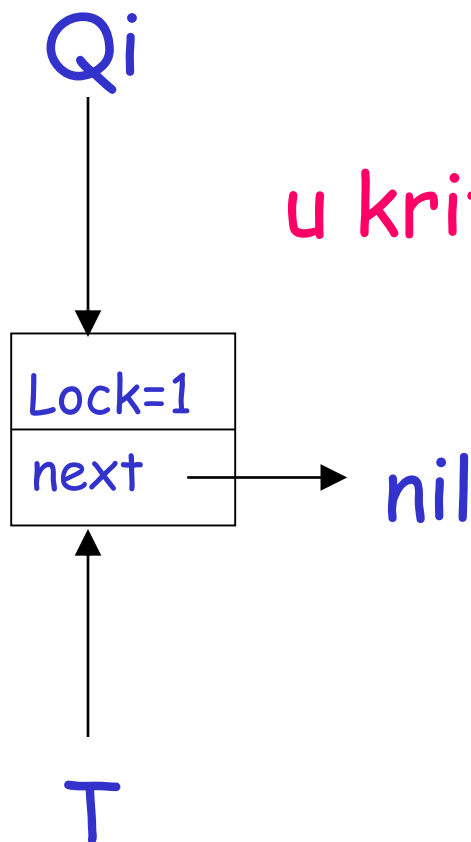
Prazan red



Qi je napravljen

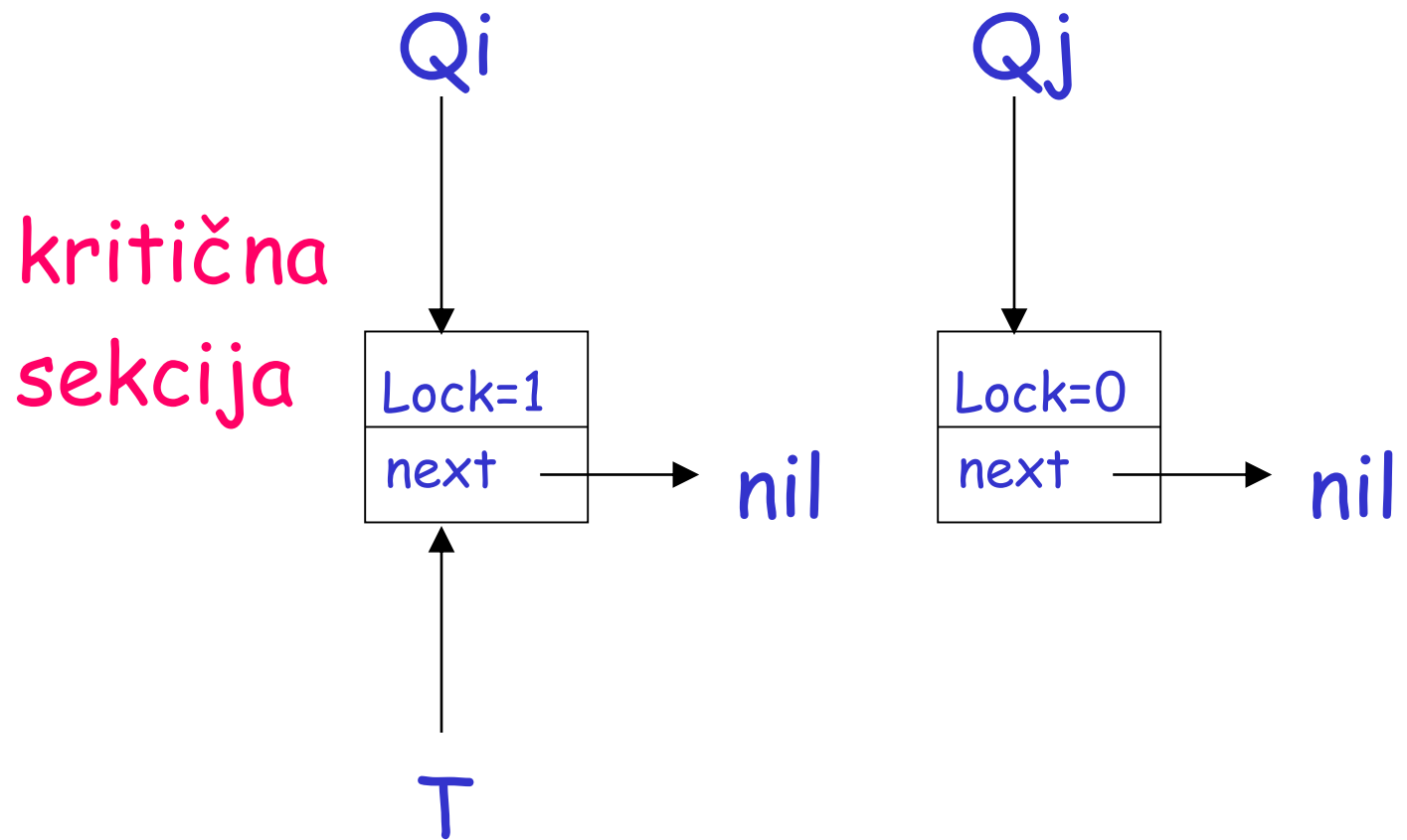


Posle operacije zamene (swap)

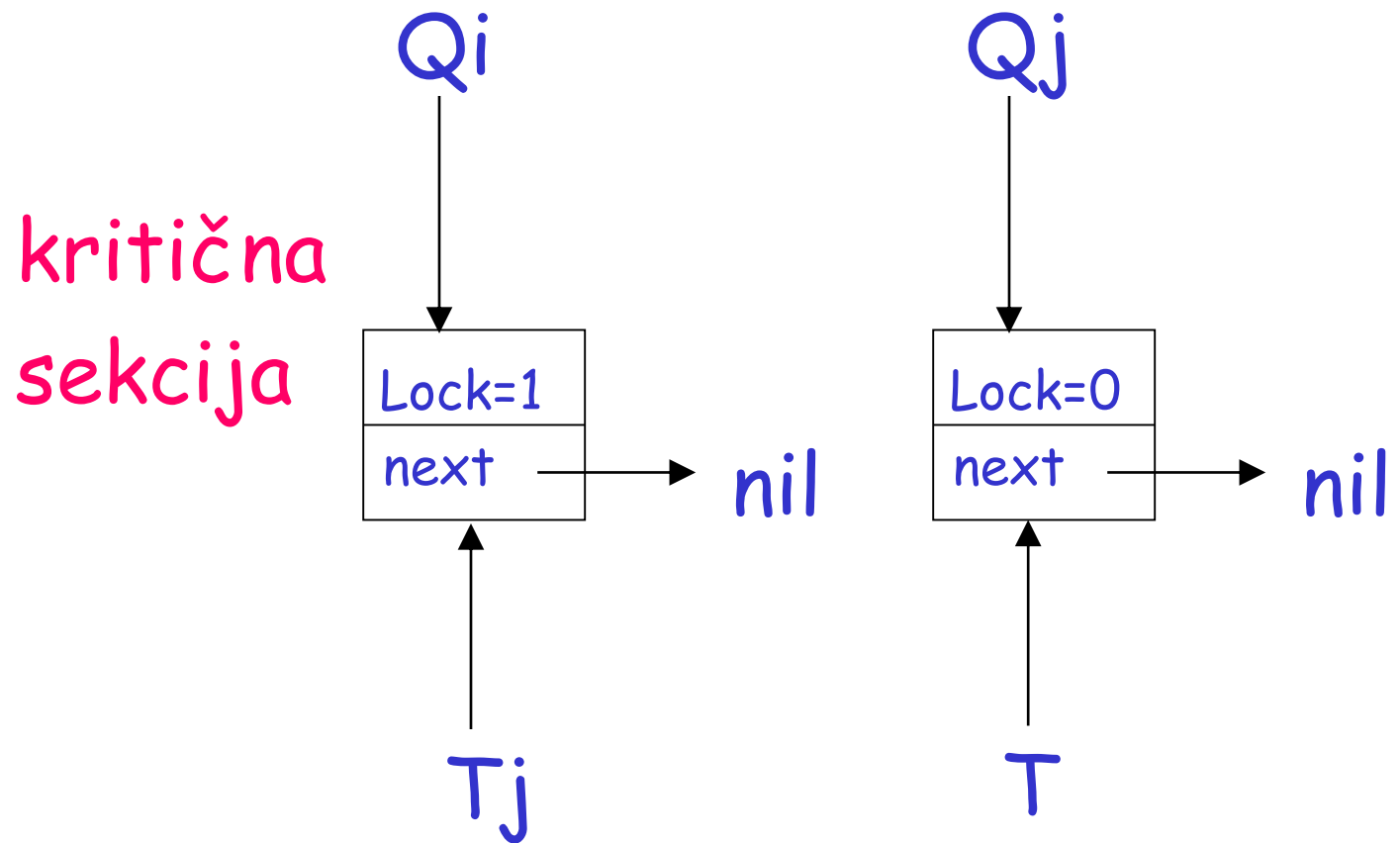


u kritičnoj sekciji

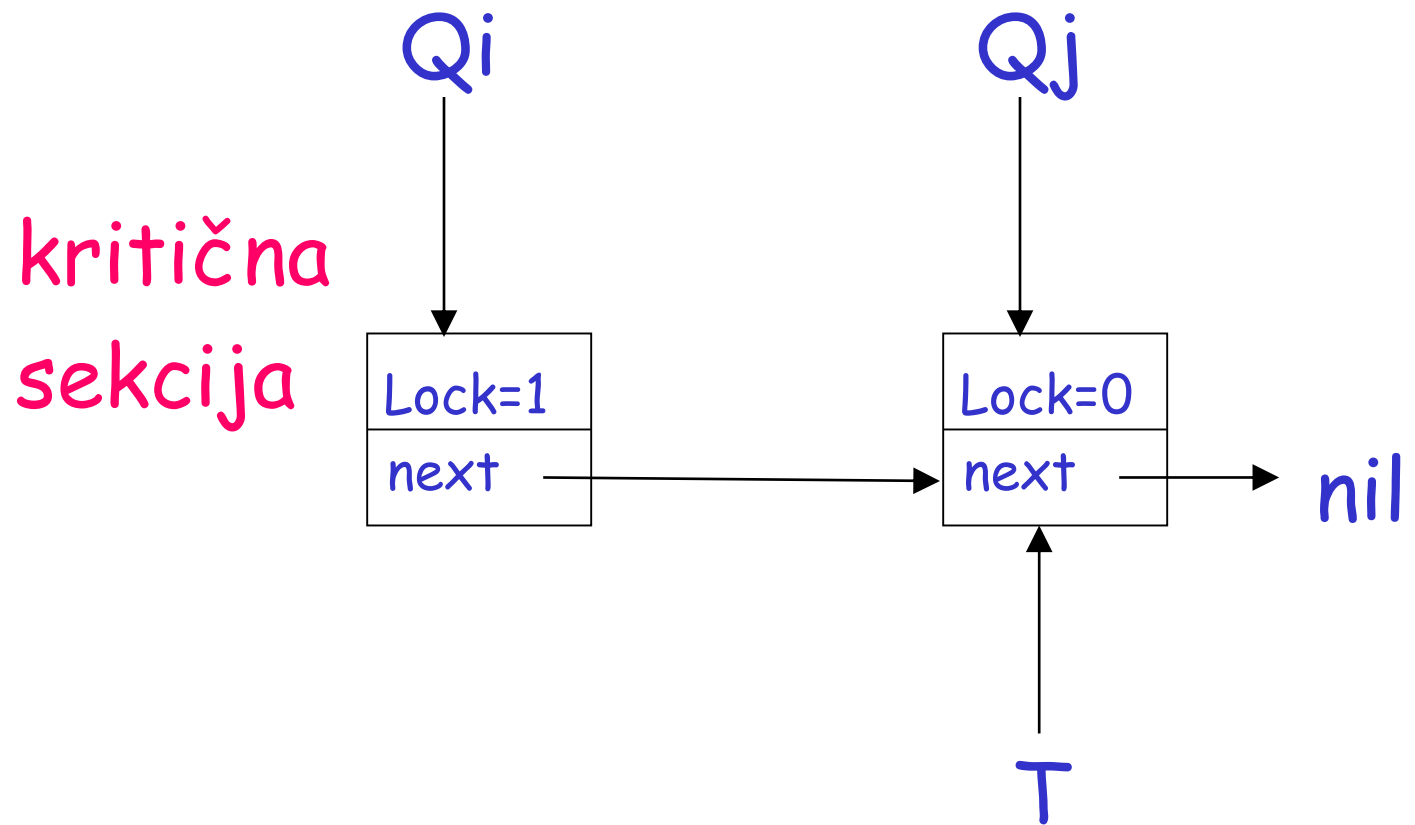
Posle iskaza if



Stiže proces j

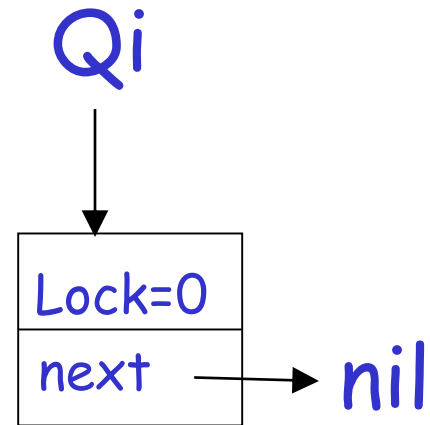


Posle operacije zamene

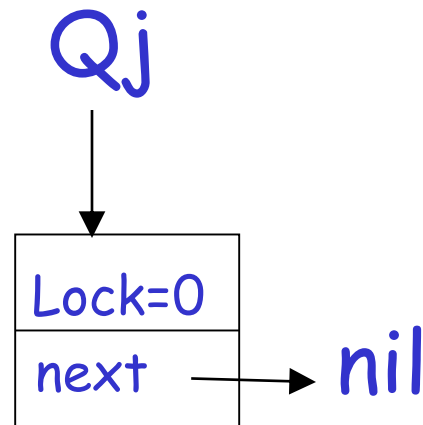
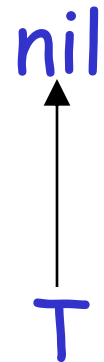


Posle operacije u iskazu if

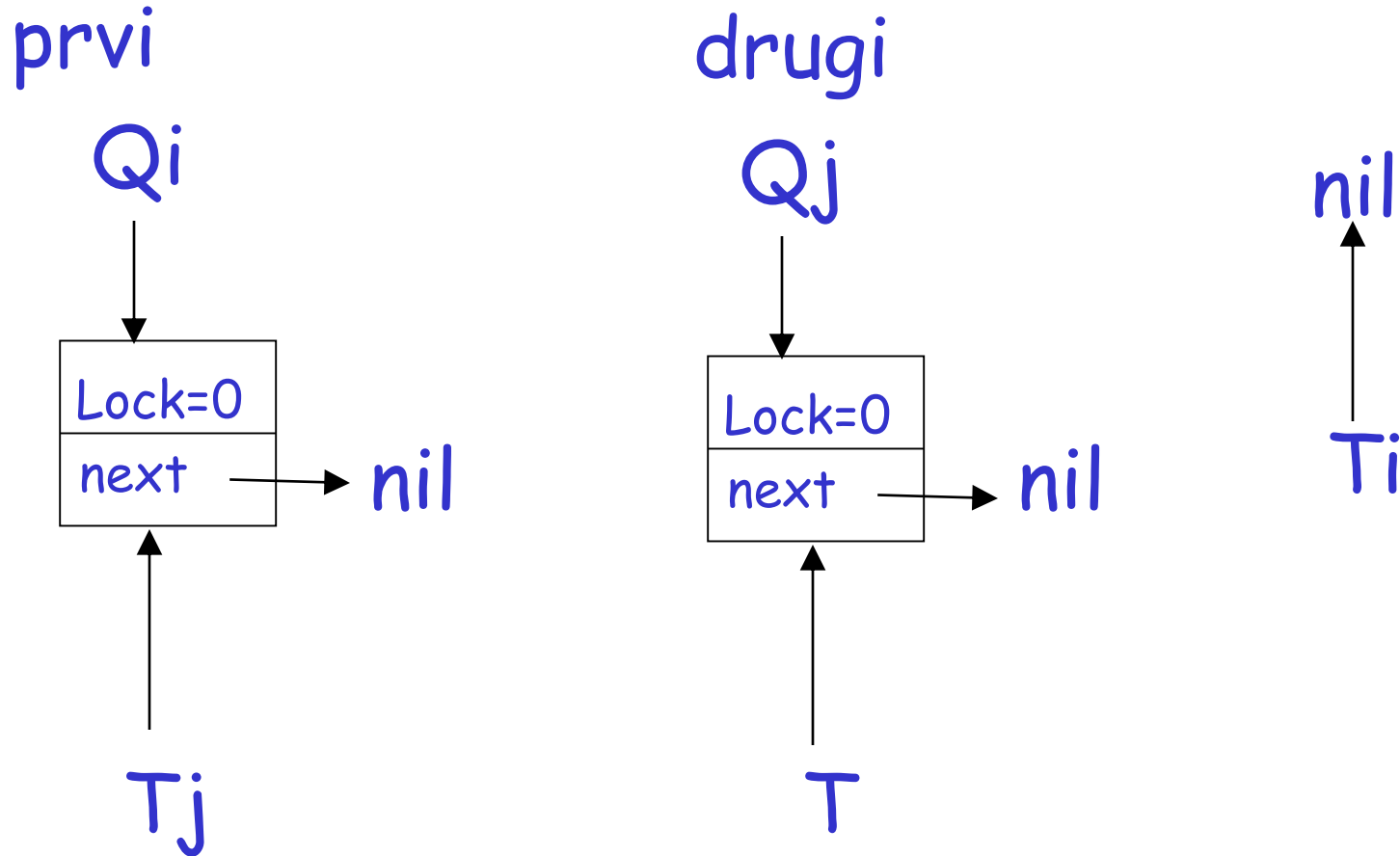
Procesi i i j
stižu simultano



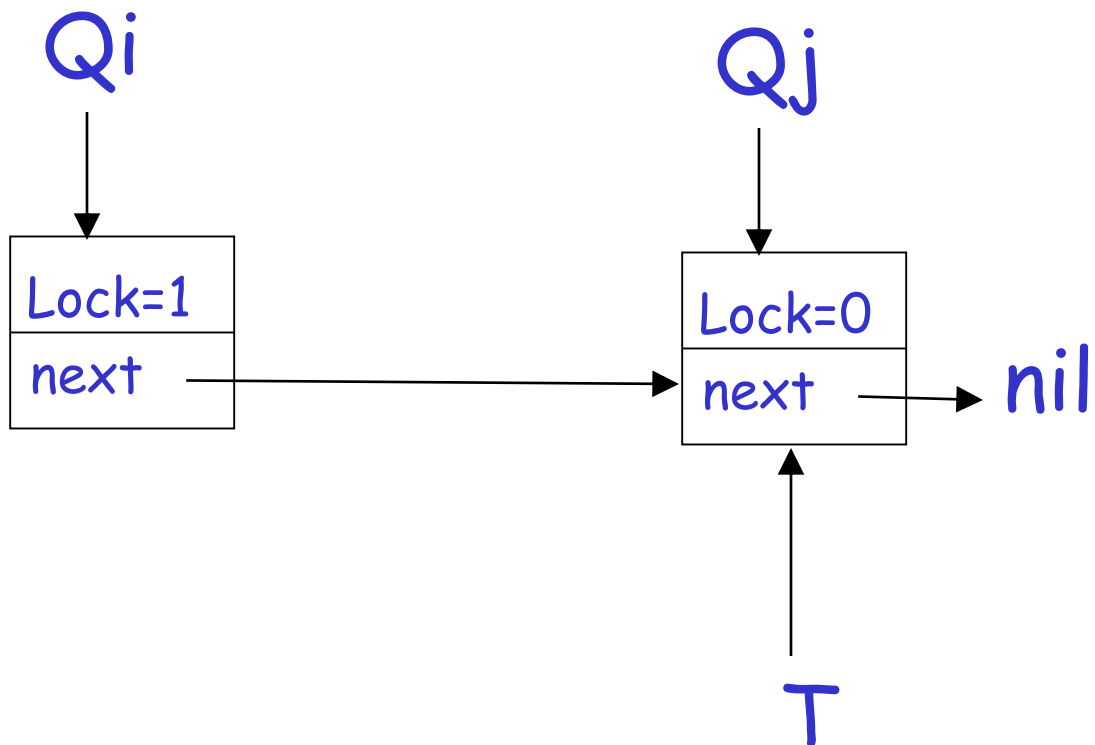
Prazan red



Izvršenje operacije zamene dodeljuje redosled



kritična sekcija



Izlazni kod za procesor i:

$T_i = \text{Compare\&Swap}(T, Q_i, \text{nil});$ // T_i je u lokalnoj mem.

If $T_i \neq Q_i$ then

\neq

 wait until $(Q_i \rightarrow \text{next} \neq \text{nil})$

$T_i \rightarrow \text{next} \rightarrow \text{lock} = 1;$

Delete Q_i and $*Q_i$

Atomska operacija

Compare&Swap(T, Qi, nil)

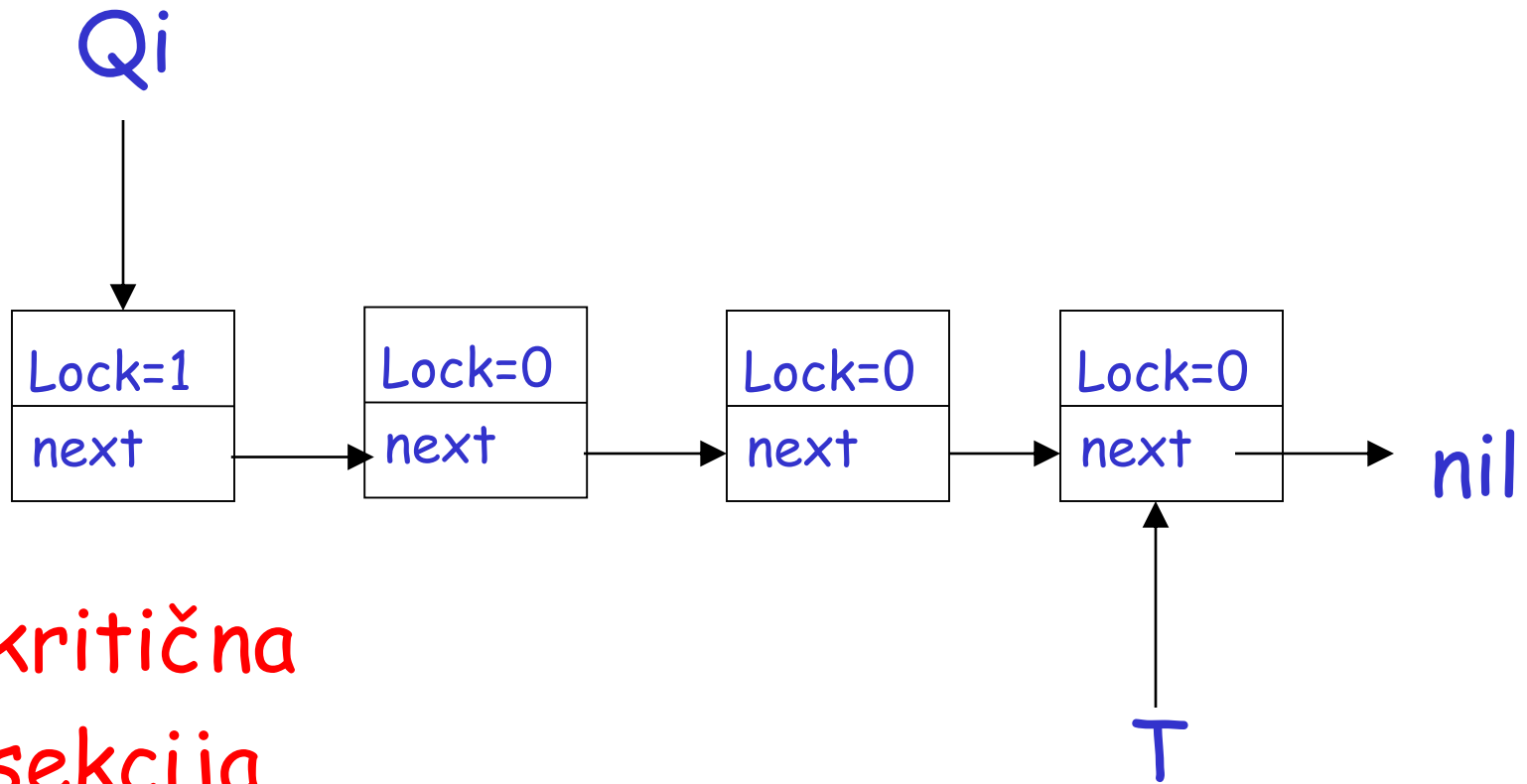
{ x = T; //čitaj vrednost T

 If T == Qi then

 T = nil; //zameni T sa nil ako su T i Qi jednaki

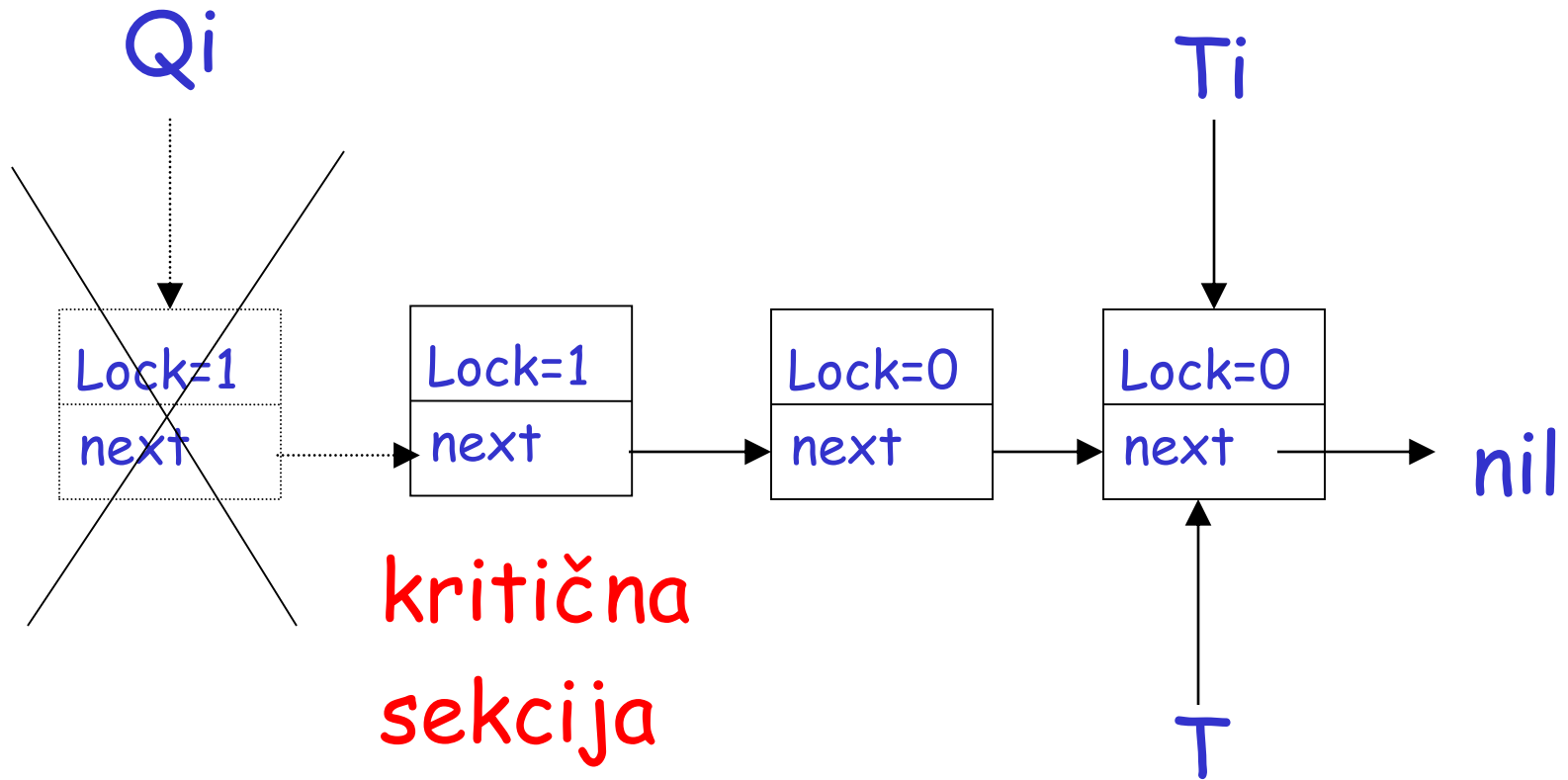
 return x; // vrati staru vrednost T

}

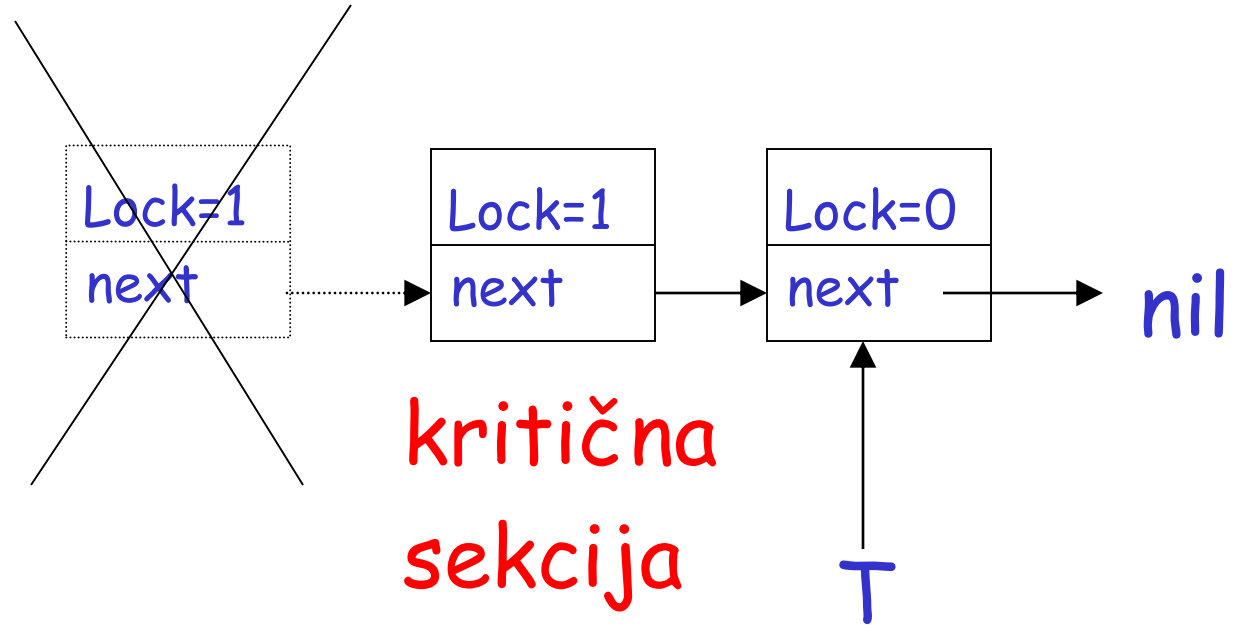


kritična
sekcija

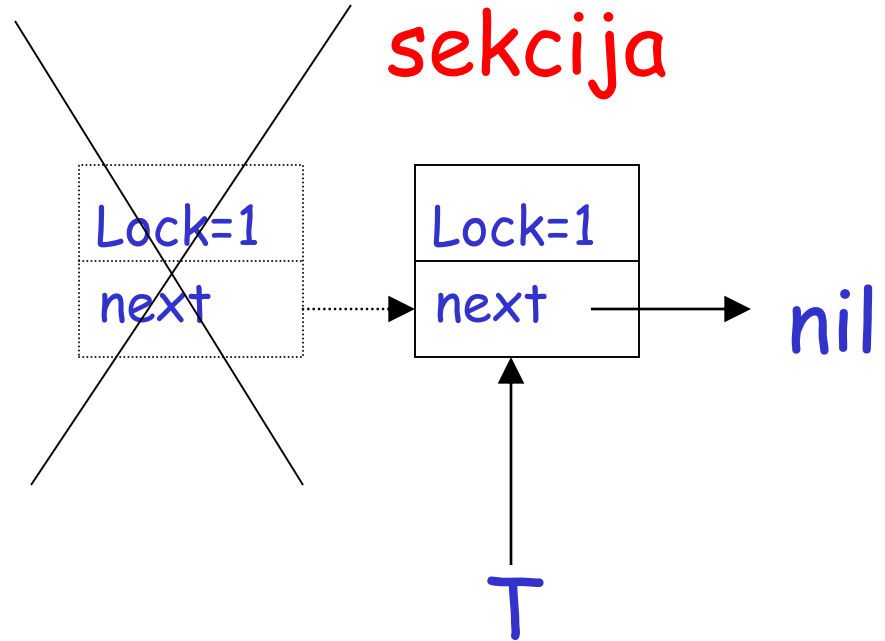
pre compare&swap



posle compare&swap

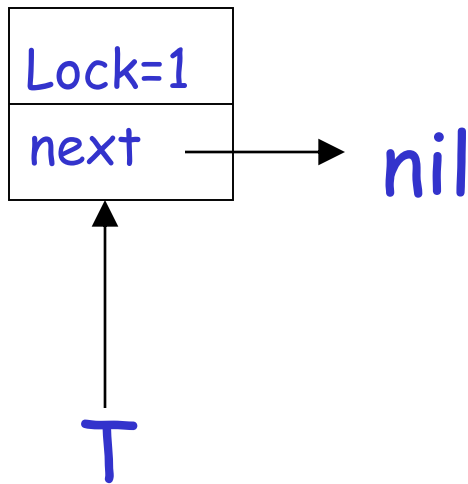


kritična
sekcija



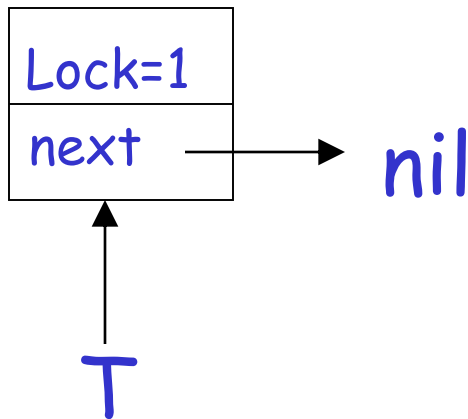
Ekstremni slučaj

kritična
sekcija



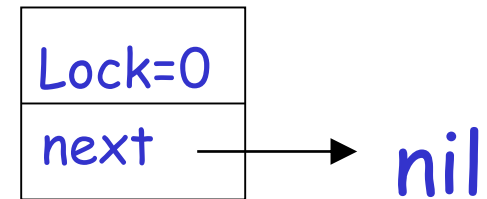
Ekstremni slučaj

kritična
sekcija



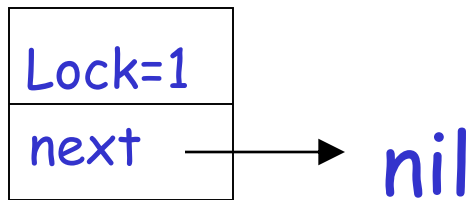
će izvršiti
compare&swap

Nov čvor
će bit umetnut

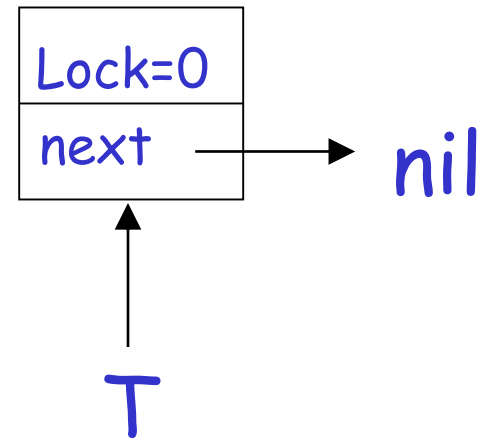


će izvršiti
swap

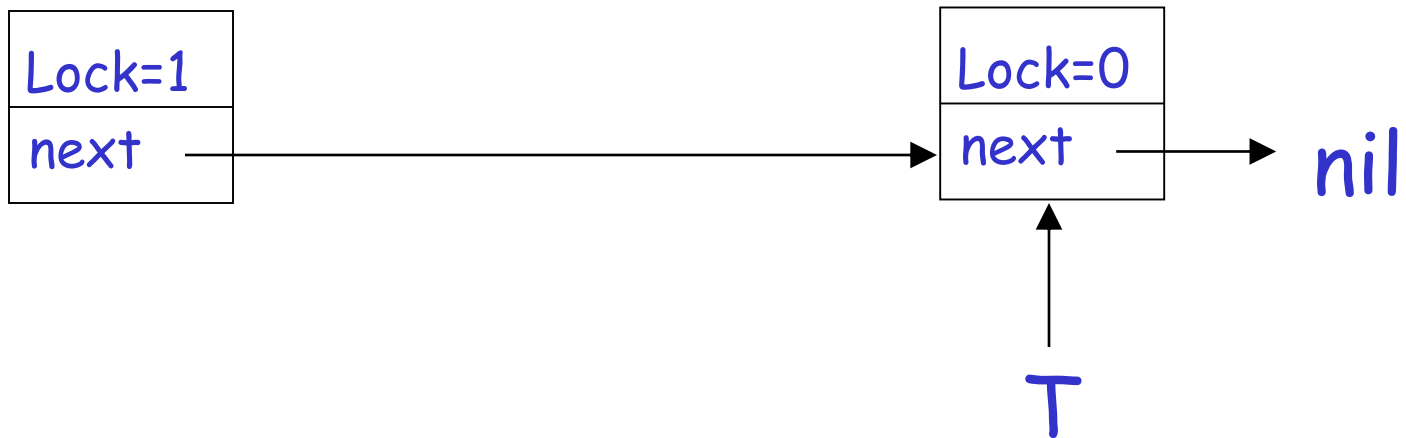
Slučaj 1: swap se izvrši prvi



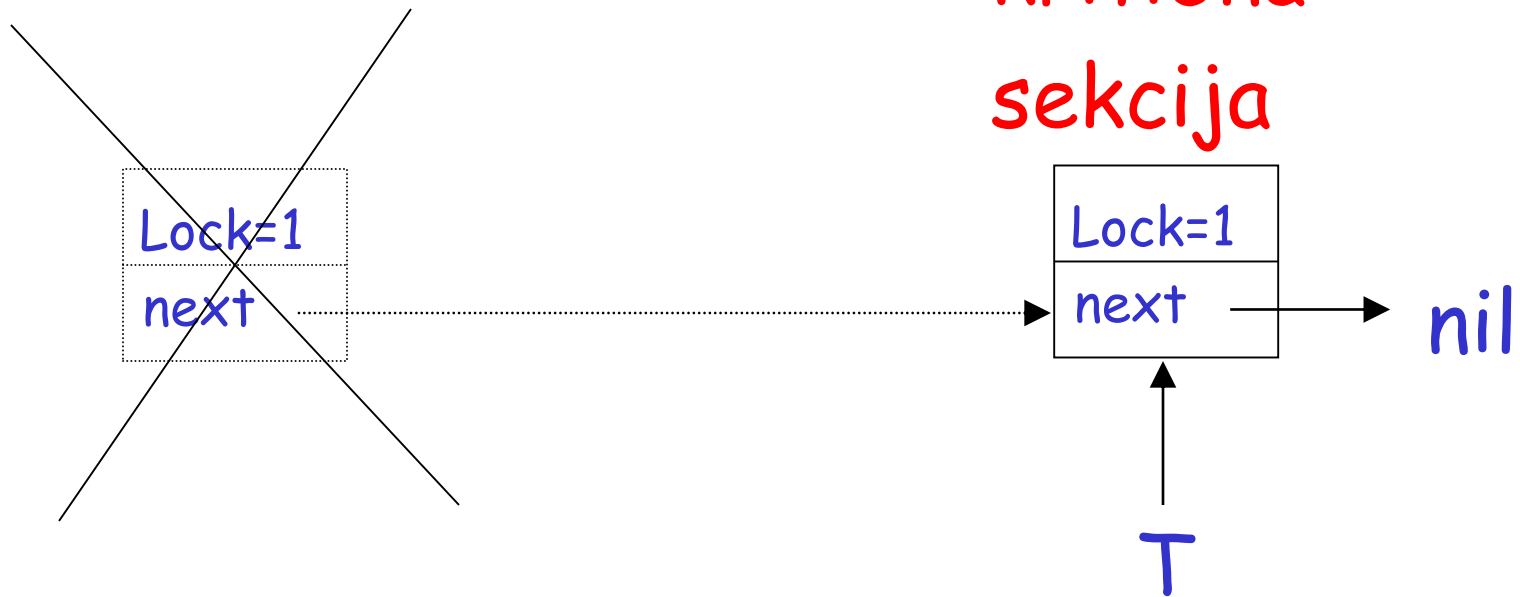
Čeka dok
next ne pokaže
na nešto



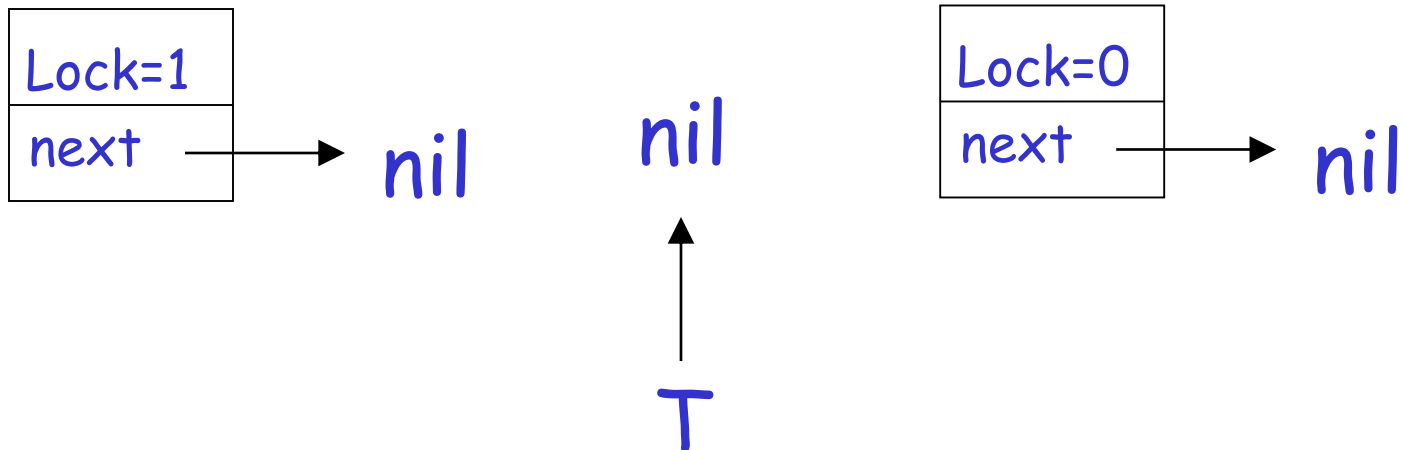
Slučaj 1: swap se izvrši prvi



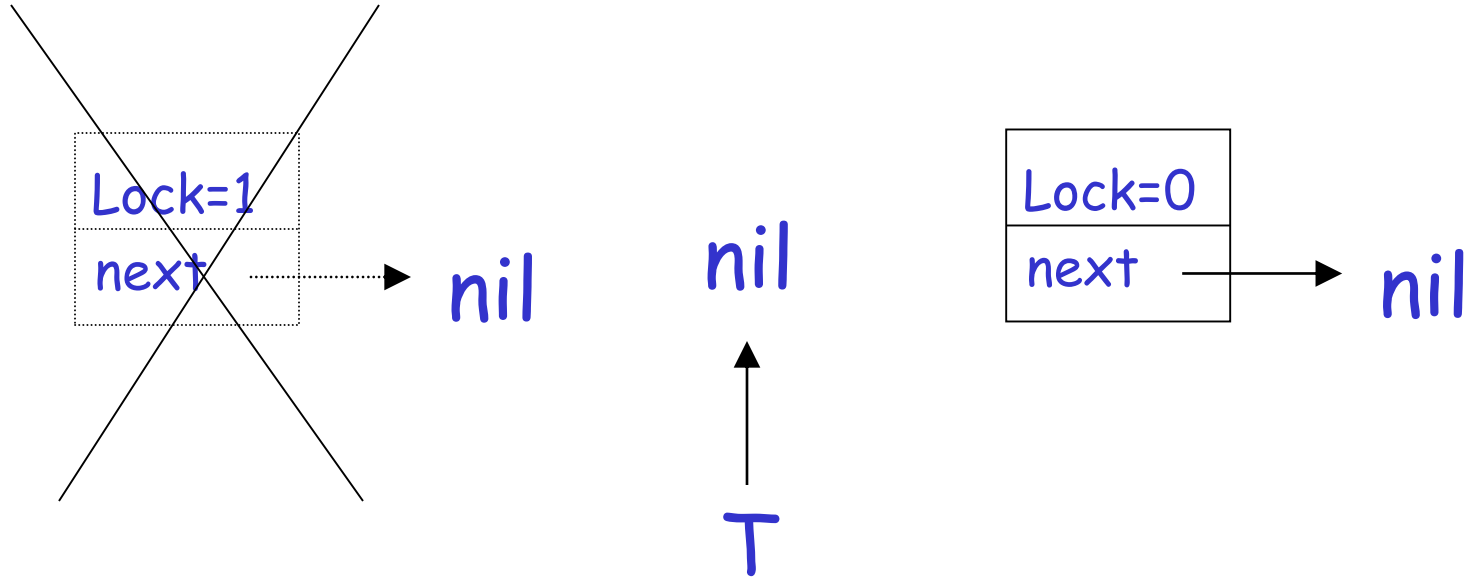
Slučaj 1: swap se izvrši prvi



Slučaj 2: compare&swap se izvrši prvi



Slučaj 2: compare&swap se izvrši prvi



Slučaj 2: compare&swap se izvrši prvi

kritična
sekcija

