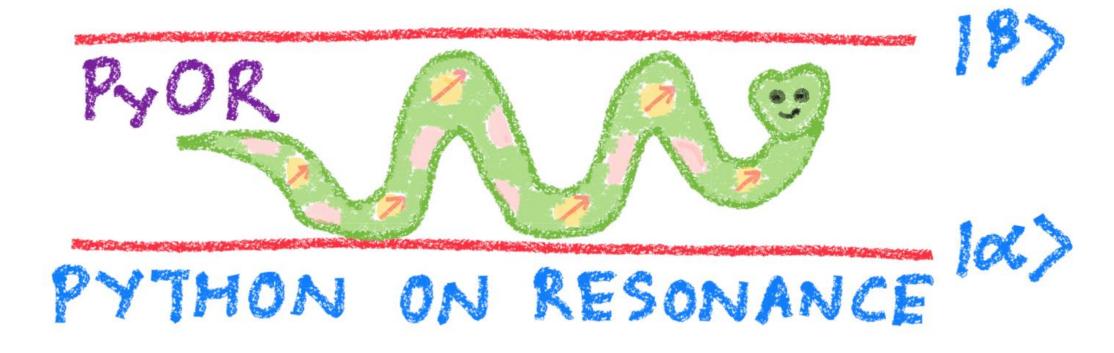
PyOR: A versatile NMR Simulator



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A notice posted outside the NMR lab at ENS, Paris

PyOR

"Everybody can simulate NMR"

Paris en résonance

Veuillez fermer cette porte à clé

lorsqu'il n'y a personne

(même pendant des pauses brèves)

- Python On Resonance
- A collection of Python functions to simulate NMR spin physics numerically (~ 2500 lines)
- Versatile: From basic to specialized NMR experiments
- <u>Beginners</u> with basic knowledge of <u>matrices</u>, <u>spin operators</u> and <u>Python</u> programming

Main Features

- Generate Spin Operators, (S_x, S_y, S_z, S₊ and S₋) for a system with any number of particles with any spin quantum number
- Generate Spherical Operator Basis for arbitrary system
- Hamiltonians: Zeeman (Lab and Rotating Frame), B1, J coupling and Dipolar Coupling
- Solve Liouville Equation in Hilbert Space or Liouville Space
 - Unitary Propagation
 - Solve ODEs
- Relaxation
 - Redfield Master Equation
 - Lindblad Master Equation
- Radiation Damping and NMR Masers (Multi-mode and J Coupling)
- <u>User can easily modify the source code according to their needs</u>

Motivations to build PyOR

• I was curious to understand "Avoided Crossing"

Representation of population exchange at level anti-crossings

Bogdan A. Rodin^{1,2} and Konstantin L. Ivanov^{1,2}

- Simulate multi-mode MASER with J-Coupling
- The driving force (catalyst) behind PyOR was my desire to escape the loneliness I experienced in academia and life.

Why reinvent the wheel?

Why develop PyOR when many NMR simulation packages are available?

- "The Pleasure of Finding Things Out"
- Deeper understanding of Spin Physics
- No black boxes
- Everything is under your control

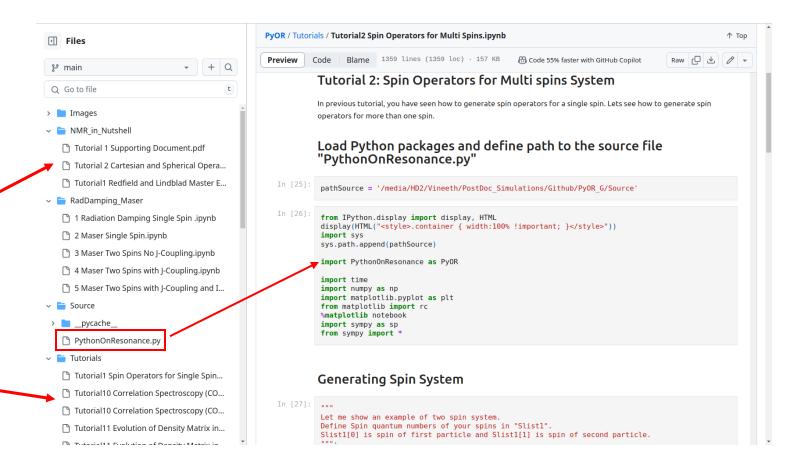


Why Python?

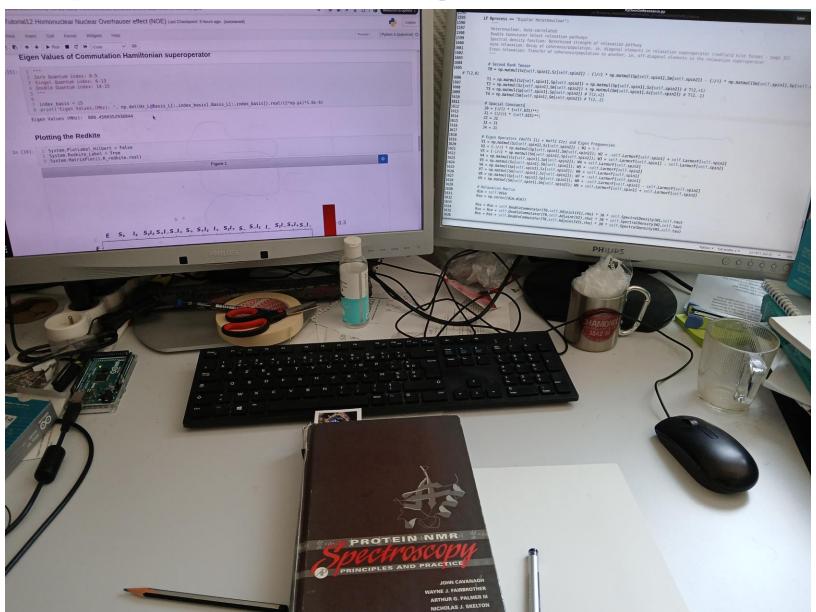
- It is free
- Easy to learn
- A lot of packages: NumPy, SciPy, SymPy, Matplotlib, ...
- Great online support

How to use PyOR?

- Install Python in your computer (I prefer Anaconda Python Distribution)
- PyOR Source code: PythonOnResonance.py
- Jupyter Notebook
- PyOR and tutorials are in the Github
 - version: Jeener-B-24.08.24
 - https://github.com/VThalakottoor/Py OR beta
 - Descriptive
 - Programming
- Modify the source code according to your need



Final requirement for PyOR: An NMR Book



Let us see how to use PyOR

First, load PyOR

Load Python packages and define path to the source file "PythonOnResonance.py"

```
pathSource = '/media/HD2/Vineeth/PostDoc Simulations/Github/PyOR v1.0/Source'
  from IPython.display import display, HTML
   display(HTML("<style>.container { width:100% !important; }</style>"))
  import sys
   sys.path.append(pathSource)
                                                                                 Enter your path here
   import PythonOnResonance as PyOR
   import time
   import numpy as np
   import matplotlib.pyplot as plt
  from matplotlib import rc
  %matplotlib notebook
   import sympy as sp
14 from sympy import *
```

Define Spin System

```
0.00
Define Spin quantum numbers of your spins
Slist1 = [2] Single Spin
0.00
Try also
Slist1 = [1/2]
Slist1 = [1]
                                  0.00
Slist1 = [3/2]
                                 Let me show an example of two spin system.
Slist1 = [2]
                                 Define Spin quantum numbers of your spins in "Slist1".
Slist1 = [5/2]
                                 Slist1[0] is spin of first particle and Slist1[1] is spin of second particle.
So on ...
                                  ини.
and compare with results in:
https://easyspin.org/easyspin/do
                                 Slist1 = [1/2,1] Multiple Spins
                                  0.00
                                 Try also
                                 Slist1 = [1/2, 1/2]
                                 Slist1 = [1/2,1]
                                 Slist1 = [1/2, 1/2, 1/2]
                                 Slist1 = [1/2, 1/2, 1/2, 1/2, 1/2, 1/2]
```

Generate Spin Operators (Heart of PyOR)

```
0.00
Define Planck constant equals 1.
Because NMR spectroscopists are more interested to write Energy in frequency units.
if False then hbarEO1 = hbar
hbarEQ1 = True
H \oplus H
Generate Spin Operators
System = PyOR.Numerical MR(Slist1, hbarEQ1
0.00
Sx, Sy and Sz Operators
Sx,Sy,Sz = System.SpinOperator()
0.00
S+ and S- Operators
Sp,Sm = System.PMoperators(Sx,Sy)
```

Documentation

```
Any PyOR functions
   help(System.SpinOperator)
Help on method SpinOperator in module PythonOnResonance:
SpinOperator() method of PythonOnResonance.Numerical_MR instance
   Generate spin operators for all spins: Sx, Sy and Sz
   INPUT
   nill
   OUTPUT
   Sx : array [Sx of spin 1, Sx of spin 2, Sx of spin 3, ...]
   Sy : array [Sy of spin 1, Sy of spin 2, Sy of spin 3, ...]
   Sz : array [Sz of spin 1, Sz of spin 2, Sz of spin 3, ...]
```

Matrix Representations

```
1 """
2 Matrix representation (Sympy)
3 In Sx[0], 0 means the index of the spin (0th spin or first spin).
4 """;
5 Matrix(Sx[0])
```

0	1.0	0	0	0	
1.0	0	1.22474487139159	0	0	
0	1.22474487139159	0	1.22474487139159	0	
0	0	1.22474487139159	0	1.0	
0	0	0	1.0	0	

1 Matrix(Sy[0])

```
 \begin{bmatrix} 0 & -1.0i & 0 & 0 & 0 \\ 1.0i & 0 & -1.22474487139159i & 0 & 0 \\ 0 & 1.22474487139159i & 0 & -1.22474487139159i & 0 \\ 0 & 0 & 1.22474487139159i & 0 & -1.0i \\ 0 & 0 & 0 & 1.0i & 0 \end{bmatrix}
```

1 Matrix(Sz[0])

```
    2.0
    0
    0
    0
    0

    0
    1.0
    0
    0
    0

    0
    0
    0
    0
    0

    0
    0
    0
    -1.0
    0

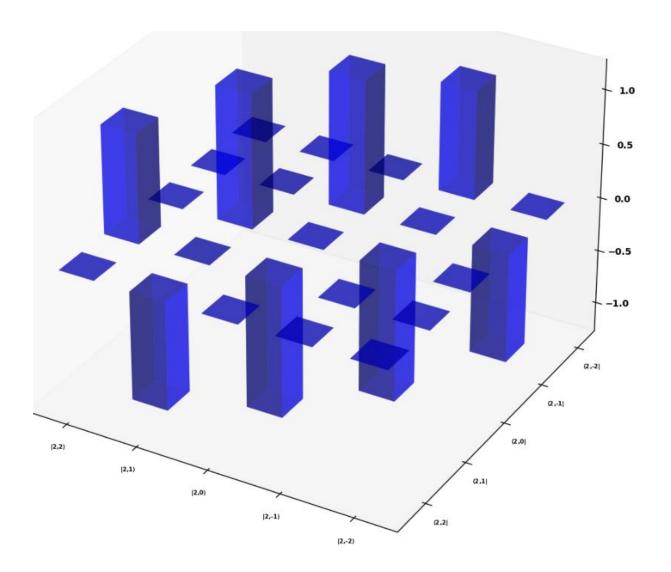
    0
    0
    0
    0
    -2.0
```

```
1 """
2 Matrix representation (Sympy)
3 In Sx[0], 0 means the index of the first spin.
4 And Sx[1], 1 means the index of the second spin.
5 """;
6 Matrix(Sz[0]) # Spin operator Sz of first spin
```

```
\begin{bmatrix} 0.5 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0.5 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0.5 & 0 & 0 & 0 \\ 0 & 0 & 0 & -0.5 & 0 & 0 \\ 0 & 0 & 0 & 0 & -0.5 & 0 \\ 0 & 0 & 0 & 0 & 0 & -0.5 \end{bmatrix}
```

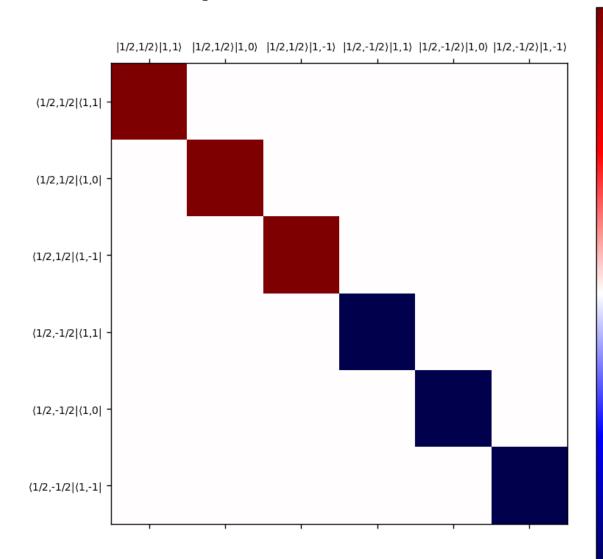
1 Matrix(Sz[1]) # Spin operator Sz of second spin

Matrix Representations



System.MatrixPlot3D(2,Sy[0].imag)

Matrix Representations



System.MatrixPlot(1,Sz[0].real)

0.4

0.2

- 0.0

- -0.2

Pre-defined Constants

```
1 print("Planck constant, h = ",System.pl)
 2 print("Planck constant, hbar = ",System.hbar)
 3 print("Permittivity of free space = ",System.ep0)
 4 print("Permeability of free space = ",System.mu0)
 5 print("Boltzmann constant = ",System.kb)
Planck constant, h = 6.626e-34
Planck constant, hbar = 1.054e-34
Permitivity of free space = 8.854e-12
Permeability of free space = 1.2566370614359173e-06
Boltzmann constant = 1.38e-23
 1 print("Gyromagnetic ratio, electron = ",System.gammaE)
 2 print("Gyromagnetic ratio, H1 = ",System.gammaH1)
   print("Gyromagnetic ratio, C13 = ",System.gammaC13)
    11 11 11
   and gyromagnetic ratio of N14, N15, O17 and F19
Gyromagnetic ratio, electron = -1761000000000.0
Gyromagnetic ratio, H1 = 267522000.0
Gyromagnetic ratio, C13 = 67282800.0
```

Zeeman Hamiltonian (Lab Frame)

```
H \oplus H
   Gyromagnetic Ratio
   Gamma = [Gyromagnetic Ratio spin 1, Gyromagnetic Ratio spin 1, ...]
   Gamma = [System.gammaH1]
   11 11 11
   Define the field of the spectromter, B0 in Tesla.
   B0 = 9.4
   Define the chemical Shift of individual spins
   Offset = [chemical Shift spin 1, chemical Shift spin 1, ...]
   Offset = [20] # Offset frequency in Hz
17
   Function "LarmorF" give the list Larmor frequencies of individual spins in lab frame
   LarmorF = System.LarmorFrequency(Gamma, B0, Offset)
```

Larmor Frequency in MHz: [-400.22803765]

Hamiltonian

1 Hz = System.Zeeman(LarmorF,Sz)

Zeeman Hamiltonian (Rotating Frame)

```
"""
2  "OmegaRF" is list of rotating frame frequencies
""";
4  OmegaRF = [-System.gammaH1*B0]
5  """
7  Hamiltonian in the rotating frame
""";
9  Hzr = System.Zeeman_RotFrame(LarmorF, Sz, OmegaRF)
```

B1 Hamiltonian

```
0.00
   So we have a spin half particle sitting at static magnetic
  When a RF field is applied the magnetic dipole of the spin
   The energy of the particle in this case is given by B1 Fie
   11 11 11
   List of RF amplitude (Hz) or Nutation frequency, "Omegal"
   Omega1 = [100] # Hz
11
12
   List of RF signal phase in degree
14
   OmegalPhase = [0] # deg
16
17
   \Pi \cdot \Pi \cdot \Pi
   B1 field hamiltonian
19
20 HzB1 = System.Zeeman B1(Sx,Sy,Omega1,Omega1Phase)
```

J Coupling Hamiltonian

```
Define J Coupling between each spins, Jlist[0][3] means J coupling between 1st spin and 4th spin.

Jlist = np.zeros((len(Slist1),len(Slist1)))

Jlist[0][3] = 7

Jlist[0][4] = 7

Jlist[1][3] = 7

Jlist[1][4] = 7

Jlist[2][3] = 7

Jlist[2][4] = 7

Jlist[2][4] = 7

Jlist[3][5] = 5

Jlist[4][5] = 5

Hj = System.Jcoupling(Jlist,Sx,Sy,Sz)
```

```
Define J Coupling between each spins, Jlist[6]

Jlist = np.zeros((len(Slist1),len(Slist1)))
Jlist[0][1] = 150

Weak

Hj = System.Jcoupling_Weak(Jlist,Sz)
```

Initialize Density Matrix

2 We will generate Initial Density Matrix in two ways:

0.00

```
First we will generate a density matrix as we prefer say, Sz.
   Second we will create density matrix at thermal equlibrium
   First Case
   Thermal DensMatrix = False
                                                     H \oplus H
10
                                                     Second Case: Initial Desnity Matrix at Thermal Equlibrium
   if Thermal DensMatrix:
       Hz EnUnit = System.Convert FregUnitsTOEn
       HT approx = False # High Temperature App
                                                     Thermal DensMatrix = True
14
       T = 300 # Temperature in Kelvin
15
       rho in = System.EqulibriumDensityMatrix(
                                                     if Thermal DensMatrix:
        rhoeq = rho in.copy()
16
17
   else:
                                                         Hz EnUnit = System.Convert FreqUnitsTOEnergy(Hz)
18
       rho in = np.sum(Sz,axis=0) # Initial Den
                                                         HT approx = False # High Temperature Approximation is False
        rhoeq = np.sum(Sz,axis=0) # Equlibrium
19
                                                         T = 1.2 # Temperature in Kelvin
        print("Trace of density metrix = ", np.t
                                                         rho in = System.EqulibriumDensityMatrix(Hz EnUnit,T,HT approx)
                                                         rhoeq = rho in.copy()
Trace of density metrix = 0i
                                                     else:
                                                 14
                                                         rho in = np.sum(Sz,axis=0) # Initial Density Matrix
                                                 15
                                                         rhoeg = np.sum(Sz,axis=0) # Equlibrium Density Matrix
```

16

print("Trace of density metrix = ", np.trace(rho in))

Liouville-von Neumann Equation

Hilbert Space

$$rac{d}{dt}
ho = rac{-i}{\hbar}[H_0,
ho]$$

$$ho(t)=e^{iH_0t}
ho(0)e^{-iH_0t}$$

$$ho = egin{bmatrix}
ho_{11} &
ho_{12} &
ho_{13} &
ho_{14} \
ho_{21} &
ho_{22} &
ho_{23} &
ho_{24} \
ho_{31} &
ho_{32} &
ho_{33} &
ho_{34} \
ho_{41} &
ho_{42} &
ho_{43} &
ho_{44} \end{bmatrix}$$

Liouville Space

$$rac{d}{dt} ilde{
ho}=rac{-i}{\hbar}\hat{H}_0 ilde{
ho}$$

Liouville Space
$$\frac{d}{dt}\tilde{\rho} = \frac{-i}{\hbar}\hat{H}_0\tilde{\rho}$$

$$\tilde{\rho} = \begin{bmatrix} \rho_{11} \\ \rho_{12} \\ \rho_{13} \\ \rho_{14} \\ \rho_{21} \\ \vdots \\ \rho_{44} \end{bmatrix}$$

$$\frac{d}{dt}\tilde{\rho} = \frac{-i}{\hbar}(H_0\otimes\mathbb{1}-\mathbb{1}\otimes H_0^T)\tilde{\rho}$$

$$\tilde{\rho}$$

$$ilde{
ho}(t)=e^{-i\hat{H}_0t} ilde{
ho}(0)$$

$$ho_{11}$$

$$\rho_{12}$$

$$ho_{13}$$

$$\rho_{14}$$

$$\rho_{21}$$

$$ho_{44}$$

Basis Operators (Example: 3 Three spin half) (Irreducible spherical tensor Operators)

An arbitrary square matrix of dimension $(2s + 1) \times (2s + 1)$, A can be written as linear combination of spherical tensor operators:

```
A = \sum_{k=0}^{2s} \sum_{q=-k}^{k} a_{q}^{k} T_{q}^{k}, where a_{q}^{k} = Tr[(T_{q}^{k})^{\dagger} A]
```

LM state: [(0, 0), (1, -1), (1, 0), (1, 1)]

```
1 """
2 Spherical Operator Basis for single spin half particle
3 let S = 1/2
4 """;
5 pol_basis_half, Coherence_order, LM_state = System.Spherical_OpBasis(1/2)
Coherence Order: [0, -1, 0, 1]
```

Basis Operators (Example: 3 Three spin half)

```
2 First make product operator basis for two spin half particle and then with the third, Spin 1 -> I, Spin 2 -> S and Spin 3 -> R
 5 Coh order = [0, -1, 0, 1]
 6 Dic 1 = ["E1 ","Im ","Iz ","Ip "]
 7 Dic 2 = ["E2 ","Sm ","Sz ","Sp "]
 8 Dic 3 = ["E3 ","Rm ","Rz ","Rp "]
11 Sorting options: 'normal', 'negative to positive', 'zero to high'
13
14 | sort = 'negative to positive'
15 indexing = False
product basis 2half, Coh order 2, Dic 2 = System.ProductOperator(pol basis half,Coh order,Dic 1,pol basis half,Coh order,Dic 2,sort,in
 1 print("Coherence order (Two spin half particles): ", Coh order 2)
Coherence order (Two spin half particles): [-2, -1, -1, -1, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 2]
 1 print("Dictionary of operator basis for two spin half particles: ", Dic 2)
Dictionary of operator basis for two spin half particles: ['Im Sm ', 'E1 Sm ', 'Im E2 ', 'Im Sz ', 'Iz Sm ', 'E1 E2 ', 'E1 Sz ', 'Im Sp
', 'Iz E2 ', 'Iz Sz ', 'Ip Sm ', 'E1 Sp ', 'Iz Sp ', 'Ip E2 ', 'Ip Sz ', 'Ip Sp ']
```

Basis Operators (Example: 3 Three spin half)

```
Product operator basis for three spin half particles
 5 indexing = True
  product basis 3half, Coh order 3, Dic 3 = System.ProductOperator(product basis 2half,Coh order 2,Dic 2,pol basis half,Coh order,Dic 3,
 1 print("Coherence order (Three spin half particles): ", Coh order 3)
Product Operator, I_-S_-R_-
 1 print("Dictionary of operator basis for three spin half particles: ", Dic 3)
Dictionary of operator basis for three spin half particles: ['Im Sm Rm [0]', 'Im Sm E3 [1]', 'Im Sm Rz [2]',
[4]', 'Im Sz Rm [5]', 'Iz Sm Rm [6]', 'Im Sm Rp [7]', 'E1 Sm E3 [8]', 'E1 Sm Rz [9]', 'Im E2 E3 [10]', 'Im E2 R
                                                                                                  Matrix(product basis 3half[0])
'Im Sz Rz [13]', 'Iz Sm E3 [14]', 'Iz Sm Rz [15]', 'E1 E2 Rm [16]', 'E1 Sz Rm [17]', 'Im Sp Rm [18]', 'Iz E2 Rm
'Ip Sm Rm [21]', 'E1 Sm Rp [22]', 'Im E2 Rp [23]', 'Im Sz Rp [24]', 'Iz Sm<mark></mark> Rp [25]', 'E1 E2 E3 [26]', 'E1 E2 Rz
'E1 Sz Rz [29]', 'Im Sp E3 [30]', 'Im Sp Rz [31]', 'Iz E2 E3 [32]', 'Iz E2 Rz [33]', 'Iz Sz E3 [34]', 'Iz Sz Rz
'Ip Sm Rz [37]', 'E1 Sp Rm [38]', 'Iz Sp Rm [39]', 'Ip E2 Rm [40]', 'Ip Sz Rm [41]', 'E1 E2 Rp [42]', 'E1 Sz Rp
'Iz E2 Rp [45]', 'Iz Sz Rp [46]', 'Ip Sm Rp [47]', 'E1 Sp E3 [48]', 'E1 Sp Rz [49]', 'Iz Sp E3 [50]', 'Iz Sp Rz
'Ip E2 Rz [53]', 'Ip Sz E3 [54]', 'Ip Sz Rz [55]', 'Ip Sp Rm [56]', 'E1 Sp Rp [57]', 'Iz Sp Rp [58]', 'Ip E2 Rp
'Ip Sp E3 [61]', 'Ip Sp Rz [62]', 'Ip Sp Rp [63]']
```

Density Matrix in terms of Basis Operators

```
1 """
2 Basis Operators in Cartesian
3 """;
4 Basis = 'Cartesian spin half'
5 B_CarT, dic = System.SingleSpinOP(Sx,Sy,Sz,Sp,Sm,Basis)
1 """
2 Dictionary
3 """;
4 dic
['E$', 'Ix', 'Iy$', 'Iz']
```

```
1 '''
2 Operator Basis
3 Option: 'Cartesian spin half' and 'PMZ spin half'
4 All the 16 operator basis are loaded in the matrix, 'B_car'
5 ''';
6 Basis = 'Cartesian spin half'
7 B_car, dic = System.TwoSpinOP(Sx,Sy,Sz,Sp,Sm,Basis)
```

+ 0.0 Sz Iy + 0.0 Sz Iz + 0.0 Sx Ix + 0.0 Sx Iy + 0.0 Sy Ix + 0.0 Sy Iy +

Two Spin Half

Projection of Density Matrix

```
System.DensityMatrix_Components_Dictionary(B_car,dic,rho)

Density Matrix = 0.0 \text{ E} + 0.0 \text{ Sx} + -1.0 \text{ Sy} + 0.0 \text{ Sz} + 0.0 \text{ Ix} + 0.0 \text{ Iy} + 1.0 \text{ Iz} + 0.0 \text{ Sx} \text{ Iz} + 0.0 \text{ Sy} \text{ Iz} + 0.0 \text{ Sz} \text{ Ix}
```

Basis States (Example: 3 Three spin half)

```
1    """
2    Basis Ket
3    """;
4    Kets = System.Basis_Ket()
5    display(Kets)

['|1/2,1/2>|1/2,1/2>|1/2,1/2>',
    '|1/2,1/2>|1/2,1/2>|1/2,-1/2>',
    '|1/2,1/2>|1/2,-1/2>|1/2,1/2>',
    '|1/2,1/2>|1/2,-1/2>|1/2,-1/2>',
    '|1/2,-1/2>|1/2,1/2>|1/2,1/2>',
    '|1/2,-1/2>|1/2,1/2>|1/2,1/2>',
    '|1/2,-1/2>|1/2,1/2>|1/2,-1/2>',
    '|1/2,-1/2>|1/2,-1/2>|1/2,-1/2>',
    '|1/2,-1/2>|1/2,-1/2>|1/2,-1/2>',
    '|1/2,-1/2>|1/2,-1/2>|1/2,-1/2>']
```

```
H H H
 2 Basis Bra
 4 Bras = System.Basis Bra()
 5 display(Bras)
['<1/2,1/2|<1/2,1/2|<1/2,1/2|',
 '<1/2,1/2|<1/2,1/2|<1/2,-1/2|',
'<1/2,1/2|<1/2,-1/2|<1/2,1/2|',
 '<1/2,1/2|<1/2,-1/2|<1/2,-1/2|',
'<1/2,-1/2|<1/2,1/2|<1/2,1/2|',
'<1/2,-1/2|<1/2,1/2|<1/2,-1/2|',
'<1/2,-1/2|<1/2,-1/2|<1/2,1/2|',
 '<1/2,-1/2|<1/2,-1/2|<1/2,-1/2|']
```

Basis State / Operator Transformation

```
H H H
                                                                                                         Singlet Triplet Basis
    Now lets see how to get the eigen vectors of the Zeman Hamiltonian (lab frame)
                                                                                                         B ST = System.STBasis(B Z)
    B Z = System.ZBasis H(Hz)
                                                                                                    Basis: T_{-}, T_{0}, T_{+}, S_{0}
|1/2,1/2\rangle |1/2,1/2\rangle, |1/2,1/2\rangle |1/2,-1/2\rangle, |1/2,-1/2\rangle |1/2,1/2\rangle, |1/2,-1/2\rangle |1/2,-1/2\rangle
    0.00
    Basis Transformation
   U = System.Transform StateBasis(B Z,B ST)
                                                                          Hj = System.Jcoupling(Jlist,Sx,Sy,Sz)
   Matrix(U)
                                                                         Matrix(Hj/(2.0*np.pi))
1.0
                                       0
               0
                                                                       1.25
      0.707106781186547
                             0.707106781186547
                                                     0
                                                                              -1.25
                                                                                       2.5
                                                                                                0
 0
                                                     1.0
                                                                               2.5
                                                                                      -1.25
      0.707106781186547
                             -0.707106781186547
                                                                        0
                                                                                               1.25
                                                                         Hj ST = System.Operator BasisChange(Hj,U)
                                                                         Matrix(System.Matrix Tol(Hj ST,1.0e-10)/(2.0*np.pi))
                                                                       1.25
                                                                               0
                                                                        0
                                                                              1.25
                                                                                             0
    Sx ST = System.SpinOperator BasisChange(Sx,U)
                                                                        0
                                                                                    1.25
                                                                               0
    Matrix(System.Matrix Tol(Sx ST[0],1.0e-10))
```

0

0

-3.75

Hilbert or Liouville?

Hilbert

Liouville

Converting to Liouvillian

```
Hz_L = System.CommutationSuperoperator(Hz)
Hzr_L = System.CommutationSuperoperator(Hzr)
rho_in_L = System.Vector_L(rho_in)
rhoeq_L = System.Vector_L(rhoeq)
```

Pulse

```
1    """
2    Rotate the magnetization about Y-axis, by an angle theta.
3    """;
4    pulse_angle = 90.0
5    rho = System.Rotate_H(rho_in,pulse_angle,np.sum(Sy,axis=0))
```

```
1 """
2 Rotate the magnetization about Y-axis, by an angle theta.
3 """;
4 pulse_angle = 90.0
5 rho_L = System.Rotate_L(rho_in_L,pulse_angle,np.sum(Sy,axis=0))
```

Evolution of Density Matrix

```
Options: "No Relaxation", "Phenomenological", "Auto-corre
""";

R1 = None
R2 = None
Rprocess = "Auto-correlated Dipolar Homonuclear"
tau = 10.0e-12
bIS = 30.0e3
System.Relaxation_Constants(R1,R2)
System.Relaxation_Parameters(LarmorF, OmegaRF, tau, bIS)
```

```
14 """
15  option for solver, "method": "Unitary Propagator" or "ODE Solver"
16  """
17  method = "Unitary Propagator"
18
19  start_time = time.time()
20  t, rho_t = System.Evolution_H(rhoeq,rho,Sx,Sy,Sz,Sp,Sm,Hzr,dt,Npoints,method,Rprocess)
21  end_time = time.time()
22  timetaken = end_time - start_time
23  print("Total time = %s seconds " % (timetaken))
```

Hilbert

```
option for solver, "method": "Unitary Propagator", "Relaxation" or "ODE Solver"

method = "Relaxation"

start_time = time.time()

t, rho_t = System.Evolution_L(rhoeq_L,rho_L,Sx,Sy,Hzr_L - 1j * R_L,dt,Npoints,method)

end_time = time.time()

timetaken = end_time - start_time

print("Total time = %s seconds " % (timetaken))
```

Liouville

Relaxation Super-operator

```
1 """
2  Options: "No Relaxation", "Phenomenological", "Auto-correlated Dipolar Homonuclear"
3 """;
4  R = None
5  Rprocess = "Auto-correlated Dipolar Homonuclear"
6  tau = 10.0e-12
7  bIS = 30.0e3
8  System Relaxation_Parameters(LarmorF, OmegaRF, tau, bIS)
9  R_L = System.Relaxation_L(Rprocess,R,Sx,Sy,Sz,Sp,Sm)
```

Redfield

```
Rprocess = "Auto-correlated Dipolar Hetronuclear"
tau = 10.0e-12
bIS = 30.0e3
System.Relaxation_Parameters(LarmorF, OmegaRF, tau, bIS)
System.Temperature(T)
R_L = System.Relaxation_Lindblad(Rprocess,Sx,Sy,Sz,Sp,Sm)
```

Lindblad

Write your own Relaxation Mechanism

```
def Relaxation Lindblad(self,Rprocess,Sx,Sy,Sz,Sp,Sm):
       Lindblad Relaxation in Liouville Space
        INPUT
       Rprocess: "No Relaxation" or "Auto-correlated Dipolar Homonuclear" or "Auto-correlated Dipolar Hetronuclear"
       Sx: Spin Operator Sx
       Sy: Spin Operator Sy
       Sz: Spin Operator Sz
                                                                        If Rprocess == "Your Relaxation Mechanism":
       Sp: Spin Operator Sp
       Sm: Spin Operator Sm
                                                                           11 11 11
        OUTPUT
                                                                           Short Description
       Rso: Relaxation Superoperator
                                                                           11 11 11 11
        0.00
       if Rprocess == "No Relaxation":
                                                                            Your code here
            No Relaxation
           Rso = np.zeros((self.Ldim,self.Ldim))
       if Rprocess == "Auto-correlated Dipolar Homonuclean
           Auto-correlated Dipolar Homonuclear Relaxation
           Extreme Narrowing
           Rso = np.zeros((self.Ldim,self.Ldim),dtype=np.cdouble)
           m = [-2, -1, 0, 1, 2]
           for i in m:
               Rso = Rso + (1)**i * self.SpectralDensity Lb(i * self.LarmorF[0], self.tau) * self.Lindblad Dissipator(self.Spherical Tensor([0,1],
2,i,Sx,Sy,Sz,Sp,Sm),self.Symerical Tensor([0,1],2,-i,Sx,Sy,Sz,Sp,Sm))
```

Relaxation Mechanisms Implemented

Redfield Master Equation

- Hilbert Space
 - Phenomenological, Auto-Correlated Random Field Fluctuation, Auto-Correlated Homonuclear, Auto-Correlated Heteronuclear
- Liouville Space
 - Phenomenological, Auto-Correlated Random Field Fluctuation, Auto-Correlated Homonuclear, Auto-Correlated Heteronuclear, Cross Correlated CSA-Dipolar Heteronuclear

Lindblad Master Equation

- Liouville Space
 - Auto-Correlated Homonuclear, Auto-Correlated Heteronuclear

Detection – Expectation Value

```
1 EXP_Z1 = Sz[0]
2 EXP_Z2 = Sz[1]
3
4 t, Mz1 = System.Expectation_H(rho_t,EXP_Z1,dt,Npoints)
5 t, Mz2 = System.Expectation_H(rho_t,EXP_Z2,dt,Npoints)
```

Hilbert

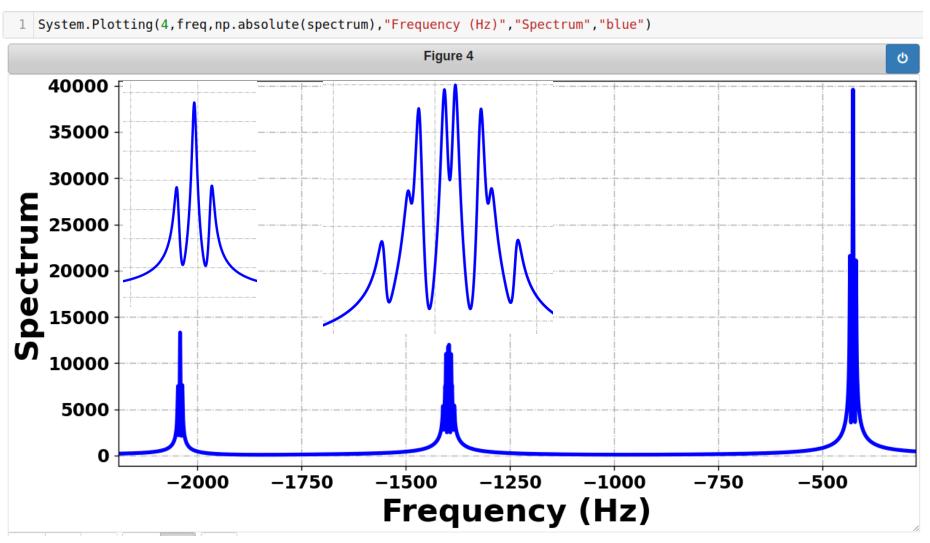
```
EXP_T = np.sum(Sx,axis=0) + 1j * np.sum(Sy,axis=0)
EXP_Z = np.sum(Sz,axis=0)

LEXP_T = System.Detection_L(EXP_T)
LEXP_Z = System.Detection_L(EXP_Z)

t, Mp = System.Expectation_L(rho_t,LEXP_T,dt,Npoints)
t, Mz = System.Expectation_L(rho_t,LEXP_Z,dt,Npoints)
```

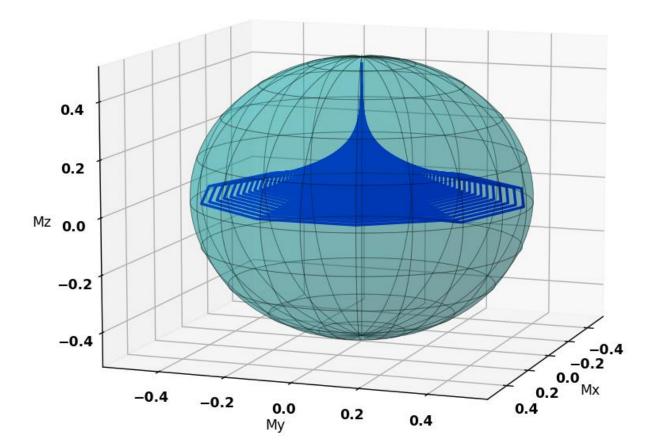
Liouville

Simulation Results Visualization: Plotting (Ethanol Spectra)

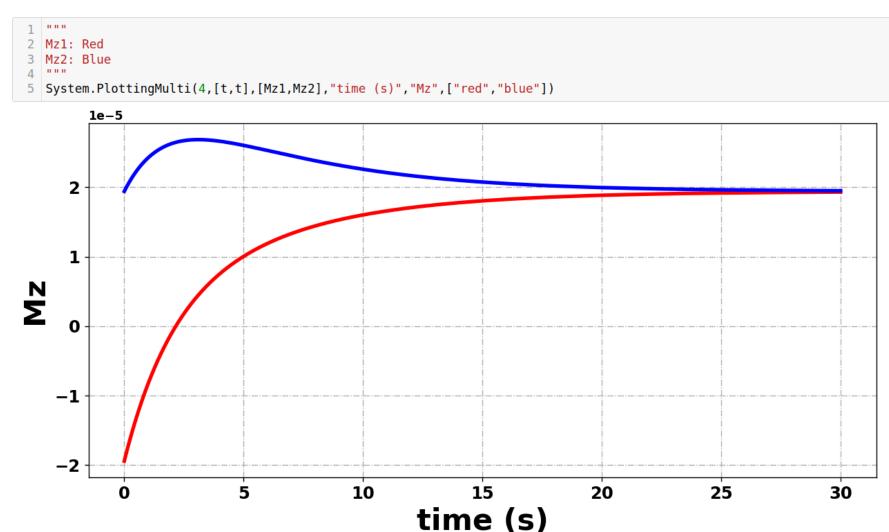


Simulation Results Visualization: Sphere

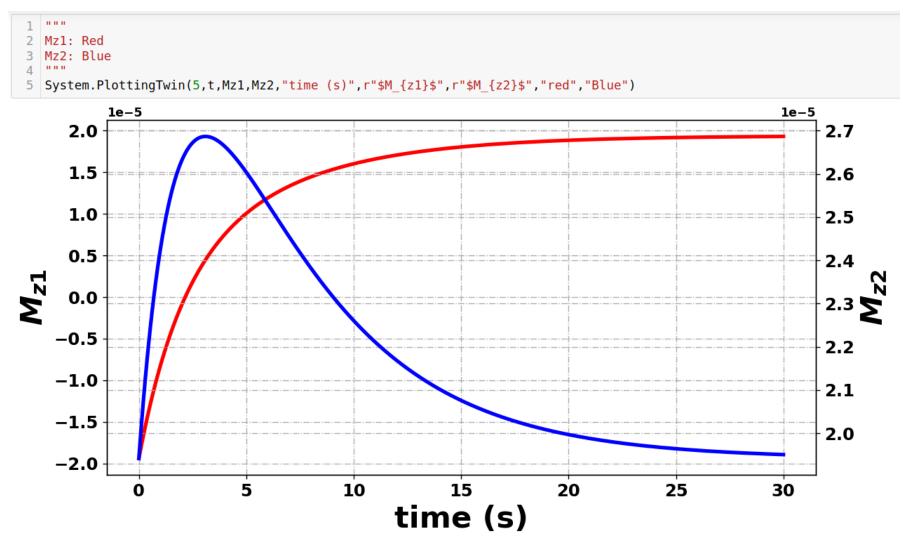
```
plot_vector = False
scale_datapoints = 2
System.PlottingSphere(8,Mp.real,Mp.imag,Mz,rhoeq,np.sum(Sz,axis=0),plot_vector,scale_datapoints)
```



Simulation Results Visualization: Multiple Plots (NOE Lindblad Homonuclear)



Simulation Results Visualization: Twin Axis Plots (NOE Lindblad Homonuclear)



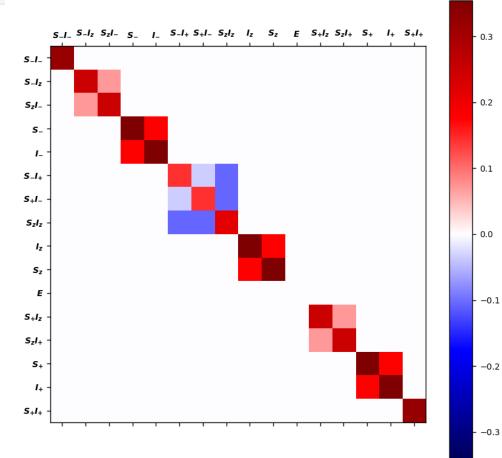
Simulation Results Visualization: RedKite

```
Coherenceorder = "-2,-1,0,1,2"

R_redkite, Basis_L = System.Transform_Redkite(R_L,Sp,Sm,Sz,Coherenceorder)
```

```
S_{-}I_{-}, S_{-}I_{z}, S_{z}I_{-}, S_{-}, I_{-}, S_{-}I_{+}, S_{+}I_{-}, S_{z}I_{z}, I_{z}, S_{z}, E, S_{+}I_{z}, S_{z}I_{+}, S_{+}, I_{+}, S_{+}I_{+}
```

```
System.PlotLabel_Hilbert = False
System.Redkite_Label_SpinDynamica = True
System.MatrixPlot(1,R_redkite.real)
```



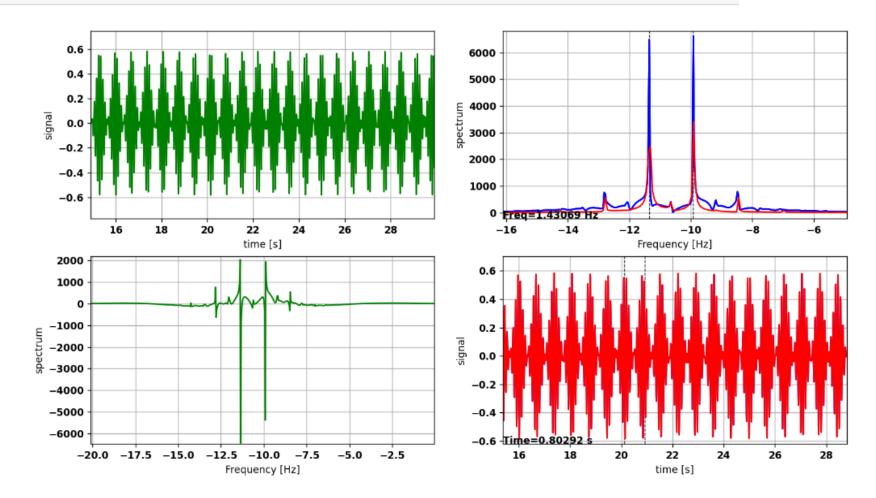
Simulation Results Visualization: Contour Plotting (COSY)

```
# Contour Plot
PH0 = 45
spectrum_PH0_2D = System.PhaseAdjust_PH0(spectrum,PH0)
System.PlottingContour(4,F2,F1,spectrum_PH0_2D,"F2 (Hz)","F1 (Hz)","COSY Spectrum")
                                       COSY Spectrum
                                                                                        48000
    -100
                                                                                        32000
    -150
                                                                                        16000
    -200
                                                                                        -16000
    -250
                                                                                        -32000
    -300
                                                                                         -48000
              -300
                            -250
                                           -200
                                                         -150
                                                                        -100
```

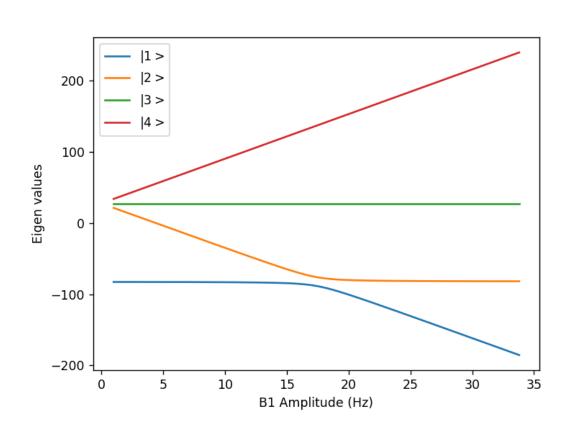
F2 (Hz)

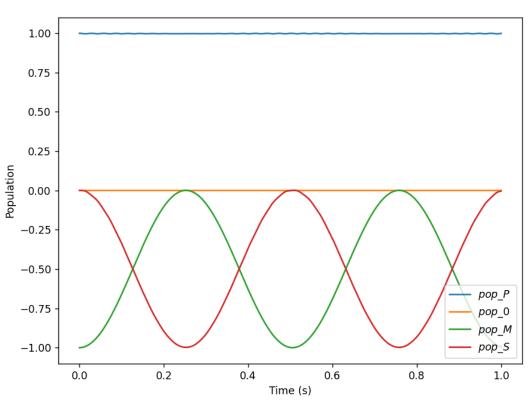
Simulation Results Visualization: Multi-mode Analyzer

fig, fourier = System.PlottingMultimodeAnalyzer(t,freq,signal,spectrum)

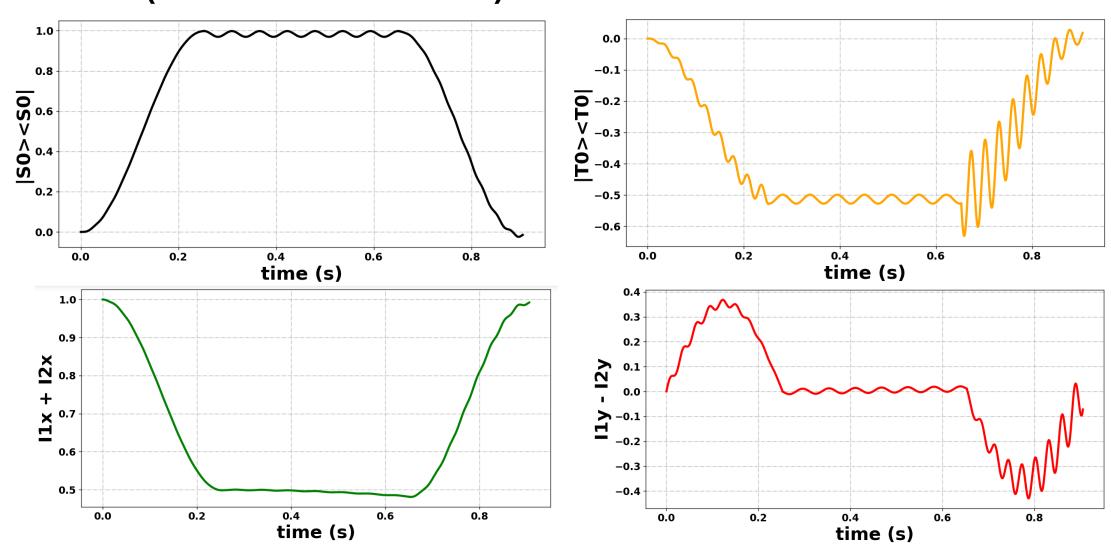


Simulation of specialized NMR Experiments: SLIC (Avoided Crossing)



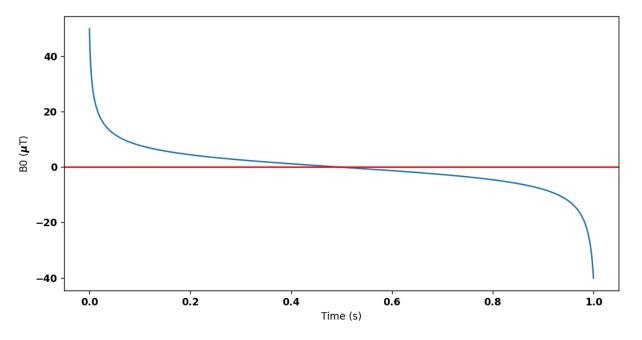


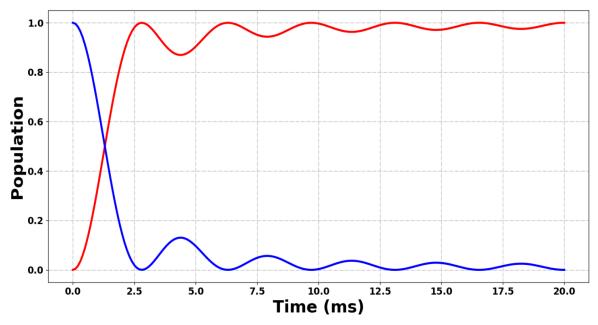
Simulation of specialized NMR Experiments: SLIC (DeVience PRL)



Simulation of specialized NMR Experiments: FIRE – dDNP (Stern - JACS)

- Field Inversion Results in Enhancement
- Constant Adiabatic Inversion
- 1H to 13 C





Future

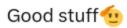
- Sparse Matrices
- Shaped Pulses
- Average Hamiltonian and Floquet Theory
- Anything I see interesting
- Anything you see interesting

Feedback and Suggestions: LinkedIn, Twitter, Email



Mohamed Sabba @ma_sabba · Jul 22

I fully support Vineeth's lovely work on implementing magnetic resonance simulations using code written from scratch, and am impressed by the breadth (which ranges from classic exps i.e. INEPT/INADEQUATE to more specialist sequences like SLIC).





Vineeth Thalakottoor @VThalakottoor · Jul 22

Dear Lindblad, I am coming for you; I am done with Redfield. See the cool features implemented and to implement in PyOR at github.com/VThalakottoor/...

Check the tutorial for the examples. If you like to add any other features and if you see mistakes, please write in the comments.



1 1

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Rudraksha Dutta Majumdar, Ph.D. (He/Him) • 1st

1mo •••

Sr. NMR Scientist

Very interesting! I would be definitely interested in taking it for a spin once you release it on GitHub. do you have or planning to have support for arbitrary RF waveforms in the pulse sequences? I have a collection of Python scripts for shaped RF pulse generation that I am happy to contribute. Includes shape families such as BURP, SNOB, E-family, SLR, Gaussian Cascade, Adiabatic etc

Like Reply · 1 Reply



Quentin Stern • 1st

5d •••

Postdoctoral researcher at the Northweste...

That's really cool to see that you choose our work as an example for your tutorial this project is probably the neatest I've worked on so far, where theory and experiment perfectly met. Congrats for your beautiful work with

ove · 🔽😂 3 | Repl

Acknowledgement

Daniel Abergel and ANR (ANR-22-CE29-0006-01-DynNonlinPol)

PyOR is all yours now

Anbe Sivam (Compassion is God)