

Python On Resonance (PyOR)

Everybody can simulate NMR

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Tutorial 5: Evolution of Density Matrix in Hilbert Space Part 3

In this tutorial you will see how to evolve the density matrix in time by solving Liouville-Von Neumann equation in Hilbert Space of 6 spin half system (ethanol).

Load Python packages and define path to the source file "PythonOnResonance.py"

```
In [25]: pathSource = '/media/HD2/Vineeth/PostDoc_Simulations/Github/PyOR_G/Source'
```

```
In [26]: from IPython.display import display, HTML
display(HTML("<style>.container { width:100% !important; }</style>"))
import sys
sys.path.append(pathSource)

import PythonOnResonance as PyOR

import time
import numpy as np
import matplotlib.pyplot as plt
from matplotlib import rc
%matplotlib notebook
import sympy as sp
from sympy import *
```

Generating Spin System

```
In [27]: """
Define Spin quantum numbers of your spins in "Slist1".
Slist1[0] is spin of first particle and Slist1[1] is spin of second particle.
""";

Slist1 = [1/2,1/2,1/2,1/2,1/2,1/2]
```

```
In [28]: """
Define Planck constant equals 1.
Because NMR spectroscopists are more interested to write Energy in frequency units.
if False then hbarEQ1 = hbar
""";

hbarEQ1 = True
```

In [29]:

```
"""
Generate Spin Operators
""";

System = PyOR.Numerical_MR(Slist1,hbarEQ1)

"""
Sx, Sy and Sz Operators
""";
Sx,Sy,Sz = System.SpinOperator()

"""
S+ and S- Operators
""";
Sp,Sm = System.PMoperators(Sx,Sy)
```

Zeeman Hamiltonian in Lab Frame

In [30]:

```
"""
Gyromagnetic Ratio
Gamma = [Gyromagnetic Ratio spin 1, Gyromagnetic Ratio spin 1, ...]
""";
Gamma = [System.gammaH1, System.gammaH1, System.gammaH1, System.gammaH1, System.gammaH1, System

"""
Define the field of the spectrometer, B0 in Tesla.
""";
B0 = 9.4

"""
Define the chemical Shift of individual spins
Offset = [chemical Shift spin 1, chemical Shift spin 1, ..]
""";
Offset = [427,427,427,1397,1397,2041] # Offset frequency in Hz

"""
Function "LarmorF" give the list Larmor frequencies of individual spins in lab frame
""";
LarmorF = System.LarmorFrequency(Gamma,B0,Offset)

Hz = System.Zeeman(LarmorF,Sz)
```

Larmor Frequency in MHz: [-400.22844465 -400.22844465 -400.22844465 -400.22941465 -400.22941465 -400.23005865]

Initialize Density Matrix

In [31]:

```
"""
We will generate Initial Density Matrix in two ways:
First we will generate a density matrix as we prefer say, Sz.
Second we will create density matrix at thermal equilibrium

First Case
""";

Thermal_DensMatrix = False

if Thermal_DensMatrix:
    Hz_EnUnit = System.Convert_FreqUnitsTOEnergy(Hz)
    HT_approx = False # High Temperature Approximation is False
```

```

T = 300 # Temperature in Kelvin
rho_in = System.EquilibriumDensityMatrix(Hz_EnUnit,T,HT_approx)
rhoeq = rho_in.copy()
else:
    rho_in = np.sum(Sz,axis=0) # Initial Density Matrix
    rhoeq = np.sum(Sz,axis=0) # Equilibrium Density Matrix
    print("Trace of density metrix = ", np.trace(rho_in))

```

Trace of density metrix = 0j

Zeeman Halitonian in Rotating Frame

```

In [32]: OmegaRF = [-System.gammaH1*B0,-System.gammaH1*B0,-System.gammaH1*B0,-System.gammaH1*B0,-Sy
Hzr = System.Zeeman_RotFrame(LarmorF, Sz, OmegaRF)

```

J Coupling Hamiltonian

```

In [42]: """
Define J Coupling between each spins, Jlist[0][3] means J coupling between 1st spin and 4th spin
"""

Jlist = np.zeros((len(Slist1),len(Slist1)))
Jlist[0][3] = 7
Jlist[0][4] = 7
Jlist[1][3] = 7
Jlist[1][4] = 7
Jlist[2][3] = 7
Jlist[2][4] = 7
Jlist[3][5] = 5
Jlist[4][5] = 5

Hj = System.Jcoupling(Jlist,Sx,Sy,Sz)

```

Pulse

```

In [34]: """
Rotate the magnetization about Y-axis, by an angle theta.
""";
pulse_angle = 90.0
rho = System.Rotate_H(rho_in,pulse_angle,np.sum(Sy,axis=0))

```

Relaxation Constant

```

In [35]: """
Define longitudinal (R1) and transverse Relaxation (R2)
R1 = [R1 of first spin, R1 of second spin,...]
R2 = [R2 of first spin, R2 of second spin,...]
""";

R1 = np.asarray([0,0])
R2 = np.asarray([0,0])
System.Relaxation_Constants(R1,R2)

"""
Options for "Rprocess": "No Relaxation" or "Phenomenological"
                        or "Random Field Fluxtuation" or "Dipolar"

```

```
"";  
Rprocess = "No Relaxation"
```

Evolution of Density Matrix

```
In [36]: """  
Sampling Rate, fs = n * Highest_Larmor_Frequency; minimum value of n = 2 (Nyquist-Shannon)  
Dwell time, dt = 1/fs  
Acquisition time, AQ is time for which we evolve the density matrix, in seconds.  
Number of points in the simulation, Npoints  
""";  
Highest_Larmor_Frequency = 2041.0  
fs = 4 * Highest_Larmor_Frequency  
dt = 1.0/fs  
AQ = 5.0  
Npoints = int(AQ/dt)  
print("Number of points in the simulation", Npoints)  
  
"""  
option for solver, "method": "Unitary Propagator" or "ODE Solver"  
"""  
method = "Unitary Propagator"  
  
start_time = time.time()  
t, rho_t = System.Evolution_H(rhoeq, rho, Sx, Sy, Sz, Sp, Sm, Hzr + Hj, dt, Npoints, method, Rprocess)  
end_time = time.time()  
timetaken = end_time - start_time  
print("Total time = %s seconds " % (timetaken))
```

Number of points in the simulation 40820
Total time = 2.7903690338134766 seconds

Expectation value

```
In [37]: """  
Lets see the expectation value of I1+, I2+, ..., I6+  
""";  
  
EXP = np.sum(Sx, axis=0) + 1j * np.sum(Sy, axis=0)  
  
t, Mp = System.Expectation_H(rho_t, EXP, dt, Npoints)
```

Windowing

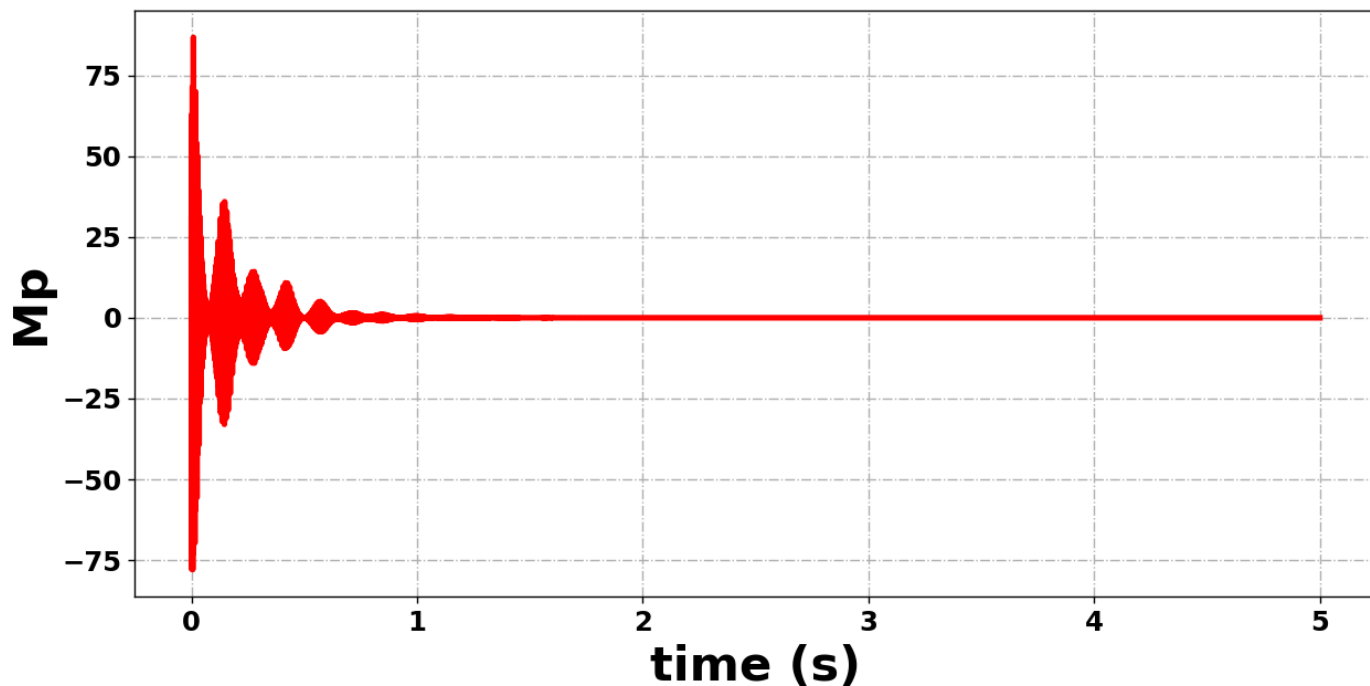
```
In [38]: Mp = System.WindowFunction(t, Mp, 5.0)
```

Fourier Transform

```
In [39]: fs = 1.0/dt  
freq, spectrum = System.FourierTransform(Mp, fs, 5)
```

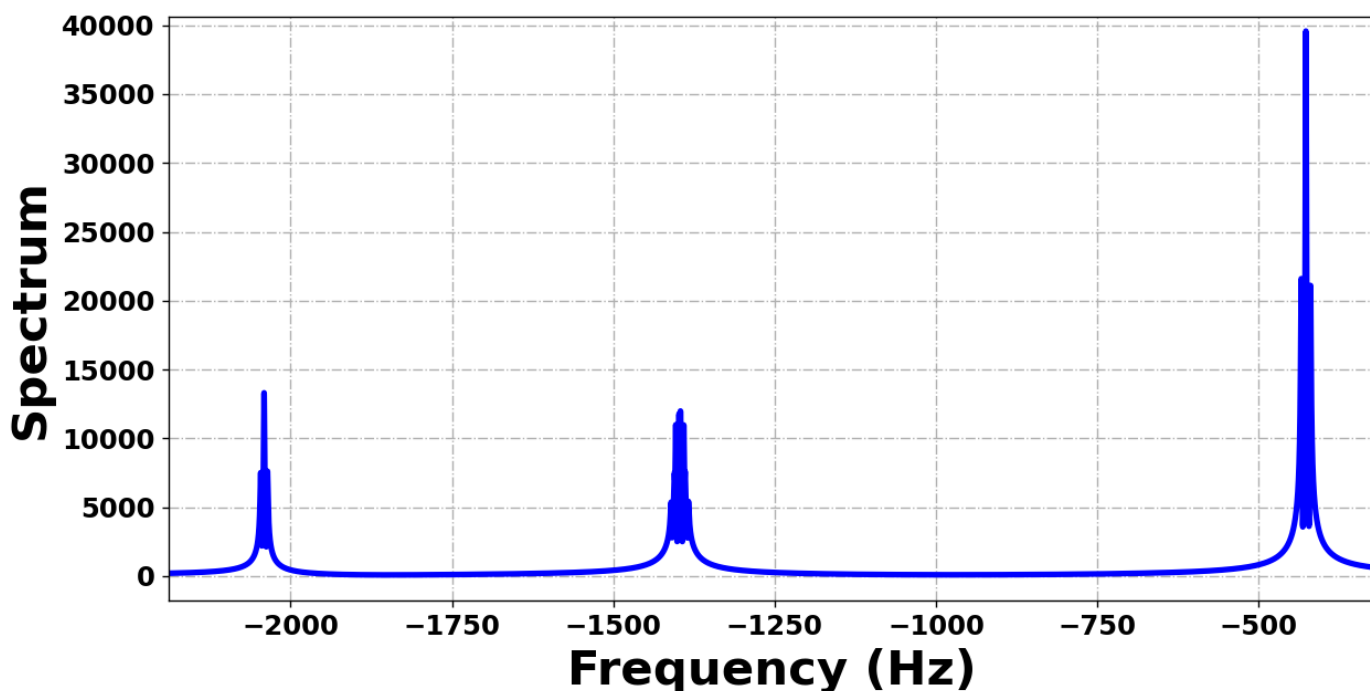
Plotting

```
In [40]: System.Plotting(3, t, Mp, "time (s)", "Mp", "red")
```



```
/opt/anaconda3/lib/python3.9/site-packages/numpy/core/_asarray.py:102: ComplexWarning: Casting complex values to real discards the imaginary part
  return array(a, dtype, copy=False, order=order)
No handles with labels found to put in legend.
```

```
In [41]: System.Plotting(4,freq,np.absolute(spectrum),"Frequency (Hz)","Spectrum","blue")
```



No handles with labels found to put in legend.

Next tutorial: Simulation of Spin-Lock Induced Crossing (SLIC) - DeVience, et.al, PRL 111, 2013.

Any suggestion? write to me

If you see something is wrong please write to me, so that the PyOR can be error free.

In []: