

# Bayesian approach of the parameter inverse problem under uncertainties

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## Table des matières

<b>1</b>	<b>(Joint) Posterior formulation</b>	<b>1</b>
1.1	Priors . . . . .	1
1.2	Likelihood model . . . . .	1

## (Joint) Posterior formulation

### Priors

$$\begin{aligned}K &\sim \mathcal{U}(\mathbb{K}), & p(k) \\U &\sim \mathcal{U}(\mathbb{U}), & p(u)\end{aligned}$$

### Likelihood model

$$\begin{aligned}p(y \mid k, u, \sigma^2) &= \frac{1}{\sqrt{2\pi}\sigma} \exp \left[ -\frac{1}{2\sigma^2} SS(k, u) \right] \\&= \frac{1}{\sqrt{2\pi}\sigma} \exp \left[ -\frac{1}{2\sigma^2} \|\mathcal{M}(k, u) - y\|_{\Sigma}^2 \right]\end{aligned}$$

Now to Bayes' theorem

$$p(k, u \mid y, \sigma^2) = \frac{p(y \mid k, u, \sigma^2)p(k, u)}{\iint_{\mathbb{K} \times \mathbb{U}} p(y \mid k, u, \sigma^2)p(k, u) \, \mathrm{d}(k, u)}$$

Let us assume an hyperprior for  $\sigma^2 : p(\sigma^2)$

$$p(k, u \mid y) = \int p(k, u, \sigma^2) \mathrm{d}(\sigma^2)$$