Table 1: The pattern names P, nodes  $V_p$  and node attributes A(v), with edges  $E_p$  and edge attributes A(e), and the rules.

P	v	A(v)	e	A(e)	Rule
P_section_change: Marks a transition to a new section using an edge with section_change=True.		A(C)[traversed]=True; A(N) [traversed]=False;	$C \to N$	$A(C, N)$ [section_change = True;	Rule-Insert-Skipped: Inserts skipped nodes from the skip graph into the main graph at the transition point into the next section.
P_user_query: User asks a question after a traversed node with no skip or abandon status.		$ \begin{array}{l} A(C)[\mathbf{traversed}] = & \text{True}; \\ A(C)[\mathbf{skipped}] = & \text{False}; \\ A(C)[\mathbf{abandoned}] = & \text{False}; \\ A(C)[\mathbf{dialogue\_act}] = & \text{'user-query'}; \end{array} $			Rule-Handle-User-Input: Inserts a system response node after the current node.
P_yes_answer: User responds with a yes answer to a yes/no question.	L	$ \begin{array}{l} A(C)[\mathbf{response\_required}] = & \text{True}; \\ A(C)[\mathbf{traversed}] = & \text{False}; \\ A(C)[\mathbf{abandoned}] = & \text{False}; \\ A(C)[\mathbf{dialogue\_act}] = & \text{('yes-answer', 'statement')}; \\ \end{array} $	$C \to L$	$A(C, L)[\mathbf{label}] =$ 'no_path'; $A(C, R)[\mathbf{label}] =$ 'yes_path';	Rule-Yes-Answer: Removes non-relevant branches and proceeds along the yes path.

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P_yn_other_answer: User responds with a no answer to a yes/no question.	R	$ \begin{array}{l} A(C)[\textbf{response\_required}] = & \text{True}; \\ A(C)[\textbf{traversed}] = & \text{False}; \\ A(C)[\textbf{abandoned}] = & \text{False}; \\ A(C)[\textbf{dialogue\_act}] = & \text{'no-answer'}, \\ \text{'other-answer'}, \\ \text{'no-response'}\}; \\ \end{array} $	$C \to L$ $C \to R$	$A(C, L)[\mathbf{label}] = $ 'no_path'; $A(C, R)[\mathbf{label}] = $ 'yes_path';	Rule-Other-Answer: Default action if 'yes- answer' not encountered. Removes non-relevant branches and proceeds along the no path.
P_yes_answer: User responds with a no answer to a yes/no question.		$ \begin{array}{c} A(C)[\mathbf{response\_required}] = & \text{True}; \\ A(C)[\mathbf{traversed}] = & \text{False}; \\ A(C)[\mathbf{abandoned}] = & \text{False}; \\ A(C)[\mathbf{dialogue\_act}] = & \text{'yes-answer'}; \\ \end{array} $		$A(C, L)[\mathbf{label}] =$ 'no_path'; $A(C, R)[\mathbf{label}] =$ 'yes_path';	Rule-No-Answer: Removes non-relevant branches and proceeds along the no path.
$P_{\mathbf{stuck}}$ _ <b>broken:</b> User is stuck on a 'broken-down' type question.		$A(C)$ [response_required]=True; A(C)[traversed]=False; A(C)[abandoned]=False; A(C)[skipped]=False; $A(C)$ [is_stuck]=True; A(C)[type]='broken-down';			Rule-Stuck- Abandon-Broken- Down: Marks traversed current node as abandoned. Removes the follow-up nodes along the broken-down path and places them in the abandoned list.

P_stuck_after_ hint: User remains stuck after a hint.	$ A(PP,P,C)  \mathbf{response\_required}  \\ = \mathbf{True}; \ A(C)[\mathbf{traversed}] = \mathbf{False}; \\ A(PP,P)[\mathbf{traversed}] = \mathbf{True}; \\ PP \ A(PP,P,C)[\mathbf{skipped}] = \mathbf{False}; \\ PP \ A(PP,P,C)[\mathbf{is\_stuck}] = \mathbf{True}; \\ PP \ A(PP,P,C)[\mathbf{is\_engaged}] = \mathbf{False}; \\ PP \ A(PP,P,C)[\mathbf{is\_stressed}] = \mathbf{False}; \\ PP \ A(PP,P)[\mathbf{type}] = \mathbf{hint}; \\ PP \ A(PP,P)[\mathbf{type}] = \mathbf{copy}; \\ PP \ A(PP,P,C)[\mathbf{type}] = c$	$\begin{array}{c} PP \rightarrow P \\ P \rightarrow C \end{array}$	Rule-Stuck-Hint-Skip: Moves the curren question and it's followups to the skip graph.
P_stuck_thrice: User is stuck three times in a row.	$ A(PP,P,C)[\mathbf{response\_required}]  = \mathrm{True}; \ A(C)[\mathbf{traversed}] = \mathrm{False}; \\ A(PP,P)[\mathbf{traversed}] = \mathrm{True}; \\ PP \ A(PP,P,C)[\mathbf{skipped}] = \mathrm{False}; \\ PP \ A(PP,P,C)[\mathbf{is\_stuck}] = \mathrm{True}; \\ PP \ A(PP,P,C)[\mathbf{is\_engaged}] = \mathrm{False}; \\ PP \ A(PP,P,C)[\mathbf{is\_engaged}] = \mathrm{False}; \\ PP \ A(PP,C)[\mathbf{type}] = \mathrm{copy'}; \\ PP \ A(PP)[\mathbf{type}] = \mathrm{normal'}; $	$\begin{array}{c} PP \rightarrow P \\ P \rightarrow C \end{array}$	Rule-Stuck-Hint: Adds a hint node after the current node.
$P_{\mathbf{stuck}_{\mathbf{twice:}}}$ User is stuck again on a rephrased question.	$A(P,C)[\mathbf{response\_required}] = \mathbf{True}; \ A(C)[\mathbf{traversed}] = \mathbf{False}; \\ A(P)[\mathbf{traversed}] = \mathbf{True}; \\ A(P,C)[\mathbf{skipped}] = \mathbf{False}; \\ A(P,C)[\mathbf{is\_stuck}] = \mathbf{True}; \\ A(P,C)[\mathbf{is\_engaged}] = \mathbf{False}; \\ A(P,C)[\mathbf{is\_stressed}] = \mathbf{False}; \\ A(C)[\mathbf{type}] = \mathbf{copy}; \\ A(P)[\mathbf{type}] = \mathbf{normal}; $	P  o C	Rule-Stuck-Repeat-Again: Inserts anoth rephrased version of the question.

P_stuck_once: User is stuck first time on the current question.	1	$ \begin{array}{l} A(C)[\mathbf{response\_required}] = & \text{True}; \\ A(C)[\mathbf{traversed}] = & \text{False}; \\ A(C)[\mathbf{is\_stuck}] = & \text{True}; \\ A(C)[\mathbf{is\_engaged}] = & \text{False}; \\ A(C)[\mathbf{is\_stressed}] = & \text{False}; \\ \end{array} $	C		Rule-Stuck-Repeat: Inserts a rephrased version of the question.
P_stressed_thrice _alt: User has been stressed for three turns and an al- ternate path is present.		$ A(PP, P, C)[response\_required] $ $= True; A(C)[traversed] = True;$ $A(PP, P)[traversed] = True;$ $A(PP, P, C)[skipped] = False;$ $A(PP, P, C)[is\_stuck] = False;$ $A(PP)[type] = `normal'$ $A(PP, P, C)[is\_stressed] = True;$	$PP \to P$ $P \to C$ $C \to N$	A(C, N)[label] = 'alternate'	Rule-Stressed- Alternate: Remove the default path and if followups while make taining the alternate path
P_stressed_alt _combo: User has been stressed for three turns and no al- ternate path is present.			$\begin{array}{c} PP \to P \\ P \to C \end{array}$		Rule-Stressed-Brea Down: Inserts simp sub-questions (e.g., what, why)

P_engaged_stuck: User is stuck but en-		$ \begin{array}{l} A(C)[\mathbf{response\_required}] \\ = & \text{True}; \ A(C)[\mathbf{traversed}] = & \text{False}; \\ A(C)[\mathbf{skipped}] = & \text{False}; \\ A(C)[\mathbf{type}] = & \text{normal'} \\ A(C)[\mathbf{is}  \mathbf{stressed}] = & \text{False}; \\ \end{array} $		Rule-Engaged-Stuck-Hint: Inserts a hint
gaged.		$A(C)$ [is_stuck]=True; $A(C)$ [is_engaged]=True;		node to support the user.
P_engaged_stuck _copy: User is stuck on a rephrased question.	C	$ A(C)[\mathbf{response\_required}]  = \mathrm{True}; \ A(C)[\mathbf{traversed}] = \mathrm{False}; \\ A(C)[\mathbf{type}] = \mathrm{'copy'} \\ A(C)[\mathbf{is\_stressed}] = \mathrm{False}; \\ A(C)[\mathbf{is\_stuck}] = \mathrm{True}; \\ A(C)[\mathbf{is\_engaged}] = \mathrm{True};$		Rule-Engaged-Stuck-Copy-Hint: Inserts a hint node to the original question instead of a rephrased question.
P_engaged_stuck2 _alt: User has been engaged and stuck for the last two turns, and an alternate path is present.	l	$ \begin{array}{l} A(P,C)[\mathbf{response\_required}] \\ = & \text{True}; \ A(P)[\mathbf{traversed}] = & \text{True}; \\ A(C)[\mathbf{traversed}] = & \text{False}; \\ A(C)[\mathbf{type}] = & \text{'hint'} \\ A(P,C)[\mathbf{is\_stressed}] = & \text{False}; \\ A(P,C)[\mathbf{is\_stuck}] = & \text{True}; \\ A(P,C)[\mathbf{is\_engaged}] = & \text{True}; \\ A(P,C)[\mathbf{skipped}] = & \text{False}; \\ \end{array} $	A(C, N)[label] = 'alternate'	Rule-Engaged-Stuck- Twice-Alternate: Removes the default path and maintains alternate path after repeated difficulty.

		A(P,C)[response required]			
		=True; $A(P)$ [traversed]=True;			
		A(C)[traversed]=False;			
D ongogod studen	P	$A(C)[\mathbf{type}]=$ 'hint'	$P \to C$		Rule-Engaged-St
P_engaged_stuck2: User has been engaged	C	$A(P,C)[is\_stressed] = False;$	$\Gamma \to C$		Twice: Inserts
and stuck for the last two		$A(P,C)[is\_stuck] = True;$			
turns.		$A(P,C)[is\_engaged] = True;$			quence of folloquestions.
turns.		$A(P,C)[\mathbf{skipped}] = \text{False};$			questions.
	C	$A(C, N)$ [response_required] =True; $A(C, N)$ [traversed]=False; $A(C)$ [dialogue_act]='other-answer'		A(C,N)[label]	
$P_{\text{other}}$ answer	N	=True; $A(C, N)$ [traversed] $=$ False;	$C \to N$	A(C, N)[label] = 'alternate'	Rule-Other-Ansv
_alt:	- '	$A(C)[\mathbf{dialogue\_act}] = \text{'other-answer'}$			Alternate: Ren
User has been engaged					the non-alternate p
and stuck for the last two					
turns.		4/6/27/			
5	C	$A(C, N)$ [response_required] =True; $A(C, N)$ [traversed]=False; $A(C)$ [dialogue_act]='other-answer'			
P_other_answer:	N	=True; $A(C, N)$ [traversed]=False;			Rule-Abandon-
User does not know the		$A(C)[\mathbf{dialogue\_act}] = \text{other-answer}'$			Other-Answer:
answer.					the node as aban
					and puts any follo
					in the abandoned l

P_off_topic_3_alt: User has been off topic for the last three turns, and an alternate path has been provided.	$egin{array}{c} P \\ C \\ N \end{array}$	$ A(PP, P, C)[\textbf{response\_required}]  = \text{True}; \ A(C)[\textbf{traversed}] = \text{False}; \\ A(PP, P)[\textbf{traversed}] = \text{True}; \\ A(PP, P, C)[\textbf{skipped}] = \text{False}; \\ A(PP, P, C)[\textbf{is\_engaged}] = \text{True}; \\ A(PP)[\textbf{type}] = \text{'normal'} \\ A(P, C)[\textbf{type}] = \text{'prompt'} \\ A(PP, P, C)[\textbf{is\_offtopic}] = \text{True}; $	$PP \to P$ $P \to C$ $C \to N$	A(C, N)[label] = 'alternate'	Rule-OffTopic- Thrice-Alternate: Removes the defaul path and it's followup while maintaining the alternate path.
P_off_topic_thrice: User has been off topic for the last three turns.	1	$ \begin{array}{l} A(PP,P,C)[\mathbf{response\_required}] \\ =& \mathrm{True}; \ A(C)[\mathbf{traversed}] =& \mathrm{False}; \\ A(PP,P)[\mathbf{traversed}] =& \mathrm{True}; \\ A(PP,P,C)[\mathbf{skipped}] =& \mathrm{False}; \\ A(PP,P,C)[\mathbf{is\_engaged}] =& \mathrm{True}; \\ A(PP)[\mathbf{type}] =& \mathrm{normal'} \\ A(P,C)[\mathbf{type}] =& \mathrm{prompt'} \\ A(PP,P,C)[\mathbf{is\_offtopic}] =& \mathrm{True}; \\ \end{array} $	$PP \to P$ $P \to C$		Rule-OffTopic- Thrice-Skip: Skip the question and it follow-sups and moves to the skip graph.
P_off_topic_twice: User has been off topic for the last two turns.	0	$A(P,C)[\mathbf{response\_required}] = \mathbf{True}; \ A(C)[\mathbf{traversed}] = \mathbf{False}; \\ A(P)[\mathbf{traversed}] = \mathbf{True}; \\ A(P,C)[\mathbf{skipped}] = \mathbf{False}; \\ A(P,C)[\mathbf{is\_engaged}] = \mathbf{True}; \\ A(P)[\mathbf{type}] = \mathbf{normal}' \\ A(C)[\mathbf{type}] = \mathbf{prompt}' \\ A(P,C)[\mathbf{is\_offtopic}] = \mathbf{True}; \\ A(P,C)[is$			Rule-OffTopic-Twice Insert-Prompt: Insert a prompt node to red rect the user back to the topic.

Rule-OffTopic-Once-

Prompt: Inserts a prompt node to redirect the user back to the

topic.

P_off_topic_once:
User has been off topic
the current turn.

C	$ A(C)[\mathbf{response\_required}]  = \mathbf{True}; \ A(C)[\mathbf{traversed}] = \mathbf{False}; \\ A(P,C)[\mathbf{skipped}] = \mathbf{False}; \\ A(P,C)[\mathbf{is\_engaged}] = \mathbf{True}; \\ A(C)[\mathbf{type}] = \mathbf{normal}' \\ A(C)[\mathbf{is\_offtopic}] = \mathbf{True};$	