

Started on	Wednesday, 7 July 2021, 10:36 AM
State	Finished
Completed on	Wednesday, 7 July 2021, 10:46 AM
Time taken	9 mins 57 secs
Marks	12.00/12.00
Grade	10.00 out of 10.00 (100%)

Question 1

Correct

Mark 1.00 out of 1.00

8221223

The induction method

Select one:

- ☐ a. is used to prove **all** mathematical problems.
- ☐ b. is used **only** to prove mathematical equalities.
- ☐ c. is used **only** to prove mathematical inequalities.
- ☒ d. is used to prove **many** mathematical problems. ✓

Question 2

Correct

Mark 1.00 out of 1.00

8221223

In using the induction method to prove that  $P(n)$  is true for every  $n \geq 5$ , we carry out the inductive step: for each [...], if  $P(k)$  is true, then  $P(k+1)$  is also true.

What is [...]?

Select one:

- ☐ a.  $k \geq 1$ .
- ☒ b.  $k \geq 5$ . ✓
- ☐ c.  $k \geq 0$ .
- ☐ d.  $k > 5$ .

Question 3

Correct

Mark 1.00 out of 1.00

8221223

We are going to use the induction method to prove that  $n! < n^n$  for all  $n$  being integers greater than 1.

What do we do in the first step?

Select one:

- ☐ a. Show that  $P(1)$  is true.
- ☐ b. Show that  $P(3)$  is true.
- ☐ c. Show that  $P(0)$  is true.
- ☒ d. Show that  $P(2)$  is true. ✓

Question 4

Correct

Mark 1.00 out of 1.00

8221223

Let  $P(n)$  be the statement that  $1 + 2 + 3 + \dots + n = \frac{n(n+1)}{2}$ .

What is  $P(1)$ ?

Select one:

- ☐ a.  $1 + 2 + 3 + \dots + n = \frac{n(n+1)}{2}$ .
- ☐ b.  $1(1+1)/2$ .
- ☒ c.  $1 = 1(1+1)/2$ . ✓
- ☐ d. 1.

Question **5**

Correct

Mark 1.00 out of 1.00

**8221223**Find  $f(4)$  if  $f$  is defined recursively by  $f(0) = 0, f(1) = 2, f(n) = 2f(n-1) - f(n-2), n \geq 2$ 

Select one:

- ☒ a. 8 ✓
- ☐ b. 9
- ☐ c. 6
- ☐ d. 10

Question **6**

Correct

Mark 1.00 out of 1.00

**8221223**

The induction method consists of

Select one:

- ☐ a. 1 step.
- ☒ b. 2 steps. ✓
- ☐ c. 3 steps.
- ☐ d. 4 steps.

Question **7**

Correct

Mark 1.00 out of 1.00

**8221223**Let  $\{a_n\}, n \geq 0$  be a sequence which is defined recursively by:

$$a_0 = 2, a_n = a_{n-1}^2 + 1 \ (n \geq 1)$$

Is the following statement True or False?

$$a_1 = 5, a_2 = 26, a_3 = 677$$

Select one:

- ☒ a. True ✓
- ☐ b. False

Question **8**

Correct

Mark 1.00 out of 1.00

**8221223**To use the induction method to prove that  $n^2 - 1 \vdots 8$  whenever  $n$  is an odd number ( $n = 1, 3, 5 \dots$ ), in the inductive step we assume that  $P(k)$  is true (for  $k$  is odd,  $k \geq 1$ ), what will we do next?

Select one:

- ☐ a. Prove  $P(k+1)$  is true.
- ☐ b. Prove  $P(k)$  is true.
- ☐ c. Prove  $P(k+3)$  is true.
- ☒ d. Prove  $P(k+2)$  is true. ✓

Question **9**

Correct

Mark 1.00 out of 1.00

**8221223**We are using the induction method to prove that  $P(n)$  is true for every  $n \geq 2$ . In the basis step, we have to specify

Select one:

- ☐ a.  $P(1)$  is true.
- ☒ b.  $P(2)$  is true. ✓
- ☐ c.  $P(0)$  is true.
- ☐ d.  $P(3)$  is true.

Question **10**

Correct

Mark 1.00 out of 1.00

**8221223**

Which of the following is the definition of the Fibonacci sequence?

Select one:

- ☐ a.  $f_0 = 0, f_1 = 1$   
 $f_n = f_{n-1} - f_{n-2}, n \geq 2$
- ☒ b.  $f_0 = 0, f_1 = 1$   
 $f_n = f_{n-1} + f_{n-2}, n \geq 2$  ✓
- ☐ c.  $f_0 = 1, f_1 = 2$   
 $f_n = f_{n-1} + f_{n-2}, n \geq 2$
- ☐ d.  $f_n = f_{n-1} + f_{n-2}, n \geq 2$

Question **11**

Correct

Mark 1.00 out of 1.00

**8221223**

Consider the sequence  $a_n = 2n, n \geq 0$ . Which of the following is the recursive definition of  $\{a_n\}, n \geq 0$  ?

Select one:

- ☒ a.  $a_0 = 0, a_n = a_{n-1} + 2, n \geq 1$  ✓
- ☐ b.  $a_0 = 0, a_n = a_{n-1} - 2, n \geq 1$
- ☐ c.  $a_0 = 1, a_n = a_{n-1} + 2, n \geq 1$
- ☐ d.  $a_0 = 0, a_n = a_{n-2} + 4, n \geq 2$

Question **12**

Correct

Mark 1.00 out of 1.00

**8221223**

How many steps do we do to define a sequence recursively?

Select one:

- ☐ a. 1 step
- ☐ b. 4 steps
- ☒ c. 2 steps ✓
- ☐ d. 3 steps

[◀ Week5-Quiz](#)

Jump to...

[Week6\\_Quiz \(Term3\\_Group3\\_20-21\) ▶](#)