2.4.9 Beam-Warming scheme

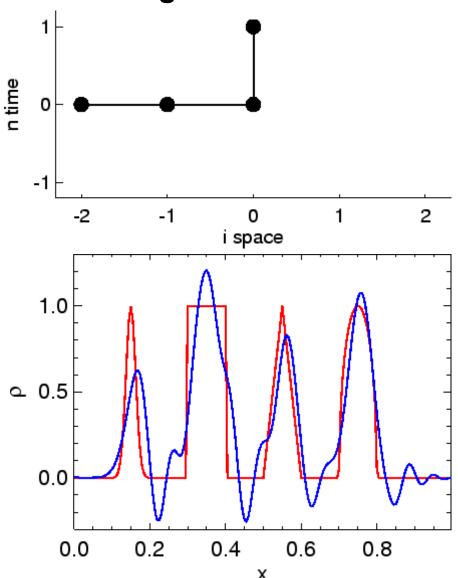


Figure 16: Stencil and example for Beam-Warming scheme. Figure 16: Beam-Warming scheme is $O(\Delta x^2, \Delta t^2)$ with flux

$$f_{i+\frac{1}{2}}^{n} = \frac{1}{2} \left[3f(\rho_{i}^{n}) - f(\rho_{i-1}^{n}) \right] - \frac{1}{2} \frac{v^{2} \Delta t}{\Delta x} \left[\rho_{i}^{n} - \rho_{i-1}^{n} \right] . \tag{117}$$

The result is smooth with considerable overshoot (that does not much grow with time anymore). This second order scheme might be useful for more regular initial conditions.