MASINDE MULIRO UNIVERSITY OF SCIENCE AND TECHNOLOGY. MAT 124 CAT 1

a. Write $\frac{x^2}{(x-2)(x^2+1)}$ into partial fractions, hence evaluate $\int \frac{x^2}{(x-2)(x^2+1)} dx$ (5 Marks)

b. Find $\int \sec(3x + \frac{1}{4})dx$ (4 Marks)

c. Decompose $\frac{4x^2 + 13x - 9}{x^3 + 2x^2 - 3x}$ into partial fractions (5 Marks)

d. Evaluate the integral $\int e^x \cos x dx$ by parts. (4 Marks)

e. Find $3\int \frac{dx}{x^2+9}$ (3 Marks)

f. Define $I_n = \int \sin^n x dx$. Show that $I_n = \frac{-\sin^{n-1} x \cos x}{n} + \frac{n-1}{n} \int \sin^{n-2} x dx$. Hence or otherwise

evaluate $\int_{0}^{\frac{\pi}{2}} \sin^4 x dx$ (9 Marks)