

# COMP 335 Assignment 6

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## Question 1.

(a)  $G_1 = (V, T, S, P)$  such that  $V$  is a set of variables  $\{S, X\}$ , where  $S$  is the start variable and  $T$  is the set of terminals  $\{0,1\}$ .

$S \rightarrow XY$

$X \rightarrow 0X0 \mid 1X1 \mid Y$

$Y \rightarrow ZZ$

$Z \rightarrow 0 \mid 1$

(b)  $G_2 = (V, T, S, P)$  such that  $V$  is a set of variables  $\{S, X\}$ , where  $S$  is the start variable and  $T$  is the set of terminals  $\{a,b,c,d\}$ .

$S \rightarrow aSc \mid aSd \mid X$

$X \rightarrow bXc \mid bXd \mid \lambda$

(c)  $G_3 = (V, T, S, P)$  such that  $V$  is a set of variables  $\{S, X, Y\}$ , where  $S$  is the start variable and  $T$  is the set of terminals  $\{a,b\}$ .

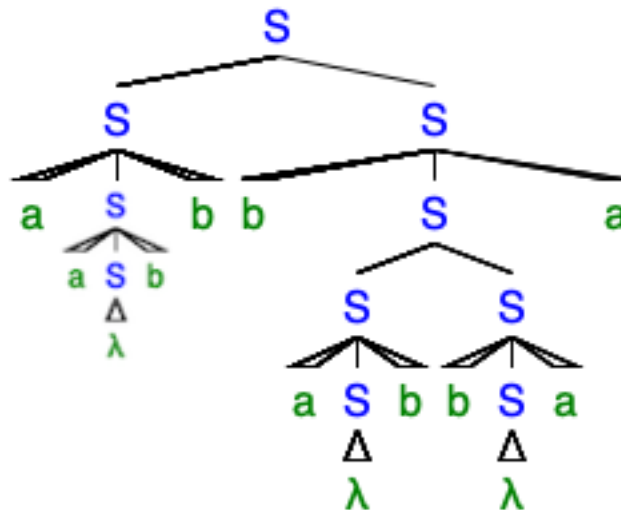
$S \rightarrow YXYaaYXY$

$X \rightarrow XaXbX \mid XbXaX \mid \lambda$

$Y \rightarrow aY \mid \lambda$

## Question 2.

(a)



(b)  $S \Rightarrow SS$   
 $\Rightarrow aSbS$   
 $\Rightarrow aaSbbS$   
 $\Rightarrow aabbS$   
 $\Rightarrow aabbbSa$   
 $\Rightarrow aabbbbSSa$   
 $\Rightarrow aabbbbaSbSa$   
 $\Rightarrow aabbbbabSa$   
 $\Rightarrow aabbbabbSaa$   
 $\Rightarrow aabbbabbbaa$

(c) Yes, the grammar  $G$  is ambiguous.

**Explanation:** a CFG is said to be ambiguous iff there exists a string in  $T$  that has more than one parse tree representation.

Lets take string  $abab$  for instance. The string exists in grammar  $G$  it can be represented as the two parse trees as seen below (Tree 1 and Tree 2). Therefore, the grammar  $G$  is ambiguous.

