



Czech Technical University in Prague  
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# General Framework for Classification at the Top

*Dissertation*



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## Poděkování:

Thanks thanks thanks thanks thanks thanks thanks thanks thanks thanks thanks  
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## Čestné prohlášení:

Prohlašuji na tomto místě, že jsem předloženou práci vypracoval samostatně, a že jsem uvedl veškerou použitou literaturu.

V Praze dne 1. prosince 2021

.....  
Ing. Václav Mácha



Název:	Title title title title title title
Autor:	Ing. Václav Mácha
Obor:	Matematické inženýrství
Druh práce:	Disertační práce
Školitel:	doc. Ing Václav Šmídl, Ph.D.
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Klíčová slova:	Keywords keywords keywords keywords keywords keywords keywords keywords keywords keywords keywords keywords keywords



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<b>Abstract:</b>	Abstract abstract
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## 1.1 Ranking Problems

[illegible]

## 1.2 Accuracy At the Top

[illegible]

### Definition 1.3

[illegible]

## 1.2 Accuracy At the Top

[illegible]

### 1.3 Hypothesis Testing

[illegible]

### Theorem 1.4

[illegible]

*Proof:*

[illegible]

text text text text text

text text text text text text text

### Proof of theorem 1.4:

text text text text text

text text text text text text



## Introduction

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Many binary classification problems focus on separating the dataset by a linear hyperplane  $\mathbf{w}^\top \mathbf{x} - t$ . A sample  $\mathbf{x}$  is deemed to be positive or relevant (depending on the application) if its score  $\mathbf{w}^\top \mathbf{x}$  is above a threshold  $t$ . Multiple problem categories belong to this framework:s





## Linear Classification at the Top

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## Non-Linear Classification at the Top



# Bibliography

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- [2] Shivani Agarwal. The infinite push: A new support vector ranking algorithm that directly optimizes accuracy at the absolute top of the list. In *Proceedings of the 2011 SIAM International Conference on Data Mining*, pages 839–850. SIAM, 2011.