Name:

University of Chicago Booth School of Business

41000: Business Statistics, Autumn 2019: Midterm. November 7, 2019

Special Notes:

- 1. You may use an 8×11 piece of paper for the formulas.
- 2. You may use a simple calculator. No internet.
- 3. This is a 3 hr exam.

Honor Code: By signing my name below, I pledge my honor that I have not violated the Booth Honor Code during this examination.

Signature:

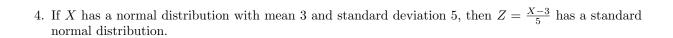
GOOD LUCK!!

Problem A. True or False: Please Explain your answers in detail. Partial credit will be given (50 points)

1. Let X and Y be independent random variables. Then the variance of the sum is given by Var(X+Y) = Var(X) + Var(Y).

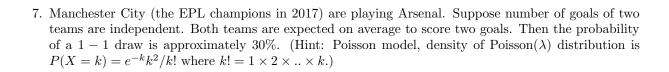
2. If P(A|B) = 0.5 and P(B) = 0.5, then we must have P(A) = 0.5

3. If a researcher has set the significance level at 5% and the test statistic yields a p-value of 0.06, the researcher should reject the null hypothesis.



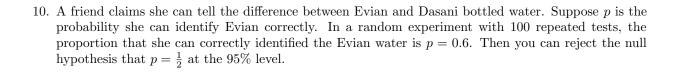
5. As the sample size (number of data observations) increases, the confidence interval of sample mean narrows, holding all else the same.

6. A prediction interval is always wider than a confidence interval.



8. A semi-conductor company knows from experience that 0.2% of chips will have imperfections. Suppose it makes 1000 such chips, then the probability that **at least one** is imperfect is over 95%.

9. Suppose that the annual returns for Tesla stock are normally distributed with a mean of 20% and a standard deviation of 10%. The probability that Tesla has returns greater than 20% for next year is approximately 30%



Problem B: Bayes (20 points)

Shipments from an online retailer take between 1 and 7 days to arrive, depending on where they ship from, when they were ordered, the size of the item, etc.

Suppose the distribution of delivery times has the following distribution function:

X	1	2	3	4	5	6	7
P(X=x)							
$P(X \leq x)$	0.10	0.20	0.70	0.75	0.80	0.90	1

- 1. Fill in the above probability table.
- 2. What is the conditional probability of a delivery arriving on day four given that it did not arrive in the first three days? (Hint: find $P(X=4\mid X>=4)$)

Problem C: A/B Testing. (20 points)

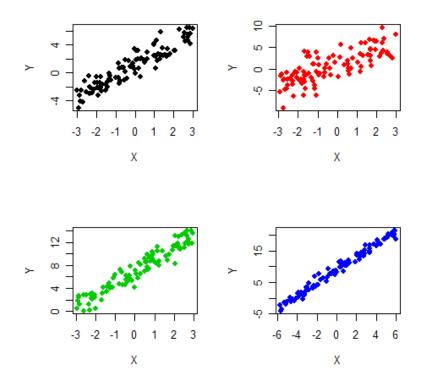
During a recent breakout of the flu, 850 out $6{,}224$ people diagnosed with the virus presented severe symptoms.

During the same flu season, a experimental anti-virus drug was being tested. The drug was given to 238 people with the flu and only 6 of them developed severe symptoms.

Based on this information, can you conclude, for sure, that the drug is a success?

Problem D: Match the Plots (20 points)

Below are 4 different scatter plots of an outcome variable y versus predictor x followed by four regression output summaries labeled A, B, C and D. Match the outputs with the plots.



Regression A:

Coefficients:

Estimate Std. Error

(Intercept) 7.03747 0.12302 (Slope) 2.18658 0.07801

Residual standard error: 1.226

R-Squared: 0.8891

Regression B:

Coefficients:

Estimate Std. Error

(Intercept) 1.1491 0.1013 (Slope) 1.4896 0.0583 Residual standard error: 1.012

R-Squared: 0.8695

Regression C:

Coefficients:

Estimate Std. Error

(Intercept) 1.2486 0.2053 (Slope) 1.5659 0.1119 Residual standard error: 2.052

R-Squared: 0.6666

Regression D:

Coefficients:

Estimate Std. Error (Intercept) 9.0225 0.0904 (Slope) 2.0718 0.0270

Residual standard error: 0.902

R-Squared: 0.9835