

$$\begin{aligned}
O_{i'k} &= \begin{bmatrix} o_{1'1} & o_{1'2} & o_{1'3} \\ o_{2'1} & o_{2'2} & o_{2'3} \\ o_{3'1} & o_{3'2} & o_{3'3} \end{bmatrix} = \begin{bmatrix} \mathbf{e}'_1 \cdot \mathbf{e}_1 & \mathbf{e}'_1 \cdot \mathbf{e}_2 & \mathbf{e}'_1 \cdot \mathbf{e}_3 \\ \mathbf{e}'_2 \cdot \mathbf{e}_1 & \mathbf{e}'_2 \cdot \mathbf{e}_2 & \mathbf{e}'_2 \cdot \mathbf{e}_3 \\ \mathbf{e}'_3 \cdot \mathbf{e}_1 & \mathbf{e}'_3 \cdot \mathbf{e}_2 & \mathbf{e}'_3 \cdot \mathbf{e}_3 \end{bmatrix} = \begin{bmatrix} \cos \angle(\mathbf{e}'_1, \mathbf{e}_1) & \cos \angle(\mathbf{e}'_1, \mathbf{e}_2) & \cos \angle(\mathbf{e}'_1, \mathbf{e}_3) \\ \cos \angle(\mathbf{e}'_2, \mathbf{e}_1) & \cos \angle(\mathbf{e}'_2, \mathbf{e}_2) & \cos \angle(\mathbf{e}'_2, \mathbf{e}_3) \\ \cos \angle(\mathbf{e}'_3, \mathbf{e}_1) & \cos \angle(\mathbf{e}'_3, \mathbf{e}_2) & \cos \angle(\mathbf{e}'_3, \mathbf{e}_3) \end{bmatrix} \\
(O_{i'k})^\top &= \begin{bmatrix} o_{1'1} & o_{2'1} & o_{3'1} \\ o_{1'2} & o_{2'2} & o_{3'2} \\ o_{1'3} & o_{2'3} & o_{3'3} \end{bmatrix} = \begin{bmatrix} \mathbf{e}'_1 \cdot \mathbf{e}_1 & \mathbf{e}'_2 \cdot \mathbf{e}_1 & \mathbf{e}'_3 \cdot \mathbf{e}_1 \\ \mathbf{e}'_1 \cdot \mathbf{e}_2 & \mathbf{e}'_2 \cdot \mathbf{e}_2 & \mathbf{e}'_3 \cdot \mathbf{e}_2 \\ \mathbf{e}'_1 \cdot \mathbf{e}_3 & \mathbf{e}'_2 \cdot \mathbf{e}_3 & \mathbf{e}'_3 \cdot \mathbf{e}_3 \end{bmatrix} = \begin{bmatrix} \cos \angle(\mathbf{e}'_1, \mathbf{e}_1) & \cos \angle(\mathbf{e}'_2, \mathbf{e}_1) & \cos \angle(\mathbf{e}'_3, \mathbf{e}_1) \\ \cos \angle(\mathbf{e}'_1, \mathbf{e}_2) & \cos \angle(\mathbf{e}'_2, \mathbf{e}_2) & \cos \angle(\mathbf{e}'_3, \mathbf{e}_2) \\ \cos \angle(\mathbf{e}'_1, \mathbf{e}_3) & \cos \angle(\mathbf{e}'_2, \mathbf{e}_3) & \cos \angle(\mathbf{e}'_3, \mathbf{e}_3) \end{bmatrix}
\end{aligned}$$