

$$\sum_{i=1}^{3} \left( \boldsymbol{a} + \frac{1}{2} d\boldsymbol{a} \cdot \boldsymbol{n}_{i} \boldsymbol{n}_{i} \right) \cdot \boldsymbol{n}_{i} d\mathcal{O}_{i} + \sum_{i=1}^{3} \left( \boldsymbol{a} - \frac{1}{2} d\boldsymbol{a} \cdot \boldsymbol{n}_{i} \boldsymbol{n}_{i} \right) \cdot (-\boldsymbol{n}_{i}) d\mathcal{O}_{i} =$$

$$= d\boldsymbol{a} \cdot \boldsymbol{n}_{i} d\mathcal{O}_{i} = da_{i} d\mathcal{O}_{i}$$

$$\sum_{i=1}^{3} \left( \boldsymbol{a} + \frac{1}{2} d\boldsymbol{a} \cdot \boldsymbol{n}^{i} \boldsymbol{n}_{i} \right) \cdot \boldsymbol{n}^{i} d\mathcal{O}_{i} + \sum_{i=1}^{3} \left( \boldsymbol{a} - \frac{1}{2} d\boldsymbol{a} \cdot \boldsymbol{n}^{i} \boldsymbol{n}_{i} \right) \cdot \left( -\boldsymbol{n}^{i} \right) d\mathcal{O}_{i} =$$

$$= d\boldsymbol{a} \cdot \boldsymbol{n}^{i} d\mathcal{O}_{i} = da^{i} d\mathcal{O}_{i}$$

$$\begin{split} \boldsymbol{r} &= \boldsymbol{r}(\xi^i) \not\equiv \operatorname{linear} \xi_i \, \boldsymbol{n}_i, \ \boldsymbol{n}_i = \frac{\partial \boldsymbol{r}}{\partial \xi^i} = \partial_i \boldsymbol{r}, \ d\boldsymbol{r} = d\xi^i \boldsymbol{n}_i, \ \boldsymbol{\nabla} = \boldsymbol{n}^i \partial_i \\ \boldsymbol{a} &= a^i \boldsymbol{n}_i, \ d\boldsymbol{a} = da^i \boldsymbol{n}_i \\ d\boldsymbol{a} &= d\boldsymbol{r} \boldsymbol{\cdot} \boldsymbol{\nabla} \boldsymbol{a} = d\xi^i \boldsymbol{n}_i \boldsymbol{\cdot} \boldsymbol{n}^j \partial_j \boldsymbol{a} = d\xi^i \partial_i \boldsymbol{a} = \frac{\partial \boldsymbol{a}}{\partial \xi^i} d\xi^i \\ d\boldsymbol{a} \boldsymbol{\cdot} \boldsymbol{n}^i &= d\xi^h \partial_h \boldsymbol{a} \boldsymbol{\cdot} \boldsymbol{n}^i = d\xi^h \partial_h a^i = \frac{\partial a^i}{\partial \xi^h} d\xi^h = da^i \\ d\boldsymbol{a} \boldsymbol{\cdot} \boldsymbol{E} &= d\boldsymbol{a} \boldsymbol{\cdot} \frac{1}{2} \boldsymbol{n}^i \boldsymbol{\epsilon}_{ijk} \boldsymbol{n}^j \times \boldsymbol{n}^k = d\boldsymbol{a} \boldsymbol{\cdot} \frac{1}{2} \boldsymbol{n}^i \boldsymbol{\epsilon}_{ijk} \boldsymbol{\epsilon}^{jkh} \boldsymbol{n}_h = d\boldsymbol{a} \boldsymbol{\cdot} \boldsymbol{n}^i \boldsymbol{n}_i \end{split}$$

$$\hat{\boldsymbol{n}} = ?$$

$$\boldsymbol{n}^i d\mathcal{O}_i = \boldsymbol{n}^i \boldsymbol{n}_i \cdot d\xi^j \boldsymbol{n}_j \times d\xi^k \boldsymbol{n}_k, \ d\mathcal{O}_i = \in_{ijk} d\xi^j d\xi^k$$

$$d\boldsymbol{a} \cdot \boldsymbol{n}^i d\mathcal{O}_i = d\boldsymbol{a} \cdot \boldsymbol{n}^i \boldsymbol{n}_i \cdot d\xi^j \boldsymbol{n}_j \times d\xi^k \boldsymbol{n}_k = da^i \in_{ijk} d\xi^j d\xi^k$$

$$d\mathcal{V} = d\xi^i \boldsymbol{n}_i \times d\xi^j \boldsymbol{n}_j \cdot d\xi^k \boldsymbol{n}_k = \in_{ijk} d\xi^i d\xi^j d\xi^k$$

$$\nabla \cdot a \, d\mathcal{V} = n^i \partial_i \cdot a^j n_i \, d\mathcal{V} = \partial_i a^i d\mathcal{V}$$

$$da^{i}d\mathcal{O}_{i} = da^{i}d\xi^{j}d\xi^{k} \in_{ijk} = d\xi^{h}\partial_{h}a^{i}d\xi^{j}d\xi^{k} \in_{ijk}$$
$$\partial_{h}a^{h}d\mathcal{V} = \partial_{h}a^{h}d\xi^{i}d\xi^{j}d\xi^{k} \in_{ijk}$$

$$\partial_h a^i d\xi^h d\xi^j d\xi^k {\in}_{ijk} \quad \partial_h a^h d\xi^i d\xi^j d\xi^k {\in}_{ijk}$$

$$\begin{split} \partial_h a^i d\xi^h d\xi^j d\xi^k &\in_{ijk} = \\ &= \partial_h a^1 d\xi^h d\xi^2 d\xi^3 \in_{123} + \partial_h a^1 d\xi^h d\xi^3 d\xi^2 \in_{132} + \\ &+ \partial_h a^2 d\xi^h d\xi^3 d\xi^1 \in_{231} + \partial_h a^2 d\xi^h d\xi^1 d\xi^3 \in_{213} + \\ &+ \partial_h a^3 d\xi^h d\xi^1 d\xi^2 \in_{312} + \partial_h a^3 d\xi^h d\xi^2 d\xi^1 \in_{321} = \\ &= \partial_h a^1 d\xi^h d\xi^2 d\xi^3 \in_{123} - \partial_h a^1 d\xi^h d\xi^3 d\xi^2 \in_{123} + \\ &+ \partial_h a^2 d\xi^h d\xi^3 d\xi^1 \in_{123} - \partial_h a^2 d\xi^h d\xi^1 d\xi^3 \in_{123} + \\ &+ \partial_h a^3 d\xi^h d\xi^1 d\xi^2 \in_{123} - \partial_h a^3 d\xi^h d\xi^2 d\xi^1 \in_{123} \end{split}$$