

## →) Multiple polynomial regression

Dataset :

1.)  $m = \text{no of training samples}$

2.)  $n = \text{no. of features}$

3.) Choosing a different power of a feature according to their graph with target variable

1.)  $x_1$  transaction date:  $\sin(x_1)$

2.)  $x_2$  house age:  $x_2^2$

3.)  $x_3$  distance to nearest HPT station:  $1/x_3$

4.)  $x_4$  number of convenience stores:  $x_4$

5.)  $x_5$  latitude:  $x_5^3$

6.)  $x_6$  longitude:  $x_6^3$

## →) Equations:

1.)  $i$  refers to one training sample meaning one row

$$1.) x_i = [\sin(x_1), x_2^2, \frac{1}{x_3}, x_4, x_5^3, x_6^3] \quad (1 \times n)$$

$$2.) W = [0, 0, 0, 0, 0, 0] \quad (1 \times n)$$

$$3.) B = 0 \quad (1 \times 1)$$

$$4.) \hat{y}_i = W @ x_i.T + B$$

$$J = \frac{1}{2m} \sum (\hat{y}_i - y_i)^2$$

$$\frac{\partial J}{\partial w} = \frac{\partial J}{\partial \hat{y}_i} \times \frac{\partial \hat{y}_i}{\partial w} = \frac{1}{m} (\hat{y}_i - y_i) x_i$$

$(1 \times n)$        $(1 \times 1)$        $(1 \times n)$

$$\frac{\partial J}{\partial B} = \frac{\partial J}{\partial \hat{y}_i} \times \frac{\partial \hat{y}_i}{\partial B} = \frac{1}{m} (\hat{y}_i - y_i)$$

$$w = w - \alpha \frac{\partial J}{\partial w}$$

$$B = B - \alpha \frac{\partial J}{\partial B}$$

→ Findings:

.) Z-Score normalization > Min Max Scaling

.) Reciprocal feature was increasing the loss

.) Linear regression converges faster

.) Sin function does not really make a difference

.) Quadratic scaling increases the error

.) Taking  $x_5$  raise to power 4 reduced loss

.) After all these adjustments linear and polynomial become comparable give same MAE but polynomial has much higher loss than linear so I think it is a more generalized model because still it is giving same MAE