

# Lab 3 Assignment: Multi Linear Regression

Aim: Write a script to implement following for the given Dataset Bengaluru Housing Dataset/ Boston Housing Dataset.

Perform the following: Exercise 1: Draw a scatter plot for the data mentioned for given attributes.

Exercise 2: Perform Data pre-processing.

Exercise 3: Performs gradient descent to learn  $\theta$  . (using the library and without using the library). Compare the values of 'theta' in both cases.

Exercise 4: Splitting data into the training and testing, 60:40, 70:30, ND 80:20.

Exercise 5: Train multilinear regression model and test USING Gradient Descent and using the library. Compare your results with Simple Linear Regression.

Exercise 6: Did you expect ridge regression to outperform the lasso, or vice versa? Which predictors turned out to be important in the final model(s)?

## Exercise 1:

Draw a scatter plot for the data mentioned for given attributes.

```
In [1]: import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
from sklearn import linear_model
import seaborn as sns
from sklearn.model_selection import train_test_split
from sklearn.linear_model import LinearRegression
from sklearn.metrics import mean_squared_error, mean_squared_log_error
```

```
In [2]: df = pd.read_csv(r"C:\Users\raval\jupyter_notebook\pdeu_data_science\prml_lab\bhp.csv")
df
```

Out[2]:

	location	size	total_sqft	bath	price	bhk	price_per_sqft
0	Electronic City Phase II	2 BHK	1056.0	2.0	39.07	2	3699.810606
1	Chikka Tirupathi	4 Bedroom	2600.0	5.0	120.00	4	4615.384615
2	Uttarahalli	3 BHK	1440.0	2.0	62.00	3	4305.555556
3	Lingadheeranahalli	3 BHK	1521.0	3.0	95.00	3	6245.890861
4	Kothanur	2 BHK	1200.0	2.0	51.00	2	4250.000000
...	...	...	...	...	...	...	...
13195	Whitefield	5 Bedroom	3453.0	4.0	231.00	5	6689.834926
13196	Richards Town	4 BHK	3600.0	5.0	400.00	4	11111.111111
13197	Raja Rajeshwari Nagar	2 BHK	1141.0	2.0	60.00	2	5258.545136
13198	Padmanabhanagar	4 BHK	4689.0	4.0	488.00	4	10407.336319
13199	Doddathoguru	1 BHK	550.0	1.0	17.00	1	3090.909091

13200 rows × 7 columns

```
In [3]: # Create subplots
fig, axes = plt.subplots(nrows=2, ncols=2, figsize=(12, 8))

# Scatter plot 1 - Total Sqft vs Price
axes[0, 0].scatter(df['total_sqft'], df['price'], c='blue', alpha=0.5)
axes[0, 0].set_title('Total Sqft vs Price')
axes[0, 0].set_xlabel('Total Sqft')
axes[0, 0].set_ylabel('Price')

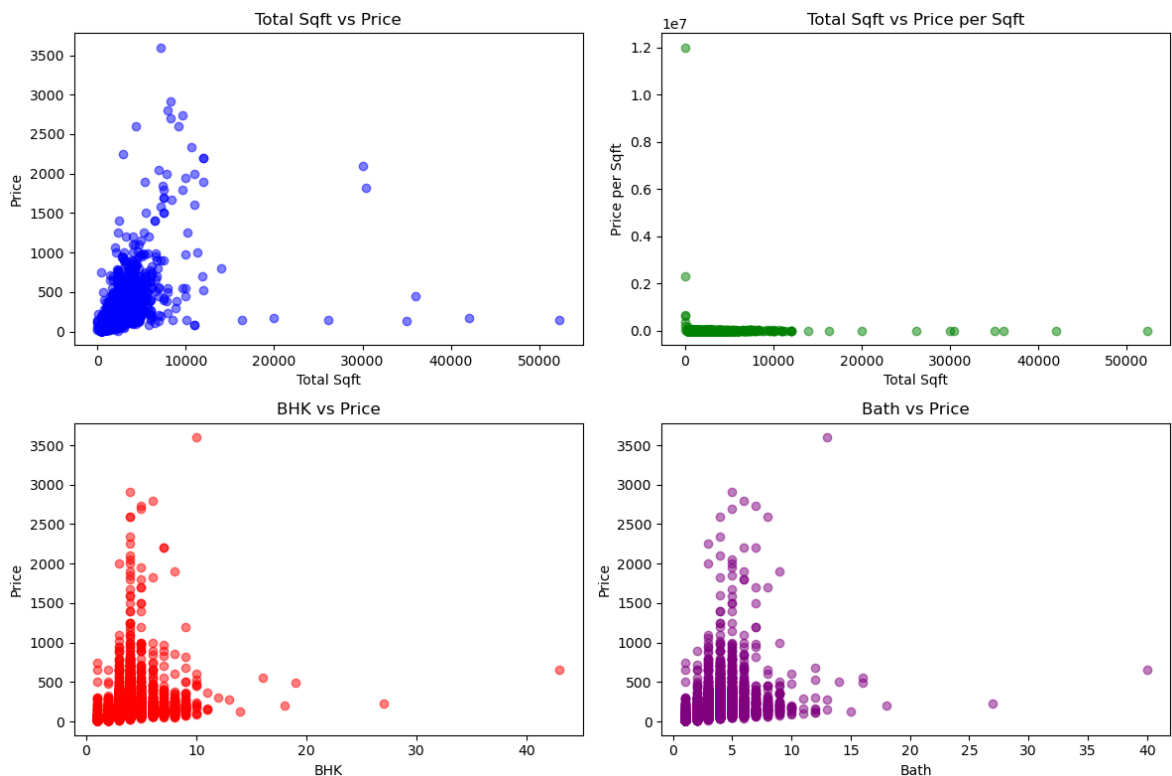
# Scatter plot 2 - Total Sqft vs Price per Sqft
axes[0, 1].scatter(df['total_sqft'], df['price_per_sqft'], c='green', alpha=0.5)
axes[0, 1].set_title('Total Sqft vs Price per Sqft')
axes[0, 1].set_xlabel('Total Sqft')
axes[0, 1].set_ylabel('Price per Sqft')

# Scatter plot 3 - BHK vs Price
axes[1, 0].scatter(df['bhk'], df['price'], c='red', alpha=0.5)
axes[1, 0].set_title('BHK vs Price')
axes[1, 0].set_xlabel('BHK')
axes[1, 0].set_ylabel('Price')

# Scatter plot 4 - Bath vs Price
axes[1, 1].scatter(df['bath'], df['price'], c='purple', alpha=0.5)
axes[1, 1].set_title('Bath vs Price')
axes[1, 1].set_xlabel('Bath')
axes[1, 1].set_ylabel('Price')

# Adjust layout
plt.tight_layout()

# Show the plots
plt.show()
```



## Exercise 2:

Perform Data pre-processing.

```
In [4]: df.isnull().sum()
```

```
Out[4]: location      0
size                0
total_sqft          0
bath                0
price               0
bhk                0
price_per_sqft      0
dtype: int64
```

data is pre-processed already

## Exercise 3:

Performs gradient descent to learn  $\theta$  . (using the library and without using the library). Compare the values of 'theta' in both cases.

```
In [5]: x = df[['bhk']].values
y = df['price_per_sqft'].values
Theta = np.zeros(x.shape[1])
Theta_0 = 0
learning_rate = 0.001
epochs = 10000
n = float(len(x))
for i in range(epochs):

    y_pred = np.dot(x, Theta) + Theta_0
    d_theta = (-2/n) * np.dot(x.T, (y - y_pred))
    d_theta_0 = (-2/n) * np.sum(y - y_pred)
    Theta = Theta - learning_rate * d_theta
    Theta_0 = Theta_0 - learning_rate * d_theta_0
print("Thetas without using a library:", Theta)
print("Intercept (Theta_0):", Theta_0)
```

```
Thetas without using a library: [2555.38725194]
Intercept (Theta_0): 763.5548130675422
```

```
In [6]: x = df[['bhk']]
y = df['price_per_sqft']

model = LinearRegression()
model.fit(x, y)
theta_values = model.coef_
theta_0 = model.intercept_

print("Theta values (Coefficients):", theta_values)
print("Theta_0 (Intercept):", theta_0)
```

```
Theta values (Coefficients): [2555.40479612]
Theta_0 (Intercept): 763.4962168177162
```

## Exercise 4:

Splitting data into the training and testing, 60:40, 70:30 ND 80:20.

```
In [7]: X= df[['bhk', 'total_sqft', 'bath']]
y = df['price_per_sqft']
```

60:40 split

```
In [8]: X_train, X_test, y_train, y_test= train_test_split(X, y, test_size=0.4, random_state=1)
X_train.shape,X_test.shape
```

```
Out[8]: ((7920, 3), (5280, 3))
```

70:30 split

```
In [9]: X_train, X_test, y_train, y_test= train_test_split(X, y, test_size=0.3, random_state=1)
X_train.shape,X_test.shape
```

```
Out[9]: ((9240, 3), (3960, 3))
```

80:20 split

```
In [10]: X_train, X_test, y_train, y_test= train_test_split(X, y, test_size=0.2, random_state=1)
X_train.shape,X_test.shape
```

```
Out[10]: ((10560, 3), (2640, 3))
```

## Exercise 5:

Train Multilinear regression model and test USING gradient descent and using the library. Compare your results with simple linear regression

In [23]: *# Performs gradient descent to Learn theta, without using the Library*

```
x1, x2, x3 = df['bhk'], df['total_sqft'], df['bath']
y = df["price_per_sqft"]

Theta_0 = 0.6
Theta_1 = 0.2
Theta_2 = 0.3
Theta_3 = 0.7

L = 0.000001
epochs = 100
n = float(len(df))

for i in range(epochs):
    y_pred = Theta_0 + Theta_1*x1 + Theta_2*x2 + Theta_3*x3
    d_theta_0 = (-2/n)*sum(y - y_pred)
    d_theta_1 = (-2/n)*sum(x1*(y - y_pred))
    d_theta_2 = (-2/n)*sum(x2*(y - y_pred))
    d_theta_3 = (-2/n)*sum(x3*(y - y_pred))

    Theta_0 = Theta_0 - L*d_theta_0
    Theta_1 = Theta_1 - L*d_theta_1
    Theta_2 = Theta_2 - L*d_theta_2
    Theta_3 = Theta_3 - L*d_theta_3

print("Theta without using library: ", Theta_0, Theta_1, Theta_2, Theta_3)
```

Theta without using library: 0.6149022487058641 0.24994557757968294 20.374742700459706 0.7485360392003488  
Theta without using library: 0.5673593202163109 0.10277101428478422 -118.13476417797173 0.6029021453037219  
Theta without using library: 0.9506665381041666 1.3156568605508223 837.533991629799 1.7969733422831333  
Theta without using library: -1.638748782602545 -6.855421677213238 -5756.261172881948 -6.252474828469451  
Theta without using library: 16.282626110699677 49.71971172090359 39738.71879906596 49.475265442449235  
Theta without using library: -107.31358961734628 -340.43235693947344 -274161.4217107906 -334.8382583248831  
Theta without using library: 745.5142200386781 2351.6837991718676 1891644.5220125094 2316.9857074613533  
Theta without using library: -5138.6570523627115 -16222.819527186166 -13051691.850775259 -15979.523170596345  
Theta without using library: 35460.21126300089 111935.23614757853 90052329.35154088 110260.4556390197  
Theta without using library: -244658.34119560994 -772312.271234107 -621330920.2087663 -760752.9713105297  
Theta without using library: 1688066.0034512822 5328699.873925075 4286975485.819262 5248948.438566756  
Theta without using library: -11647085.26481693 -36766242.44221652 -29578696485.441196 -36215980.363229975  
Theta without using library: 80360996.84166227 253674775.53206635 204083109276.41473 249878155.144988  
Theta without using library: -554463985.4016504 -1750271071.994307 -1408105171476.5745 -1724075657.761787  
Theta without using library: 3825615991.203103 12076284792.186947 9715454556749.955 11895545202.327057  
Theta without using library: -26395470351.966526 -83322324555.55527 -67033385826604.75 -82075281853.88602  
Theta without using library: 182119913988.39792 574896161299.0133 462507934048040.3 566291983899.1912  
Theta without using library: -1256566472492.9268 -3966591163125.725 -3191149998162203.0 -3907225217864.912  
Theta without using library: 8669888235847.399 27368151876085.62 2.201786728638658e+16 26958546716558.82  
Theta without using library: -59819328039925.32 -188831091057559.47 -1.5191591749686634e+17 -186004952503280.75  
Theta without using library: 412733349012875.94 1302871348837690.2 1.0481690024167055e+18 1283371938387894.8  
Theta without using library: -2847722015093376.0 -8989376389848560.0 -7.232015418330909e+18 -8854836981894113.0  
Theta without using library: 1.9648329107988436e+16 6.2023689407596984e+16 4.989848668524388e+19 6.109541250715797e+16  
Theta without using library: -1.355668968704357e+17 -4.2794270491046355e+17 -3.44282862999217e+20 -4.215379048820592e+17  
Theta without using library: 9.353662301801894e+17 2.952661482011918e+18 2.3754365638906285e+21 2.90847050474586e+18  
Theta without using library: -6.453714031661346e+18 -2.0372376318883107e+19 -1.6389717512838906e+22 -2.0067473361247207e+19  
Theta without using library: 4.452846752275687e+19 1.4056258037253662e+20 1.130835671362624e+23 1.3845885197985124e+20  
Theta without using library: -3.072315274891128e+20 -9.698347748795941e+20 -7.802387775289045e+23 -9.553197528394303e+20  
Theta without using library: 2.119794745576044e+21 6.691535457537135e+21 5.383386511200702e+24 6.591386661923275e+21  
Theta without using library: -1.4625874499586048e+22 -4.61693557905634e+22 -3.7143565743762008e+25 -4.547836260879909e+22  
Theta without using library: 1.0091364049471137e+23 3.1855310752551984e+23 2.5627817606829333e+26 3.137854857651368e+23  
Theta without using library: -6.962703555390241e+23 -2.19790985983185e+24 -1.7682336688399576e+27 -2.1650148648449974e+24  
Theta without using library: 4.8040324937819586e+24 1.5164842652049692e+25 1.220022069606901e+28 1.493787819270942e+25  
Theta without using library: -3.3146216864922606e+25 -1.0463234041773686e+26 -8.417744083022753e+28 -1.0306636158648178e+26  
Theta without using library: 2.286978062447577e+26 7.219281407983204e+26 5.807961774830446e+29 7.111234108107847e+26  
Theta without using library: -1.577938344949282e+27 -4.981062627441443e+27 -4.0072993007621e+30 -4.9065136055941926e+27

Theta without using library: 1.0887246630588494e+28 3.43676655560993e+28 2.76490244055666  
35e+31 3.3853302248104342e+28  
Theta without using library: -7.5118359075728995e+28 -2.371253935392933e+29 -1.9076901753  
613305e+32 -2.3357645881076617e+29  
Theta without using library: 5.182915443815123e+29 1.6360858775636027e+30 1.3162423931447  
64e+33 1.6115994153459825e+30  
Theta without using library: -3.5760382452785186e+30 -1.1288445150517404e+31 -9.081632121  
858189e+33 -1.1119496753942124e+31  
Theta without using library: 2.467346741485967e+31 7.7886494629487e+31 6.2660223091367155  
e+34 7.672080722018788e+31  
Theta without using library: -1.7023866986767504e+32 -5.373907535344526e+32 -4.3233457435  
58534e+35 -5.293479004281567e+32  
Theta without using library: 1.1745898633145426e+33 3.707816398184888e+33 2.9829639117452  
61e+36 3.652323402744296e+33  
Theta without using library: -8.104277060398153e+33 -2.55826925793336e+34 -2.058145294539  
985e+37 -2.5199809477743774e+34  
Theta without using library: 5.591680017257677e+34 1.7651201929228704e+35 1.4200513914225  
487e+38 1.7387025399706178e+35  
Theta without using library: -3.858072124432355e+35 -1.2178738753953818e+36 -9.7978794773  
66146e+38 -1.1996465787450957e+36  
Theta without using library: 2.661940681759892e+36 8.402922261710142e+36 6.76020902009937  
7e+39 8.277160013346172e+36  
Theta without using library: -1.836650006705353e+37 -5.797735214035971e+37 -4.66431803953  
1262e+40 -5.710963470441643e+37  
Theta without using library: 1.2672270536473593e+38 4.000243315975998e+38 3.2182233876516  
05e+41 3.940373716121116e+38  
Theta without using library: -8.74344267897004e+38 -2.760034047134952e+39 -2.220466461559  
8484e+42 -2.7187260263632657e+39  
Theta without using library: 6.032682908749734e+39 1.90433114678785e+40 1.532047565694308  
5e+43 1.8758299945469328e+40  
Theta without using library: -4.1623493644046957e+40 -1.3139247758160725e+41 -1.057061560  
7951898e+44 -1.2942599343667228e+41  
Theta without using library: 2.8718817967760546e+41 9.065641337722904e+41 7.2933710958536  
06e+44 8.929960511221833e+41  
Theta without using library: -1.9815023518174053e+42 -6.254989203106147e+42 -5.0321820331  
653504e+45 -6.161373972454835e+42  
Theta without using library: 1.3671703252778781e+43 4.3157332695451315e+43 3.472037235196  
8615e+46 4.2511418925916224e+43  
Theta without using library: -9.433017814014024e+43 -2.9777115593755597e+44 -2.3955895242  
14919e+47 -2.933145670388002e+44  
Theta without using library: 6.508466679996184e+44 2.054521347139117e+45 1.65287661962611  
15e+48 2.0237723748315432e+45  
Theta without using library: -4.49062424770229e+45 -1.4175509889666406e+46 -1.14042956528  
70514e+49 -1.3963352268792725e+46  
Theta without using library: 3.098380482768933e+46 9.78062753700951e+46 7.868582433424586  
e+49 9.63424587701608e+46  
Theta without using library: -2.137778866917106e+47 -6.748305758471996e+47 -5.42905861056  
0863e+50 -6.647307310741476e+47  
Theta without using library: 1.4749958919678126e+48 4.6561051872699655e+48 3.745868794828  
961e+51 4.5864196375608523e+48  
Theta without using library: -1.0176978147694666e+49 -3.2125567943783976e+49 -2.584524138  
4535413e+52 -3.1644760966312373e+49  
Theta without using library: 7.021774418671881e+49 2.2165567017952816e+50 1.7832351820411  
538e+53 2.1833826290427403e+50  
Theta without using library: -4.844789413042407e+50 -1.529349962270233e+51 -1.23037261179  
23078e+54 -1.506460962015299e+51  
Theta without using library: 3.342742597129367e+51 1.055200304689521e+52 8.48915936099823  
5e+54 1.0394076603380622e+52  
Theta without using library: -2.3063805499125125e+52 -7.280529051467029e+52 -5.8572359272  
07717e+55 -7.171565089374434e+52  
Theta without using library: 1.5913254121279896e+53 5.023321452210034e+53 4.0412968172786  
53e+56 4.948139964102753e+53  
Theta without using library: -1.097961291505165e+54 -3.465923730796677e+54 -2.78835958945  
78364e+57 -3.414051019438938e+54  
Theta without using library: 7.575565553444132e+54 2.3913714107255522e+55 1.9238748232694  
624e+58 2.3555809754556126e+55  
Theta without using library: -5.22688676718773e+55 -1.6499662624488737e+56 -1.32740925869  
2423e+59 -1.6252720595956873e+56  
Theta without using library: 3.6063769872050194e+56 1.1384215162100831e+57 9.158679757906  
321e+59 1.1213833424646227e+57  
Theta without using library: -2.4882794583359562e+57 -7.854727566650438e+57 -6.3191826001  
35758e+60 -7.73716986847085e+57

Theta without using library: 1.7168295729324997e+58 5.419499216045198e+58 4.3600245657008755e+61 5.338388337568748e+58  
Theta without using library: -1.1845549633186322e+59 -3.7392731324532223e+59 -3.008271071816578e+62 -3.683309340127386e+59  
Theta without using library: 8.173032916284323e+59 2.5799733520932765e+60 2.0756063882575074e+63 2.5413602078354878e+60  
Theta without using library: -5.639119257372896e+60 -1.7800952917135682e+61 -1.4320989618711127e+64 -1.753453514101481e+61  
Theta without using library: 3.8908036128809885e+61 1.2282061925213235e+62 9.881003682562374e+64 1.209824257354569e+62  
Theta without using library: -2.6845243136530817e+62 -8.474211792872688e+62 -6.81756194049948e+65 -8.347382590484334e+62  
Theta without using library: 1.8522319571042845e+63 5.8469226053197056e+63 4.7038896356826785e+66 5.759414699146897e+63  
Theta without using library: -1.2779780780788336e+64 -4.03418097024098e+64 -3.2455264650022215e+67 -3.9738034428376056e+64  
Theta without using library: 8.817621150449449e+64 2.7834498930852215e+65 2.2393046714203534e+68 2.741791419299475e+65  
Theta without using library: -6.083863572193335e+65 -1.9204872970419396e+66 -1.5450453002057363e+69 -1.8917443439468188e+66  
Theta without using library: 4.1976623097687554e+66 1.3250719789359485e+67 1.066029562727434e+70 1.3052403029873968e+67  
Theta without using library: -2.896246547569988e+67 -9.142553309597695e+67 -7.355247308655209e+70 -9.005721380871897e+67  
Theta without using library: 1.9983132146648553e+68 6.308055890364562e+68 5.0748745497325e+71 6.2136464376920185e+68  
Theta without using library: -1.378769258181601e+69 -4.3523475082382036e+69 -3.5014936432139914e+72 -4.287208144663254e+69  
Theta without using library: 9.513046570257102e+69 3.00297415902777e+70 2.415913460188719e+73 2.9580301776060716e+70  
Theta without using library: -6.5636838441867e+70 -2.0719516956583301e+71 -1.6668994554460095e+74 -2.0409418522214778e+71  
Theta without using library: 4.528722243527658e+71 1.4295773462570646e+72 1.1501048528241367e+75 1.4081815918187796e+72  
Theta without using library: -3.1246668251986558e+72 -9.863605378512628e+72 -7.93533868025489e+75 -9.71598183151996e+72  
Theta without using library: 2.1559155637003188e+73 6.805557692821083e+73 5.475118187330615e+76 6.703702384612445e+73  
Theta without using library: -1.4875096059271771e+74 -4.695607106424807e+74 -3.7776483617301794e+77 -4.625330351654759e+74  
Theta without using library: 1.0263318587152539e+75 3.2398117969326135e+75 2.6064509763286635e+78 3.1913231874740967e+75  
Theta without using library: -7.081346433103066e+75 -2.2353617416547034e+76 -1.79836396654269e+79 -2.2019062234692892e+76  
Theta without using library: 4.885892109828162e+76 1.5423248105906295e+77 1.24081096691665e+80 1.5192416224036745e+77  
Theta without using library: -3.3711020826898527e+77 -1.0641525159156887e+78 -8.561180518871915e+80 -1.0482258883883098e+78  
Theta without using library: 2.3259476460922796e+78 7.342296313680123e+78 5.90692811644328e+81 7.2324079125020474e+78  
  
Theta without using library: -1.6048260538124782e+79 -5.065938796516543e+79 -4.075582765240592e+82 -4.990119476370354e+79  
Theta without using library: 1.1072762825604548e+80 3.4953282724690217e+80 2.812015746405881e+83 3.4430154783451415e+80  
Theta without using library: -7.639835875098354e+80 -2.4116595606567755e+81 -1.9401967800714904e+84 -2.3755654830025396e+81



```
In [14]: # # Create a DataFrame with your features
# data = pd.DataFrame({'x1': x1, 'x2': x2, 'x3': x3})

# Split the dataset into training and testing sets
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=42)

# Initialize the Linear Regression model
model = LinearRegression()

# Fit the model to the training data
model.fit(X_train, y_train)

# Get the coefficients and intercept
coefficients = model.coef_
intercept = model.intercept_

# Make predictions on the test set
y_pred = model.predict(X_test)

# Calculate the Mean Squared Error (MSE) to evaluate the model
mse = mean_squared_error(y_test, y_pred)

print(f"Coefficients: {coefficients}")
print(f"Intercept: {intercept}")
print(f"Mean Squared Error: {mse}")
```

```
Coefficients: [1491.71288993  -1.94961844 1933.72142831]
Intercept: 1717.623832424195
Mean Squared Error: 1986674652.4347043
```

The Value of Thetas for without library and with library are different to each other , the without library falling short by a very large numbers at 100 epochs and 0.0001 learning rate

```
In [13]: X= df[['bhk', 'total_sqft', 'bath']]
```

## Exercise 6

Did you expect ridge regression to outperform the lasso ,or vice versa ?

```
In [24]: from sklearn.linear_model import Lasso, Ridge
from sklearn.metrics import mean_squared_error, r2_score
```

```
In [25]: X= df[['bhk', 'total_sqft', 'bath']]
y = df['price']
```

```
In [26]: X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=3)
```

Lasso

```
In [27]: lasso_model = Lasso(alpha=1.0)
lasso_model.fit(X_train, y_train)
lasso_pred = lasso_model.predict(X_test)
l_mse = mean_squared_error(y_test, lasso_pred)
l_r2 = r2_score(y_test, lasso_pred)
```

```
In [28]: print("Mean Square Error:", l_mse)
print("R-2 :", l_r2)
```

```
Mean Square Error: 11553.307662056648
R-2 : 0.46703493251013517
```

## Ridge

```
In [29]: ridge_model = Ridge(alpha=1.0)
         ridge_model.fit(X_train, y_train)
         ridge_pred = ridge_model.predict(X_test)
         r_mse = mean_squared_error(y_test, ridge_pred)
         r_r2 = r2_score(y_test, ridge_pred)
```

```
In [30]: print("Mean Square Error:", r_mse)
         print("R-2:", r_r2)
```

```
Mean Square Error: 11582.80239988878
R-2: 0.46567431220994837
```

Expected Ridge to perform better due to regularization factor/ bias being squared allowing for faster regularization but here

## Exercise 7

Which predictors turned out to be important in the final models(s)?

"bath" appears to be the most important feature for price prediction in your model, as it has the largest positive coefficient. This suggests that the number of bathrooms has a significant impact on the price.

"bhk" is also important, but it has a slightly smaller positive coefficient, indicating that the number of bedrooms (bhk) is another influential factor in price prediction.

"total\_sqft" has a negative coefficient, which suggests that an increase in total square footage is associated with a decrease in price in your model. This may be counterintuitive and could indicate an issue with the model or data. You should further investigate this feature and its relationship with the target variable.

In [ ]: