

Spring 2019

BUAN 6337: Predictive Analytics using SAS

A Report of

**Group Assignment 4 on
Crackers Data Analysis**

Submitted by Group 7

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1. Summary Statistics

There are 3292 observations consisting of 3 main brands with rest of them combine as Private: Sunshine, Keebler and Nabisco.

Feature Relevance:

Quantitative variable: PricePrivate, PriceNabisco, PriceKeebler and PriceSunshine .

Qualitative variable: DisplPrivate, DisplKeebler, DisplSunshine, DisplNabisco, FeatPrivate, FeatKeebler, FeatSunshin, and FeatNabisco.

Market Share:

Nabisco has the highest market share- 1792 purchases. So 54.4% market share.

Keebler has lowest market share: 226 purchases. So, 7.2% market share.

The FREQ Procedure

| PRIVATE | Frequency | Percent | Cumulative Frequency | Cumulative Percent |
|---------|-----------|---------|----------------------|--------------------|
| 0 | 2257 | 68.56 | 2257 | 68.56 |
| 1 | 1035 | 31.44 | 3292 | 100.00 |

| SUNSHINE | Frequency | Percent | Cumulative Frequency | Cumulative Percent |
|----------|-----------|---------|----------------------|--------------------|
| 0 | 3053 | 92.74 | 3053 | 92.74 |
| 1 | 239 | 7.26 | 3292 | 100.00 |

| KEEBLER | Frequency | Percent | Cumulative Frequency | Cumulative Percent |
|---------|-----------|---------|----------------------|--------------------|
| 0 | 3066 | 93.13 | 3066 | 93.13 |
| 1 | 226 | 6.87 | 3292 | 100.00 |

| NABISCO | Frequency | Percent | Cumulative Frequency | Cumulative Percent |
|---------|-----------|---------|----------------------|--------------------|
| 0 | 1500 | 45.57 | 1500 | 45.57 |
| 1 | 1792 | 54.43 | 3292 | 100.00 |

Average price of brands:

Average Price of Keenler is highest= 1.1259 and average price of private is lowest = 0.6807.

| Variable | N | Mean | Std Dev | Minimum | Maximum |
|---------------|------|-----------|-----------|-----------|-----------|
| PRICEPRIVATE | 3292 | 0.6807290 | 0.1240652 | 0.3800000 | 1.1500000 |
| PRICESUNSHINE | 3292 | 0.9570322 | 0.1329214 | 0.4900000 | 1.2900000 |
| PRICEKEEBLER | 3292 | 1.1259386 | 0.1063765 | 0.8800000 | 1.3900000 |
| PRICENABISCO | 3292 | 1.0792254 | 0.1447765 | 0 | 1.6900001 |

Display or store feature:

Nabisco provides display and store feature more frequently.

| FeatPrivate | Frequency | Percent | Cumulative Frequency | Cumulative Percent |
|-------------|-----------|---------|----------------------|--------------------|
| 0 | 3137 | 95.29 | 3137 | 95.29 |
| 1 | 155 | 4.71 | 3292 | 100.00 |

| DisplPrivate | Frequency | Percent | Cumulative Frequency | Cumulative Percent |
|--------------|-----------|---------|----------------------|--------------------|
| 0 | 2967 | 90.13 | 2967 | 90.13 |
| 1 | 325 | 9.87 | 3292 | 100.00 |

| FeatSunshine | Frequency | Percent | Cumulative Frequency | Cumulative Percent |
|--------------|-----------|---------|----------------------|--------------------|
| 0 | 3168 | 96.23 | 3168 | 96.23 |
| 1 | 124 | 3.77 | 3292 | 100.00 |

| DisplSunshine | Frequency | Percent | Cumulative Frequency | Cumulative Percent |
|---------------|-----------|---------|----------------------|--------------------|
| 0 | 2868 | 87.12 | 2868 | 87.12 |
| 1 | 424 | 12.88 | 3292 | 100.00 |

| FeatKeebler | Frequency | Percent | Cumulative Frequency | Cumulative Percent |
|-------------|-----------|---------|----------------------|--------------------|
| 0 | 3152 | 95.75 | 3152 | 95.75 |
| 1 | 140 | 4.25 | 3292 | 100.00 |

| DisplKeebler | Frequency | Percent | Cumulative Frequency | Cumulative Percent |
|--------------|-----------|---------|----------------------|--------------------|
| 0 | 2942 | 89.37 | 2942 | 89.37 |
| 1 | 350 | 10.63 | 3292 | 100.00 |

| FeatNabisco | Frequency | Percent | Cumulative Frequency | Cumulative Percent |
|-------------|-----------|---------|----------------------|--------------------|
| 0 | 3007 | 91.34 | 3007 | 91.34 |
| 1 | 285 | 8.66 | 3292 | 100.00 |

| DisplNabisco | Frequency | Percent | Cumulative Frequency | Cumulative Percent |
|--------------|-----------|---------|----------------------|--------------------|
| 0 | 2172 | 65.98 | 2172 | 65.98 |
| 1 | 1120 | 34.02 | 3292 | 100.00 |

2. Sampling Dataset

| The SAS System | |
|----------------------------|------------------------|
| The SURVEYSELECT Procedure | |
| Selection Method | Simple Random Sampling |
| Input Data Set | CRACKERS |
| Random Number Seed | 2 |
| Sampling Rate | 0.8 |
| Sample Size | 2634 |
| Selection Probability | 0.800122 |
| Sampling Weight | 0 |
| Output Data Set | CRACKERS_SAMPLED |

3. General Utility Model Equation

Allowing for the effect of price, display, and feature on utility to vary across brands, the utility equations are:

$$U_{ip} = \beta_p + \beta_{p1} price_{ip} + \beta_{p2} display_{ip} + \beta_{p3} feature_{ip} + \beta_{p4} price_{ip} * feature_{ip} + \epsilon_{ip}$$

$$U_{is} = \beta_s + \beta_{s1} price_{is} + \beta_{s2} display_{is} + \beta_{s3} feature_{is} + \beta_{s4} price_{is} * feature_{is} + \epsilon_{is}$$

$$U_{ik} = \beta_k + \beta_{k1} price_{ik} + \beta_{k2} display_{ik} + \beta_{k3} feature_{ik} + \beta_{k4} price_{ik} * feature_{ik} + \epsilon_{ik}$$

$$U_{in} = \beta_n + \beta_{n1} price_{in} + \beta_{n2} display_{in} + \beta_{n3} feature_{in} + \beta_{n4} price_{in} * feature_{in} + \epsilon_{in}$$

4. Formatted Data set

The data is not formatted as needed for using PROC LOGISTIC or PROC MDC. For each observation (purchase event for a single individual), each potential choice (brand) in the choice set should have its own row, as shown here:

Total rows: 13168 Total columns: 6

| | id | brand | brand_chosen | price | feature | displ |
|----|----|-------|--------------|-------------|---------|-------|
| 1 | 1 | 1 | 0 | 0.709999979 | 0 | 0 |
| 2 | 1 | 2 | 0 | 0.980000019 | 0 | 0 |
| 3 | 1 | 3 | 0 | 0.879999995 | 0 | 0 |
| 4 | 1 | 4 | 1 | 1.199999928 | 0 | 0 |
| 5 | 2 | 1 | 0 | 0.709999979 | 0 | 0 |
| 6 | 2 | 2 | 0 | 0.990000001 | 0 | 0 |
| 7 | 2 | 3 | 0 | 1.089999914 | 0 | 0 |
| 8 | 2 | 4 | 1 | 0.990000001 | 0 | 0 |
| 9 | 3 | 1 | 0 | 0.779999912 | 0 | 0 |
| 10 | 3 | 2 | 1 | 0.490000001 | 0 | 1 |
| 11 | 3 | 3 | 0 | 1.089999914 | 0 | 0 |
| 12 | 3 | 4 | 0 | 1.089999914 | 0 | 0 |

5. Multi-Logit Model using Logistic

We have used LOGISTIC to build a multi-logit model and have used Price, Feature, Display metrics along with a interaction variable of Price * Feature.

Model-Fit Statistics

| Model Fit Statistics | | |
|----------------------|--------------------|-----------------|
| Criterion | Without Covariates | With Covariates |
| AIC | 7302.999 | 5301.795 |
| SC | 7302.999 | 5417.996 |
| -2 Log L | 7302.999 | 5269.795 |

Model performance compared to the null model

| Testing Global Null Hypothesis: BETA=0 | | | |
|--|------------|----|------------|
| Test | Chi-Square | DF | Pr > ChiSq |
| Likelihood Ratio | 2033.2040 | 16 | <.0001 |
| Score | 1931.3418 | 16 | <.0001 |
| Wald | 1316.8636 | 16 | <.0001 |

Parameter Estimates

- We can see from the Logit model that result for the Intercept of Nabisco, Sunshine are significant with the intercept 1.6671 and -0.8448 respectively. It is insignificant for Keebler at $Pr > 0.0085$ level.
- Price is a significant variable in the model and has an intercept of -2.9949 for all the crackers
- Feature variable is only significant for Nabisco brand with intercept of 8.3761.
- All the brand variables if they are on display are insignificant $Pr > 0.0001$. The intercept for Keebler, Nabisco, Sunshine and Private cracker while on display are 9.1745, 8.37, 1.44 and 2.12 respectively
- If the interaction of Price and Feature takes place, then the results are only consistent for Nabisco brand with the intercept of -7.4445

| Analysis of Conditional Maximum Likelihood Estimates | | | | | | |
|--|----------|----|----------|----------------|-----------------|------------|
| Parameter | | DF | Estimate | Standard Error | Wald Chi-Square | Pr > ChiSq |
| cracker_choice | Keebler | 1 | -0.3728 | 0.1417 | 6.9200 | 0.0085 |
| cracker_choice | Nabisco | 1 | 1.6671 | 0.1168 | 203.6067 | <.0001 |
| cracker_choice | Sunshine | 1 | -0.8448 | 0.1170 | 52.1311 | <.0001 |
| cracker_choice | Private | 0 | 0 | . | . | . |
| price | | 1 | -2.9949 | 0.2425 | 152.5672 | <.0001 |
| feature*cracker_choi | Keebler | 1 | 9.1745 | 3.8512 | 5.6751 | 0.0172 |
| feature*cracker_choi | Nabisco | 1 | 8.3761 | 1.9827 | 17.8464 | <.0001 |
| feature*cracker_choi | Sunshine | 1 | 1.4477 | 1.2261 | 1.3941 | 0.2377 |
| feature*cracker_choi | Private | 1 | 2.1290 | 2.0448 | 1.0840 | 0.2978 |
| displ*cracker_choice | Keebler | 1 | 0.3339 | 0.2361 | 2.0005 | 0.1573 |
| displ*cracker_choice | Nabisco | 1 | 0.1294 | 0.0880 | 2.1652 | 0.1412 |
| displ*cracker_choice | Sunshine | 1 | 0.4357 | 0.1890 | 5.3165 | 0.0211 |
| displ*cracker_choice | Private | 1 | -0.2728 | 0.1724 | 2.5036 | 0.1136 |
| price*featur*cracker | Keebler | 1 | -8.3964 | 3.8483 | 4.7603 | 0.0291 |
| price*featur*cracker | Nabisco | 1 | -7.4445 | 1.8708 | 15.8350 | <.0001 |
| price*featur*cracker | Sunshine | 1 | -0.9238 | 1.7107 | 0.2916 | 0.5892 |
| price*featur*cracker | Private | 1 | -3.7874 | 3.9808 | 0.9052 | 0.3414 |

Explanation of Parameter Estimates

- 1 Keebler and Sunshine generate lower Utility than Private cracker if everything else is same
- 2 Nabisco generate higher Utility than Private crackers if everything else is same
- 3 If price increases, the purchase probabilities will drop for all the brands
- 4 If there is a feature for a product in store, the purchase probability will increase, Keebler store feature has the strongest effect than Nabisco, Sunshine and Private cracker brands
- 5 If there is a display for a product in store, the purchase probability will increase for all the brand except for Private Cracker. Keebler has the strongest effect of Store Display when compared to other brands.
- 5 Interaction effect of Price and Feature indicate that the purchase probability will decrease if the price of cracker is increased and is on feature for each particular crackers brand

| Analysis of Conditional Maximum Likelihood Estimates | | | | | | | |
|--|----------------------|----------|----------|----------------|-----------------|------------|--------|
| Parameter | | DF | Estimate | Standard Error | Wald Chi-Square | Pr > ChiSq | |
| 1 | cracker_choice | Keebler | 1 | -0.3728 | 0.1417 | 6.9200 | 0.0085 |
| | cracker_choice | Nabisco | 1 | 1.6671 | 0.1168 | 203.6067 | <.0001 |
| | cracker_choice | Sunshine | 1 | -0.8448 | 0.1170 | 52.1311 | <.0001 |
| | cracker_choice | Private | 0 | 0 | . | . | . |
| 2 | price | | 1 | -2.9949 | 0.2425 | 152.5672 | <.0001 |
| 3 | feature*cracker_choi | Keebler | 1 | 9.1745 | 3.8512 | 5.6751 | 0.0172 |
| | feature*cracker_choi | Nabisco | 1 | 8.3761 | 1.9827 | 17.8464 | <.0001 |
| | feature*cracker_choi | Sunshine | 1 | 1.4477 | 1.2261 | 1.3941 | 0.2377 |
| | feature*cracker_choi | Private | 1 | 2.1290 | 2.0448 | 1.0840 | 0.2978 |
| 4 | displ*cracker_choice | Keebler | 1 | 0.3339 | 0.2361 | 2.0005 | 0.1573 |
| | displ*cracker_choice | Nabisco | 1 | 0.1294 | 0.0880 | 2.1652 | 0.1412 |
| | displ*cracker_choice | Sunshine | 1 | 0.4357 | 0.1890 | 5.3165 | 0.0211 |
| | displ*cracker_choice | Private | 1 | -0.2728 | 0.1724 | 2.5036 | 0.1136 |
| 5 | price*featur*cracker | Keebler | 1 | -8.3964 | 3.8483 | 4.7603 | 0.0291 |
| | price*featur*cracker | Nabisco | 1 | -7.4445 | 1.8708 | 15.8350 | <.0001 |
| | price*featur*cracker | Sunshine | 1 | -0.9238 | 1.7107 | 0.2916 | 0.5892 |
| | price*featur*cracker | Private | 1 | -3.7874 | 3.9808 | 0.9052 | 0.3414 |

6. Multi Logit Model using PROC MDC

Parameter Estimates using MDC commands

We have reproduced the above Multi Logit model using PROC MDC and the result are consistent with the PROC LOGISTIC command.

Logit Model using MDC commands

The MDC Procedure

Conditional Logit Estimates

| Parameter Estimates | | | | | | |
|-------------------------------|----|-----------|----------------|---------|----------------|-----------------|
| Parameter | DF | Estimate | Standard Error | t Value | Approx Pr > t | Parameter Label |
| CRACKER_CHOICEPrivate | 0 | 0 | 0 | | | |
| CRACKER_CHOICESunshine | 1 | -0.8448 | 0.1170 | -7.22 | <.0001 | |
| CRACKER_CHOICEKeebler | 1 | -0.3728 | 0.1417 | -2.63 | 0.0085 | |
| CRACKER_CHOICENabisco | 1 | 1.6671 | 0.1168 | 14.27 | <.0001 | |
| price | 1 | -2.9949 | 0.2425 | -12.35 | <.0001 | |
| CRACKER_CHOICEPrivateFEATURE | 1 | 2.1290 | 2.0448 | 1.04 | 0.2978 | |
| CRACKER_CHOICESunshineFEATURE | 1 | 1.4477 | 1.2261 | 1.18 | 0.2377 | |
| CRACKER_CHOICEKeeblerFEATURE | 1 | 9.1745 | 3.8512 | 2.38 | 0.0172 | |
| CRACKER_CHOICENabiscoFEATURE | 1 | 8.3761 | 1.9827 | 4.22 | <.0001 | |
| CRACKER_CHOICEPrivateDISPL | 1 | -0.2728 | 0.1724 | -1.58 | 0.1136 | |
| CRACKER_CHOICESunshineDISPL | 1 | 0.4357 | 0.1890 | 2.31 | 0.0211 | |
| CRACKER_CHOICEKeeblerDISPL | 1 | 0.3339 | 0.2361 | 1.41 | 0.1573 | |
| CRACKER_CHOICENabiscoDISPL | 1 | 0.1294 | 0.0880 | 1.47 | 0.1412 | |
| CRACKER_CHOICEPrivate2 | 1 | -3.7874 | 3.9808 | -0.95 | 0.3414 | |
| CRACKER_CHOICESunshine2 | 1 | -0.9238 | 1.7107 | -0.54 | 0.5892 | |
| CRACKER_CHOICEKeebler2 | 1 | -8.3964 | 3.8483 | -2.18 | 0.0291 | |
| CRACKER_CHOICENabisco2 | 1 | -7.4445 | 1.8708 | -3.98 | <.0001 | |
| Restrict1 | 1 | 5.0749E-7 | 12.2611 | 0.00 | 1.0000* | Linear EC [1] |

Goodness of Fit measures

| Model Fit Summary | |
|-------------------------------|----------------|
| Dependent Variable | brand_chosen |
| Number of Observations | 2634 |
| Number of Cases | 10536 |
| Log Likelihood | -2635 |
| Log Likelihood Null (LogL(0)) | -3651 |
| Maximum Absolute Gradient | 7.28365E-7 |
| Number of Iterations | 5 |
| Optimization Method | Newton-Raphson |
| AIC | 5302 |
| Schwarz Criterion | 5396 |

| Goodness-of-Fit Measures | | |
|--|--------|--|
| Measure | Value | Formula |
| Likelihood Ratio (R) | 2033.2 | $2 * (\text{LogL} - \text{LogL0})$ |
| Upper Bound of R (U) | 7303 | $-2 * \text{LogL0}$ |
| Aldrich-Nelson | 0.4356 | $R / (R+N)$ |
| Cragg-Uhler 1 | 0.5379 | $1 - \exp(-R/N)$ |
| Cragg-Uhler 2 | 0.5737 | $(1 - \exp(-R/N)) / (1 - \exp(-U/N))$ |
| Estrella | 0.5953 | $1 - (1 - R/U)^{(U/N)}$ |
| Adjusted Estrella | 0.588 | $1 - ((\text{LogL} - K) / \text{LogL0})^{(-2/N * \text{LogL0})}$ |
| McFadden's LRI | 0.2784 | R / U |
| Veall-Zimmermann | 0.5928 | $(R * (U+N)) / (U * (R+N))$ |
| N = # of observations, K = # of regressors | | |

7. PROBIT Model using PROC MDC

Model Fit Statistics

- While comparing the Model Fit summary, we see that PROBIT model perform better than Logit Model since it has less AIC, though it is very minute difference

| PROBIT Model Fit Summary | |
|-------------------------------|----------------|
| Dependent Variable | brand_chosen |
| Number of Observations | 2634 |
| Number of Cases | 10536 |
| Log Likelihood | -2635 |
| Log Likelihood Null (LogL(0)) | -3651 |
| Maximum Absolute Gradient | 7.28365E-7 |
| Number of Iterations | 5 |
| Optimization Method | Newton-Raphson |
| AIC | 5302 |
| Schwarz Criterion | 5396 |

| LOGIT Model Fit Summary | |
|-----------------------------------|-------------------|
| Dependent Variable | brand_chosen |
| Number of Observations | 2634 |
| Number of Cases | 10536 |
| Log Likelihood | -2632 |
| Log Likelihood Null (LogL(0)) | -3651 |
| Maximum Absolute Gradient | 0.06861 |
| Number of Iterations | 90 |
| Optimization Method | Dual Quasi-Newton |
| AIC | 5306 |
| Schwarz Criterion | 5430 |
| Number of Simulations | 100 |
| Starting Point of Halton Sequence | 11 |

Ques 7

Goodness of Fit Measures

| Goodness-of-Fit Measures | | |
|--|--------|--|
| Measure | Value | Formula |
| Likelihood Ratio (R) | 2038.9 | $2 * (\text{LogL} - \text{LogL0})$ |
| Upper Bound of R (U) | 7303 | $-2 * \text{LogL0}$ |
| Aldrich-Nelson | 0.4363 | $R / (R+N)$ |
| Cragg-Uhler 1 | 0.5389 | $1 - \exp(-R/N)$ |
| Cragg-Uhler 2 | 0.5748 | $(1 - \exp(-R/N)) / (1 - \exp(-U/N))$ |
| Estrella | 0.5965 | $1 - (1 - R/U)^{(U/N)}$ |
| Adjusted Estrella | 0.5893 | $1 - ((\text{LogL} - K) / \text{LogL0})^{(-2/N * \text{LogL0})}$ |
| McFadden's LRI | 0.2792 | R / U |
| Veall-Zimmermann | 0.5937 | $(R * (U+N)) / (U * (R+N))$ |
| N = # of observations, K = # of regressors | | |

Ques 7

Ques 6

| Goodness-of-Fit Measures | | |
|--|--------|--|
| Measure | Value | Formula |
| Likelihood Ratio (R) | 2033.2 | $2 * (\text{LogL} - \text{LogL0})$ |
| Upper Bound of R (U) | 7303 | $-2 * \text{LogL0}$ |
| Aldrich-Nelson | 0.4356 | $R / (R+N)$ |
| Cragg-Uhler 1 | 0.5379 | $1 - \exp(-R/N)$ |
| Cragg-Uhler 2 | 0.5737 | $(1 - \exp(-R/N)) / (1 - \exp(-U/N))$ |
| Estrella | 0.5953 | $1 - (1 - R/U)^{(U/N)}$ |
| Adjusted Estrella | 0.588 | $1 - ((\text{LogL} - K) / \text{LogL0})^{(-2/N * \text{LogL0})}$ |
| McFadden's LRI | 0.2784 | R / U |
| Veall-Zimmermann | 0.5928 | $(R * (U+N)) / (U * (R+N))$ |
| N = # of observations, K = # of regressors | | |

Ques 6

Like-hood Ratio are different in two results, Probit model is better than Multi-logit model on goodness-of-fit.

Difference: Logit vs Probit model

- Multi-Logit model suffers from IIA issue to capture asymmetric switching patterns
- Estimates under multinomial PROBIT model are different from conditional LOGIT model since all the intercept are bit increased for Probit Model
- In Logit model, five significant variables are in the result, which are Intercept for Sunshine& Nabisco, price, Nabisco when featured and when Nabisco when featured and price is increased.
- However, we can see in the Probit model, only Nabisco and price are significant parameter.
- Estimates for Intercept of Keebler brand has a positive effect compared to -ve intercept in Logit model
- Other Estimates of PROBIT model have consistent sign but increased value

PROBIT Model using MDC commands**The MDC Procedure****Multinomial Probit Estimates**

| Parameter Estimates | | | | | | |
|-------------------------------|----|----------|----------------|---------|----------------|-----------------|
| Parameter | DF | Estimate | Standard Error | t Value | Approx Pr > t | Parameter Label |
| CRACKER_CHOICEPrivate | 0 | 0 | 0 | | | |
| CRACKER_CHOICESunshine | 1 | -0.4672 | 0.3484 | -1.34 | 0.1799 | |
| CRACKER_CHOICEKeebler | 1 | 0.2625 | 0.3673 | 0.71 | 0.4747 | |
| CRACKER_CHOICENabisco | 1 | 1.6545 | 0.3006 | 5.50 | <.0001 | |
| price | 1 | -2.6182 | 0.4121 | -6.35 | <.0001 | |
| CRACKER_CHOICEPrivateFEATURE | 1 | 1.7677 | 1.9531 | 0.91 | 0.3654 | |
| CRACKER_CHOICESunshineFEATURE | 1 | 1.1725 | 1.1719 | 1.00 | 0.3171 | |
| CRACKER_CHOICEKeeblerFEATURE | 1 | 4.6624 | 2.6488 | 1.76 | 0.0784 | |
| CRACKER_CHOICENabiscoFEATURE | 1 | 6.8948 | 1.9342 | 3.56 | 0.0004 | |
| CRACKER_CHOICEPrivateDISPL | 1 | -0.2656 | 0.1819 | -1.46 | 0.1442 | |
| CRACKER_CHOICESunshineDISPL | 1 | 0.2250 | 0.1668 | 1.35 | 0.1774 | |
| CRACKER_CHOICEKeeblerDISPL | 1 | 0.1617 | 0.1529 | 1.06 | 0.2903 | |
| CRACKER_CHOICENabiscoDISPL | 1 | 0.0908 | 0.0790 | 1.15 | 0.2507 | |
| CRACKER_CHOICEPrivate2 | 1 | -2.9178 | 3.7479 | -0.78 | 0.4363 | |
| CRACKER_CHOICESunshine2 | 1 | -0.8477 | 1.5730 | -0.54 | 0.5900 | |
| CRACKER_CHOICEKeebler2 | 1 | -4.3079 | 2.6163 | -1.65 | 0.0996 | |
| CRACKER_CHOICENabisco2 | 1 | -6.1862 | 1.7958 | -3.44 | 0.0006 | |
| STD_1 | 1 | 1.4471 | 0.3864 | 3.75 | 0.0002 | |
| STD_2 | 1 | 1.1337 | 0.3654 | 3.10 | 0.0019 | |
| RHO_21 | 1 | -0.4053 | 0.5582 | -0.73 | 0.4678 | |
| RHO_31 | 1 | -0.0865 | 0.4985 | -0.17 | 0.8623 | |
| RHO_32 | 1 | 0.4856 | 0.2121 | 2.29 | 0.0220 | |
| Restrict1 | 1 | 0.0137 | . | . | . * | Linear EC [1] |

8. Probit Logit Model Selection

- We can compare the likelihood among four models below, which is indicating the goodness-of-fit. The highest one is Probit model in question 7, which doesn't have any RESTRICT when coding.
- Yes, there is IIA property associated with the Logit Model since the intercept are not consistent for Logit model when compared to all the other model shown below.

PROBIT

| Goodness-of-Fit Measures | | |
|--|--------|--|
| Measure | Value | Formula |
| Likelihood Ratio (R) | 2038.9 | $2 * (\text{LogL} - \text{LogL0})$ |
| Upper Bound of R (U) | 7303 | $-2 * \text{LogL0}$ |
| Aldrich-Nelson | 0.4363 | $R / (R+N)$ |
| Cragg-Uhler 1 | 0.5389 | $1 - \exp(-R/N)$ |
| Cragg-Uhler 2 | 0.5748 | $(1 - \exp(-R/N)) / (1 - \exp(-U/N))$ |
| Estrella | 0.5965 | $1 - (1 - R/U)^{(U/N)}$ |
| Adjusted Estrella | 0.5893 | $1 - ((\text{LogL} - K) / \text{LogL0})^{(-2/N * \text{LogL0})}$ |
| McFadden's LRI | 0.2792 | R / U |
| Veall-Zimmermann | 0.5937 | $(R * (U+N)) / (U * (R+N))$ |
| N = # of observations, K = # of regressors | | |

Result in question 7

| Goodness-of-Fit Measures | | |
|--|--------|--|
| Measure | Value | Formula |
| Likelihood Ratio (R) | 2037.2 | $2 * (\text{LogL} - \text{LogL0})$ |
| Upper Bound of R (U) | 7303 | $-2 * \text{LogL0}$ |
| Aldrich-Nelson | 0.4361 | $R / (R+N)$ |
| Cragg-Uhler 1 | 0.5386 | $1 - \exp(-R/N)$ |
| Cragg-Uhler 2 | 0.5745 | $(1 - \exp(-R/N)) / (1 - \exp(-U/N))$ |
| Estrella | 0.5962 | $1 - (1 - R/U)^{(U/N)}$ |
| Adjusted Estrella | 0.5889 | $1 - ((\text{LogL} - K) / \text{LogL0})^{(-2/N * \text{LogL0})}$ |
| McFadden's LRI | 0.279 | R / U |
| Veall-Zimmermann | 0.5934 | $(R * (U+N)) / (U * (R+N))$ |
| N = # of observations, K = # of regressors | | |

Result in question 8 - I

| Goodness-of-Fit Measures | | |
|--|--------|--|
| Measure | Value | Formula |
| Likelihood Ratio (R) | 2035.1 | $2 * (\text{LogL} - \text{LogL0})$ |
| Upper Bound of R (U) | 7303 | $-2 * \text{LogL0}$ |
| Aldrich-Nelson | 0.4359 | $R / (R+N)$ |
| Cragg-Uhler 1 | 0.5382 | $1 - \exp(-R/N)$ |
| Cragg-Uhler 2 | 0.5741 | $(1 - \exp(-R/N)) / (1 - \exp(-U/N))$ |
| Estrella | 0.5957 | $1 - (1 - R/U)^{(U/N)}$ |
| Adjusted Estrella | 0.5884 | $1 - ((\text{LogL} - K) / \text{LogL0})^{(-2/N * \text{LogL0})}$ |
| McFadden's LRI | 0.2787 | R / U |
| Veall-Zimmermann | 0.5931 | $(R * (U+N)) / (U * (R+N))$ |
| N = # of observations, K = # of regressors | | |

Result in question 8 - II

| Goodness-of-Fit Measures | | |
|--|--------|--|
| Measure | Value | Formula |
| Likelihood Ratio (R) | 2030.8 | $2 * (\text{LogL} - \text{LogL0})$ |
| Upper Bound of R (U) | 7303 | $-2 * \text{LogL0}$ |
| Aldrich-Nelson | 0.4353 | $R / (R+N)$ |
| Cragg-Uhler 1 | 0.5375 | $1 - \exp(-R/N)$ |
| Cragg-Uhler 2 | 0.5733 | $(1 - \exp(-R/N)) / (1 - \exp(-U/N))$ |
| Estrella | 0.5948 | $1 - (1 - R/U)^{(U/N)}$ |
| Adjusted Estrella | 0.5875 | $1 - ((\text{LogL} - K) / \text{LogL0})^{(-2/N * \text{LogL0})}$ |
| McFadden's LRI | 0.2781 | R / U |
| Veall-Zimmermann | 0.5924 | $(R * (U+N)) / (U * (R+N))$ |
| N = # of observations, K = # of regressors | | |

Result in question 8 - III

9. Analysis for Nabisco

Normal Model

There are 418 Nabisco customer who predicted probability of more than 0.5 in the test dataset.

Nabisco Market Share = $418 / 2632 = 15.88\%$

1st Model: 10% Price Decrease

We decreased the Price of Nabisco by 10% and re analyzed the Market Share of the model.

Market Share = $548 / 2632 = 20.8\%$

There is increase of 4.92% market share using strategy 1.

2nd Model: Always on Feature

We put Nabisco always on feature and re-analyzed the Market Share of the model.

Market Share = $655 / 2632 = 24.8\%$

There is increase of 9% market share using strategy 2.

Conclusion: Since the Market Share increase more if we put Nabisco on Feature by 9%. Therefore, the brand Manager should implement second strategy.

Note: see code below

10. Conclusion:

Dataset has 3 main brands with all other brands combines as private. Dataset has (i) price of each 4 categories, (ii) display and store feature. By analyzing dataset, Nabisco has highest market share, and display and store feature have been used more frequently for Nabisco.

As per Logit model, price is significant for all category. Feature is significant only for Nabisco, display feature is insignificant for all brand and price-feature factor is significant for Nabisco only.

So, feature has positive effect on sales of Nabisco. Price has negative effect on sales of all brand.

As a brand manager of Nabisco, we would recommend decreasing price, and increasing store feature and price-feature factor to increase market share.

As a brand manager of Keeble, we would recommend decreasing price, increasing feature and display.

As a brand manager of Sunshine, we would recommend decreasing price, increasing feature and display.

As a brand manager of Private, we would recommend decreasing price, increasing feature and decrease display.

APPENDIX

```
/*Homework:4*/
```

```
LIBNAME HW4 'H:\My SAS Files\HW4';
```

```
PROC IMPORT OUT= HW4.Crackers
```

```
    DATAFILE= "H:\My SAS Files\HW4\crackers.csv"
```

```
    DBMS=CSV REPLACE;
```

```
    GETNAMES=YES;
```

```
    DATAROW=2;
```

```
RUN;
```

```
DATA Crackers;
```

```
SET HW4.Crackers;
```

```
RUN;
```

```
/*1. Based on the previous lectures, provide a professional summary statistic of this
dataset.
Your summary should briefly explain the status of crackers brands in the market, based on
the above dataset?
For example: which brand has the highest market share? Is there any difference between
the average prices of these brands?
Which brand does provide display or feature in store more frequently? And, ... */
```

```
proc freq data=Crackers;
```

```
tables PRIVATE SUNSHINE KEEBLER NABISCO;
```

```
run;
```

```
PROC MEANS DATA=Crackers;
```

```
VAR PRICEPRIVATE PRICESUNSHINE PRICEKEEBLER PRICENABISCO;
```

```
RUN;
```

```
proc freq data=Crackers;
```

```
tables FeatPrivate FeatSunshine FeatKeebler FeatNabisco DisplPrivate DisplSunshine
DisplKeebler DisplNabisco;
```

```
run;
```



```

/*2*/

proc surveyselect
data= Crackers
out=crackers_sampled
outall samprate=0.8
seed=2;
run;

data crackers_training crackers_test;
set crackers_sampled;
if selected=1 then
output crackers_training;
else
output crackers_test;
run;
/*3*//*no code*/

/*4*//*need numeric choice in order to convert format*/
data crackers_training;

set crackers_training;

if (Private=1) & (Sunshine=0) & (Keebler=0) & (Nabisco=0) then Choice=1;
if (Private=0) & (Sunshine=1) & (Keebler=0) & (Nabisco=0) then Choice=2;
if (Private=0) & (Sunshine=0) & (Keebler=1) & (Nabisco=0) then Choice=3;
if (Private=0) & (Sunshine=0) & (Keebler=0) & (Nabisco=1) then Choice=4;

run;

data crackers_test;

set crackers_test;

if (Private=1) & (Sunshine=0) & (Keebler=0) & (Nabisco=0) then Choice=1;
if (Private=0) & (Sunshine=1) & (Keebler=0) & (Nabisco=0) then Choice=2;
if (Private=0) & (Sunshine=0) & (Keebler=1) & (Nabisco=0) then Choice=3;
if (Private=0) & (Sunshine=0) & (Keebler=0) & (Nabisco=1) then Choice=4;

run;

/*converting data*/

data crackers_training(keep=id brand brand_chosen price feature displ);
set crackers_training;
array price_vector{4} priceprivate pricesunshine pricekeebler pricenabisco;
array feature_vector{4} featprivate featsunshine featkeebler featnabisco;
array display_vector{4} displprivate displsunshine displkeebler displnabisco;
retain id 0;
id + 1;
do i=1 to 4;
brand=i;
brand_chosen=(choice=i);
price=price_vector{i};

```

```

feature=feature_vector{i};
displ=display_vector{i};
output;
end;
run;

data crackers_test(keep=id brand brand_chosen price feature displ);
set crackers_test;
array price_vector{4} priceprivate pricesunshine pricekeebler pricenabisco;
array feature_vector{4} featprivate featsunshine featkeebler featnabisco;
array display_vector{4} displprivate displsunshine displkeebler displnabisco;
retain id 0;
id + 1;
do i=1 to 4;
brand=i;
brand_chosen=(choice=i);
price=price_vector{i};
feature=feature_vector{i};
displ=display_vector{i};
output;
end;
run;

```

```

data crackers_training;

set crackers_training;

if brand='1' then cracker_choice='Private ';
if brand='2' then cracker_choice='Sunshine';
if brand='3' then cracker_choice='Keebler';
if brand='4' then cracker_choice='Nabisco';

drop brand;

run;

```

```

data crackers_test;

set crackers_test;

if brand='1' then cracker_choice='Private ';
if brand='2' then cracker_choice='Sunshine';
if brand='3' then cracker_choice='Keebler';
if brand='4' then cracker_choice='Nabisco';

drop brand;

run;

```

```

/* Ques 5: Estimate the logit model on the training sample using PROC LOGISTIC and report
the estimation results.
Please set the Private intercept equal to zero as the based. You need to report model
parameters, significance.
Also, provide bullet points on the meaning of the estimations results in terms of
consumers' utility by purchasing a brand. */

```

```
proc logistic data=crackers_training;
  strata id;
  class cracker_choice (ref = 'Private') / param=glm;
  model brand_chosen (event='1') = cracker_choice price cracker_choice*feature
  cracker_choice*displ cracker_choice*price*feature;
```

```
  title 'Logit Model using Logistic commands';
```

```
run;
```

/*Ques 6: Reproduce your results in Q5 using PROC MDC (HINT: See the SAS code posted for the lecture for examples of replicating the results with PROC MDC. You can use the same dataset format. Refer to the SAS manual for more details about PROC MDC.

You will need to use "type=clogit" to estimate a multinomial model, and "nchoice=4" to indicate there are four alternatives for each choice occasion.

In PROC MDC, using the CLASS statement for a categorical variable with N levels will create N dummy variables, each for one level of the categorical variable. Use the restrict statement to set the coefficient for one of the dummy variables to zero - effectively omitting this dummy variable. You will need to do this for the main effects and any interaction effects that involve the variable used in the CLASS statement - refer to the SAS code for the lecture for an example. Also, you cannot insert the interaction effect price *feature directly into PROC MDC. First define a new variable as price *feature, then insert it into model.

```
*/
```

```
data crackers_training1;
set crackers_training;
price_feature=price*feature;
run;
```

```
proc mdc data = crackers_training1;
  id id;
  class cracker_choice;
  model brand_chosen = cracker_choice price cracker_choice*feature cracker_choice*displ
  cracker_choice*price_feature / type = clogit
  nchoice = 4;
  restrict cracker_choicePrivate=0; /* mdc does not allow flexible options to code class
  variable. Need to explicitly force reference levels to zero */
  title 'Logit Model using MDC commands';
```

```
run;
```

/*7. Now use the model in Q5, and estimate the PROBIT model using PROC MDC.

Do the estimation results look similar to Q6? Explain the differences.*/

/* Multinomial Probit with out restricting errors (it follows the basic setting in SAS) */

```
proc mdc data = crackers_sampled_mdc;
  id id;
  class cracker_purchase;
```

```

model Brand_purchase = cracker_purchase price cracker_purchase*feature
cracker_purchase*displ cracker_purchase*pricefeature / type = mprobit nchoice = 4;
restrict cracker_purchasePrivate=0;
/* mdc does not allow flexible options to code class variable. Need to explicitly force
reference levels to zero */
run;
ODS RTF close;

```

```

data crackers_training1;
set crackers_training;
price_feature=price*feature;
run;

```

```

proc mdc data = crackers_training1;
  id id;
  class cracker_choice;
  model brand_chosen = cracker_choice price cracker_choice*feature cracker_choice*displ
cracker_choice*price_feature / type = mprobit
nchoice = 4;
restrict cracker_choicePrivate=0; /* mdc does not allow flexible options to code class
variable. Need to explicitly force reference levels to zero */
title 'PROBIT Model using MDC commands';

run;

```

/*8. In this Question, you need to estimate three new versions of the PROBIT model used in Q7.

I. Estimate the model where the error terms are normally distributed, independently and identically.

This is equivalent that the covariance matrix is the identity matrix. II.

Estimate the model where the error terms are normally and independently distributed, but allow for existence of heteroscedasticity.

This is equivalent that the covariance matrix is a diagonal matrix. III. Estimate the model where the error terms are normally distributed,

there is no existence of heteroscedasticity, and the errors are correlated. This is equivalent that the covariance matrix is a matrix

such that (1) all diagonal elements are equal to 1, and (2) there are non-zero correlations among alternatives

(i.e., the off-diagonal elements are non-zero). (HINT: See the SAS code posted for the lecture about PROC MDC.

Use the restrict statement to set the right parameters to zero to generate the above models.

Note that all the above four models (Q7 and three models in Q8) are nested

model. Therefore, you can use the Loglikelihood to choose the

best model that fits into data. Now, based on your answer, is there any evidence against IIA property in this data, which is existed by

using logit model in Q6? /*I: Multinomial Probit allowing errors to be correlated, but restricting them to be unit variance*/

```

proc mdc data = crackers_sampled_mdc;
  id id;
  class cracker_purchase;
  model Brand_purchase = cracker_purchase price cracker_purchase*feature
cracker_purchase*displ cracker_purchase*pricefeature / type = mprobit nchoice = 4
unitvariance= (1 2 3 4);
/*diagonal elements equal to each other*/

```

```

restrict cracker_purchasePrivate=0; /* mdc does not allow flexible options to code class
variable.
Need to explicitly force reference levels to zero */
run;
ODS RTF close; /*II:multinomial Probitrestricting errors to be uncorrelated, but allowing
heteroschedasticity*/
proc mdc data = crackers_sampled_mdc;
id id;class cracker_purchase;
model Brand_purchase =cracker_purchase price cracker_purchase*feature
cracker_purchase*displ cracker_purchase*pricefeature/ type = mprobit nchoice = 4 ;
restrict cracker_purchasePrivate=0;
/* mdc does not allow flexible options to code class variable. Need to explicitly force
reference levels to zero */
restrict rho_21=0;
restrict rho_31=0;
restrict rho_32=0;
/* Allows heteroschedasticity, the variance of each predictor does not need to be the
same; error terms uncorrelated, then covariance
must be equal to zero,And because SAS automatically defaults the RHO of the bottom row to
zero (rho_41 ~ rho_43),
you only need to define the first two rows separately.*/
run;
ODS RTF close;
/*III:Multinomial Probit restricting errors to be iid*/
proc mdc data= crackers_sampled_mdc;
id id;
class cracker_purchase;
model Brand_purchase =cracker_purchaseprice cracker_purchase*feature
cracker_purchase*displ cracker_purchase*pricefeature /type = mprobit nchoice = 4
unitvariance= (1 2 3 4);
restrict cracker_purchasePrivate=0;
/* mdc does not allow flexible options to code class variable. Need to explicitly force
reference levels to zero */
restrict rho_21=0;
restrict rho_31=0;
restrict rho_32=0;
run;
ODS RTF close;
/*9. Now re-consider your model in Q6, i.e., the logit model. First, find the
predicted probability for each brand on your test dataset.
Nabisco brand manager believes if the predicted probability of busying Nabisco is greater
than 50%, the consumer will buy it for sure.
Use the predicted probabilities and 50% threshold to find Nabisco market share based on
test dataset. */

/*Now, the Nabisco brand manager has two strategies to increase its market share. I-
reducing their price by 10% or II-having feature in store
always. Now, based on test dataset and your model in Q6, find how far the Nabisco's
market share will increase by implementing one of these two
strategies? If we assume the implementation cost of both strategies are equal, which one
will be more profitable?
(Hint: You can follow the threshold 50% to find who buys Nabisco under the above
strategies in test dataset.) */

/*Taking the training data set and adding a new column selected which is equal to 1*/
data crackers_training;
set crackers_training;
selected=1;

```

```
run;
```

```
/*Taking the test data and making the field brand_chosen as null*/
```

```
data crackers_test;
set crackers_test;
brand_chosen = .;
selected=0;
price_feature=price*feature;
run;
```

```
/*Aggregating training and test data*/
```

```
data extdata;
set crackers_training crackers_test;
run;
```

```
/*Using proc mdc data and getting the predicting probabilities*/
```

```
proc mdc data = extdata;
id id;
class cracker_choice;
model brand_chosen = cracker_choice price cracker_choice*feature cracker_choice*displ
cracker_choice*price_feature / type = clogit nchoice = 4;
restrict cracker_choicePrivate=0;
output out= probdata pred = p;
run;
```

```
/*Getting the data for Nabisco for the probability greater than 0.5*/
```

```
data probdata_nabisco;
set probdata;
where cracker_choice = 'Nabisco' and p >= 0.50 and brand_chosen=.;
run;
```

9.I

```
/*Reducing the price by 10% and creating new data set with price reduced by 10$*/
```

```
data crackers_test_price;
set crackers_test;
if cracker_choice = 4 then price = price -(0.1 * price);
run;
```

```
/*Aggregating test and training data set*/
```

```
data extdata_price;
set crackers_training1 crackers_test_price;
run;
```

```
/*Predicting probabilities for new price data set*/
```

```
proc mdc data = extdata_price;
id id;
class cracker_choice;
model brand_chosen = cracker_choice price feature displ price_feature / type =
clogitcovest = hess nchoice = 4;
restrict cracker_choicePrivate=0;
output out= probdata_price pred = p;
run;
```

```
/*Getting the data for Nabisco for the probability greater than 0.5*/
```

```
data probdata_nabisco;
set probdata;
where cracker_choice = 'Nabisco' and p >= 0.50 and brand_chosen=.;
run;
```

```
9.II
/*Creating new data set with feature for Nebisco*/
data crackers_test_feature;
set crackers_test;
if cracker_choice = 4 then feature = 1;
run;

/*Aggregating training and test data*/
data extdata_feature;
set crackers_training1 crackers_test_feature;
run;

/*Predicting probabilities for feature data set*/
proc mdc data = extdata_feature;
id id;
class cracker_choice;
model brand_chosen = cracker_choice price feature displ price_feature / type =
clogitcovest = hess nchoice = 4;
restrict cracker_choicePrivate=0;
output out= probdata_feature pred = p;
run;

/*Getting the data for Nabisco for the probability greater than 0.5*/
data probdata_nabisco;
set probdata;
where cracker_choice = 'Nabisco' and p >= 0.50 and ;
run;
```