

Lab-4_Documentation

11.c

```
#include <stdio.h>
#include <stdlib.h>
#include <string.h>
```

```
//Code to parse integer from a string
```

```
int stoi(char *str)           // converts string input str to integer
{
    int x;
    sscanf(str, "%d", &x);
    return x;
}
```

```
int heapSize=0;
```

```
void swap(int *x, int *y)     // swap the input integer pointer values
{
    int temp;
    temp = *x;
    *x = *y;
    *y = temp;
}
```

```
void maxHeapify(int A[],int i) // takes an index i , makes it max_heapify until it
reach condition of max_heapify at that index or until it reaches a leaf (as leaf are
by default max_heapify).
```

```
{
    if(i>heapSize)
        // checks if the index is greater than heapSize, if yes return -1
```

```
        return -1;
```

```
    int lar = i;           // store index in an integer lar
```

```
    if(A[i]<A[2*i+1] && 2*i+1<heapSize)
```

```
    // if A[i] is smaller than A[2i+1] (it's child) then store the larger value in the integer
    lar
```

```
        lar = 2*i+1;           // now lar can be i or 2*i+1
```

if(A[2*i+2]>A[lar] && 2*i+2<heapSize) // now if A[2*i+2] is the greater A[lar], means A[2*i+2] is the largest , swap it with the A[i] and do max_heapify at 2*i +2 th position

```
{
    lar = 2*i+2;
    swap(&A[i], &A[lar]);
    maxHeapify(A, lar);
}
```

else if(lar!=i) // means A[2*i+1] is the largest , swap A[i] and A[2*i+1] and do maxHeapify at 2*i+1 th position

```
{
    swap(&A[i], &A[2*i+1]);
    maxHeapify(A, 2*i+1);
}
```

```
else
    // means A[i] is already maximum , therefore come out of the maxHeapify
    return;

}
```

int insertKey(int A[], int key) // insert key

```
{
    int flag=0;
    A[heapSize]=key;
    // first insert key at the end , and increasing the heapSize

    int i = heapSize;
    heapSize++;
    while(i>0) // now inserted value can be greater than its parent , so swap
    {
        if(A[i]>A[(i-1)/2]) // if greater than its parent swap
        {
            swap(&A[i], &A[(i-1)/2]);
            i= (i-1)/2;
        }
        else // else maxheap condition is verified , come out
            return 1;
        flag=1;
    }
}
```

```
//printf("%d\n", A[heapSize-1]);
if(flag==1 || i==0)
    return 1;
```

```

return -1;
}

```

```

int increaseKey(int A[], int i, int newVal)    // increase the value at index i to a
newValue
{
    if(i >= heapSize)
        return -1;
    A[i] = newVal;    // increase the value at index i to a newValue
    while(i > 0)    // now increased value can be greater than its parent , so swap
    {
        if(A[i] > A[(i-1)/2])    // if greater than its parent swap
        {
            swap(&A[i], &A[(i-1)/2]);
            i = (i-1)/2;
        }
        else    // else maxheap condition is verified , come out
            return 1;
    }
    return 1;
}

```

```

int extractMax(int A[])    // takes out the maximum element out of the maxHeap
{
    int val;
    if(heapSize == 0)
        return -1;
    val = A[0];    // A[0] is the maximum element in the maxHeap, store in val
    A[0] = A[heapSize-1];    // now changing value at A[0]
    heapSize--;    // decrease the heapSize
    maxHeapify(A, 0);
    // now if A[0] is smaller than its child , swap , means maxheapify
    return val;    // extract the maximum
}

```

```

void print(int A[])    // print the elements of the maxheap
{
    int i = 0;
    while(i < heapSize)    // while the i < heapSize , print the value of A[i]

```

```

{
    printf("%d\n",A[i]);
    i++;
}
return;
}

```

```
int main (int argc, char **argv)
```

```

{
    char line[128];
    char v1[15];
    char v2[15];
    char v3[15];

    int *A = NULL;
    int ret;
    int lineNo = 0;

    while (fgets(line, sizeof line, stdin) != NULL )
// takes infinite line input from standard input
    {
        sscanf(line, "%s %s %s", v1, v2, v3); // takes out the three strings v1, v2,
v3 out of the line . If only one string is present , it takes it in v1.
        lineNo++;

        if(lineNo == 1) // first line gives the maximum size of heap
        {
            A = (int*) malloc(sizeof(int)* stoi(v1)); // allocating memory
            continue;
        }

        if(strcmp(v1,"INS") == 0)
        {
            ret = insertKey(A, stoi(v2));
            if(ret < 0)
                printf("%d\n", -1);
        }
        else if(strcmp(v1,"EXT") == 0)
        {
            ret = extractMax(A);
            printf("%d\n", ret);
        }
    }
}

```

```

        else if(strcmp(v1,"PRT") == 0)
        {
            print(A);
        }
        else if(strcmp(v1,"INC")==0)
    {
        ret = increaseKey(A, stoi(v2) , stoi(v3));
        if(ret<0)
            printf("%d\n", -1);
    }
    else
    {
        printf("INVALID\n");
    }
    }
    if(A)
        free(A);

    return 0;
}

```

Time Complexity:

1. Swap: $O(1)$ - Takes constant amount of time to swap .
2. maxHeapify: $O(\log n)$ - If we start from first node at index 0 till to the end at a leaf (case in which $A[0]$ is the minimum among all the elements), we need to go to its height level , height is $\log n$.
3. insertKey: $O(\log n)$ - If inserted value is maximum , we need to go up till its first node.
4. increaseKey: $O(\log n)$ - If the increased index is the last one and the increased value is maximum , it will go up till its first node.
5. extractMax: $O(1)$ - constant amount of time to access its first element
6. Print: $O(n)$ - It will go through each element to print it, hence linear.

Space Complexity:

1. Swap: $O(1)$ - Makes only one variable temp to swap .
2. maxHeapify: $O(\log n)$ - Start from index 0 till its base , its variables go only after the function call.
3. insertKey: $O(1)$ - Initializes constant number of variables independent of n .
4. increaseKey: $O(\log n)$ - Initializes constant number of variables independent of n .

5. **extractMax: $O(\log n)$ - Uses maxHeapify.**
6. **Print: $O(1)$ - Initializes constant number of variables independent of n .**

21.c

```
#include <stdio.h>
#include <stdlib.h>
#include <string.h>

//Code to parse integer from a string
int stoi(char *str)           // converts string input str to integer
{
    int x;
    sscanf(str, "%d", &x);
    return x;
}

typedef struct stack           // defining a data type of type stack
{
    int top, capacity;
    int *s;                   // s contains the array on which we are working
} stack;

stack* make_stack(int capacity) // allocation of memory to the stack
{
    stack *stk;               // pointer to return
    stk = (stack*)malloc(sizeof(stack)); // giving memory to the pointer
    stk->top = -1;              // initializing top to -1
    stk->capacity = capacity;   // storing maximum capacity of stack in capacity
    variable
    stk->s = (int*)malloc(capacity*sizeof(int)); // allocating memory to the array to work on
    return stk;
}

int push(stack *stk,int key)   // inserts a new key value into the stack
{
```

```

if(stk->top==(stk->capacity)-1)           // check if stack is full
    return -1;
(stk->top)++;

                                     // if no then increase the top and insert the key
(stk->s)[stk->top]=key;
return 1;

    }

int pop(stack *stk)                     // takes out the element at the top in the stack
{
    int output=-1 ;
    if(stk->top==-1)                     // if stack is empty , no item to take out
        return -1;
    output = (stk->s)[stk->top];
                                     // else increase the top and take out the value in output
    (stk->top)--;
    return output;
}

int top(stack *stk)                     // return the top element in the stack
{
    if(stk->top==-1)                     // if stack is empty
        return -1;
    return (stk->s)[stk->top];           // else return the value at the top
}

void print(stack *stk)                  // prints the values in the stack
{
    int tpo;
    if(stk->top==-1)                     // if stack is empty
        return;
    tpo = stk->top;
    while(tpo>=0)                       // while tpo is greater than 0 print the value in the stack
    {
        printf("%d\n", (stk->s)[tpo]);
        tpo--;
    }
}

int size(stack *stk)                    // gives the no of elements in the stack

```

```

{
    if(stk->top== -1)           // if stack is empty return 0
        return 0;
    return (stk->top)+1;        // else return top+1
}

int isEmpty(stack *stk)        // gives 1 if stack is empty
{
    if(stk->top== -1)           // if stack is empty

        return 1;
    return -1;
}

int isFull(stack *stk)         // gives 1 if stack is full
{
    if(stk->top==(stk->capacity)-1) // if full
        return 1;
    return -1;
}

int main (int argc, char **argv)
{
    char line[128];
    char v1[15];
    char v2[15];
    char v3[15];

    stack* stk = NULL;
    int ret;
    int lineNo = 0;

    while (fgets(line, sizeof line, stdin) != NULL )
        // takes line input from standard input
    {
        sscanf(line, "%s %s %s", v1, v2, v3); // takes 3 strings from input line
        lineNo++;

        if(lineNo == 1) // first line gives the capacity of the stack
        {
            stk = make_stack(stoi(v1));
            continue;

```



```

}

if(strcmp(v1,"PSH") == 0)
{
ret =push(stk,stoi(v2));
if(ret < 0)
    printf("%d\n", -1);
}
else if(strcmp(v1,"POP") == 0)
{
ret = pop(stk);
    printf("%d\n", ret);
}
else if(strcmp(v1,"TOP") == 0)
{
ret = top(stk);
printf("%d\n", ret);
}
else if(strcmp(v1,"PRT") == 0)
{
print(stk);
}
else if(strcmp(v1,"SZE") == 0)
{
ret = size(stk);
    printf("%d\n", ret);
}
else if(strcmp(v1,"EMP") == 0)
{
ret = isEmpty(stk);
    printf("%d\n", ret);
}
else if(strcmp(v1,"FUL") == 0)
{
ret = isFull(stk);
    printf("%d\n", ret);
}
else
{
printf("INVALID\n");
}
}

```

```

    if(stk)
        free(stk);

    return 0;
}

```

Time Complexity:

1. Push: $O(1)$ - Access the element at top in constant time.
2. Pop: $O(1)$ - Delete the top element in constant time.
3. Top: $O(1)$ - gives the top element in constant time.
4. Print: $O(n)$ - Access each element in the stack takes linear time.
5. Size: $O(1)$ - value is top+1 , output in constant time.
6. isEmpty and isFull : $O(1)$ - checks only one condition and returns, takes constant amount of time.

Space Complexity:

All functions take $O(1)$ complexity to work.

22.c

```

#include <stdio.h>
#include <stdlib.h>
#include <string.h>

//Code to parse integer from a string
int stoi(char *str)           // converts string input str to integer
{
    int x;
    sscanf(str, "%d", &x);
    return x;
}

typedef struct Queue          // define data type named queue
{
    int front, rear, capacity, current_size;
    int *q;
} queue;

```

```

queue* make_queue(int capacity)
    // gives actual memory to the queue data type and return its pointer
{
    queue* que;           // pointer to return which stores the queue data
    que = (queue*)malloc(sizeof(queue)); // memory to the pointer
    que->front=0;          // front stores the index of first filled
element
    que->rear = -1;        // rear stores the index of last filled element
    que->capacity = capacity; // stores the capacity of the queue
    que->current_size = 0;  // stores the current size of the queue
    que->q = (int*)malloc(capacity*sizeof(int)); // actual array which stores the
values
    return que;
}

```

```

int enqueue(queue *que, int key) // add one value to the queue
{
    if(que->current_size==que->capacity) // if queue is full return -1
        return -1;

    (que->current_size)++;
    // else add the value of current size, rear value and insert the key into the
queue. Take mod by capacity to make it a circular queue
    (que->rear)++;
    que->rear = (que->rear)%(que->capacity);
    (que->q)[que->rear]=key;

    return 1;
}

```

```

int dequeue(queue *que) // extract the value from the front of the queue
{
    int output ;
    if(que->current_size==0) // if queue is empty return -1
        return -1;

    (que->current_size)--;
    // else increase the current capacity , front and extract the element at the front
// Take mod by capacity to make it a circular queue
    output = (que->q)[que->front];
    (que->front)++;
}

```

```

    que->front = (que->front)%(que->capacity);
    return output;
}

int peekFront(queue *que)           // gives the element at the front of queue
{
    if(que->current_size==0)         // if queue is empty return -1
        return -1;
    return (que->q)[que->front];      // else return queue front element
}

void print(queue *que)               // print the element of the queue
{
    int front=que->front;
    int rear=que->rear;
    int helper=0;
    int cap = que->capacity;
    int steps=0;
    if(que->current_size==0)         // if queue is empty
        return;
    if(front<rear)                   // if it is in linear array
    {
        steps=rear-front+1;         // number of steps to be taken
        while(steps--)
        {
            printf("%d\n", (que->q)[(que->front)+helper]); // printing the values
            helper++;
        }
        return;
    }
    else if(front>rear)               // means it is in circular form now
    {
        steps = cap-(que->front-que->rear)+1; // number of steps to be taken
        while(steps--)
        {
            printf("%d\n", (que->q)[((que->front)+helper)%cap]);
            // printing the values and mod by capacity to ensure that it doesn't overflow
            helper++;
        }
        return;
    }
    Else                             // else it has only one element which is being printed here

```

```

        printf("%d\n", que->front);
    return;
}

```

```

int size(queue *que) // gives the current size of the queue stored in current capacity
{
    return que->current_size;
    /* Decrease the value of A[i] to newVal. Return 1 if the
       operation is successful and -1 otherwise. */
}

```

```

int isEmpty(queue *que) // empty if current size is 0
{
    if(que->current_size==0)
        return 1;
    return 0;
    /* Ensure that the subtree rooted at A[i] is a min heap. */
}

```

```

int isFull(queue *que) // is full if current size is capacity
{
    if(que->current_size==que->capacity)
        return 1;
    return 0;
    /* Display the heap represented by A in the increasing order
       of their indices, one element per line.*/
}

```

```

int main (int argc, char **argv)
{
    char line[128];
    char v1[15];
    char v2[15];
    char v3[15];

    queue* que;
    int ret;
    int lineNo = 0;

    while (fgets(line, sizeof line, stdin) != NULL )//takes line input from standard input
    {
        sscanf(line, "%s %s %s", v1, v2, v3);
    }
}

```

```
lineNo++;
```

// first line gives the capacity of the queue.

```
if(lineNo == 1)
{
    que = make_queue(stoi(v1)-1);
    continue;
}

if(strcmp(v1,"ENQ") == 0)
{
    ret = enqueue(que, stoi(v2));
    if(ret < 0)
        printf("%d\n", -1);
}
else if(strcmp(v1,"DEQ") == 0)
{
    ret = dequeue(que);
    printf("%d\n", ret);
}
else if(strcmp(v1,"FRN") == 0)
{
    ret = peekFront(que);
    printf("%d\n", ret);
}
else if(strcmp(v1,"PRT") == 0)
{
    print(que);
}
else if(strcmp(v1,"SIZE") == 0)
{
    ret = size(que);
    printf("%d\n", ret);
}
else if(strcmp(v1,"EMP") == 0)
{
    ret = isEmpty(que);
    printf("%d\n", ret);
}
else if(strcmp(v1, "FUL")==0)
{
    ret = isFull(que);
    printf("%d\n", ret);
}
```

```
else
{
printf("INVALID\n");
}
}

if(que)
free(que);

return 0;
}
```

Time Complexity: All take $O(1)$ time except the print which takes $O(n)$ time, time to access each element and printing it.

Space Complexity: All functions take $O(1)$ complexity to work.