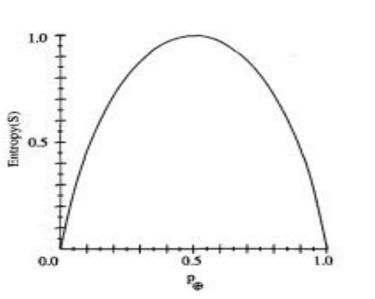
Decision Tree Classifier



ID3(Examples, Target_attribute, Attributes)

Examples are the training examples. Target_attribute is the attribute whose value is to be predicted by the tree. Attributes is a list of other attributes that may be tested by the learned decision tree. Returns a decision tree that correctly classifies the given Examples.

- · Create a Root node for the tree
- If all Examples are positive, Return the single-node tree Root, with label = +
- If all Examples are negative, Return the single-node tree Root, with label = -
- If Attributes is empty, Return the single-node tree Root, with label = most common value of Target_attribute in Examples
- Otherwise Begin
 - A ← the attribute from Attributes that best* classifies Examples
 - The decision attribute for Root ← A
 - For each possible value, vi, of A,
 - Add a new tree branch below Root, corresponding to the test A = vi
 - Let Examples_{vi} be the subset of Examples that have value v_i for A
 - If Examples_{vi} is empty
 - Then below this new branch add a leaf node with label = most common value of Target_attribute in Examples
 - Else below this new branch add the subtree
 ID3(Examples_v, Target_attribute, Attributes {A}))

- End
- Return Root

Day	Outlook	Temperature	Humidity	Wind	PlayTennis
DI	Sunny	Hot	High	Weak	No
D2	Sunny	Hot	High	Strong	No
D3	Overcast	Hot	High	Weak	Yes
D4	Rain	Mild	High	Weak	Yes
D5	Rain	Cool	Normal	Weak	Yes
D6	Rain	Cool	Normal	Strong	No
D7	Overcast	Cool	Normal	Strong	Yes
D8	Sunny	Mild	High	Weak	No
D9	Sunny	Cool	Normal	Weak	Yes
D10	Rain	Mild	Normal	Weak	Yes
D11	Sunny	Mild	Normal	Strong	Yes
D12	Overcast	Mild	High	Strong	Yes
D13	Overcast	Hot	Normal	Weak	Yes
D14	Rain	Mild	High	Strong	No

$Entropy([9+, 5-]) = -(9/14) \log_2(9/14) - (5/14) \log_2(5/14)$

= 0.940

 $Gain(S, A) \equiv Entropy(S) - \sum_{v \in Values(A)} \frac{|S_v|}{|S|} Entropy(S_v)$ (

$$S = [9+, 5-]$$

$$S_{Weak} \leftarrow [6+, 2-]$$

$$S = [9+, 5-]$$

 $S_{Strong} \leftarrow [3+, 3-]$

= 0.048

 $Gain(S, Wind) = Entropy(S) - \sum_{v \in \{Weak, Strong\}} \frac{|S_v|}{|S|} Entropy(S_v)$

 $-(6/14)Entropy(S_{Strong})$

= $Entropy(S) - (8/14)Entropy(S_{weak})$

= 0.940 - (8/14)0.811 - (6/14)1.00

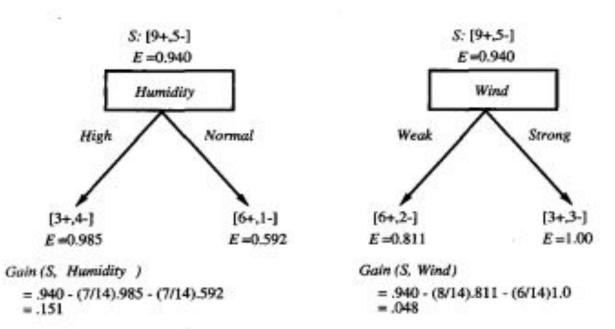
$$S = [9+, 5-]$$

$$S = [9+, 5-]$$

$$S = [9+,5-1]$$

$$Values(Wind) = Weak, Strong$$

Which attribute is the best classifier?

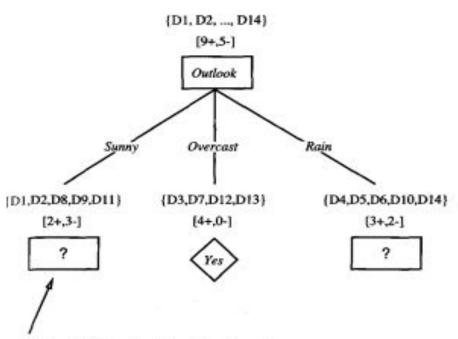


Gain(S, Outlook) = 0.246

Gain(S, Temperature) = 0.029

Gain(S, Humidity) = 0.151

Gain(S, Wind) = 0.048



Which attribute should be tested here?

$$S_{sunny} = \{D1,D2,D8,D9,D11\}$$

 $Gain (S_{sunny}, Humidity) = .970 - (3/5) 0.0 - (2/5) 0.0 = .970$
 $Gain (S_{sunny}, Temperature) = .970 - (2/5) 0.0 - (2/5) 1.0 - (1/5) 0.0 = .570$
 $Gain (S_{sunny}, Wind) = .970 - (2/5) 1.0 - (3/5) .918 = .019$

$$E(S) = -p_{(+)}^{\log p}(+) - p_{(-)}^{\log p}(-)$$

Decision Tree

RID	age	income	student	credit_rating	Class: buys_computer
1	youth	high	no	fair	no
2	youth	high	no	excellent	no
3	middle_aged	high	no	fair	yes
4	senior	medium	no	fair	yes
5	senior	low	yes	fair	yes
6	senior	low	yes	excellent	no
7	middle_aged	low	yes	excellent	yes
8	youth	medium	no	fair	no
9	youth	low	yes	fair	yes
10	senior	medium	yes	fair	yes
11	youth	medium	yes	excellent	yes
12	middle_aged	medium	no	excellent	yes
13	middle_aged	high	yes	fair	yes
14	senior	medium	no	excellent	no

Attribute Selection Methods

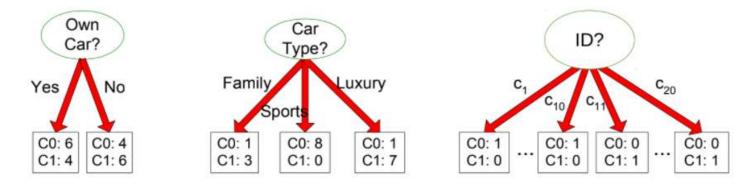
Ex. information gain, Gain Ratio, Gini index.

Gini Index in Cart Algorithm considers Binary Split

- Others, like information gain, do not,
 - Therein allowing multiway splits
 - (i.e., two or more branches to be grown from a node)

Attribute Selection Methods

- These methods are defined in terms of the class distribution of the records before and after splitting.
- Let p(i|t) denote the fraction of records belonging to class i at a given node t.
 We sometimes omit the reference to node t and express the fraction as p i.
- In a two-class problem, the class distribution at any node can be written as (p 0,p1), where p1=1-p0
- Before Splitting: 10 records of class 0, 10 records of class 1



Which test condition is the best?

ОС	CT	ID	Class		ОС	СТ	ID	Class
yes	Family	1	0		no	Family	11	1
yes	Sports	2	0		no	Family	12	1
yes	Sports	3	0		no	Family	13	1
yes	Sports	4	0		no	Luxury	14	1
yes	Sports	5	0		yes	Luxury	15	1
yes	Sports	6	0		yes	Luxury	16	1
no	Sports	7	0		yes	Luxury	17	1
no	Sports	8	0		yes	Luxury	18	1
no	Sports	9	0		no	Luxury	19	1
no	Luxury	10	0		no	Luxury	20	1
	Own Car?		Car	?)			ID?	
Yes	Yes No Family Luxury $c_1 c_{20}$ Sports							
C0: C1:		C0 C1	200		C0: C1:			C0: 0 C1: 1

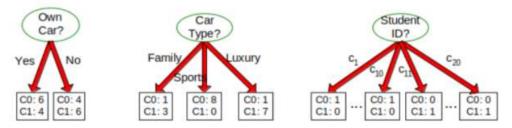
Which test condition is the best?

Attribute Selection Methods

- The class distribution before splitting is (0.5, 0.5) because there are an equal number of records from each class.
- If we split the data using the Own Car? attribute, then the class distributions of the child nodes are (0.6, 0.4) and (0.4, 0.6), respectively.
- Although the classes are no longer evenly distributed, the child nodes still contain records from both classes.
- Splitting on the second attribute, Car Type, will result in purer partitions.
- The measures developed for selecting the best split are often based on the degree of impurity of the child nodes.
- The smaller the degree of impurity, the more skewed the class distribution.
- For example, a node with class distribution (0, 1) has zero impurity, whereas a node with uniform class distribution (0.5, 0.5) has the highest impurity.
- Some of the popular impurity measures are Entropy, Gini and Classification Error.

Gain Ratio

- The information gain measure is biased toward tests with many outcomes.
- It prefers to select attributes having a large number of values.



- Comparing the first test condition, OwnCar, with the second, Car Type:
- Car Type provide a better way of splitting the data since it produces purer descendent nodes.
- However, if we compare both conditions with Customer ID, the latter appears to produce purer partitions.
- Yet Customer ID is not a predictive attribute because its value is unique for each record.

Gain Ratio

- For each outcome, it considers the number of tuples having that outcome with respect to the total number of tuples in D.
- It differs from information gain, which measures the information with respect to classification that is acquired based on the same partitioning

$$GainRatio(A) = \frac{Gain(A)}{SplitInfo_A(D)}$$

- The attribute with the maximum gain ratio is selected as the splitting attribute.
- Note, however, that as the split information approaches 0, the ratio becomes unstable.
- A constraint is added to avoid this, whereby the information gain of the test selected must be large—at least as great as the average gain over all tests examined

Outlook	Tempreature	Humidity	Windy	Class
sunny	hot	high	false	N
sunny	hot	high	true	N
overcast	hot	high	false	Р
rain	mild	high	false	Р
rain	cool	normal	false	Р
rain	cool	normal	true	N
overcast	cool	normal	true	Р
sunny	mild	high	false	N
sunny	cool	normal	false	Р
rain	mild	normal	false	Р
sunny	mild	normal	true	Р
overcast	mild	high	true	Р
overcast	hot	normal	false	Р
rain	mild	high	true	N

Outloo	k	Humidi	ty	
Info	0.693	Info	?	
Gain: 0.940-0.693	0.247	Gain: 0.940-0.788	?	
Split info: info ([5,4,5])	1.577	Split info: info ([7,7])	?	
Gain ratio: 0.247/1.577	0.156	Gain ratio: 0.152/1	?	
Temperat	ure	Windy		
Info	?	Info	?	
Gain: 0.940-0.911	?	Gain: 0.940-0.892	?	
Split info: info ([4,6,4])	?	Split info: info ([8,6])	?	
Gain ratio: 0.029/1.362	?	Gain ratio: 0.048/0.985	?	

Outlook	Tempreature	Humidity	Windy	Class
sunny	hot	high	false	N
sunny	hot	high	true	N
overcast	hot	high	false	Р
rain	mild	high	false	Р
rain	cool	normal	false	Р
rain	cool	normal	true	N
overcast	cool	normal	true	Р
sunny	mild	high	false	N
sunny	cool	normal	false	Р
rain	mild	normal	false	Р
sunny	mild	normal	true	Р
overcast	mild	high	true	Р
overcast	hot	normal	false	Р
rain	mild	high	true	N

Outloo	k	Class: P-9 N-5
Info	0.693	Outlook:
Gain: 0.940-0.693	0.247	Sunny : P-2 N-3 Overcast : P-4 N-0
Split info: info ([5,4,5])	1.577	rain : P-3 N-2
Gain ratio: 0.247/1.577	0.156	

Outlook	Tempreature	Humidity	Windy	Class
sunny	hot	high	false	N
sunny	hot	high	true	N
overcast	hot	high	false	Р
rain	mild	high	false	Р
rain	cool	normal	false	Р
rain	cool	normal	true	N
overcast	cool	normal	true	Р
sunny	mild	high	false	N
sunny	cool	normal	false	Р
rain	mild	normal	false	Р
sunny	mild	normal	true	Р
overcast	mild	high	true	Р
overcast	hot	normal	false	Р
rain	mild	high	true	N

Outlook		Class: P-9 N-5
Info _{Outlook}	0.693	Outlook:
Gain: 0.940-0.693	0.247	Sunny : P - 2 N - 3 Overcast : P - 4 N - 0
Split info: info ([5,4,5])	1.577	rain : P-3 N-2
Gain ratio: 0.247/1.577	0.156	

$$Info_A(D) = \sum_{j=1}^{\nu} \frac{|D_j|}{|D|} \times Info(D_j)$$

=
$$(5/14)[-2/5 \log_2(2/5) - 3/5 \log_2(3/5)]$$

+
$$(5/14)[-3/5 \log_2(3/5) - 2/5 \log_2(2/5)]$$

= 0.693

Outlook	Tempreature	Humidity	Windy	Class
sunny	hot	high	false	N
sunny	hot	high	true	N
overcast	hot	high	false	Р
rain	mild	high	false	Р
rain	cool	normal	false	Р
rain	cool	normal	true	N
overcast	cool	normal	true	Р
sunny	mild	high	false	N
sunny	cool	normal	false	Р
rain	mild	normal	false	Р
sunny	mild	normal	true	Р
overcast	mild	high	true	Р
overcast	hot	normal	false	Р
rain	mild	high	true	N

Outlook		Class: P-9 N-5
Info	0.693	Outlook:
Gain: 0.940-0.693	0.247	Sunny : P-2 N-3 Overcast : P-4 N-0
Split info: info ([5,4,5])	1.577	rain : P-3 N-2
Gain ratio: 0.247/1.577	0.156	

$$Info(D) = -\sum_{i=1}^{m} p_i \log_2(p_i),$$

$$= -(9/14)\log_2(9/14) - (5/14)\log_2(5/14)$$

$$= 0.940$$

Outlook	Tempreature	Humidity	Windy	Class
sunny	hot	high	false	N
sunny	hot	high	true	N
overcast	hot	high	false	Р
rain	mild	high	false	Р
rain	cool	normal	false	Р
rain	cool	normal	true	N
overcast	cool	normal	true	Р
sunny	mild	high	false	N
sunny	cool	normal	false	Р
rain	mild	normal	false	Р
sunny	mild	normal	true	Р
overcast	mild	high	true	Р
overcast	hot	normal	false	Р
rain	mild	high	true	N

Outlook		Class: P-9 N-5
Info	0.693	Outlook:
Gain: 0.940-0.693	0.247	Sunny : P - 2 N - 3 Overcast : P - 4 N - 0
Split info: info ([5,4,5])	1.577	rain : P-3 N-2
Gain ratio: 0.247/1.577	0.156	

$$SplitInfo_A(D) = -\sum_{j=1}^{\nu} \frac{|D_j|}{|D|} \times \log_2 \left(\frac{|D_j|}{|D|}\right)$$

=
$$-2*$$
 [(5/14)log₂(5/14)] -(4/14)log₂(4/14)
= **1.577**

Outlook	Tempreature	Humidity	Windy	Class
sunny	hot	high	false	N
sunny	hot	high	true	N
overcast	hot	high	false	Р
rain	mild	high	false	Р
rain	cool	normal	false	Р
rain	cool	normal	true	N
overcast	cool	normal	true	Р
sunny	mild	high	false	N
sunny	cool	normal	false	Р
rain	mild	normal	false	Р
sunny	mild	normal	true	Р
overcast	mild	high	true	Р
overcast	hot	normal	false	Р
rain	mild	high	true	N

· LACIT	ipic		
Outlook	k	Class: P-9	N-5
Info	0.693	Outlook:	
Gain: 0.940-0.693	0.247	Sunny : P - 2 Overcast : P - 4	N - 3
Split info: info ([5,4,5])	1.577	rain : P-3	
Gain ratio: 0.247/1.577	0.156		
GainRatio(A) =	= Gain SplitInf		

= 0.247 / 1.577

= 0.156

Outlook	Tempreature	Humidity	Windy	Class
sunny	hot	high	false	N
sunny	hot	high	true	N
overcast	hot	high	false	Р
rain	mild	high	false	Р
rain	cool	normal	false	Р
rain	cool	normal	true	N
overcast	cool	normal	true	Р
sunny	mild	high	false	N
sunny	cool	normal	false	Р
rain	mild	normal	false	Р
sunny	mild	normal	true	Р
overcast	mild	high	true	Р
overcast	hot	normal	false	Р
rain	mild	high	true	N

Outlook		Humidity		
Info	0.693	Info	0.788	
Gain: 0.940-0.693	0.247	Gain: 0.940-0.788	0.152	
Split info: info ([5,4,5])	1.577	Split info: info ([7,7])	1	
Gain ratio: 0.247/1.577	0.156	Gain ratio: 0.152/1	0.152	
Temperat	ure	Windy		
Info	0.911	Info	0.892	
Gain: 0.940-0.911	0.029	Gain: 0.940-0.892	0.048	
Split info: info ([4,6,4])	1.362	Split info: info ([8,6])	0.985	
Gain ratio: 0.029/1.362	0.021	Gain ratio: 0.048/0.985	0.049	

- The Gini index is used in CART.
- Gini Index is a metric to measure how often a randomly chosen element would be incorrectly identified
- Impurity of D, a data partition or set of training tuples:

$$Gini(D) = 1 - \sum_{i=1}^{m} p_i^2$$

- p_i is the probability that a tuple in D belongs to class C_i and is estimated by |C_i,D| / |D|.
- The sum is computed over m classes

- The Gini index considers a binary split for each attribute. In CART Algorithm
- Let's first consider the case where A is a discrete-valued attribute having v distinct values, {a 1, a 2,..., a v }, occurring in D.
- To determine the best binary split on A, we examine all the possible subsets that can be formed using known values of A.
- If A has v possible values, then there are 2^v possible subsets.
- For example, if income has three possible values, namely {low, medium, high}, then the possible subsets are {low, medium, high}, {low, medium}, {low, high}, {medium, high}, {low}, {medium}, {high}, and {}.
- We exclude the power set, {low, medium, high}, and the empty set from consideration since, conceptually, they do not represent a split.
- Therefore, there are 2 ^ v 2 possible ways to form two partitions of the data, D, based on a binary split on A

- When considering a binary split, we compute a weighted sum of the impurity of each resulting partition.
- For example, if a binary split on A, partitions D into D 1 and D 2, the Gini index of D given that partitioning is:

$$Gini_A(D) = \frac{|D_1|}{|D|}Gini(D_1) + \frac{|D_2|}{|D|}Gini(D_2).$$

- For each attribute, each of the possible binary splits is considered.
- For a discrete-valued attribute, the subset that gives the minimum Gini index for that attribute is selected as its splitting subset.
- For continuous-valued attributes, each possible split-point must be considered
- The strategy is similar to that described earlier for information gain, where the midpoint between each pair of (sorted) adjacent values is taken as a possible split-point.
- The point giving the minimum Gini index for a given (continuous-valued) attribute is taken as the split-point of that attribute

 The reduction in impurity that would be incurred by a binary split on a discrete-or continuous-valued attribute A is:

$$\Delta Gini(A) = Gini(D) - Gini_A(D)$$

- The attribute that maximizes the reduction in impurity (or, equivalently, has the minimum Gini index) is selected as the splitting attribute.
- This attribute and either its splitting subset (for a discrete-valued splitting attribute) or split-point (for a continuous-valued splitting attribute) together form the splitting criterion

Gini Index: Example

For Var1

Var1	Var2
0	33
0	54
0	56
0	42
1	50
1	55
1	31
0	-4
1	77
0	49
	0 0 0 0 1 1 1 0

Var1 has 4 instances (4/10) where it's equal to 1 and 6 instances (6/10) when it's equal to 0.

For Var1 == 1 & Class == A: 1 / 4 instances

For Var1 == 1 & Class == B: 3 / 4 instances

Gini Index here is $1-((1/4)^2 + (3/4)^2) = 0.375$

For Var1 == 0 & Class== A: 4 / 6 instances

For Var1 == 0 & Class == B: 2 / 6 instances

Gini Index here is $1-((4/6)^2 + (2/6)^2) = 0.4444$

We then weight and sum each of the splits based on the proportion of the data each split takes up.

Gini Index: Example

For Var2 (Let's Threshold T>=32)

Class	Var1	Var2
Α	0	33
Α	0	54
Α	0	56
Α	0	42
Α	1	50
В	1	55
В	1	31
В	0	-4
В	1	77
В	0	49

Var2 has 8 instances (8/10) where it's >= 32 and 2 instances (2/10) when it's < 32.

For Var2 >=32 & Class == A: 5 / 8 instances

For Var2 >=32 & Class == B: 3 / 8 instances

Gini Index here is $1-((5/8)^2 + (3/8)^2) = 0.46875$

For Var2 < 32 & Class== A: 0 / 2 instances

For Var1 < 32 & Class == B: 2 / 2 instances

Gini Index here is $1-((0/2)^2 + (2/2)^2) = 0$

We then weight and sum each of the splits based on the proportion of the data each split takes up.

$$8/10 * 0.46875 + 2/10 * 0 = 0.375$$

Gini Index: Example

Class	Var1	Var2
Α	0	33
Α	0	54
Α	0	56
Α	0	42
Α	1	50
В	1	55
В	1	31
В	0	-4
В	1	77
В	0	49

For Var1
$$= 0.41667$$

For
$$Var2 (T>=32) = 0.375$$

Based on these results, Var2>=32 is selected as the split.(since its weighted Gini Index is smallest)

The next step would be to take the results from the split and further partition.

Another Example

Past Trend	Open Interest	Trading Volume	Return
Positive	Low	High	Up
Negative	High	Low	Down
Positive	Low	High	Up
Positive	High	High	Up
Negative	Low	High	Down
Positive	Low	Low	Down
Negative	High	High	Down
Negative	Low	High	Down
Positive	Low	Low	Down
Positive	High	High	Up

Calculating the Gini Index for Past Trend

- P(Past Trend=Positive): 6/10
- P(Past Trend=Negative): 4/10
- If (Past Trend = Positive & Return = Up), probability = 4/6
- If (Past Trend = Positive & Return = Down), probability = 2/6
- Gini index = $1 ((4/6)^2 + (2/6)^2) = 0.45$
- If (Past Trend = Negative & Return = Up), probability = 0
- If (Past Trend = Negative & Return = Down), probability = 4/4
- Gini index = $1 ((0)^2 + (4/4)^2) = 0$
- Weighted sum of the Gini Indices can be calculated as follows:
- Gini Index for Past Trend = (6/10)0.45 + (4/10)0 = 0.27

- Calculation of Gini Index for Open Interest
- P(Open Interest=High): 4/10
- P(Open Interest=Low): 6/10
- If (Open Interest = High & Return = Up), probability = 2/4
- If (Open Interest = High & Return = Down), probability = 2/4
- Gini index = $1 ((2/4)^2 + (2/4)^2) = 0.5$
- If (Open Interest = Low & Return = Up), probability = 2/6
- If (Open Interest = Low & Return = Down), probability = 4/6
- Gini index = $1 ((2/6)^2 + (4/6)^2) = 0.45$
- Weighted sum of the Gini Indices can be calculated as follows:
- Gini Index for Open Interest = (4/10)0.5 + (6/10)0.45 = 0.47

- Calculation of Gini Index for Trading Volume
- P(Trading Volume=High): 7/10

•

P(Trading Volume=Low): 3/10

•

- If (Trading Volume = High & Return = Up), probability = 4/7
- If (Trading Volume = High & Return = Down), probability = 3/7
- Gini index = $1 ((4/7)^2 + (3/7)^2) = 0.49$

•

- If (Trading Volume = Low & Return = Up), probability = 0
- If (Trading Volume = Low & Return = Down), probability = 3/3
- Gini index = $1 ((0)^2 + (1)^2) = 0$

•

- Weighted sum of the Gini Indices can be calculated as follows:
- Gini Index for Trading Volume = (7/10)0.49 + (3/10)0 = 0.34

Attributes/Features	Gini Index
Past Trend	0.27
Open Interest	0.47
Trading Volume	0.34

 From the above table, we observe that 'Past Trend' has the lowest Gini Index and hence it will be chosen as the root node for how decision tree works.

 We will repeat the same procedure to determine the sub-nodes or branches of the decision tree. We will calculate the Gini Index for the 'Positive' branch of Past Trend as follows:

Past Trend	Open Interest	Trading Volume	Return
Positive	Low	High	Up
Positive	Low	High	Up
Positive	High	High	Up
Positive	Low	Low	Down
Positive	Low	Low	Down
Positive	High	High	Up

- Calculation of Gini Index of Open Interest for Positive Past Trend
- P(Open Interest=High): 2/6

P(Open Interest=Low): 4/6

- If (Open Interest = High & Return = Up), probability = 2/2
- If (Open Interest = High & Return = Down), probability = 0
- Gini index = 1 (sq(2/2) + sq(0)) = 0
- If (Open Interest = Low & Return = Up), probability = 2/4
- If (Open Interest = Low & Return = Down), probability = 2/4
- Gini index = 1 (sq(0) + sq(2/4)) = 0.50
- Weighted sum of the Gini Indices can be calculated as follows:
- Gini Index for Open Interest = (2/6)0 + (4/6)0.50 = 0.33

- Calculation of Gini Index for Trading Volume
- P(Trading Volume=High): 4/6

•

P(Trading Volume=Low): 2/6

•

- If (Trading Volume = High & Return = Up), probability = 4/4
- If (Trading Volume = High & Return = Down), probability = 0
- Gini index = 1 (sq(4/4) + sq(0)) = 0

•

- If (Trading Volume = Low & Return = Up), probability = 0
- If (Trading Volume = Low & Return = Down), probability = 2/2
- Gini index = 1 (sq(0) + sq(2/2)) = 0

•

- Weighted sum of the Gini Indices can be calculated as follows:
- Gini Index for Trading Volume = (4/6)0 + (2/6)0 = 0

Attributes/Features	Gini Index
Open Interest	0.33
Trading Volume	0

We will split the node further using the 'Trading Volume' feature, as it has the minimum Gini index.

Incorporating Continuous valued Attribute

- Temperature: 40 48 60 72 80 90
- Play Tennis: N N Y Y N
- What threshold based Boolean attribute should be defined based on Temperature?
- We would pick a threshold c, that gives the maximum information gain.
- Steps: By sorting the examples according to the continuous attribute Temperature, then identifying adjacent examples that differ in their target classification we can generate a set of candidate thresholds midway between the corresponding values of A.

Temperature : 40 48 60 72 80 90
 Play Tennis : N N Y Y N

- The data is already sorted here. So, here two candidate threshold corresponding to temperature are found. 1) (48+60)/2 and 2) (80+90)/2.
- The information gain can then be computed for each of the candidate attributes, Temperature > 54 and Temperature > 85 and the best can be selected. Here the best is Temperature > 54.

Overfitting Due to Noise: An Example

An example training set for classifying mammals. Asterisks denote mislabelings.

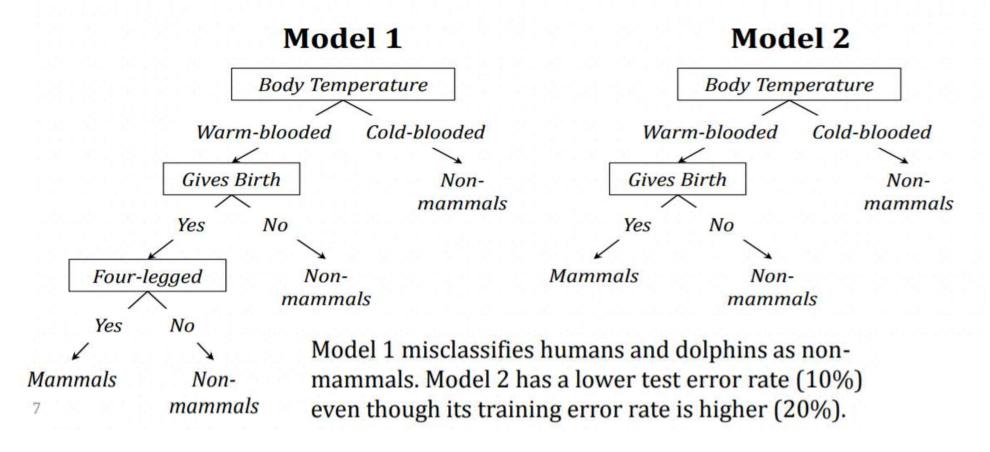
Name	Body Temperature	Gives Birth	Four-legged	Hibernates	Class Label
Porcupine	Warm-blooded	Yes	Yes	Yes	Yes
Cat	Warm-blooded	Yes	Yes	No	Yes
Bat	Warm-blooded	Yes	No	Yes	No*
Whale	Warm-blooded	Yes	No	No	No*
Salamander	Cold-blooded	No	Yes	Yes	No
Komodo dragon	Cold-blooded	No	Yes	No	No
Python	Cold-blooded	No	No	Yes	No
Salmon	Cold-blooded	No	No	No	No
Eagle	Warm-blooded	No	No	No	No
Guppy	Cold-blooded	Yes	No	No	No

Overfitting Due to Noise

An example testing set for classifying mammals.

Name	Body Temperature	Gives Birth	Four-legged	Hibernates	Class Label
Human	Warm-blooded	Yes	No	No	Yes
Pigeon	Warm-blooded	No	No	No	No
Elephant	Warm-blooded	Yes	Yes	No	Yes
Leopard shark	Cold-blooded	Yes	No	No	No
Turtle	Cold-blooded	No	Yes	No	No
Penguin	Cold-blooded	No	No	No	No
Eel	Cold-blooded	No	No	No	No
Dolphin	Warm-blooded	Yes	No	No	Yes
Spiny anteater	Warm-blooded	No	Yes	Yes	Yes
Gila monster	Cold-blooded	No	Yes	Yes	No

Overfitting Due to Noise

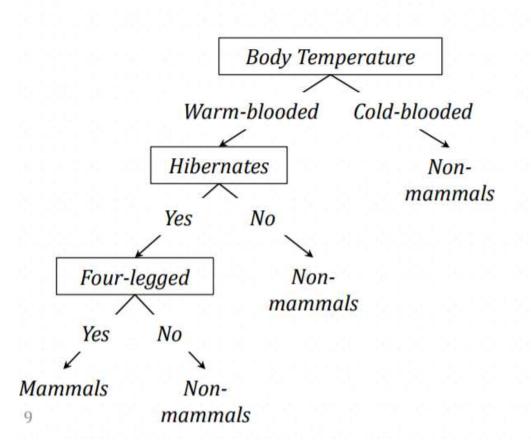


Overfitting Due to Lack of Samples

An example training set for classifying mammals.

Name	Body Temperature	Gives Birth	Four-legged	Hibernates	Class Label
Salamander	Cold-blooded	No	Yes	Yes	No
Guppy	Cold-blooded	Yes	No	No	No
Eagle	Warm-blooded	No	No	No	No
Poorwill	Warm-blooded	No	No	Yes	No
Platypus	Warm-blooded	No	Yes	Yes	Yes

Overfitting Due to Lack of Samples



Although the model's training error is zero, its error rate on the test set if 30%.

Humans, elephants, and dolphins are misclassified because the decision tree classifies all warmblooded vertebrates that do not hibernate as non-mammals. The tree arrives at this classification decision because there is only one training records, which is an eagle, with such characteristics.