

# Model Checking

CS511

# Summary

- ▶ We've seen some examples of Promela models
- ▶ We've verified some Promela models that involved the `assert` statement
- ▶ This lecture:
  - ▶ Channels in Promela
  - ▶ An example from distributed programming: distributed mutual exclusion

Channels in Promela

Synchronous Channels

Asynchronous Channels

Distributed Mutual Exclusion

# Channels

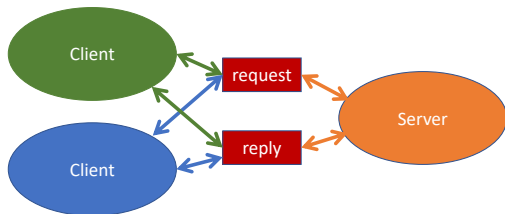
- ▶ Inspired in CSP (1978, Tony Hoare)
- ▶ A channel is a **data type** with two operations
  - ▶ send
  - ▶ receive
- ▶ Channels are global: any process can send on a channel and receive from a channel
- ▶ Every channel has a message type

```
chan ch = [capacity] of { typename, ..., typename }
```

- ▶ 0 capacity: rendezvous channels (=synchronous)
- ▶ > 0 capacity: buffered channels

## Example 1 (eg1.pml)

```
1 chan request=[0] of {byte};
2
3 active proctype Server() {
4   byte client;
5 end:
6   do
7     ::request ? client -> pri
8   od
9 }
10
11 active proctype Client0() {
12   request ! 0;
13 }
14
15 active proctype Client1() {
16   request ! 1;
17 }
```



- ▶ label `end` ensures that an end state with the server blocked on a receive statement is not considered invalid

# Running the Example

```
1 > spin eg1.pml
2     Client 0
3     Client 1
4     timeout
5 #processes: 1
6 6: proc 0 (Server:1) eg1.pml:8 (state 3) <valid end state>
7 3 processes created
```

- ▶ Computation in which execution terminates with the output `timeout` means that no statements are executable (deadlock)

# Symbolic Names as Values

## ► Example:

```
1 mtype { open, close, reset }
2 init {
3     mtype x = reset;
4     printm(x);
5 }
```

## ► Shorthand for send and receive commands

- `ch!e1,e2,...` can be written: `ch!e1(e2,...)`
- `ch?e1,e2,...` can be written: `ch?e1(e2,...)`

when `e1` is an `mtype`

```
1 mtype { open, close, reset };
2 chan ch = [0] of { mtype, byte, byte };
3 byte id, n;
4 /* send statement can be in either of the formats: */
5 ch ! open, id, n;
6 ch ! open(id, n);
```

# Example

```
1 mtype { red, yellow, green };
2 chan ch = [0] of { mtype, byte, bool };
3
4 active proctype Sender() {
5     ch ! red, 20, false;
6     printf("Sent message\n")
7 }
8
9 active proctype Receiver() {
10    mtype color;
11    byte time;
12    bool flash;
13    ch ? color, time, flash;
14    printf("Received message %e, %d, %d\n",color,time,flash)
15 }
```



## Example: Rendezvous

```
1 chan request = [0] of { byte };
2 chan reply = [0] of { bool };
3
4 active proctype Server() {
5     byte client;
6 end:
7     do
8         :: request ? client ->
9             printf("Client %d\n", client);
10            reply ! true
11    od
12 }
13
14 active proctype Client0() {
15     request ! 0;
16     reply ? _
17 }
18
19 active proctype Client1() {
20     request ! 1;
21     reply ? _
22 }
```

► `_` is an anonymous variable

## Another Example (eg4.pml)

```
1 chan request = [0] of { byte };
2 chan reply = [0] of { byte };
3
4 active [2] proctype Server() {
5     byte client;
6 end:
7     do
8         :: request ? client ->
9             printf("Client %d processed by server %d\n", client, _pid)
10            reply ! _pid
11     od
12 }
13
14 active [2] proctype Client() {
15     byte server;
16     request ! _pid;
17     reply ? server;
18     printf("Reply received from server %d by client %d\n", server,
19 }
```

► Note quite right, why?

## Verifying Previous Example

- ▶ Use Spin to verify that this program is not correct
  - ▶ In Server: Send back `client`
  - ▶ In Client: insert an `assert` to compare the received pid with its own

## Verifying Previous Example (eg5.pml)

```
1 chan request = [0] of { byte };
2 chan reply = [0] of { byte, byte };
3
4 active [2] proctype Server() {
5     byte client;
6 end:
7     do
8         :: request ? client ->
9             printf("Client %d processed by server %d\n", client, _pid)
10            reply ! _pid, client
11     od
12 }
13
14 active [2] proctype Client() {
15     byte server;
16     byte whichClient;
17     request ! _pid;
18     reply ? server, whichClient;
19     printf("Reply received from server %d by client %d\n", server, _pid);
20     assert (whichClient == _pid);
21 }
```

# Channels as Values

```
1 chan request = [0] of { byte, chan };
2 chan reply [2] = [0] of { byte, byte }; /* array of 2 channels */
3
4 active [2] proctype Server() {
5     byte client;
6     chan replyChannel;
7 end:
8     do
9         :: request ? client, replyChannel ->
10             printf("Client %d processed by server %d\n", client, _pid);
11             replyChannel ! _pid, client;
12     od
13 }
14
15 active [2] proctype Client() {
16     byte server;
17     byte whichClient;
18     request ! _pid, reply[_pid-2];
19     reply[_pid-2] ? server, whichClient;
20     printf("Reply received from server %d by client %d\n", server,
21         _pid);
22 }
```

## Slight Improvement on the Previous Example

- ▶ Problem: depends on `pid` to access array of channels
- ▶ We can correct this by passing arguments on to Client and Server with these indices

## Previous Example Improved

```
1  chan request = [0] of { byte, chan };
2  chan reply [2] = [0] of { byte, byte };
3
4  proctype Server(byte me) {
5      byte client;
6      chan replyChannel;
7  end:
8      do
9          :: request ? client, replyChannel ->
10             printf("Client %d processed by server %d\n", client,
11                 replyChannel ! me, client;
12      od
13 }
14
15 proctype Client(byte me; byte myChannel) {
16     byte server;
17     byte whichClient;
18     request ! me, reply[myChannel];
19     reply[myChannel] ? server, whichClient;
20     printf("Reply received from server %d by client %d\n", server,
21         assert (whichClient == me);
22 }
23 /* continued */
```

## Previous Example Improved

```
1 init {  
2     atomic {  
3         run Server('s');  
4         run Server('t');  
5         run Client('c', 0);  
6         run Client('d', 1);  
7     }  
8 }
```



## Exercise

- ▶ Spawn an additional client so that there are three of them
- ▶ Prove that at most two clients can be served at any given time
- ▶ For that
  - ▶ add a global variable `numClients`
  - ▶ count the clients that have sent a request but not yet received a reply
  - ▶ insert an appropriate `assert`

## Exercise: Solution

Replace `client` and modify `init` as indicated below

```
1  proctype Client(byte me; byte myChannel) {
2      byte server;
3      request ! me, reply[myChannel];
4      numClients++;
5      assert (numClients <= 2);
6      numClients--;
7      reply[me] ? server;
8      printf("Client %d received reply on channel %d, processed by ser
9  }
10
11  init {
12      atomic {
13          run Server('s');
14          run Server('t');
15          run Client('c', 0);
16          run Client('d', 1);
17          run Client('e', 2);
18      }
19  }
```

## Channels in Promela

Synchronous Channels

Asynchronous Channels

Distributed Mutual Exclusion

# Buffered Channels

```
chan ch = [3] of mtype, byte, bool ;
```

- ▶ Send and receive statements treat the channel as a FIFO (first in-first out) queue.
- ▶ Send statement is executable if there is room in the channel for another message (the channel is not full)
  - ▶ The `-m` option in `spin` causes send not to block when channel is full but message is discarded
- ▶ Receive statement is executable if there are messages in the channel (the channel is not empty)
- ▶ The channel is part of the states of the computation.

# Operations on Buffered Channels

- ▶ `full` and `empty`, and their negations `nfull` and `nempty`.
  - ▶ The negations `!full` and `!empty` are not allowed in Promela
- ▶ `len(ch)` returns the number of messages in channel `ch`

## Example

```
1 chan request = [2] of { byte, chan};
2 chan reply[4] = [2] of { byte };
3
4 active [2] proctype Server() {
5     byte client;
6     chan replyChannel;
7     do
8         :: empty(request) ->
9             printf("No requests for server %d\n", _pid)
10        :: request ? client, replyChannel ->
11            printf("Client %d processed by server %d\n", client, _pid);
12            replyChannel ! _pid
13        od
14 }
15 active [4] proctype Client() {
16     byte server;
17     do
18         :: full(request) ->
19             printf("Client %d waiting for non-full channel\n", _pid)
20        :: request ! _pid, reply[_pid-2] ->
21            reply[_pid-2] ? server;
22            printf("Reply received from server %d by client %d\n", serv
23        od
24 }
```

## Example: Random Receive

- ▶ Suppose we want to replace the array of four reply channels with just one channel
- ▶ The message sent on the reply channel contains the server ID, as well as the ID of the client that was received from the request channel
- ▶ We must ensure that it is possible for a client to receive only messages meant for it
- ▶ A random receive statement (denoted  $??$ ) will remove the first message that matches the variables and values in the statement

## Example: Random Receive

```
1 chan request = [4] of { byte };
2 chan reply = [4] of { byte, byte };
3
4 active [2] proctype Server() {
5     byte client;
6 end:
7     do
8         :: request ? client ->
9             printf("Client %d processed by server %d\n", client, _pid);
10            reply ! _pid, client
11        od
12 }
13
14 active [4] proctype Client() {
15     byte server;
16     request ! _pid;
17     reply ?? server, eval(_pid);
18     printf("Reply received from server %d by client %d\n", server, _pid);
19 }
```

Note the use of `eval(_pid)` given that the value of `_pid` is only known at runtime



Channels in Promela

Synchronous Channels

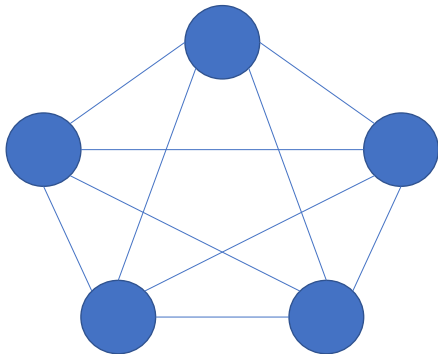
Asynchronous Channels

Distributed Mutual Exclusion

# Assumptions on our Distributed Model

- ▶ Nodes communicate through message passing with every other node
- ▶ Nodes execute one or more processes
- ▶ Nodes do not fail
- ▶ Channels deliver messages without error, though not necessarily in the order in which they were sent
- ▶ Transit time of messages is arbitrary but finite

Problem: given a set of distributed nodes connected as indicated below, devise an algorithm for mutual exclusion



---

<sup>1</sup>Ricart, Glenn; Agrawala, Ashok K. (1 January 1981). "An optimal algorithm for mutual exclusion in computer networks". *Communications of the ACM*. 24 (1): 9–17.

# Ricart-Agrawala (Outline)

1. Each node picks a **ticket** number
2. Sends a request with the number to all other nodes
3. Waits to receive a reply
4. Once it gets a reply from all other nodes, it enters the CS
5. A node only sends a reply to a request if the number is smaller than its own

This is best implemented with two processes per node

- ▶ main
- ▶ receive

# Preliminary Version

```
1 integer myNum := 0
2 set of node IDs deferred := empty set
```

## Main:

```
1 // non-CS
2 myNum = chooseNumber
3 for all other nodes N
4   send(request,N,myID,myNum)
5 await replies from all other nodes
6 // CS
7 for all nodes N in deferred
8   remove N from deferred
9   send(reply,N,myID)
```

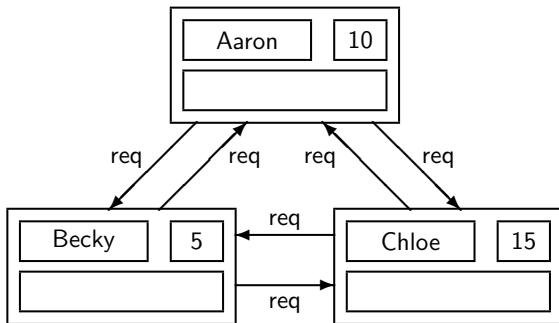
## Receive

```
1 int source, reqNum
2 receive(request,source,reqNum)
3 if reqNum < myNum
4   send(reply,source,myID)
5 else
6   add source to deferred
```

NB: Code in each process above runs inside an infinite loop

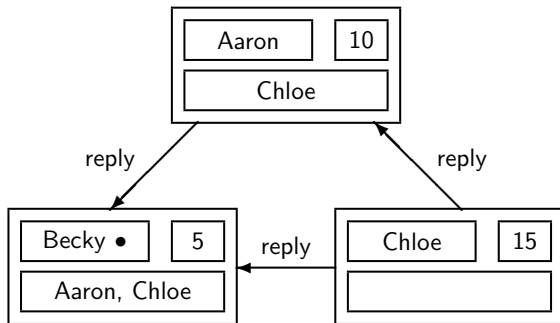
## Scenario of an Example

- ▶ All nodes have chosen ticket numbers and sent `request` messages to all other nodes



## Scenario of an Example

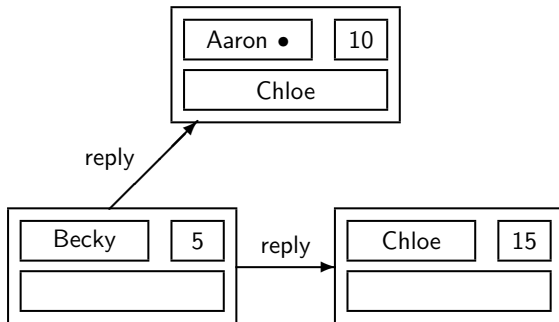
- ▶ Result of executing the **receive** process of each node



- ▶ Note the virtual queue:  $\text{Becky} \leftarrow \text{Aaron} \leftarrow \text{Chloe}$
- ▶ Becky executes her CS (indicated with the bullet)

## Scenario of an Example

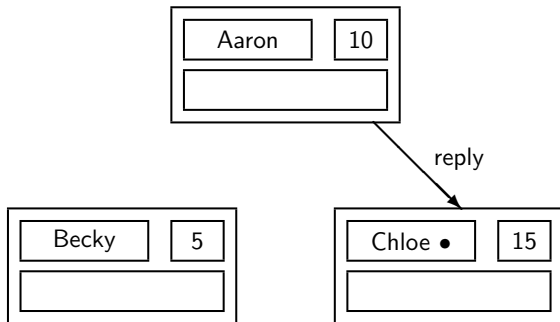
- ▶ After completing her CS, Becky sends the two deferred reply messages to Aaron and Chloe
- ▶ Aaron now has both replies and can execute his CS





## Scenario of an Example

- Upon completion Aaron sends a `reply` message to Chloe who can now enter her CS



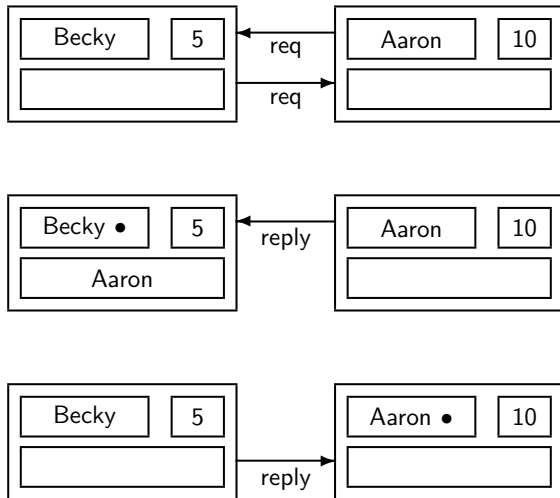
# Equal Ticket Numbers

- ▶ Several nodes could choose the same number
- ▶ We break symmetry using the ID
- ▶ The **Receive** process is modified as follows:

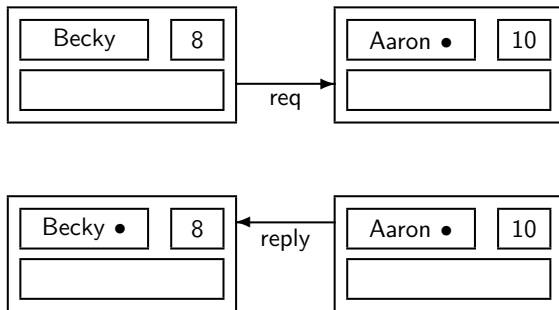
```
1 int source, reqNum
2 receive(request, source, reqNum)
3 if (reqNum < myNum) || ((reqNum == myNum) && (source < myId))
4     send(reply, source, myID)
5 else
6     add source to deferred
```

## Choosing Ticket Numbers

There is still a problem with our current algorithm



## Choosing Ticket Numbers



# Choosing Ticket Numbers

## Main:

```
1 // non-CS
2 myNum = highestNum + 1
3 for all other nodes N
4     send(request, N, myID, myNum)
5 await replies from all other nodes
6 // CS
7 for all nodes N in deferred
8     remove N from deferred
9     send(reply, N, myID)
```

## Receive

```
1 int source, reqNum
2 receive(request, source, reqNum)
3 highestNum = max(highestNum, reqNum)
4 if reqNum < myNum
5     send(reply, source, myID)
6 else
7     add source to deferred
```

# Quiescent Nodes

- ▶ What if a node N does not want to enter its CS?
- ▶ N will never send a reply since its initial value of `myNum` is 0
- ▶ Solution:
  - ▶ We add a flag `requestCS`
  - ▶ **Main** process sets before choosing a ticket number and then resets it after exiting the CS
  - ▶ We update the **receive** accordingly

# Quiescent Nodes

```
1 int myNum = 0
2 set of node IDs deferred = empty set
3 int highestNum = 0
4 boolean requestCS = false
```

## Main:

```
1 while (true) {
2   // non-CS
3   requestCS := true
4   myNum := highestNum + 1
5   for all other nodes N
6     send(request, N, myID, myNum)
7   await replies from all other nodes
8   // CS
9   requestCS := false
10  for all nodes N in deferred
11    remove N from deferred
12    send(reply, N, myID)
13 }
```

## Receive

```
1 int source, requestedNum
2 while (true) {
3   receive(request, source, requestNum)
4   highestNum := max(highestNum, requestNum)
5   if not requestCS or requestedNum == myNum
6     send(reply, source, myID)
7   else
8     add source to deferred
9 }
```

## Additional Comments

- ▶ What happens if a node fails?
- ▶ Does performance improve if there is no contention?
- ▶ If all nodes enter their CSs once, how many total number of messages were sent?



# R-A in Promela

```
1 init {  
2     atomic {  
3         int i;  
4         for (i : 0 .. NPROCS-1){  
5             run Main(i);  
6             run Receive(i);  
7         }  
8     }  
9 }
```

Channel declaration:

```
1 mtype={request, reply};  
2 chan ch[NPROCS]=[NPROCS] of {mtype, byte, byte};
```

```

1  proctype Main(byte myID) {
2      do ::
3          atomic {
4              requestCS[myID] = true ;
5              myNum[myID] = highestNum[myID] + 1;
6          }
7      int J;
8      for (J : 0 .. NPROCS-1){
9          if
10             :: J != myID -> ch[J] ! request, myID, myNum[myID]
11             :: else
12             fi;
13     }
14     int K;
15     for (K : 0 .. NPROCS-2){
16         ch[myID] ?? reply, -, -;
17     }
18     /* critical_section */
19     requestCS[myID] = false;
20     byte N;
21     do
22         :: empty(deferred[myID]) -> break;
23         :: deferred[myID] ? N -> ch[N] ! reply, 0, 0
24     od
25 od
26 }

```

```

1 proctype Receive( byte myID ) {
2     byte reqNum;
3     byte source;
4
5 end2:
6     do ::
7         ch[myID] ?? request, source, reqNum;
8         highestNum[myID] = ((reqNum > highestNum[myID]) ->
9             reqNum : highestNum[myID]);
10        atomic {
11            if
12                :: requestCS[myID] &&
13                    ( (myNum[myID] < reqNum) ||
14                      ( (myNum[myID] == reqNum) &&
15                        (myID < source) ) )
16                ->
17                    deferred[myID] ! source /* I have priority */
18            :: else ->
19                ch[source] ! reply,0,0 /* source has priority */
20            fi
21        }
22    od
23 }

```