

# Model-Checking

CS511

# Program Correctness

## Model-Checking

### Introduction to Promela

### Model-Checking: Stating properties within the model

- Assertions

- Non-Progress Cycles

- End States

### Model-Checking: Stating Properties Outside the Model

# Program Correctness

Main approaches to demonstrating that a program does what it's supposed to do:

1. Testing
2. Deductive verification
3. Model-checking

# Testing

- ▶ Fast and simple way to detect errors
- ▶ Can never be **sure** there are no defects (cannot cover all the cases) – maybe tests weren't comprehensive enough  
*Testing shows the presence, not the absence of bugs<sup>1</sup>*

## Testing Concurrent Programs

- ▶ More difficult since we would like to test all interleavings
- ▶ But since interleaving is controlled by OS scheduler, user cannot arrange arbitrary interleavings
- ▶ Consequence: **very** few of possible interleavings are tested

---

<sup>1</sup>Dijkstra (1969) J.N. Buxton and B. Randell, eds, Software Engineering Techniques, April 1970, p. 16. Report on a conference sponsored by the NATO Science Committee, Rome, Italy, 27–31 October 1969.

# Proving Programs Correct

- ▶ Holy Grail of computer science
- ▶ Using special **specification language**, describe
  1. State of program's variables
  2. How each programming language statement uses variables
- ▶ Specification language is mixture of mathematics & programming language

# How to Prove a Program Correct

## Hoare Triples

$$\llbracket A \rrbracket P \llbracket B \rrbracket$$

- ▶  $P$  program
- ▶  $A$  precondition
- ▶  $B$  postcondition
- ▶  $A$  and  $B$  are predicate logic formulae over an extended first-order language

# Example

```
1  y:=1;  
2  z:=0;  
3  while (z!= x) {  
4      z:=z+1;  
5      y:=y*z  
6  }
```

## Assertion

- ▶ Using hoare triples:  $\llbracket x > 0 \rrbracket P \llbracket y = z! \wedge z = x \rrbracket$
- ▶ In prose: Under any state  $\sigma$  such that  $x > 0$ , if  $P$  terminates in a state  $\rho$ , then  $\rho$  satisfies  $y = z! \wedge z = x$

## Provable Assertion

- ▶ Prove  $\llbracket x > 0 \rrbracket P \llbracket y = z! \wedge z = x \rrbracket$  in some deductive proof system

# Sample Deductive Proof System for Partial Correctness

$$\frac{\llbracket A \rrbracket C_1 \llbracket B \rrbracket \quad \llbracket B \rrbracket C_2 \llbracket C \rrbracket}{\llbracket A \rrbracket C_1; C_2 \llbracket C \rrbracket} \text{ (COMPOSITION)}$$

$$\frac{}{\llbracket A\{x/E\} \rrbracket x := E \llbracket A \rrbracket} \text{ (ASSIGNMENT)}$$

$$\frac{\llbracket A \wedge B \rrbracket C_1 \llbracket D \rrbracket \quad \llbracket A \wedge \neg B \rrbracket C_2 \llbracket D \rrbracket}{\llbracket A \rrbracket \text{if } B \text{ then } \{C_1\} \text{ else } \{C_2\} \llbracket D \rrbracket} \text{ (CONDITIONAL)}$$

$$\frac{A \rightarrow A' \quad \llbracket A' \rrbracket P \llbracket B' \rrbracket \quad B' \rightarrow B}{\llbracket A \rrbracket P \llbracket B \rrbracket} \text{ (IMPLICATION)}$$

$$\frac{\llbracket A \wedge B \rrbracket C \llbracket A \rrbracket}{\llbracket A \rrbracket \text{while } B \{C\} \llbracket A \wedge \neg B \rrbracket} \text{ (WHILE-PARTIAL)}$$



# Example of Partial Correctness Proof

$$\boxed{\llbracket x > 0 \rrbracket y := 1; z := 0; \text{while } (z \neq x) \{ z := z + 1; y := y * z \} \llbracket y = z! \wedge z = x \rrbracket}$$

$$\frac{}{\llbracket y * (z + 1) = (z + 1)! \rrbracket z := z + 1 \llbracket y * z = z! \rrbracket}$$

$$\frac{}{\llbracket y = z! \wedge z \neq x \rrbracket z := z + 1 \llbracket y * z = z! \rrbracket}$$

$$\frac{}{\llbracket y * z = z! \rrbracket y := y * z \llbracket y = z! \rrbracket}$$

$$\frac{}{\llbracket y = z! \wedge z \neq x \rrbracket z := z + 1; y := y * z \llbracket y = z! \rrbracket}$$

$$\frac{}{\llbracket y = z! \rrbracket Q \llbracket y = z! \wedge z = x \rrbracket}$$

$$Q = \text{while } (z \neq x) \{ z := z + 1; y := y * z \}.$$

$$\frac{}{\llbracket 1 = 0! \rrbracket y := 1 \llbracket y = 0! \rrbracket}$$

$$\frac{}{\llbracket y = 0! \rrbracket z := 0 \llbracket y = z! \rrbracket}$$

$$\frac{}{\llbracket x > 0 \rrbracket y := 1; z := 0; \llbracket y = z! \rrbracket}$$

$$\frac{}{\llbracket y = z! \rrbracket Q \llbracket y = z! \wedge z = x \rrbracket}$$

$$\frac{}{\llbracket x > 0 \rrbracket y := 1; z := 0; Q \llbracket y = z! \wedge z = x \rrbracket}$$

# Drawbacks of Program Proof

- ▶ Proving that arbitrary program  $X$  has property  $Y$  is undecidable
- ▶ Precisely specifying all of program's intended actions is notoriously hard
  - ▶ Doing such a detailed spec & associated proofs usually much harder than writing & testing the program!
- ▶ Dynamic memory management (heap) is difficult to reason about
- ▶ Concurrency is even more difficult to reason about
  - ▶ See well-known books by Manna and Pnueli (1992,1995) or text by Apt et al (2009)

# Research in Program Proof is Active

- ▶ Still too complicated for realistic programs/languages
- ▶ But it is growing fast!
  - ▶ The Atelier B system was used to develop part of the embedded software of the Paris metro line 14 and other railroad-related systems
  - ▶ Formally proved C compiler was developed using the Coq proof assistant (<http://compcert.inria.fr>)
  - ▶ Microsoft's hypervisor for highly secure virtualization was verified using VCC and the Z3 prover
  - ▶ L4-verified project developed a formally verified micro-kernel with high security guarantees, using analysis tools on top of the Isabelle/HOL proof assistant (<https://sel4.systems>)
  - ▶ <https://deepspec.org/main>
  - ▶ Facebook's Infer tool based on Separation Logic  
<https://fbinfer.com>

Program Correctness

## Model-Checking

Introduction to Promela

Model-Checking: Stating properties within the model

- Assertions

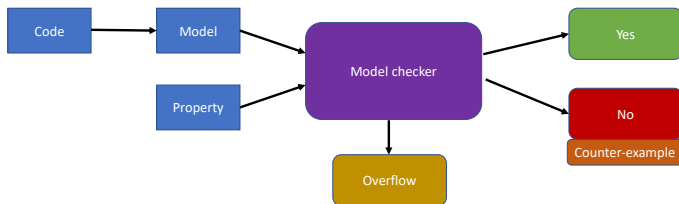
- Non-Progress Cycles

- End States

Model-Checking: Stating Properties Outside the Model

# Model-Checking

1. Develop a **model** of the program
  - ▶ This helps abstract away from unnecessary details
  - ▶ Provides a different way of thinking about your problem
  - ▶ Must be careful to not oversimplify
2. Prove properties of the model
  - ▶ Use tools to analyze the model



# Software Model Checking

Software model checking is the algorithmic analysis of programs to prove properties of their executions

- ▶ There is an extensive literature on this topic
- ▶ We only focus on one example (explicit state, automated, model-checking for temporal logic based on automata techniques)
- ▶ Survey:  
*Ranjit Jhala, Rupak Majumdar: Software model checking. ACM Comput. Surv. 41(4): 21:1-21:54 (2009)*

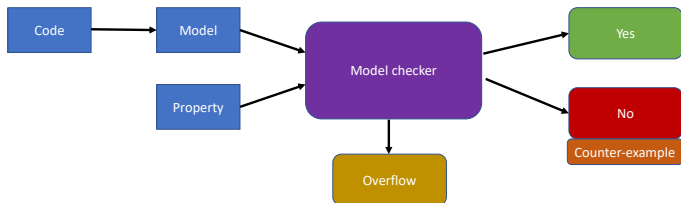
# Model-Checking

Two well-known [explicit-state](#) model-checkers for [concurrent/distributed computing](#)

- ▶ Spin (we'll use this one)
  - ▶ Developed by Gerard Holzmann (1980s)
  - ▶ Awarded ACM's Software System Award in 2001
  - ▶ Example of use:  
[Mars Code](#), Gerard J. Holzmann, Communications of the ACM, Vol. 57 No. 2, Pages 64-73, Feb 2014
- ▶ TLA+
  - ▶ Developed by Leslie Lamport (1994)
  - ▶ Example of use:  
[How Amazon Web Services Uses Formal Methods](#), Chris Newcombe, Tim Rath, Fan Zhang, Bogdan Munteanu, Marc Brooker, Michael Deardeuff, Communications of the ACM, Vol. 58 No. 4, Pages 66-73, April 2015

# Model-Checking: Plan

1. Introduction to Promela
2. Stating properties within the model
  - ▶ Assertion statements
  - ▶ Meta labels
    - ▶ end labels
    - ▶ progress labels
    - ▶ accept labels
3. Stating properties outside the model
  - ▶ Never claims
  - ▶ Temporal logic formulas

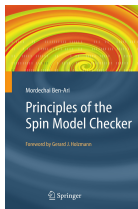




# Bibliography - Spin and Promela

## Tutorial on Promela and Spin:

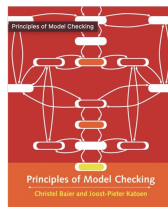
- ▶ Model Checking Concurrent Programs, Ian Barland, Moshe Vardi and John Greiner. Available here: <https://cnx.org> (search for title above) or download it here <https://cnx.org/exports/cd5745fd-3270-46ee-9b64-6e4843b67c43@3.4.pdf/model-checking-concurrent-programs-3.4.pdf>
- ▶ Principles of the Spin Model Checker, Mordechai Ben-Ari, Springer-Verlag London, 2008.



- ▶ Some slides: <http://spinroot.com/spin/Doc/SpinTutorial.pdf>

# Bibliography - Foundations of Model Checking

- ▶ Principles of Model Checking, Christel Baier and Joost-Pieter Katoen, MIT Press, April 2008



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Model-Checking: Stating properties within the model

- Assertions

- Non-Progress Cycles

- End States

Model-Checking: Stating Properties Outside the Model

# Promela

- ▶ Spin uses Promela (PROcess MEta LAnguage) for representing models
- ▶ The aim of Promela is to model concurrent and distributed systems
- ▶ We'll look at some examples of Promela code
- ▶ Spin can be used in two modes
  - ▶ Simulation mode: this runs the Promela model
  - ▶ Verification mode: this checks the Promela model

# Promela Models

Consist of:

- ▶ type declarations
- ▶ channel declarations
- ▶ variable declarations
- ▶ process declarations
- ▶ `init` process

Corresponds to a (usually large, but) finite transition system, so

- ▶ no unbounded data
- ▶ no unbounded channels
- ▶ no unbounded processes
- ▶ no unbounded process creation

```
1  mtype = {MSG, ACK};
2  chan toS = ...
3  chan toR = ...
4  bool flag;
5
6  proctype Sender() {
7      ... process body ...
8  }
9
10 proctype Receiver() {
11     ...
12 }
13
14 init {
15     ...
16 }
```

# Simple Sequential Program (eg1.pml)

```
1  active proctype P() {  
2      byte N = 10;  
3      byte sum = 0;  
4      byte i;  
5      for (i : 1 .. N) {  
6          sum = sum + i;  
7      }  
8      printf("The sum of the first %d numbers = %d\n",  
9          N, sum);  
10 }
```

- ▶ P is referred to as the process **type**
- ▶ **active** spawns a process type

# Simple Sequential Program

```
1  active proctype P() {
2      byte N = 10;
3      byte sum = 0;
4      byte i=1;
5      do
6          :: i > N -> break
7          :: else ->
8              sum = sum + i;
9              i++;
10     od;
11     printf("The sum of the first %d numbers = %d\n",
12           N, sum);
13 }
```

- ▶ Same as previous example only uses `do-od`

## Simple Interleaving (eg2.pml)

```
1 byte n = 0;
2
3 active proctype P() {
4     n = 1;
5     printf("Process P, n = %d\n", n);
6 }
7
8 active proctype Q() {
9     n = 2;
10    printf("Process Q, n = %d\n", n);
11 }
```



## Simple Interleaving with Race Condition (eg3.pm1)

```
1  byte      n = 0;
2
3  active proctype P() {
4      byte temp;
5      temp = n + 1;
6      n = temp;
7      printf("Process P, n = %d\n", n)
8  }
9
10 active proctype Q() {
11     byte temp;
12     temp = n + 1;
13     n = temp;
14     printf("Process Q, n = %d\n", n)
15 }
```

- ▶ Statements are atomic in Promela; interleaving occurs in an if- or do-statement (more later)

## Simple Interleaving with Race Condition (eg4.pm1)

- ▶ Same as previous example but shorter
- ▶ Note the use of [2] and \_pid (predefined variables start with an underscore)

```
1 byte    n = 0;
2
3 active [2] proctype P() {
4     byte temp;
5     temp = n + 1;
6     n = temp;
7     printf("Process P%d, n = %d\n", _pid, n);
8 }
```

## Simple Interleaving with Race Condition (eg5.pm1)

- ▶ `init` is the first process that is activated
- ▶ `run` instantiates a process
- ▶ Convention: run expressions are enclosed in `atomic` so that all processes are instantiated before any of them begins execution

```
1  byte n;
2
3  proctype P(byte id; byte incr) {
4      byte temp;
5      temp = n + incr;
6      n = temp;
7      printf("Process P%d, n = %d\n", id, n)
8  }
9
10 init {
11     n = 1;
12     atomic {
13         run P(1, 10);
14         run P(2, 15)
15     }
16 }
```

## Simple Interleaving with Race Condition (eg6.pm1)

- ▶ The body of a process consists of a sequence of **statements**. A statement is either
  - ▶ **executable**: the statement can be executed immediately.
  - ▶ **blocked**: the statement cannot be executed.
- ▶ An assignment is always **executable**.
- ▶ An expression is also a statement; it is executable if it evaluates to non-zero.
  - $2 < 3$       always executable
  - $x < 27$      only executable if value of  $x$  is smaller 27
  - $3 + x$        executable if  $x$  is not equal to  $-3$

## Simple Interleaving with Race Condition (eg6.pm1)

- ▶ `(_nr_pr == 1)` causes `init` to block until the expression is true (`_nr_pr` is number of processes currently running)

```
1  byte    n = 0;
2  proctype P() {
3      byte temp, i;
4      for (i:1..10) {
5          temp = n;
6          n=temp+1
7      }
8  }
9  init {
10     atomic {
11         run P();
12         run P()
13     }
14     (_nr_pr == 1);
15     printf("The value is %d\n", n);
16 }
```

# Model-Checking: Stating properties within the model

- ▶ Assertion statements
- ▶ Meta labels
  - ▶ end labels
  - ▶ progress labels
  - ▶ accept labels

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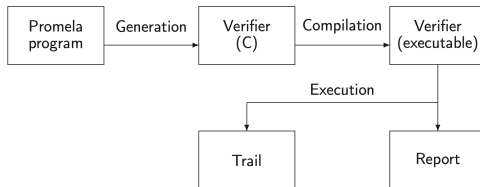
Model-Checking: Stating Properties Outside the Model

## Assert (eg8.pml)

```
1 byte    n = 0;
2 byte    finished = 0;
3
4 active [2] proctype P() {
5     byte  i = 1;
6     byte  temp;
7     for (i:1..10) {
8         temp = n;
9         n = temp + 1
10    }
11    finished++; /* Process terminates */
12 }
13
14 active proctype Finish() {
15     finished == 2; /* Wait for termination */
16     printf("n = %d\n", n);
17     assert (n > 2); /* Assert can't be 2 */
18 }
```



# Verification in Spin using Assertions



```
1 $ spin -a eg8.pml
2 $ gcc -o pan pan.c
3 $ ./pan
```

# Verification in Spin using Assertions

- ▶ Since there was an assertion violation, it also generates a trail counterexample (eg8.pml.trail)

```
1 pan:1: assertion violated (n>2) (at depth 88)
2 pan: wrote eg8.pml.trail
3
4 (Spin Version 6.4.8 -- 2 March 2018)
5 Warning: Search not completed
6   + Partial Order Reduction
7
8 Full statespace search for:
9   never claim           - (none specified)
10  assertion violations   +
11  acceptance cycles     - (not selected)
12  invalid end states    +
13
14 State-vector 36 byte (size of a state), depth
15 reached 92 (longest path), errors: 1
16 138429 states (total number of states), stored
17 87813 states, matched
18 226242 transitions (= stored+matched)
19 0 atomic steps
20 hash conflicts: 4500 (resolved)
21
22 Stats on memory usage (in Megabytes):
23 8.449 equivalent memory usage for states (stored*(State-vector + overhead))
24 5.565 actual memory usage for states (compression: 65.86%)
25 state-vector as stored = 14 byte + 28 byte overhead
26 128.000 memory used for hash table (-w24)
27 0.534 memory used for DFS stack (-m10000)
28 134.003 total actual memory usage (memory used)
```

# Inspecting the Trail

We can replay the counterexample in `eg8.pml.trail`

```
1 $ ./pan -r
```

```
1      1:      proc    1 (P) eg8.pml:7 (state 1) [i = 1]
2      2:      proc    1 (P) eg8.pml:7 (state 8) [((i<=10))]
3      3:      proc    0 (P) eg8.pml:7 (state 1) [i = 1]
4      4:      proc    0 (P) eg8.pml:7 (state 8) [((i<=10))]
5      5:      proc    1 (P) eg8.pml:8 (state 3) [temp = n]
6      6:      proc    0 (P) eg8.pml:8 (state 3) [temp = n]
7      7:      proc    1 (P) eg8.pml:9 (state 4) [n = (temp+1)]
8      8:      proc    1 (P) eg8.pml:7 (state 5) [i = (i+1)]
9      9:      proc    1 (P) eg8.pml:7 (state 8) [((i<=10))]
10     10:      proc    1 (P) eg8.pml:8 (state 3) [temp = n]
11     ...
```

## Critical Section - Revisiting Attempt III

```
1 boolean wantP = false;
2 boolean wantQ = false;
```

1	Thread.start { //P	1	Thread.start { // Q
2	while (true) {	2	while (true) {
3	// non-critical section	3	// non-critical section
4	wantP = true;	4	wantQ = true;
5	await (!wantQ);	5	await (!wantP);
6	// CRITICAL SECTION	6	// CRITICAL SECTION
7	wantP = false;	7	wantQ = false;
8	// non-critical section	8	// non-critical section
9	}	9	}
10	}	10	}

- ▶ **Mutex:** Yes (we'll prove this using spin; we introduce assertions using a ghost variable `critical`)
- ▶ **Absence livelock:** No
- ▶ **Free from starvation:** No

## Attempt III in Promela

```
1  bool wantP = false; bool wantQ = false;
2  byte critical = 0;
3
4  active proctype P() {
5      do ::
6          wantP = true;
7          do
8              :: wantQ==false -> break
9              :: else
10                 od;
11         critical++;
12         assert (critical == 1);
13         critical--;
14         wantP = false
15     od
16 }
17
18 // Similar with Q
```

## Critical Section

### ► We verify:

```
1 $ spin -a eg9.pml
2 $ gcc -o pan pan.c
3 $ ./pan
```

### ► Result:

```
1 $ ./pan
2
3 (Spin Version 6.5.1 -- 20 December 2019)
4   + Partial Order Reduction
5
6 Full statespace search for:
7   never claim                - (none specified)
8   assertion violations       +
9   acceptance cycles         - (not selected)
10  invalid end states        +
11
12 State-vector 28 byte, depth reached 12, errors: 0
```

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Assertions

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End States

Model-Checking: Stating Properties Outside the Model

# Non-Progress Cycles

- ▶ SPIN can check for some simple liveness properties without the need to use Linear Temporal Logic
- ▶ We designate states as progress states by using a label prefixed with `progress`
- ▶ An infinite computation that does not include infinitely many occurrences of a progress state is called a *non-progress cycle*



## Revisiting Attempt III

```
1 boolean wantP = false;
2 boolean wantQ = false;
```

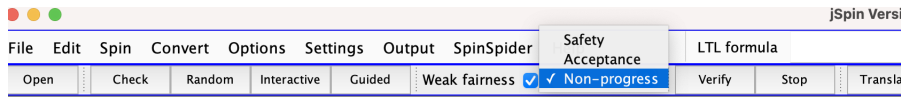
1	Thread.start { //P	1	Thread.start { // Q
2	while (true) {	2	while (true) {
3	// non-critical section	3	// non-critical section
4	wantP = true;	4	wantQ = true;
5	await (!wantQ);	5	await (!wantP);
6	// CRITICAL SECTION	6	// CRITICAL SECTION
7	wantP = false;	7	wantQ = false;
8	// non-critical section	8	// non-critical section
9	}	9	}
10	}	10	}

- ▶ Mutex: Yes
- ▶ Absence livelock: No (we'll prove this using spin)
- ▶ Free from starvation: No

## Attempt III in Promela

```
1  bool wantP = false; bool wantQ = false;
2
3  active proctype P() {
4      do ::
5          wantP = true;
6          do
7              :: wantQ==false -> break
8              :: else
9          od;
10 progress1:
11     wantP = false
12     od
13 }
14 active proctype Q() {
15     do ::
16         wantQ = true;
17         do
18             :: wantP==false -> break
19             :: else
20         od;
21 progress2:
22     wantQ = false
```

# We Verify...



```
pan:1: non-progress cycle (at depth 4) pan: wrote  
a4.pml.trail
```

This can be done in the command line

```
# spin -a file.pml  
# gcc -DNP -o pan pan.c  
# ./pan -l -f
```

To see the trail file (guided simulation):

```
# spin -p -t file.pml
```

## We Verify...

The trail

```
starting claim 2
spin: couldn't find claim 2 (ignored)
1 Q:1  1)  wantQ = 1
Process Statement          wantQ
0 P:1  1)  wantP = 1      1
<<<<<START OF CYCLE>>>>>
Process Statement          wantP          wantQ
1 Q:1  1)  else            1              1
0 P:1  1)  else            1              1
spin: trail ends after 8 steps
#processes: 2
    8: proc  1 (Q:1) a4.pml:19 (state 5)
    8: proc  0 (P:1) a4.pml:7 (state 5)
2 processes created
Exit-Status 0
```

## Revisiting Attempt IV

```
1  boolean wantP = false;
2  boolean wantQ = false;

1  Thread.start { //P          1  Thread.start { //Q
2      while (true) {          2      while (true) {
3          // non-critical section3      // non-critical section
4          wantP = true;        4          wantQ = true;
5          while (wantQ) {      5          while (wantP) {
6              wantP = false;    6              wantQ = false;
7              wantP = true;     7              wantQ = true;
8          }                    8          }
9          // CRITICAL SECTION  9          // CRITICAL SECTION
10         wantP = false;        10         wantQ = false;
11         // non-critical section11        // non-critical section
12     }                        12     }
13 }                            13 }
```

- ▶ Mutex: Yes
- ▶ Absence of livelock: No
- ▶ Free from starvation: No

## Revisiting Attempt IV

```
1  bool wantP = false, wantQ = false;
2
3  active proctype P() {
4      do
5          :: wantP = true;
6          do
7              :: wantQ -> wantP = false; wantP = true
8              :: else -> break
9          od;
10         wantP = false
11     od
12 }
13
14 active proctype Q() {
15     do
16         :: wantQ = true;
17         do
18             :: wantP -> wantQ = false; wantQ = true
19             :: else -> break
20         od;
21     wantQ = false
22     od
```

## Revisiting Attempt IV

- ▶ Check that there is no deadlock using spin
- ▶ Check that absence of livelock fails

# Starvation

- ▶ Livelock: computation continues but no process makes actual progress
- ▶ Starvation: computation continues, and some processes make progress but others don't.

```
1  int turn = 1;

Thread.start { // P      Thread.start { // Q
  while (true) {        while (true) {
    await (turn==1);    await (turn==2);
    turn = 2;          turn = 1;
  }                    }
}                      }
```

- ▶ Mutex: Yes
- ▶ Absence livelock: Yes
- ▶ Free from starvation: No (a process could remain indefinitely in its non-critical section)



# Starvation

- ▶ **Mutex:** Yes
- ▶ **Absence livelock:** Yes
- ▶ **Free from starvation:** No (a process could remain indefinitely in its non-critical section)

Show that Attempt I does not enjoy freedom from starvation

Here is how you code a simple infinite loop:

```
1 do
2 :: else
3 od;
```

## Exercise: Write Dekker's Algorithm in Promela

```
1  int turn = 1;
2  boolean wantP = false;
3  boolean wantQ = false;

1  Thread.start { //P      1  Thread.start { //Q
2    while (true) {        2    while (true) {
3      // non-CS           3      // non-CS
4      wantP = true        4      wantQ = true
5      while wantQ         5      while wantP
6        if (turn == 2) {  6        if (turn == 1) {
7          wantP = false   7          wantQ = false
8          await (turn==1) 8          await (turn==2)
9          wantP = true    9          wantQ = true
10         }               10         }
11       // CS             11       // CS
12       turn = 2          12       turn = 1
13       wantP = false     13       wantQ = false
14       // non-CS         14       // non-CS
15     }                   15     }
16   }                     16   }
```

Right to insist on entering is passed between the two processes

## Exercise: Write Dekker's Algorithm in Promela

```
1  bool    wantp = false, wantq = false;
2  byte    turn = 1;
3
4  active proctype P() {
5      do
6          :: wantp = true;
7          do
8              :: !wantq -> break;
9              :: else ->
10                 if
11                     :: (turn == 1) /* no statements, leaves if */
12                     :: (turn == 2) ->
13                         wantp = false;
14                         do
15                             :: turn==1 -> break
16                             :: else
17                                 od;
18                         wantp = true
19                 fi
20             od;
21             wantp = false;
22             turn = 2
```

Program Correctness

Model-Checking

Introduction to Promela

Model-Checking: Stating properties within the model

- Assertions

- Non-Progress Cycles

- End States

Model-Checking: Stating Properties Outside the Model

## Additional Comment on End States

```
1  byte request = 0;
2
3  active proctype Server1() {
4      do
5          :: request == 1 ->
6              printf("Service 1\n");
7              request = 0;
8      od
9  }
10 active proctype Server2() {
11     do
12         :: request == 2 ->
13             printf("Service 2\n");
14             request = 0;
15     od
16 }
17 active proctype Client() {
18     request = 1;
19     request == 0;
20     request = 2;
21     request == 0;
22 }
```

## Additional Comments on End States

- ▶ A process that does not terminate in its last instruction is said to be in an **invalid end state**
- ▶ Servers are always blocked at the guard of the do-statement waiting for it to become executable
- ▶ To avoid this: use a label to indicate that a control point is a valid end point, even if it is not the last instruction

```
1  active proctype Server1() {  
2      endserver:  
3      do  
4      :: request == 1 -> ...  
5      od  
6  }
```

# Model Checking: Stating Properties Outside the Model

Stating properties inside the model has various drawbacks:

- ▶ misplaced
- ▶ updating is error prone
- ▶ no separation of concerns (model vs. property of the model)
- ▶ many interesting properties not expressible via assertions

Model Checking: Stating Properties Outside the Model

- ▶ never claims
- ▶ temporal logic formulas

# Appendix

Installing Spin and jSpin

More Details on Promela Syntax



# Installing Spin

- ▶ Binaries: <https://github.com/nimble-code/Spin>
- ▶ OS X: Make executable (`chmod +x spin651_mac64`)

# Installing jSpin

<http://www.weizmann.ac.il/sci-tea/benari/software-and-learning-materials/jspin>

- ▶ Compile and create .jar file
- ▶ Configuration:
  - ▶ Create a jspin-5-0/bin directory
  - ▶ Add binary file for spin in jspin-5-0/bin (eg. spin651\_mac64).
  - ▶ Modify the following items in config.cfg:

```
SPIN=../bin/spin651_mac64
C_COMPILER=/usr/bin/gcc
DOT=/usr/local/bin/dot
```
- ▶ Somewhat outdated reference manual: <http://wwinf.u-szeged.hu/~gombas/HSRV/jspin-user.pdf>

# Emacs and Dot

- ▶ Emacs
  - ▶ Promela mode:  
<https://github.com/rudi/promela-mode>
  - ▶ Place in `~/.emacs.d/plugins`
  - ▶ Install by adding this to `.emacs`  

```
(add-to-list 'load-path "~/.emacs.d/plugins")  
(require 'promela-mode)
```
- ▶ Install dot
  - ▶ `brew install graphviz`

# Execution using Spin/jSpin

- ▶ From command line: `../bin/spin651_mac64 count.pml`
- ▶ Using jSpin
- ▶ Modes:
  - ▶ Random
  - ▶ Interactive
  - ▶ Guided: follows the error trail that was produced by an earlier verification (not presented yet) run

# Appendix

Installing Spin and jSpin

More Details on Promela Syntax

## Promela Summary

FEATURE	C	PROMELA
integers	char, short, int, long	byte, short, int
bit field	unsigned	unsigned
floats	float, double	NONE
boolean	int	bool
strings	char, char*	NONE
arrays	yes	1D & limited
operators	many	mostly same
if	as usual	similar to Erlang
loops	while, for, do	do, similar to if
output	printf	printf
input	scanf	NONE
functions	yes	NO
pointers	yes	NO
enum	enum	mtype
comments	/* */ and //	/* */
cpp	full	1-line #define, #include

# If Syntax

- ▶ “Guarded commands” wrapped inside “if ... fi”

```
1 disc = b*b - 4*a*c;  
2 if  
3 :: disc > 0 ->  
4     printf("two real roots\n")  
5 :: disc < 0 ->  
6     printf("no real roots\n")  
7 :: disc == 0 ->  
8     printf("duplicate real roots\n")  
9 fi
```

# If Semantics

- ▶ First: evaluate all guards
- ▶ Then:
  - ▶ If no guard true: statement blocks until at least one guard becomes true (which could happen due to action of some concurrent process)
  - ▶ If one guard true: execute its command(s)
  - ▶ If more than one guard true: execute command(s) of randomly chosen guard



# Else

- ▶ Guard consisting of “else” keyword is true if all other guards are blocked
- ▶ Example:

```
1  disc = b*b - 4*a*c;  
2  if  
3  :: else ->  
4      printf("two real roots\n")  
5  :: disc < 0 ->  
6      printf("no real roots\n")  
7  :: disc == 0 ->  
8      printf("duplicate real roots\n")  
9  fi
```

# Do Syntax

- ▶ Similar to if statement
- ▶ Example: compute GCD by repeated subtraction

```
1  /* assume x and y are initialized */
2  int a = x, b = y;
3  do  :: a > b -> a = a - b
4      :: b > a -> b = b - a
5      :: a == b -> break
6  od
7  printf("GCD(%d, %d) = %d\n", x, y, a);
```

- ▶ Notes:
  - No loop test; only way out is via break
  - Body consists of guarded commands
  - Some true guard is chosen at random
  - Block if no true guard

# Do Semantics

- ▶ Promela has no other type of loop
- ▶ Most common loop has only 2 guarded commands:

```
1 do
2     :: [exit test] -> break
3     :: else -> [body statements]
4 od
```

- ▶ This structure provides deterministic operation like:

```
1 while (not [exit test])
2     { [body statements] }
```

## Another Example

```
1  proctype P() {
2      int x = 15, y = 20;
3      int a = x, b = y;
4
5      do
6          :: a > b    ->    a = a - b
7          :: b > a    ->    b = b - a
8          :: a == b   ->    break
9      od
10     printf("GCD(%d, %d) = %d\n", x, y, a);
11 }
```

Note:

- ▶ `proctype P()` declares no-argument program P
- ▶ Can include arguments:

```
1      proctype P(int x, int y) {
2          int a = x, b = y;
3          etc. }
```

# Spawning a Process

- ▶ Can start processes using `run` operator: `run P(15, 20)`
- ▶ Also, can declare process with `active proctype`
  - ▶ Adding “active” means “define and run this program”
- ▶ To start two processes executing same code, use:  
`active [2] proctype P(int x, int y)`
- ▶ Can create an initial process that runs before any of the “proctype” processes
  - ▶ This process must be named `init`

# Predefined Variables

- ▶ `_pid` is process ID
- ▶ `_nr_pr` is number of active processes
- ▶ Examples:

```
1 printf("process %d: n goes from %d to %d\n", _pid, temp, n)
2
3 if
4 :: _nr_pr == 1 -> printf("at end n = %d\n", n);
5 fi
```

# Blocking Statements, I

- ▶ Concurrent programs must often wait for some event
- ▶ Possible to guard any statement
- ▶ This:

```
1  _nr_pr == 1 -> printf("at end n = %d\n", n)
```

is the same as:

```
1  if
2  :: _nr_pr == 1 -> printf("at end n = %d\n", n)
3  fi
```

## Blocking Statements, II

- ▶ “->” arrow is just syntactic sugar
- ▶ Can write expression by itself; if it doesn't evaluate to non-zero then program will block
- ▶ This:

```
1 _nr_pr == 1;  
2 printf("at end n = %d\n", n)
```

is the same as:

```
1 _nr_pr == 1 -> printf("at end n = %d\n", n)
```



# Atomicity, I

- ▶ Individual Promela statements are atomic
- ▶ Warning! In Promela, expressions are statements too (hence expressions are atomic)
- ▶ Example – here, division by zero is possible:

```
1  if
2      :: a != 0 -> c = b / a ;
3      :: else   -> c = b
4  fi
```

- ▶ In an if (and do) statement, interleaving may occur between the evaluation of the guard and the execution of the statement after the guard

## Atomicity, II

- ▶ It is tempting to regard the entirety of `a != 0 -> c = b / a` as atomic
- ▶ But it consists of two atomic parts, `a != 0` and `c = b / a`
- ▶ Remember that this:

```
1   a != 0 -> c = b / a
```

could be written as:

```
1   a != 0; /* may block */  
2   c = b / a
```

- ▶ The latter more obviously contains two atomic parts

# Atomicity, III

- ▶ To group statements together atomically use `atomic`

```
1 atomic {  
2     a != 0;      /* may block */  
3     c = b / a  
4 }
```

- ▶ If any statement within the atomic sequence blocks, atomicity is lost, and other processes may start executing statements.
- ▶ When the blocked statement becomes executable again, the execution of the atomic sequence can be resumed at any time (but it has to compete with other active processes)

# Atomic & Run

- ▶ `run` only starts a concurrent process
- ▶ `atomic` prevents execution of any other actions besides those in its body
- ▶ Therefore, to start a group of processes that should run concurrently:

```
1  atomic {  
2      run P1(...);  
3      run P2(...);  
4      ...  
5      run PN(...)  
6  }
```

- ▶ At conclusion of `atomic` block: all processes have been started but none is yet running

# Variable Size

- ▶ Use smallest integer variable that will fit the need
- ▶ E.g., for integers known to be small use “byte” (8 bits) instead of “int” (32 bits)
- ▶ Reason: “verification” simulates all possible values of variable