

Rabin Cryptosystem

1. Rabin cryptosystem is published in Jan. 1979 by Michael O. Rabin.
2. It is based on quadratic congruence.
3. It is Asymmetric key algo
4. Encryption is very simple

1. Key generation:

Step-1 : Choose two large distinct prime p, q

$$p \equiv q \equiv 3 \pmod{4}$$

Step-2 : Let $n = p * q$

Public key = n

Private key = p, q

2. Encryption:-

For encryption only public key n is used

Let Z_n , the plain text space and

$C = m^2 \pmod{n}$, m -plain text , C -cipher text

3. Decryption:

1. Compute under root $c \pmod{n}$

2. There are four square roots .out of which correct plain text is selected.

3. By adding some redundancy bits into plain text .we can recognize correct plain text.

Step:1 Using Euclidean algo find a & b

$$a*p+b*q=1$$

Step:2 Compute

$$r=C^{(p+1)/4} \bmod p$$

$$s=C^{(q+1)/4} \bmod q$$

$$x=(a*p*s+b*q*r) \bmod n$$

$$y=(a*p*s-b*q*r) \bmod n$$

Step 3: $m1=x$

$$m2=n-x$$

$$m3=y$$

$$m4=n-y$$

Example:

1. Let $p=7, q=11, m=5$

2. $n=p*q=7*11=77$ (public key)

3.private key=7,11

Encryption:

$$C = m^2 \bmod n$$

$$C = 52 \bmod 77$$

$$C = 25 \bmod 77$$

$$C = 25$$

Decryption:-

$$\text{Step:1} \quad a \cdot p + b \cdot q = 1$$

$$-3 \cdot 7 + 2 \cdot 11 = 1 \quad (a = -3, b = 2)$$

$$\text{Step-2} \quad r = C^{(p+1)/4} \bmod p$$

$$R = 25^2 \bmod 7$$

$$r = 2$$

$$\text{Step:-3} \quad s = C^{(q+1)/4} \bmod q$$

$$S = 25^3 \bmod 11$$

$$S = 5$$

$$\text{Step:4} \quad x = (a \cdot p \cdot s + b \cdot q \cdot r) \bmod n$$

$$X = (-3 \cdot 7 \cdot 5 + 2 \cdot 11 \cdot 2) \bmod 77$$

$$X = -61 \bmod 77$$

$$X = 16$$

$$\text{Step:5} \quad y=(a*p*s-b*q*r) \bmod n$$

$$y=149 \bmod 77$$

$$y=5$$

so

$$m1=16$$

$$m2=61$$

$$m3=5$$

$$m4=72$$

Security of Rabin System:

1. Secure as long as p & q large no
2. Rabin as secure as RSA.
3. It has been proven that any algorithm which decrypts a Rabin-encrypted value can be used to factor the modulus . Thus, Rabin decryption is at least as hard as the integer factorization problem, something that has not been proven for RSA. It is generally believed that there is no polynomial-time algorithm for factoring, which implies that there is no efficient algorithm for decrypting a Rabin-encrypted value without the private key .

