exp-1-ml

April 23, 2025

```
[2]: import numpy as np
[3]: X = \text{np.array}([[0, 0, 1, 1],
                  [0, 1, 0, 1]])
     W = np.array([1, 1])
                                            #Polar OR
     theta = 1
     Z = W@X
     y_pred = [int(i>=theta) for i in Z]
     print(y_pred)
    [0, 1, 1, 1]
[4]: X = np.array([[0, 0, 1, 1],
                  [0, 1, 0, 1]])
     W = np.array([1, 1])
     theta = 2
     Z = W@X
                                                      #Polar AND
     y_pred = [int(i>=theta) for i in Z]
     print(y_pred)
    [0, 0, 0, 1]
[5]: X = np.array([[-1, -1, 1, 1],
                  [-1, 1, -1, 1]])
     W = np.array([1, 1])
     theta = 0
                                                    #Bipolar OR
     Z = W@X
     y_pred = [int(i>=theta)*2-1 for i in Z]
     print(y_pred)
    [-1, 1, 1, 1]
[6]: X = np.array([[-1, -1, 1, 1],
                  [-1, 1, -1, 1]])
     W = np.array([1, 1])
                                             #Bipolar AND
     theta = 1
     Z = W@X
     y_pred = [int(i>=theta)*2-1 for i in Z]
```

	<pre>print(y_pred)</pre>
	[-1, -1, -1, 1]
[]:	
[]:	

mlp-backward-pass-2-layered-1

April 23, 2025

```
[7]: import numpy as np
     np.set_printoptions(precision=4)
     # Initialize weights
     W_0 = np.array([[1, 0, 1],
                     [-1, -1, 1]], dtype=float) # Hidden layer weights
     W_1 = np.array([[0, 1, -1]], dtype=float) # Output layer weights
     # Input and target
     X = np.array([[1, -1, 1],
                   [0, -1, 1]], dtype=float) # Shape: (2, 2)
     t = np.array([[0, 0, 1]], dtype=float) # Shape: (1, 2)
     # Hyperparameters
     f 1 = "Lin"
     f_2 = "ReLU"
     lr = 1
     MAX\_EPOCHS = 1
     # Activation Functions
     def USigmoid(x, direction='F'):
        fx = 1 / (1 + np.exp(-x))
        return fx if direction == 'F' else fx * (1 - fx)
     def BSigmoid(x, direction='F'):
        fx = (1 - np.exp(-x)) / (1 + np.exp(-x))
        return fx if direction == 'F' else 0.5 * (1 - fx ** 2)
     def TanH(x, direction='F'):
        fx = np.tanh(x)
        return fx if direction == 'F' else 1 - fx ** 2
     def ReLU(x, direction='F'):
        return np.maximum(0, x) if direction == 'F' else (x > 0).astype(float)
     def Lin(x, direction='F'):
        return x if direction == 'F' else np.ones_like(x)
```

```
# Wrapper for activation
def activation(Z, fcn="Lin", direction='F'):
    return np.array([globals()[fcn](z, direction) for z in Z]).reshape(-1, 1)
A_0 = \text{np.vstack}((\text{np.ones}((1, 1)), x.reshape(-1, 1)))
# Training loop
for ep in range(MAX_EPOCHS):
    print('\nEPOCH-', ep + 1, '=' * 80)
    for itr, (x, y) in enumerate(zip(X.T, t.T)):
        print(f'\nITER-\{itr + 1\} ' + '-' * 80)
        # Forward Pass: Input -> Hidden
        A_0 = x.reshape(-1, 1)
        # Conditionally add bias to A_O
        if W_0.shape[1] == A_0.shape[0] + 1:
            A_0 = \text{np.vstack}((\text{np.ones}((1, 1)), A_0)) + Add bias at the top
            print('Bias added to A_0')
        Z_1 = W_0 @ A_0
        A_1 = activation(Z_1, f_1)
        # Forward Pass: Hidden -> Output
        # Conditionally add bias to A 1
        if W_1.shape[1] == A_1.shape[0] + 1:
            A_1 = \text{np.vstack}((\text{np.ones}((1, 1)), A_1))  # Add bias at the top
            print('Bias added to A_1')
        Z_2 = W_1 @ A_1
        A_2 = activation(Z_2, f_2)
        print(f'A_0 (input):\n{A_0}')
        print(f'Z_1 (hidden pre-activation):\n{Z_1}')
        print(f'A_1 (hidden post-activation):\n{A_1}')
        print(f'Z_2 (output pre-activation):\n{Z_2}')
        print(f'A_2 (output post-activation):\n{A_2}')
       # Backward Pass: Output -> Hidden
        delta_2 = (A_2 - y.reshape(-1, 1)) * activation(Z_2, f_2, 'B')
        dW_1 = delta_2 @ A_1.T
        # Remove bias from W_1 if necessary
        if W_1.shape[1] == Z_1.shape[0] + 1:
            W_1_{no_bias} = W_1[:, 1:]
            print("Bias column removed from W_1 for backpropagation.")
```

```
else:
        W_1_no_bias = W_1

print(W_1_no_bias)

# Backward Pass: Hidden -> Input
delta_1 = (W_1_no_bias.T @ delta_2) * activation(Z_1, f_1, 'B')
dW_0 = delta_1 @ A_0.T

# Update weights
W_1 -= lr * dW_1
W_0 -= lr * dW_0

print(f'dW_1:\n{dW_1}')
print(f'dW_0:\n{dW_0}')
print(f'Updated W_1:\n{W_1}')
print(f'Updated W_0:\n{W_0}')
```

EPOCH- 1

```
ITER-1
_____
Bias added to A_0
Bias added to A_1
A_0 (input):
[[1.]
[1.]
 [0.1]
Z_1 (hidden pre-activation):
[[ 1.]
[-2.]]
A_1 (hidden post-activation):
[[ 1.]
[ 1.]
[-2.]]
Z_2 (output pre-activation):
[[3.]]
A_2 (output post-activation):
[[3.]]
Bias column removed from W_1 for backpropagation.
[[ 1. -1.]]
dW_1:
[[ 3. 3. -6.]]
dW 0:
[[ 3. 3. 0.]
```

```
[-3. -3. 0.]]
Updated W_1:
[[-3. -2. 5.]]
Updated W_0:
[[-2. -3. 1.]
 [ 2. 2. 1.]]
ITER-2
Bias added to A_0
Bias added to A_1
A_0 (input):
[[ 1.]
[-1.]
 [-1.]]
Z_1 (hidden pre-activation):
[[ 0.]
[-1.]]
A_1 (hidden post-activation):
[[ 1.]
[ 0.]
 [-1.]]
Z_2 (output pre-activation):
[[-8.]]
A_2 (output post-activation):
Bias column removed from W_1 for backpropagation.
[[-2. 5.]]
dW_1:
[[0. 0. 0.]]
dW_0:
[[0. 0. 0.]
[0. 0. 0.]]
Updated W_1:
[[-3. -2. 5.]]
Updated W_0:
[[-2. -3. 1.]
 [ 2. 2. 1.]]
TTER-3
Bias added to A_0
Bias added to A_1
A_0 (input):
[[1.]
[1.]
 [1.]]
Z_1 (hidden pre-activation):
```

```
[[-4.]
[ 5.]]
A_1 (hidden post-activation):
[[ 1.]
[-4.]
[ 5.]]
Z_2 (output pre-activation):
[[30.]]
A_2 (output post-activation):
[[30.]]
Bias column removed from W_1 for backpropagation.
[[-2. 5.]]
dW_1:
[[ 29. -116. 145.]]
dW_0:
[[-58. -58. -58.]
[145. 145. 145.]]
Updated W_1:
[[ -32. 114. -140.]]
Updated W_0:
[[ 56. 55.
              59.]
 [-143. -143. -144.]]
```

gradient-tape-activations7

April 23, 2025

```
[]: # import numpy as np
     # # Initial weights
     \# W_0 = np.array([[1, 0, 1]], dtype=float)
     # print("Initial W_0 shape:", W_0.shape) # (1, 3)
     # # Targets
     \# \ t = np.array([[1 ,-1 ,-1]], \ dtype=float)
     # # Inputs
     \# X = np.array([
          [1, 1, -1],
          [0, 1, 1]
     # ], dtype=float)
     # print("X shape:", X.shape) # (2, 3)
     # # Activation function name
     # f_1 = "Lin"
     # # Learning rate
     # lr = 0.1
     # # Activation Functions
     # def USigmoid(x, direction):
         if direction == 'F':
               return 1 / (1 + np.exp(-x))
     #
           else: # derivative
               fx = USigmoid(x, 'F')
               return fx * (1 - fx)
     # def BSigmoid(x, direction):
     #
           if direction == 'F':
     #
               return (1 - np.exp(-x)) / (1 + np.exp(-x))
     #
           else:
              fx = BSigmoid(x, 'F')
               return 0.5 * (1 - fx ** 2)
```

```
# def ReLU(x, direction):
     if direction == 'F':
          return np.maximum(0, x)
      else:
          return float(x > 0)
# def Lin(x, direction):
     if direction == 'F':
          return x
      else:
          return 1
# # Activation wrapper
# def activation(Z, fcn="Lin", direction='F'):
      Z = np.atleast_1d(Z)
      return np.array([globals()[fcn](z, direction) for z in Z])
# # Training loop
# MAX_EPOCH = 1
# # Pad bias term to input
# print('Pad bias at top of input')
\# A_0 = np.vstack((np.ones((1, X.shape[1])), X))
# print(A 0)
# for ep in range(MAX EPOCH):
     print('\nEPOCH-', ep + 1, '=' * 80)
     for itr, (x, y) in enumerate(zip(A_0.T, t.T)):
#
          print('\nITER-', itr + 1, '-' * 80)
#
          print(f'\{y = \}')
          # Forward pass
          print('Input -> Output')
          Z_1 = W_0 \otimes x
#
          print(f'\{Z_1 = \}')
          A_1 = activation(Z_1, f_1)
#
          print(f'\{A_1 = \}')
          # Backward pass
          print('\nOutput -> Input')
          Error = 0.5 * (A_1 - y) ** 2
#
          print(f'{Error = }')
          dE_dW = (A_1 - y) * activation(Z_1, f_1, 'B') * x
#
          print(f'\{dE_dW = \}')
#
          # Weight update
```

```
W_{-}O = W_{-}O - lr * dE_{-}dW
           print(f'{W_0 = }')
#
Initial W_0 shape: (1, 3)
X shape: (2, 3)
Pad bias at top of input
[[ 1. 1. 1.]
[ 1. 1. -1.]
 [ 0. 1. 1.]]
EPOCH- 1
ITER- 1
y = array([1.])
Input -> Output
Z_1 = array([1.])
A_1 = array([1.])
Output -> Input
Error = array([0.])
dE_dW = array([0., 0., 0.])
W_0 = array([[1., 0., 1.]])
ITER- 2
y = array([-1.])
Input -> Output
Z_1 = array([2.])
A_1 = array([2.])
Output -> Input
Error = array([4.5])
dE_dW = array([3., 3., 3.])
W_0 = array([[ 0.7, -0.3, 0.7]])
ITER- 3
y = array([-1.])
Input -> Output
Z_1 = array([1.7])
A_1 = array([1.7])
Output -> Input
Error = array([3.645])
dE_dW = array([2.7, -2.7, 2.7])
```

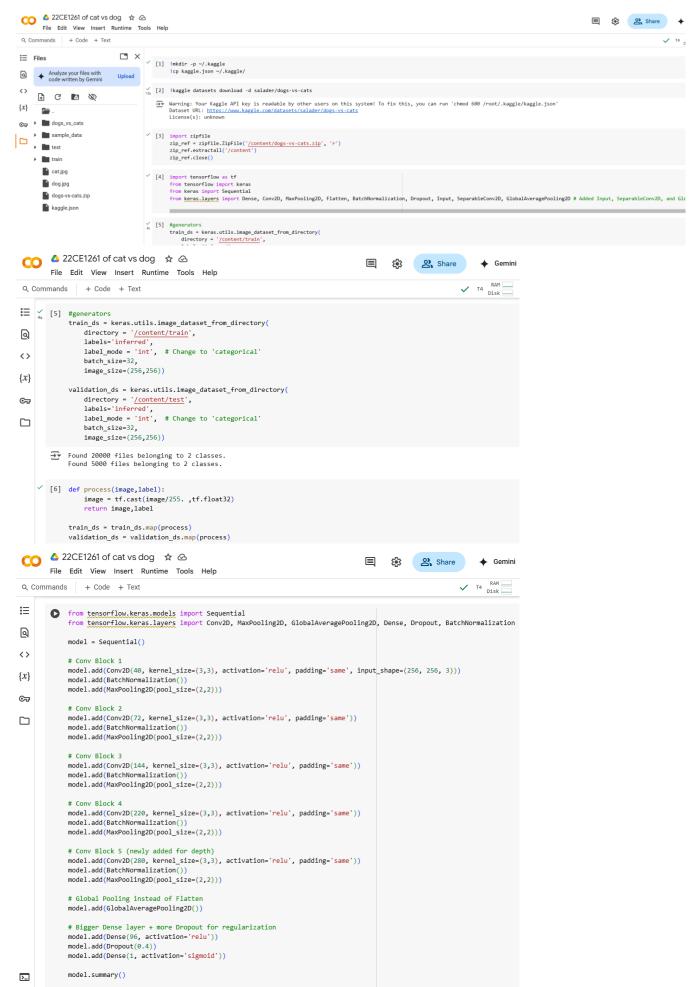
```
W_0 = array([[ 0.43, -0.03, 0.43]])
```

```
[4]: import numpy as np
     import tensorflow as tf
     # Initial weights
     W_0 = tf.Variable([[1.0, 0.0, 1.0]], dtype=tf.float32)
     print("Initial W_0 shape:", W_0.shape)
     # Targets
     t = tf.constant([[1.0, -1.0, -1.0]], dtype=tf.float32)
     # Inputs
     X = tf.constant([
         [1.0, 1.0, -1.0],
         [0.0, 1.0, 1.0]
     ], dtype=tf.float32)
     print("X shape:", X.shape)
     # Activation function name
     f_1 = "Lin"
     # Learning rate
     lr = 0.1
     # Activation Functions
     def USigmoid(x):
         return tf.math.sigmoid(x)
     def USigmoid_deriv(x):
         fx = tf.math.sigmoid(x)
         return fx * (1 - fx)
     def BSigmoid(x):
         return (1 - tf.exp(-x)) / (1 + tf.exp(-x))
     def BSigmoid_deriv(x):
         fx = BSigmoid(x)
         return 0.5 * (1 - tf.square(fx))
     def ReLU(x):
         return tf.nn.relu(x)
     def ReLU_deriv(x):
         return tf.cast(x > 0, tf.float32)
     def Lin(x):
```

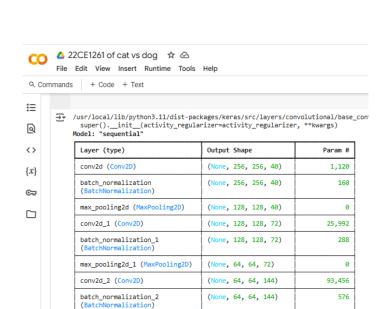
```
return x
def Lin_deriv(x):
    return tf.ones_like(x)
# Activation function dictionary
activation_map = {
    "USigmoid": (USigmoid, USigmoid_deriv),
    "BSigmoid": (BSigmoid, BSigmoid deriv),
    "ReLU": (ReLU, ReLU_deriv),
    "Lin": (Lin, Lin_deriv),
}
# Select activation function and its derivative
activation_fn, activation_deriv = activation_map[f_1]
# Add bias term to input (pad bias row at the top)
A_0 = \text{np.vstack}((\text{np.ones}((1, X.shape[1])), X))
A_0 = tf.constant(A_0, dtype=tf.float32)
# Training loop
MAX\_EPOCH = 1
# Epoch loop
# Epoch loop
for ep in range(MAX EPOCH):
    print(f"\nEPOCH-\{ep + 1\} " + "=" * 80)
    for itr, (x, y) in enumerate(zip(tf.transpose(A_0), tf.transpose(t))):
        print(f"\nITER-\{itr + 1\} " + "-" * 80)
        # Forward pass
        Z_1 = tf.matmul(W_0, tf.reshape(x, [-1, 1]))
        A_1 = activation_fn(Z_1)
        print(f"Target (y): {y.numpy()[0]:.2f}")
        print(f"Z_1 (Weighted sum): {Z_1.numpy()[0][0]:.4f}")
        print(f"A_1 (Activated output): {A_1.numpy()[0][0]:.4f}")
        # Error and gradient
        Error = 0.5 * (A_1 - y) ** 2
        dE_dZ = (A_1 - y) * activation_deriv(Z_1)
        dE_dW = tf.matmul(dE_dZ, tf.reshape(x, [1, -1]))
        print(f"Error: {Error.numpy()[0][0]:.4f}")
        print(f"dE_dW (Gradients): {np.round(dE_dW.numpy(), 4)}")
```

```
# Update weights
        W_0.assign_sub(lr * dE_dW)
        print(f"Updated W_0: {np.round(W_0.numpy(), 4)}")
Initial W_0 shape: (1, 3)
X shape: (2, 3)
EPOCH-1
ITER-1
Target (y): 1.00
Z_1 (Weighted sum): 1.0000
A_1 (Activated output): 1.0000
Error: 0.0000
dE_dW (Gradients): [[0. 0. 0.]]
Updated W_0: [[1. 0. 1.]]
ITER-2
Target (y): -1.00
Z_1 (Weighted sum): 2.0000
A_1 (Activated output): 2.0000
Error: 4.5000
dE_dW (Gradients): [[3. 3. 3.]]
Updated W_0: [[ 0.7 -0.3 0.7]]
ITER-3
Target (y): -1.00
Z_1 (Weighted sum): 1.7000
A_1 (Activated output): 1.7000
Error: 3.6450
dE_dW (Gradients): [[ 2.7 -2.7 2.7]]
Updated W_0: [[ 0.43 -0.03 0.43]]
```









(None, 32, 32, 144)

(None, 32, 32, 220)

(None, 32, 32, 220)

(None, 16, 16, 220)

(None, 16, 16, 280)

(None, 16, 16, 280)

(None, 8, 8, 280)

(None, 280)

(None, 96)

(None, 96)

285.340

554,680

1,120

880

ø

0

0

0 97

26,976

dense 1 (Dense) (None, 1) Total params: 990,685 (3.78 MB) Trainable params: 989,173 (3.77 MB) Non-trainable params: 1,512 (5.91 KB)

max_pooling2d_2 (MaxPooling2D)

max pooling2d 3 (MaxPooling2D)

max_pooling2d_4 (MaxPooling2D)

conv2d 3 (Conv2D)

conv2d_4 (Conv2D)

batch_normalization_4

global_average_pooling2d
(GlobalAveragePooling2D)

dense (Dense)

dropout (Dropout)

batch_normalization_3

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4 6

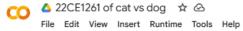
>_

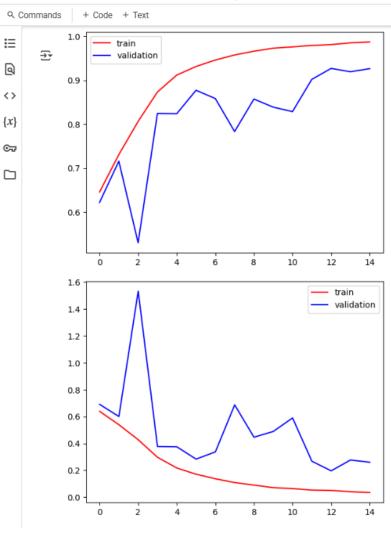
```
File Edit View Insert Runtime Tools Help
 Q Commands + Code + Text
E | [8] model.compile(optimizer='adam', loss='binary_crossentropy', metrics=['accuracy'])
Q
    history= model.fit(train_ds,epochs=15,validation_data=validation_ds)
        ∓ Epoch 1/15
             625/625 —
Epoch 2/15
625/625 —
Epoch 3/15
625/625 —
{x}
                                         - 98s 132ms/step - accuracy: 0.6086 - loss: 0.6955 - val_accuracy: 0.6216 - val_loss: 0.6908
                                     ----- 121s 118ms/step - accuracy: 0.7172 - loss: 0.5547 - val_accuracy: 0.7156 - val_loss: 0.6006
©7
                                       Epoch 4/15
625/625 —
                                         - 71s 113ms/step - accuracy: 0.8648 - loss: 0.3143 - val_accuracy: 0.8244 - val_loss: 0.3770
             Epoch 5/15
625/625 —
Epoch 6/15
625/625 —
                                         -- 82s 113ms/step - accuracy: 0.9073 - loss: 0.2286 - val_accuracy: 0.8238 - val_loss: 0.3751
                                       --- 71s 113ms/step - accuracy: 0.9282 - loss: 0.1798 - val_accuracy: 0.8772 - val_loss: 0.2834
             Epoch 7/15
625/625 —

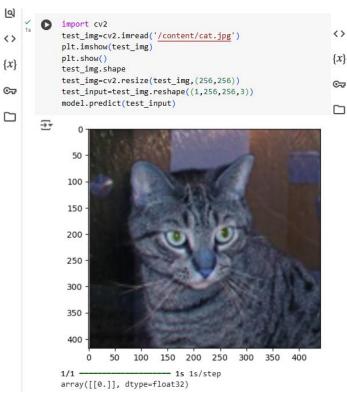
    71s 114ms/step - accuracy: 0.9445 - loss: 0.1435 - val accuracy: 0.8584 - val loss: 0.3372

             Epoch 8/15
625/625
                                         - 71s 114ms/step - accuracy: 0.9565 - loss: 0.1116 - val_accuracy: 0.7832 - val_loss: 0.6871
             625/625 —
Epoch 9/15
625/625 —
Epoch 10/15
                                    ------ 75s 120ms/step - accuracy: 0.9660 - loss: 0.0919 - val_accuracy: 0.8572 - val_loss: 0.4465
             625/625
                                       Epoch 11/15
             Epoch 11/15
625/625 —
Epoch 12/15
625/625 —
Epoch 13/15
625/625 —
Epoch 14/15
                                       - 79s 114ms/step - accuracy: 0.9796 - loss: 0.0528 - val_accuracy: 0.9020 - val_loss: 0.2678
                                         -- 82s 114ms/step - accuracy: 0.9805 - loss: 0.0514 - val_accuracy: 0.9270 - val_loss: 0.1962
             625/625
                                         - 86s 120ms/step - accuracy: 0.9842 - loss: 0.0452 - val_accuracy: 0.9194 - val_loss: 0.2767
             Epoch 15/15
625/625
                                          - 77s 113ms/step - accuracy: 0.9879 - loss: 0.0343 - val_accuracy: 0.9264 - val_loss: 0.2602
    [10] import matplotlib.pyplot as plt plt.plot(history.history['accuracy'],color='red',label='train') plt.plot(history.history['val_accuracy'],color='blue',label='validation') plt.legend() plt.show()
             plt.plot(history.history['loss'],color='red',label='train')
plt.plot(history.history['val_loss'],color='blue',label='validation')
plt.legend()
plt.show()
```

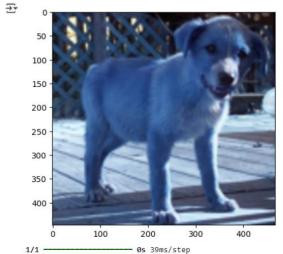












array([[1.]], dtype=float32)