

AES – Advanced Encryption Standard

The AES Cipher - Rijndael

- designed by Vincent Rijmen and Joan Daemen in Belgium (UCL)
- Characteristics
 - an iterative rather than feistel cipher
 - processes data as block of 4 columns of 4 bytes
 - operates on entire data block in every round
 - 128/192/256 bit keys, 128 bit data
 - expanded key size of 44, 52 or 60 words
 - algorithm is Not a Feistel structure
 - processes entire data block in parallel
 - designed to be
 - resistant against known attacks
 - speed and code compactness on many CPUs
 - design simplicity

The AES Cipher vrs Rijndael

- AES is not precisely Rijndael
- Rijndael
 - supports a larger range of block and key sizes
 - the key and block sizes in any multiple of 32 bits, with a minimum of 128 bits and a maximum of 256 bits.
- AES
 - has a fixed block size of 128 bits and a key size of 128, 192 or 256 bits,

AES inputs

Input

State

32	88	31	e0
43	5a	31	37
f6	30	98	07
a8	8d	a2	34



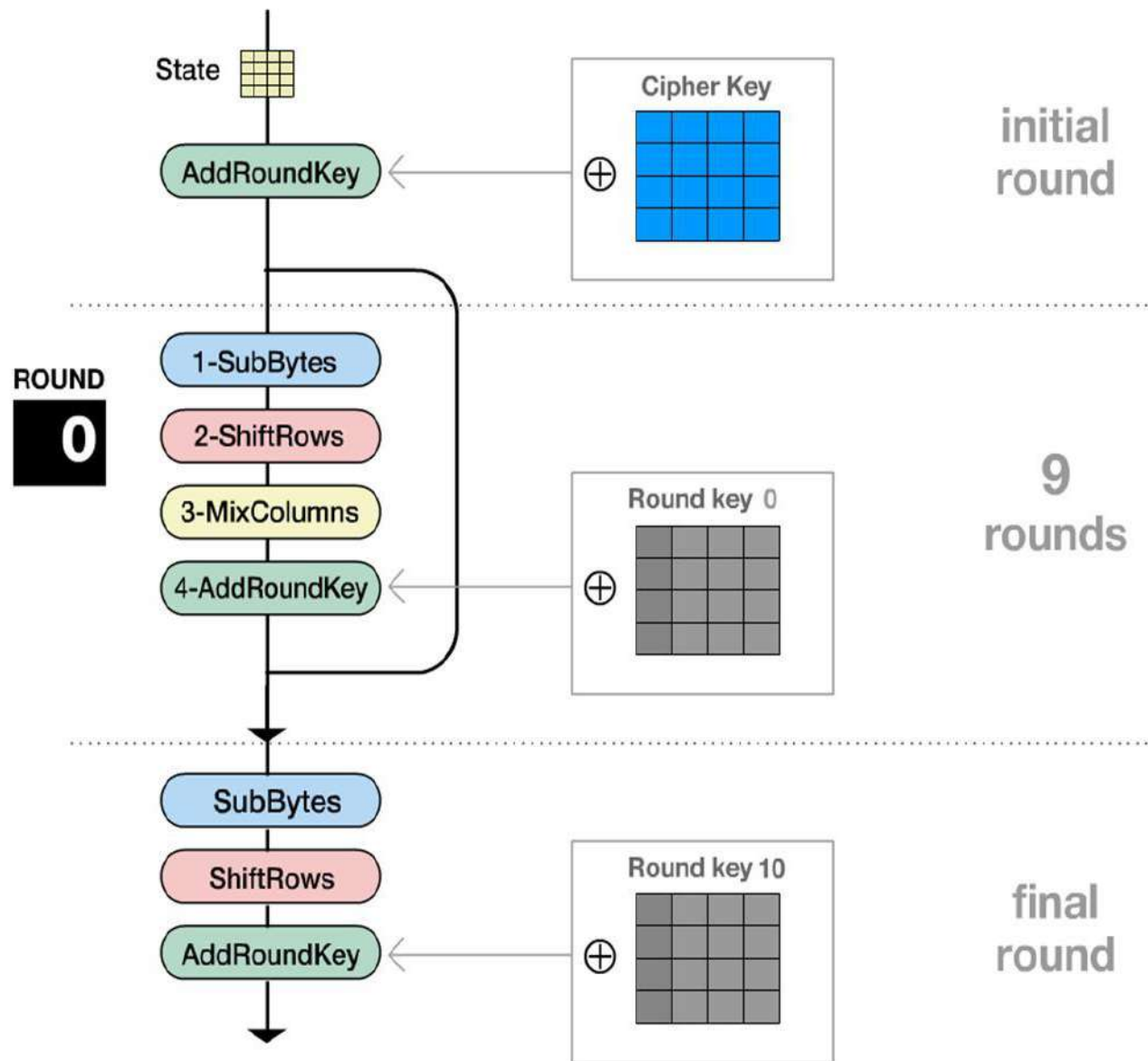
to
Encryption
Process

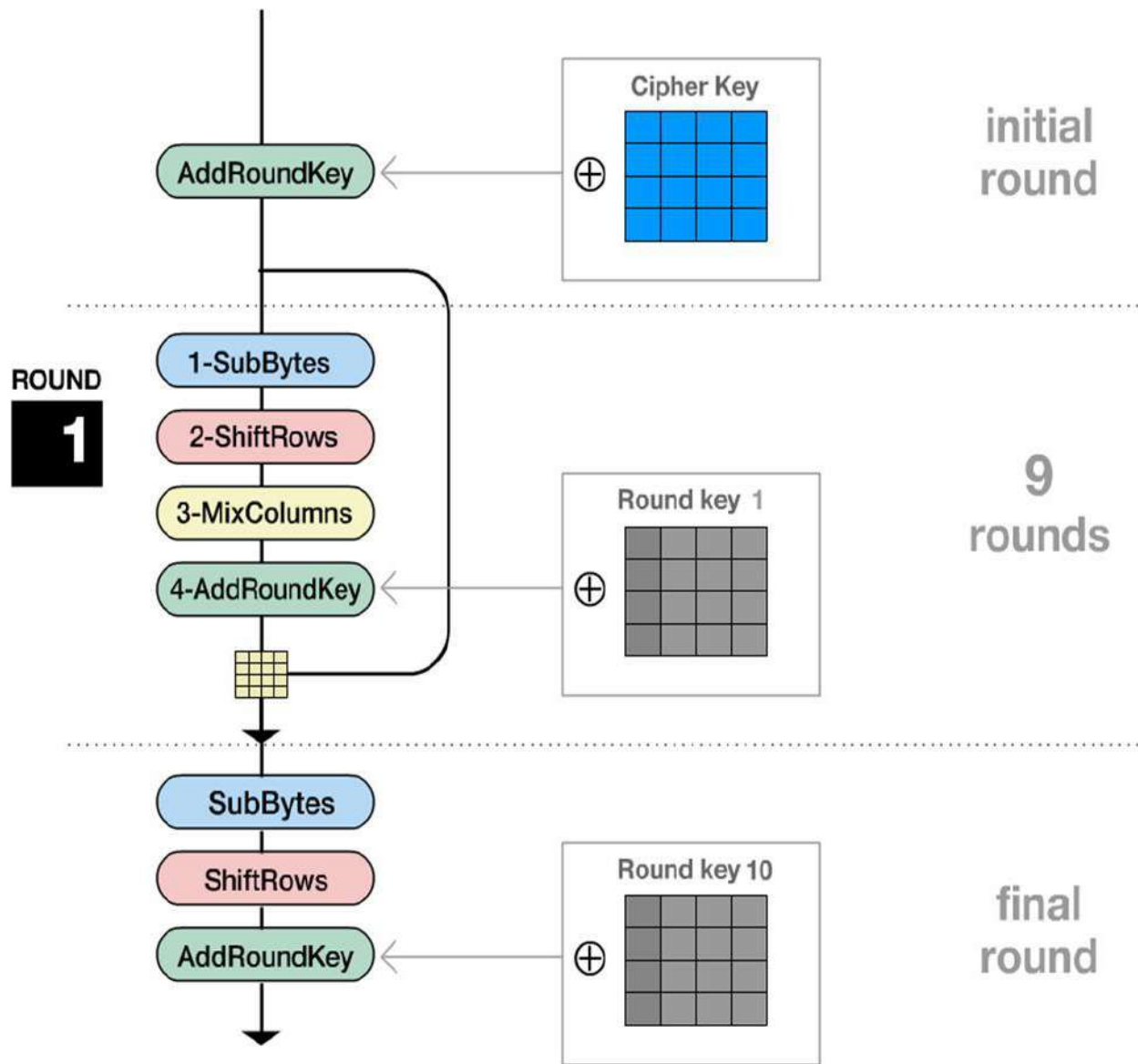
Cipher Key

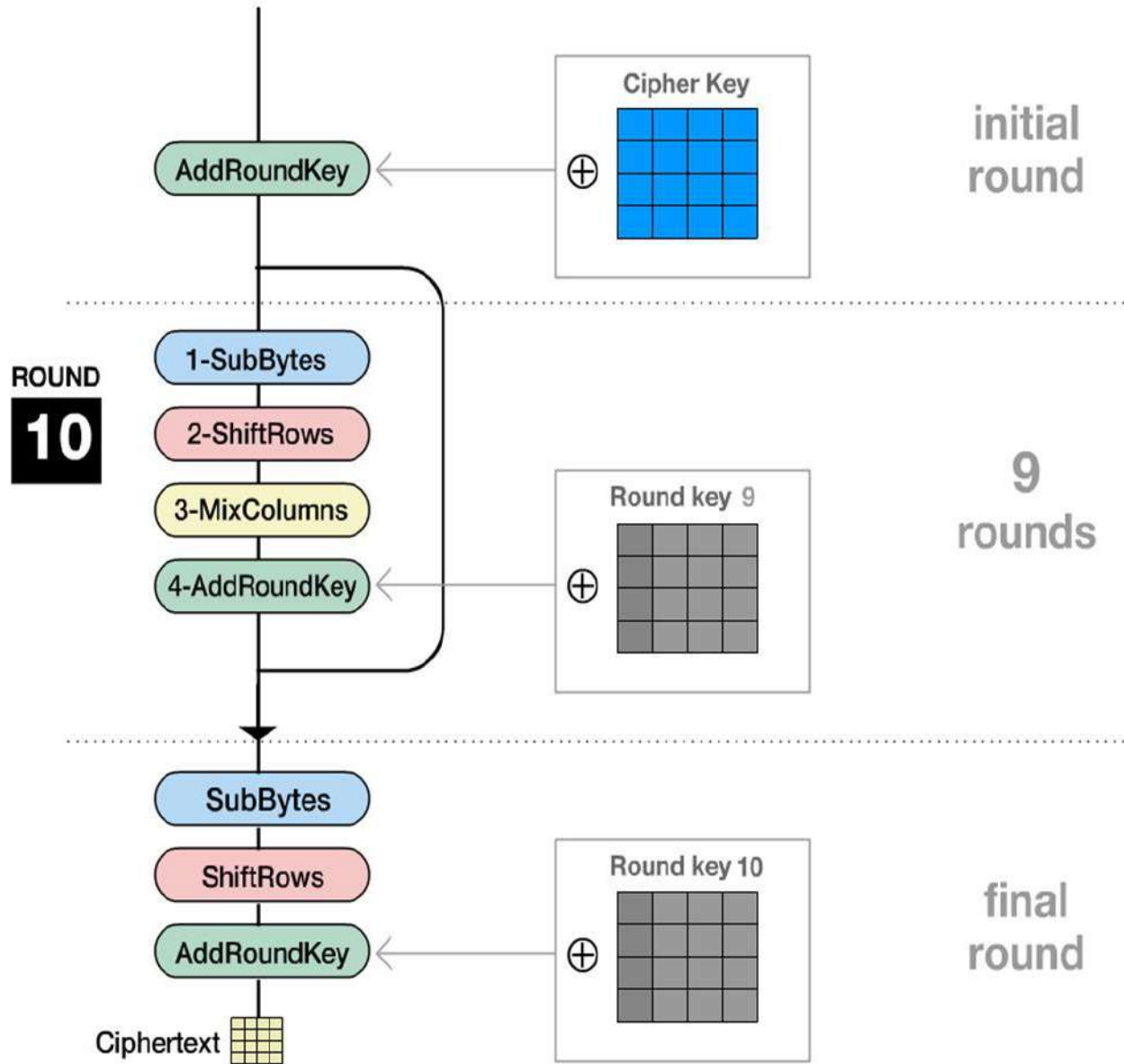
2b	28	ab	09
7e	ae	f7	cf
15	d2	15	4f
16	a6	88	3c

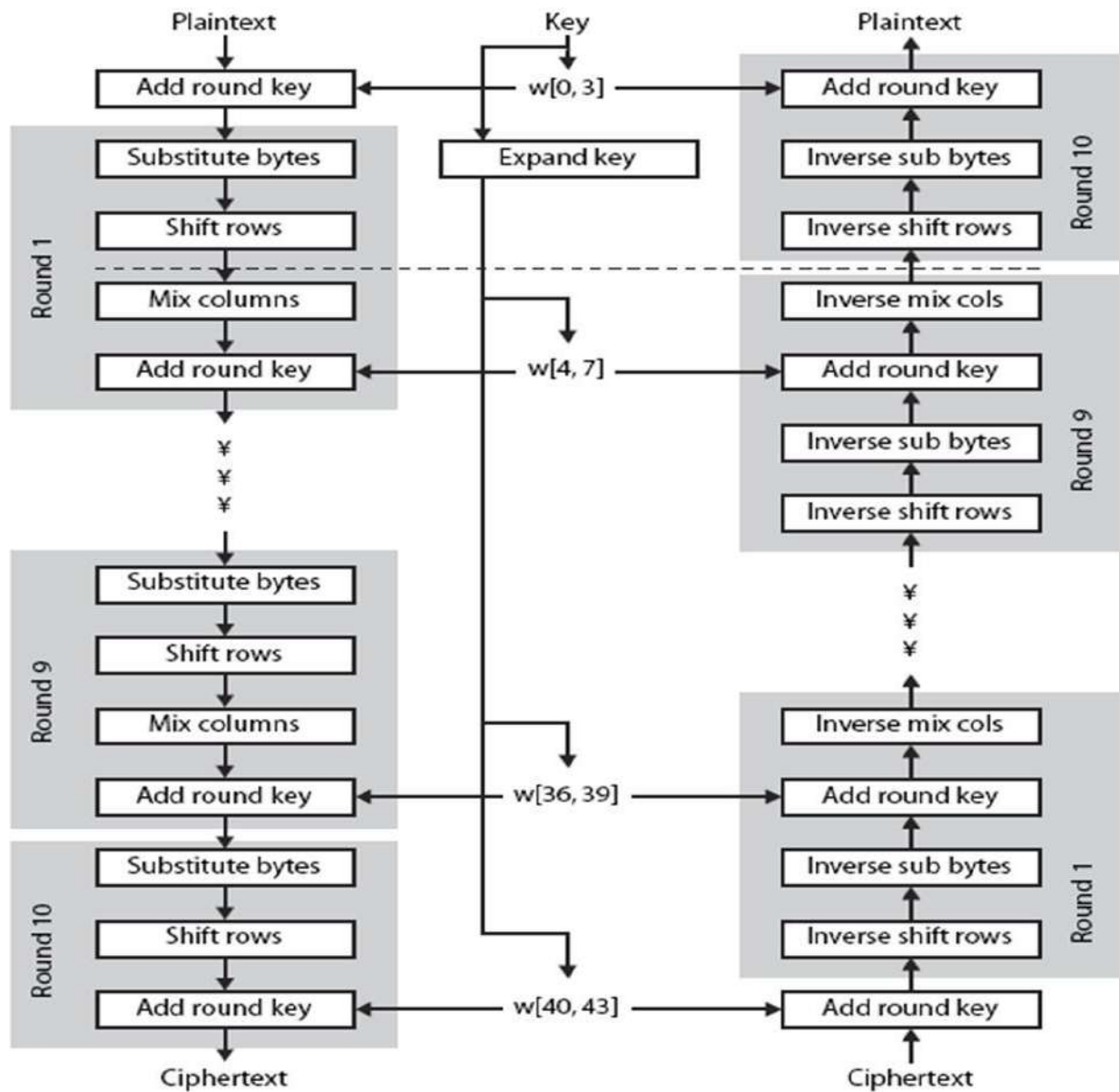


to
Key
Schedule









(a) Encryption

(b) Decryption

AES illustration - input key value

Input

State

32	88	31	e0
43	5a	31	37
f6	30	98	07
a8	8d	a2	34



to
Encryption
Process

Cipher Key

2b	28	ab	09
7e	ae	f7	cf
15	d2	15	4f
16	a6	88	3c



to
Key
Schedule

AES Key schedule generation (contd)

2b	28	ab	09												
7e	ae	f7	cf												
15	d2	15	4f												
16	a6	88	3c												

...

01	02	04	08	10	20	40	80	1b	36
00	00	00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00	00	00

Rcon

AES Key schedule generation (contd)

2b	28	ab	09
7e	ae	f7	cf
15	d2	15	4f
16	a6	88	3c

...

09
cf
4f
3c

RotWord

01	02	04	08	10	20	40	80	1b	36
00	00	00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00	00	00

Rcon

AES Key schedule generation (contd)

2b	28	ab	09
7e	ae	f7	cf
15	d2	15	4f
16	a6	88	3c

cf
4f
3c
09

SubBytes

hex	y															
	0	1	2	3	4	5	6	7	8	9	a	b	c	d	e	f
0	63	7c	77	7b	f2	6b	6f	c5	30	01	67	2b	fe	d7	ab	76
1	ca	82	c9	7d	fa	59	47	f0	ad	d4	a2	af	9c	a4	72	c0
2	b7	fd	93	26	36	3f	e7	cc	34	a5	e5	f1	71	d8	31	15
3	04	e7	23	c3	18	96	05	9a	07	12	80	e2	eb	27	b2	75
4	09	83	2c	1a	1b	6e	5a	a0	52	3b	d6	b3	29	e3	2f	84
5	53	d1	00	ed	20	fc	b1	5b	6a	cb	be	39	4a	4c	58	cf
6	d0	ef	aa	fb	43	4d	33	85	45	f9	02	7f	50	3c	9f	a8
7	51	a3	40	8f	92	9d	38	f5	bc	b6	da	21	10	ff	f3	d2
8	cd	0c	13	ec	5f	97	44	17	c4	a7	7e	3d	64	5d	19	73
9	60	81	4f	dc	22	2a	90	88	46	ee	b8	14	de	5e	0b	db
a	e0	32	3a	0a	49	06	24	5c	c2	d3	ac	62	91	95	e4	79
b	e7	c8	37	6d	8d	d5	4e	a9	6c	56	f4	ea	65	7a	ae	08
c	ba	78	25	2e	1c	a6	b4	c6	e8	dd	74	1f	4b	bd	8b	3a
d	70	3e	b5	66	48	03	f6	0e	61	35	57	b9	86	c1	1d	9e
e	e1	f8	98	11	69	d9	8e	94	9b	1e	87	e9	co	55	28	df
f	8c	a1	89	0d	bf	e6	42	68	41	99	2d	0f	b0	54	bb	16

S-BOX

01	02	04	08	10	20	40	80	1b	36
00	00	00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00	00	00

Rcon

AES Key schedule generation (contd)

2b	28	ab	09
7e	ae	f7	cf
15	d2	15	4f
16	a6	88	3c

...

8a
84
3c
09

SubBytes

hex	y															
	0	1	2	3	4	5	6	7	8	9	a	b	c	d	e	f
0	63	7c	77	7b	f2	6b	6f	c5	30	01	67	2b	fe	d7	ab	76
1	ca	82	c9	7d	fa	59	47	f0	ad	d4	a2	af	9c	a4	72	c0
2	b7	fd	93	26	36	3f	e7	cc	34	a5	e5	f1	71	d8	31	15
3	04	e7	23	c3	18	96	05	9a	07	12	80	e2	eb	27	b2	75
4	09	83	2c	1a	1b	6e	5a	a0	52	3b	d6	b3	29	e3	2f	84
5	53	d1	00	ed	20	fc	b1	5b	6a	cb	be	39	4a	4c	58	cf
6	d0	ef	aa	fb	43	4d	33	85	45	f9	02	7f	50	3c	9f	a8
7	51	a3	40	8f	92	9d	38	f5	bc	b6	da	21	10	ff	f3	d2
8	cd	0c	13	ec	5f	97	44	17	c4	a7	7e	3d	64	5d	19	73
9	60	81	4f	dc	22	2a	90	88	46	ee	b8	14	de	5e	0b	db
a	e0	32	3a	0a	49	06	24	5c	c2	d3	ac	62	91	95	e4	79
b	e7	c8	37	6d	8d	d5	4e	a9	6c	56	f4	ea	65	7a	ae	08
c	ba	78	25	2e	1c	a6	b4	c6	e8	dd	74	1f	4b	bd	8b	8a
d	70	3e	b5	66	48	03	f6	0e	61	35	57	b9	86	c1	1d	9e
e	e1	f8	98	11	69	d9	8e	94	9b	1e	87	e9	co	55	28	df
f	8c	a1	89	0d	bf	e6	42	68	41	99	2d	0f	b0	54	bb	16

S-BOX

01	02	04	08	10	20	40	80	1b	36
00	00	00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00	00	00

Rcon

AES Key schedule generation (contd)

2b	28	ab	09
7e	ae	f7	cf
15	d2	15	4f
16	a6	88	3c

...

8a
84
eb
01

SubBytes

hex	y															
	0	1	2	3	4	5	6	7	8	9	a	b	c	d	e	f
0	63	7c	77	7b	f2	6b	6f	c5	30	01	67	2b	fe	d7	ab	76
1	ca	82	e9	7d	fa	59	47	f0	ad	d4	a2	af	9c	a4	72	e0
2	b7	fd	93	26	3e	f7	ec	34	a5	e5	f1	71	d8	31	15	
3	04	c7	23	c3	18	96	05	9a	07	12	80	e2	eb	27	b2	75
4	09	83	2c	1a	1b	6e	5a	a0	52	3b	d6	b3	29	e3	2f	84
5	53	d1	00	ed	20	fc	b1	5b	6a	cb	be	39	4a	4c	58	cf
6	d0	ef	aa	fb	43	4d	33	85	45	f9	02	7f	50	3c	9f	a8
7	51	a3	40	8f	92	9d	38	f5	bc	b6	da	21	10	ff	f3	d2
8	cd	0c	13	ec	5f	97	44	17	c4	a7	7e	3d	64	5d	19	73
9	60	81	4f	dc	22	2a	90	88	46	ee	b8	14	de	5e	0b	db
a	e0	32	3a	0a	49	06	24	5c	c2	d3	ac	62	91	95	e4	79
b	e7	c8	37	6d	8d	d5	4e	a9	6c	56	f4	ea	65	7a	ae	08
c	ba	78	25	2e	1c	a6	b4	c6	e8	dd	74	1f	4b	bd	8b	8a
d	70	3e	b5	66	48	03	f6	0e	61	35	57	b9	86	c1	1d	9e
e	e1	f8	98	11	69	d9	8e	94	9b	1e	87	e9	ce	55	28	df
f	8c	a1	89	0d	bf	e6	42	68	41	99	2d	0f	b0	54	bb	16

S-BOX

01	02	04	08	10	20	40	80	1b	36
00	00	00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00	00	00

Rcon

AES Key schedule generation (contd)

2b	28	ab	09
7e	ae	f7	cf
15	d2	15	4f
16	a6	88	3c

...

2b	⊕	8a	⊕	01	=	a0
7e		84		00		fa
15		eb		00		fe
16		01		00		17

Rcon(4)

02	04	08	10	20	40	80	1b	36
00	00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00	00

Rcon

AES Key schedule generation (contd)

2b	28	ab	09	a0											
7e	ae	f7	cf	fa											
15	d2	15	4f	fe											
16	a6	88	3c	17											

...

02	04	08	10	20	40	80	1b	36
00	00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00	00

Rcon

AES Key schedule generation (contd)

2b	28	ab	09	a0											
7e	ae	f7	cf	fa											
15	d2	15	4f	fe											
16	a6	88	3c	17											

...

28	a0	88
ae	fa	54
d2	fe	2c
a6	17	b1

\oplus =

02	04	08	10	20	40	80	1b	36
00	00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00	00

Rcon

AES Key schedule generation (contd)

2b	28	ab	09	a0	88										
7e	ae	f7	cf	fa	54										
15	d2	15	4f	fe	2c										
16	a6	88	3c	17	b1										

...

ab		88		23
f7	\oplus	54	=	a3
15		2c		39
88		b1		39

02	04	08	10	20	40	80	1b	36
00	00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00	00

Rcon

AES Key schedule generation (contd)

2b	28	ab	09	a0	88	23									
7e	ae	f7	cf	fa	54	a3									
15	d2	15	4f	fe	2c	39									
16	a6	88	3c	17	b1	39									

...

09	23	2a
cf	a3	6c
4f	39	76
3c	39	05

\oplus =

02	04	08	10	20	40	80	1b	36
00	00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00	00

Rcon

AES Key schedule generation (contd)

2b	28	ab	09	a0	88	23	2a
7e	ae	f7	cf	fa	54	a3	6c
15	d2	15	4f	fe	2c	39	76
16	a6	88	3c	17	b1	39	05

6c
76
05
2a

SubBytes

50

hex	y															
	0	1	2	3	4	5	6	7	8	9	a	b	c	d	e	f
0	63	7c	77	7b	f2	6b	6f	c5	30	01	67	2b	fe	d7	ab	76
1	ca	82	c9	7d	fa	59	47	f0	ad	d4	a2	af	9c	a4	72	c0
2	b7	fd	93	26	36	3f	f7	cc	34	a5	e5	f1	71	d8	31	15
3	04	c7	23	c3	18	96	05	9a	07	12	80	e2	eb	27	b2	75
4	09	83	2c	1a	1b	6e	5a	a0	52	3b	d6	b3	29	e3	2f	84
5	53	d1	00	ed	20	fc	b1	5b	6a	cb	be	39	4a	4c	58	cf
6	d0	ef	aa	fb	43	4d	33	85	45	f9	02	7f	50	3c	9f	a8
7	51	a3	40	8f	92	9d	38	f5	bc	b6	da	21	10	ff	f3	d2
8	cd	0c	13	ec	5f	97	44	17	c4	a7	7e	3d	64	5d	19	73
9	60	81	4f	dc	22	2a	90	88	46	ee	b8	14	de	5e	0b	db
a	e0	32	3a	0a	49	06	24	5c	c2	d3	ac	62	91	95	e4	79
b	e7	c8	37	6d	8d	d5	4e	a9	6c	56	f4	ea	65	7a	ae	08
c	ba	78	25	2e	1c	a6	b4	c6	e8	dd	74	1f	4b	bd	8b	8a
d	70	3e	b5	66	48	03	f6	0e	61	35	57	b9	86	c1	1d	9e
e	e1	f8	98	11	69	d9	8e	94	9b	1e	87	e9	ce	55	28	df
f	8c	a1	89	0d	bf	e6	42	68	41	99	2d	0f	b0	54	bb	16

S-BOX

02	04	08	10	20	40	80	1b	36
00	00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00	00

Rcon

AES Key schedule generation (contd)

2b	28	ab	09	a0	88	23	2a								
7e	ae	f7	cf	fa	54	a3	6c								
15	d2	15	4f	fe	2c	39	76								
16	a6	88	3c	17	b1	39	05								

...

a0		50		02		f2
fa	\oplus	38	\oplus	00	=	c2
fe		6b		00		95
17		e5		00		f2

Rcon(8)

04	08	10	20	40	80	1b	36
00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00

Rcon

AES Key schedule generation (contd)

2b	28	ab	09	a0	88	23	2a	f2											
7e	ae	f7	cf	fa	54	a3	6c	c2											
15	d2	15	4f	fe	2c	39	76	95											
16	a6	88	3c	17	b1	39	05	f2											

...

88		f2		7a
54		c2		96
2c	\oplus	95	=	b9
b1		f2		43

04	08	10	20	40	80	1b	36
00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00

Rcon

AES Key schedule generation (contd)

2b	28	ab	09	a0	88	23	2a	f2	7a						
7e	ae	f7	cf	fa	54	a3	6c	c2	96						
15	d2	15	4f	fe	2c	39	76	95	b9						
16	a6	88	3c	17	b1	39	05	f2	43						

...

$$\begin{array}{|c|} \hline 23 \\ \hline a3 \\ \hline 39 \\ \hline 39 \\ \hline \end{array} \oplus \begin{array}{|c|} \hline 7a \\ \hline 96 \\ \hline b9 \\ \hline 43 \\ \hline \end{array} = \begin{array}{|c|} \hline 23 \\ \hline a3 \\ \hline 39 \\ \hline 39 \\ \hline \end{array}$$

04	08	10	20	40	80	1b	36
00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00
00	00	00	00	00	00	00	00

Rcon

AES Key schedule generation (contd)

2b	28	ab	09	a0	88	23	2a	f2	7a	23	73	3d	47	1e	6d
7e	ae	f7	cf	fa	54	a3	6c	c2	96	a3	59	80	16	23	7a
15	d2	15	4f	fe	2c	39	76	95	b9	39	f6	47	fe	7e	88
16	a6	88	3c	17	b1	39	05	f2	43	39	7f	7d	3e	44	3b

Cipher Key

Round key 1

Round key 2

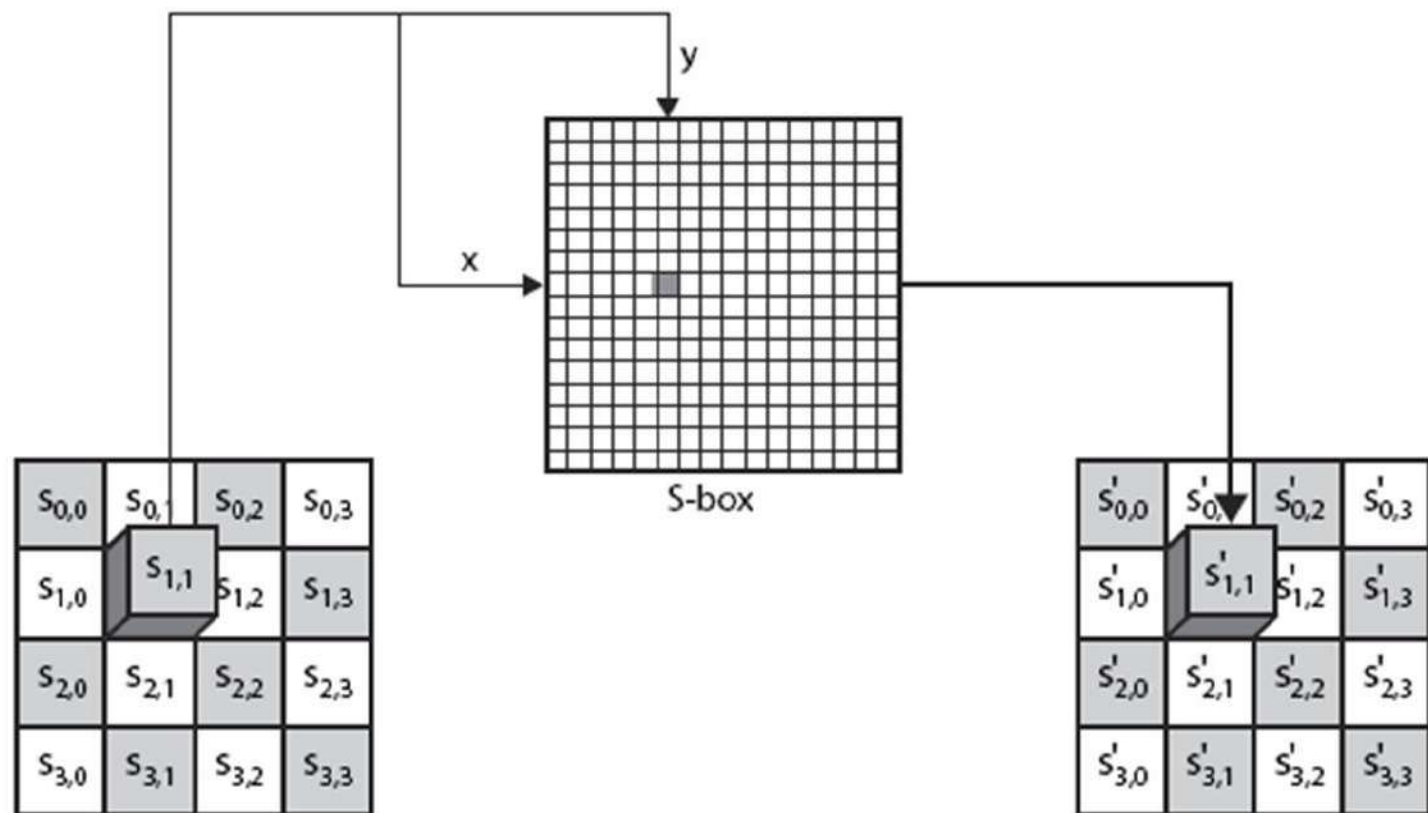
Round key 3

...

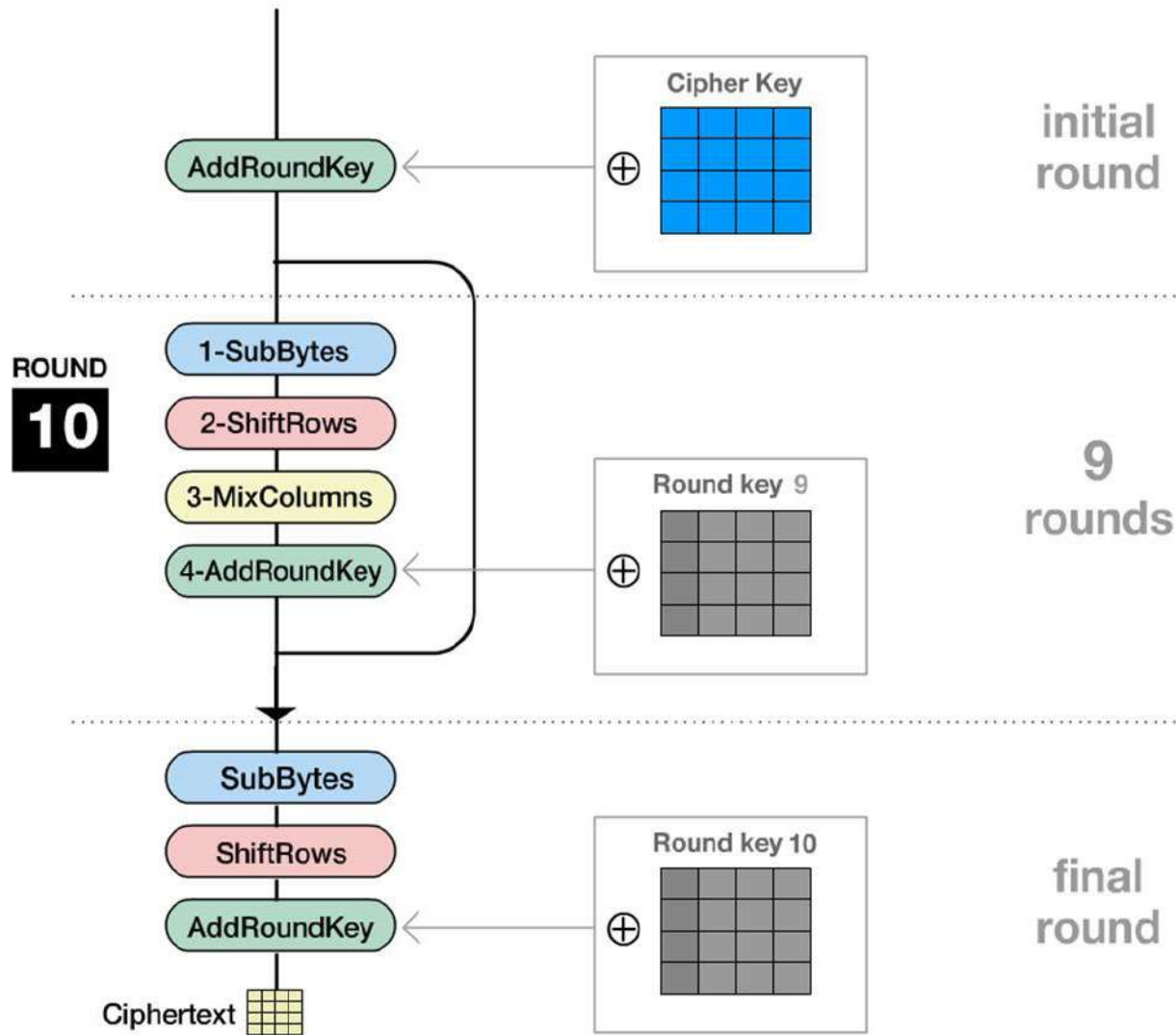
d0	c9	e1	b6
14	ee	3f	63
f9	25	0c	0c
a8	89	c8	a6

Round key 10

AES Round - subBytes transformation



Recollecting AES phases.....



AES illustration – EX-OR State with Original Key

Input

State

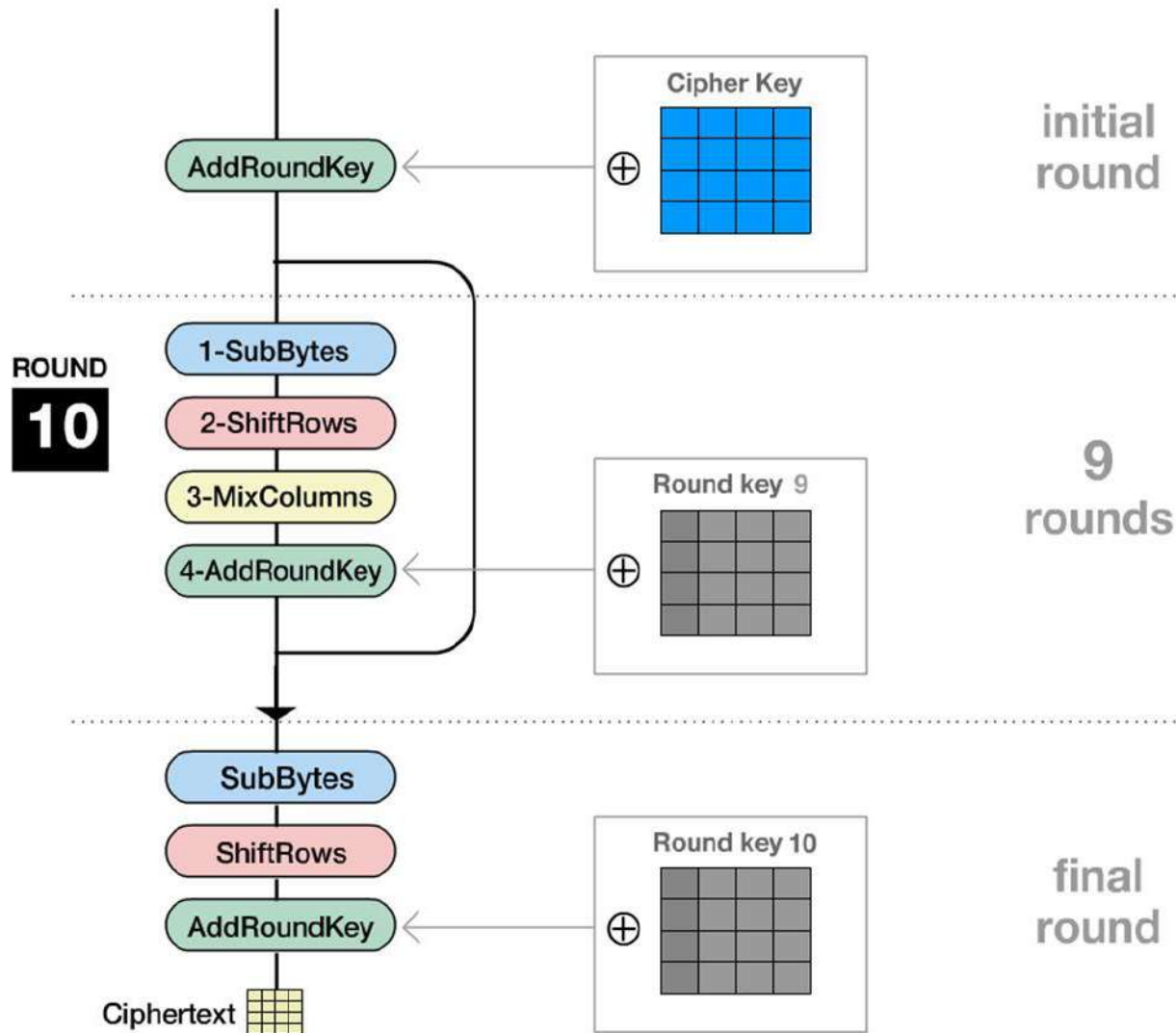
32	88	31	e0
43	5a	31	37
f6	30	98	07
a8	8d	a2	34



Cipher Key

2b	28	ab	09
7e	ae	f7	cf
15	d2	15	4f
16	a6	88	3c

Recollecting AES phases.....



AES Round - subBytes transformation

19	a0	9a	e9
3d	f4	c6	f8
e3	e2	8d	48
be	2b	2a	08

hex		y															
		0	1	2	3	4	5	6	7	8	9	a	b	c	d	e	f
x	0	63	7c	77	7b	f2	6b	6f	c5	30	01	67	2b	fe	d7	ab	76
	1	ca	82	c9	7d	fa	59	47	f0	ad	d4	a2	af	9c	a4	72	c0
	2	b7	fd	93	26	36	3f	f7	cc	34	a5	e5	f1	71	d8	31	15
	3	04	c7	23	c3	18	96	05	9a	07	12	80	e2	eb	27	b2	75
	4	09	83	2c	1a	1b	6e	5a	a0	52	3b	d6	b3	29	e3	2f	84
	5	53	d1	00	ed	20	fc	b1	5b	6a	cb	be	39	4a	4c	58	cf
	6	d0	ef	aa	fb	43	4d	33	85	45	f9	02	7f	50	3c	9f	a8
	7	51	a3	40	8f	92	9d	38	f5	bc	b6	da	21	10	ff	f3	d2
	8	cd	0c	13	ec	5f	97	44	17	c4	a7	7e	3d	64	5d	19	73
	9	60	81	4f	dc	22	2a	90	88	46	ee	b8	14	de	5e	0b	db
	a	e0	32	3a	0a	49	06	24	5c	c2	d3	ac	62	91	95	e4	79
	b	e7	c8	37	6d	8d	d5	4e	a9	6c	56	f4	ea	65	7a	ae	08
	c	ba	78	25	2e	1c	a6	b4	c6	e8	dd	74	1f	4b	bd	8b	8a
	d	70	3e	b5	66	48	03	f6	0e	61	35	57	b9	86	c1	1d	9e
	e	e1	f8	98	11	69	d9	8e	94	9b	1e	87	e9	ce	55	28	df
	f	8c	a1	89	0d	bf	e6	42	68	41	99	2d	0f	b0	54	bb	16

S-BOX

AES Round - subBytes transformation

19

	a0	9a	e9
3d	f4	c6	f8
e3	e2	8d	48
be	2b	2a	08

hex		y															
		0	1	2	3	4	5	6	7	8	9	a	b	c	d	e	f
x	0	63	7c	77	7b	f2	6b	6f	c5	30	01	67	2b	fe	d7	ab	76
	1	ca	82	c9	7d	fa	59	47	f0	ad	d4	a2	af	9c	a4	72	c0
	2	b7	fd	93	26	36	3f	f7	cc	34	a5	e5	f1	71	d8	31	15
	3	04	c7	23	c3	18	96	05	9a	07	12	80	e2	eb	27	b2	75
	4	09	83	2c	1a	1b	6e	5a	a0	52	3b	d6	b3	29	e3	2f	84
	5	53	d1	00	ed	20	fc	b1	5b	6a	cb	be	39	4a	4c	58	cf
	6	d0	ef	aa	fb	43	4d	33	85	45	f9	02	7f	50	3c	9f	a8
	7	51	a3	40	8f	92	9d	38	f5	bc	b6	da	21	10	ff	f3	d2
	8	cd	0c	13	ec	5f	97	44	17	c4	a7	7e	3d	64	5d	19	73
	9	60	81	4f	dc	22	2a	90	88	46	ee	b8	14	de	5e	0b	db
	a	e0	32	3a	0a	49	06	24	5c	c2	d3	ac	62	91	95	e4	79
	b	e7	c8	37	6d	8d	d5	4e	a9	6c	56	f4	ea	65	7a	ae	08
	c	ba	78	25	2e	1c	a6	b4	c6	e8	dd	74	1f	4b	bd	8b	8a
	d	70	3e	b5	66	48	03	f6	0e	61	35	57	b9	86	c1	1d	9e
	e	e1	f8	98	11	69	d9	8e	94	9b	1e	87	e9	ce	55	28	df
	f	8c	a1	89	0d	bf	e6	42	68	41	99	2d	0f	b0	54	bb	16

S-BOX

AES Round - subBytes transformation

19

	a0	9a	e9
3d	f4	c6	f8
e3	e2	8d	48
be	2b	2a	08

hex	y															
	0	1	2	3	4	5	6	7	8	9	a	b	c	d	e	f
x	0	63	7c	77	7b	f2	6b	6f	c5	30	01	67	2b	fe	d7	ab
	1	ca	82	c9	7d	fa	59	47	f0	ad	d4	a2	af	9c	a4	72
	2	b7	fd	93	26	36	3f	f7	cc	34	a5	e5	f1	71	d8	31
	3	04	c7	23	c3	18	96	05	9a	07	12	80	e2	eb	27	b2
	4	09	83	2c	1a	1b	6e	5a	a0	52	3b	d6	b3	29	e3	2f
	5	53	d1	00	ed	20	fc	b1	5b	6a	cb	be	39	4a	4c	58
	6	d0	ef	aa	fb	43	4d	33	85	45	f9	02	7f	50	3c	9f
	7	51	a3	40	8f	92	9d	38	f5	bc	b6	da	21	10	ff	f3
	8	cd	0c	13	ec	5f	97	44	17	c4	a7	7e	3d	64	5d	19
	9	60	81	4f	dc	22	2a	90	88	46	ee	b8	14	de	5e	0b
	a	e0	32	3a	0a	49	06	24	5c	c2	d3	ac	62	91	95	e4
	b	e7	c8	37	6d	8d	d5	4e	a9	6c	56	f4	ea	65	7a	ae
	c	ba	78	25	2e	1c	a6	b4	c6	e8	dd	74	1f	4b	bd	8b
	d	70	3e	b5	66	48	03	f6	0e	61	35	57	b9	86	c1	1d
	e	e1	f8	98	11	69	d9	8e	94	9b	1e	87	e9	ce	55	28
	f	8c	a1	89	0d	bf	e6	42	68	41	99	2d	0f	b0	54	bb

S-BOX

AES Round - subBytes transformation

d4	a0	9a	e9
3d	f4	c6	f8
e3	e2	8d	48
be	2b	2a	08

hex		y															
		0	1	2	3	4	5	6	7	8	9	a	b	c	d	e	f
x	0	63	7c	77	7b	f2	6b	6f	c5	30	01	67	2b	fe	d7	ab	76
	1	ca	82	c9	7d	fa	59	47	f0	ad	d4	a2	af	9c	a4	72	c0
	2	b7	fd	93	26	36	3f	f7	cc	34	a5	e5	f1	71	d8	31	15
	3	04	c7	23	c3	18	96	05	9a	07	12	80	e2	eb	27	b2	75
	4	09	83	2c	1a	1b	6e	5a	a0	52	3b	d6	b3	29	e3	2f	84
	5	53	d1	00	ed	20	fc	b1	5b	6a	cb	be	39	4a	4c	58	cf
	6	d0	ef	aa	fb	43	4d	33	85	45	f9	02	7f	50	3c	9f	a8
	7	51	a3	40	8f	92	9d	38	f5	bc	b6	da	21	10	ff	f3	d2
	8	cd	0c	13	ec	5f	97	44	17	c4	a7	7e	3d	64	5d	19	73
	9	60	81	4f	dc	22	2a	90	88	46	ee	b8	14	de	5e	0b	db
	a	e0	32	3a	0a	49	06	24	5c	c2	d3	ac	62	91	95	e4	79
	b	e7	c8	37	6d	8d	d5	4e	a9	6c	56	f4	ea	65	7a	ae	08
	c	ba	78	25	2e	1c	a6	b4	c6	e8	dd	74	1f	4b	bd	8b	8a
	d	70	3e	b5	66	48	03	f6	0e	61	35	57	b9	86	c1	1d	9e
	e	e1	f8	98	11	69	d9	8e	94	9b	1e	87	e9	ce	55	28	df
	f	8c	a1	89	0d	bf	e6	42	68	41	99	2d	0f	b0	54	bb	16

S-BOX

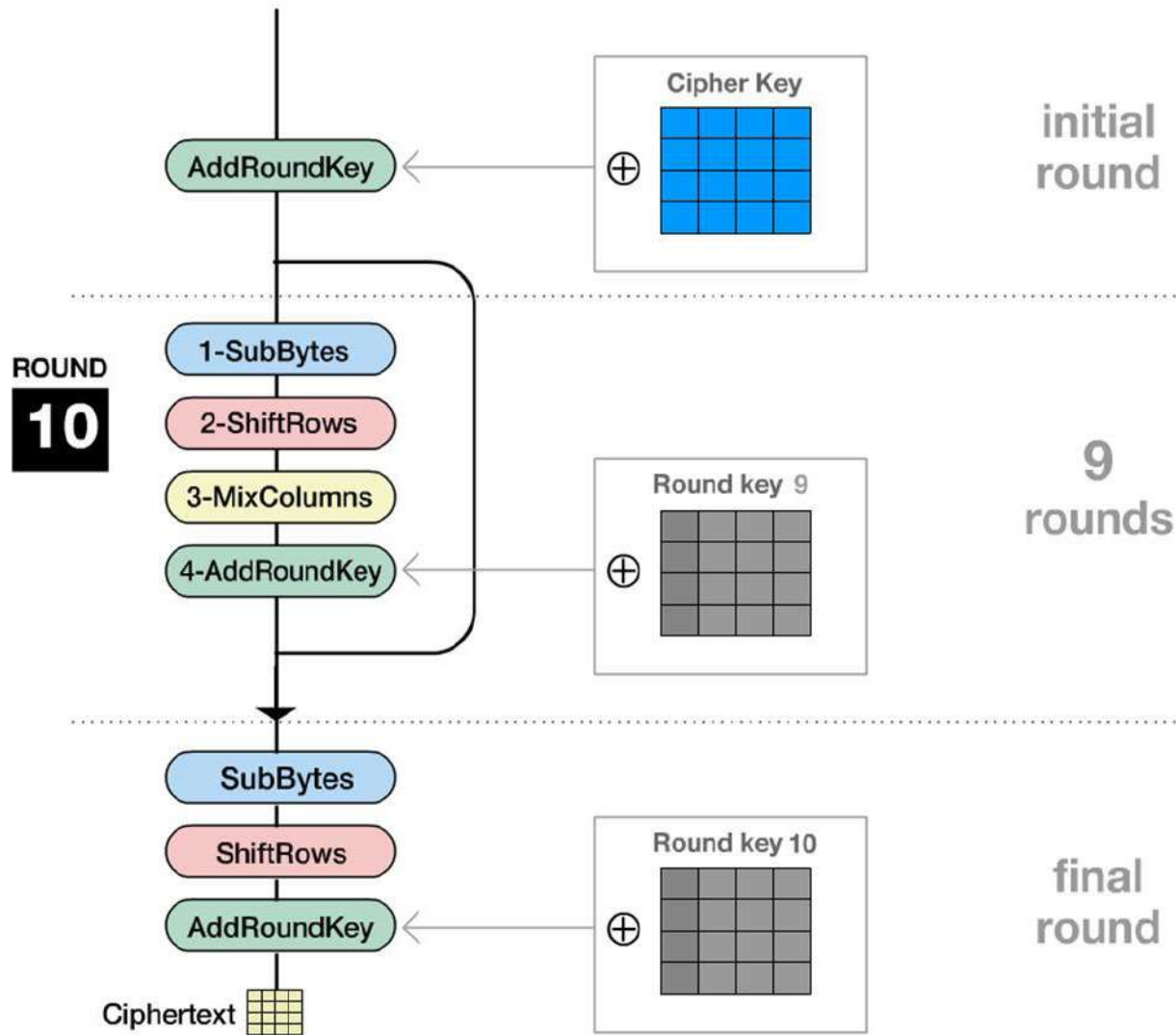
AES Round - subBytes transformation

d4	e0	b8	1e
27	bf	b4	41
11	98	5d	52
ae	f1	e5	30

hex		y															
		0	1	2	3	4	5	6	7	8	9	a	b	c	d	e	f
x	0	63	7c	77	7b	f2	6b	6f	c5	30	01	67	2b	fe	d7	ab	76
	1	ca	82	c9	7d	fa	59	47	f0	ad	d4	a2	af	9c	a4	72	c0
	2	b7	fd	93	26	36	3f	f7	cc	34	a5	e5	f1	71	d8	31	15
	3	04	c7	23	c3	18	96	05	9a	07	12	80	e2	eb	27	b2	75
	4	09	83	2c	1a	1b	6e	5a	a0	52	3b	d6	b3	29	e3	2f	84
	5	53	d1	00	ed	20	fc	b1	5b	6a	cb	be	39	4a	4c	58	cf
	6	d0	ef	aa	fb	43	4d	33	85	45	f9	02	7f	50	3c	9f	a8
	7	51	a3	40	8f	92	9d	38	f5	bc	b6	da	21	10	ff	f3	d2
	8	cd	0c	13	ec	5f	97	44	17	c4	a7	7e	3d	64	5d	19	73
	9	60	81	4f	dc	22	2a	90	88	46	ee	b8	14	de	5e	0b	db
	a	e0	32	3a	0a	49	06	24	5c	c2	d3	ac	62	91	95	e4	79
	b	e7	c8	37	6d	8d	d5	4e	a9	6c	56	f4	ea	65	7a	ae	08
	c	ba	78	25	2e	1c	a6	b4	c6	e8	dd	74	1f	4b	bd	8b	8a
	d	70	3e	b5	66	48	03	f6	0e	61	35	57	b9	86	c1	1d	9e
	e	e1	f8	98	11	69	d9	8e	94	9b	1e	87	e9	ce	55	28	df
	f	8c	a1	89	0d	bf	e6	42	68	41	99	2d	0f	b0	54	bb	16

S-BOX

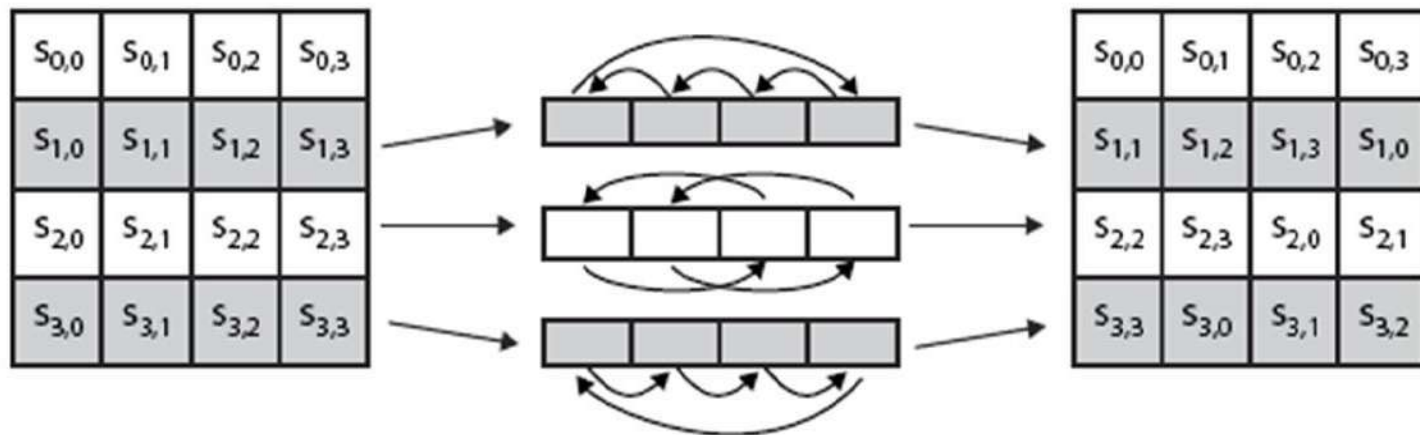
Recollecting AES phases.....



AES Round - Shift Rows transformation

- a circular byte shift in each row
 - 1st row is unchanged
 - 2nd row does 1 byte circular shift to left
 - 3rd row does 2 byte circular shift to left
 - 4th row does 3 byte circular shift to left
- decrypt inverts using shifts to right
- since state is processed by columns, this step permutes bytes between the columns

AES Round - Shift Rows transformation



AES Round - Shift Rows transformation

d4	e0	b8	1e
27	bf	b4	41
11	98	5d	52
ae	f1	e5	30

 rotate over 1 byte

AES Round - Shift Rows transformation

d4	e	27	3	1e
	bf	b4	41	
11	98	5d	52	
ae	f1	e5	30	

.....rotate over 1 byte

AES Round - Shift Rows transformation

d4	e0	b8	1e
bf	b4	41	27
11	98	5d	52
ae	f1	e5	30

.....rotate over 1 byte

AES Round - Shift Rows transformation

d4	e0	b8	1e
bf	b4	41	27
11	98	5d	52
ae	f1	e5	30



rotate over 2 bytes

AES Round - Shift Rows transformation

d4	e0	b8	1e
bf	b4	41	27
5d	52	11	98
ae	f1	e5	30



rotate over 2 bytes

AES Round - Shift Rows transformation

d4	e0	b8	1e
bf	b4	41	27
5d	52	11	98
ae	f1	e5	30



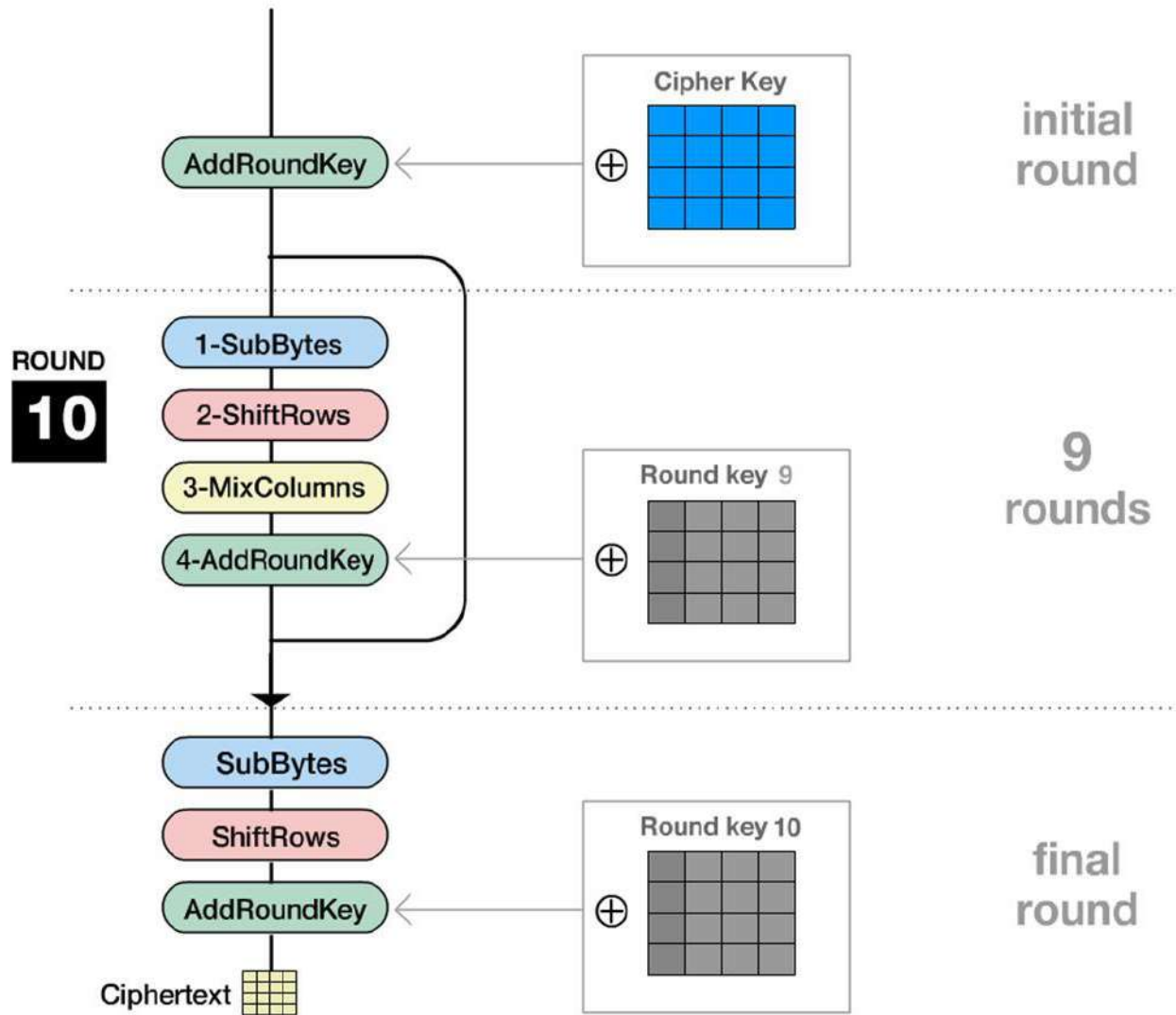
rotate over 3 bytes

AES Round - Shift Rows transformation

d4	e0	b8	1e
bf	b4	41	27
5d	52	11	98
30	ae	f1	e5

 rotate over 3 bytes

Recollecting AES phases.....



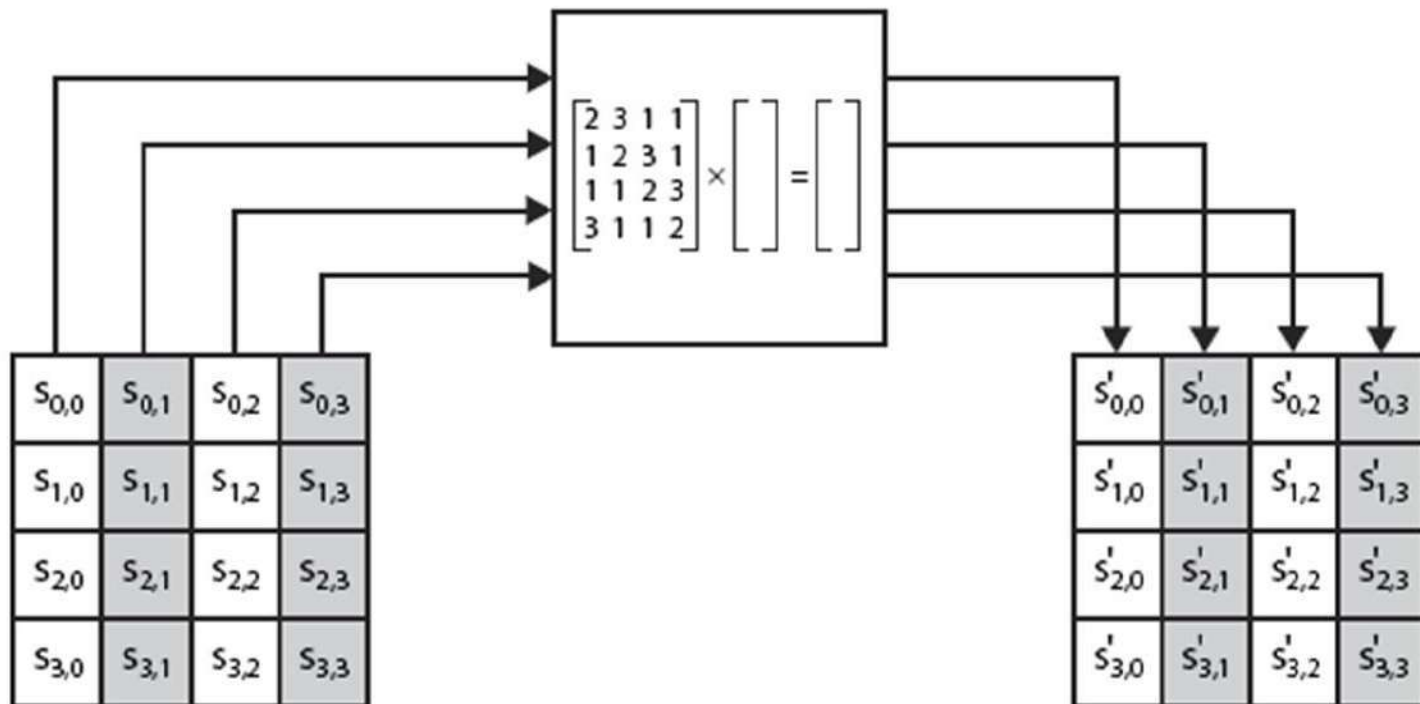
AES Round - Mix Columns

transformation

- the MixColumns stage is a substitution that makes use of arithmetic over $GF(2^8)$.
- each column is processed separately
- each byte is replaced by a value dependent on all 4 bytes in the column
- effectively a matrix multiplication in $GF(2^8)$ using prime poly $m(x) = x^8 + x^4 + x^3 + x + 1$

$$\begin{bmatrix} 02 & 03 & 01 & 01 \\ 01 & 02 & 03 & 01 \\ 01 & 01 & 02 & 03 \\ 03 & 01 & 01 & 02 \end{bmatrix} \begin{bmatrix} s_{0,0} & s_{0,1} & s_{0,2} & s_{0,3} \\ s_{1,0} & s_{1,1} & s_{1,2} & s_{1,3} \\ s_{2,0} & s_{2,1} & s_{2,2} & s_{2,3} \\ s_{3,0} & s_{3,1} & s_{3,2} & s_{3,3} \end{bmatrix} = \begin{bmatrix} s'_{0,0} & s'_{0,1} & s'_{0,2} & s'_{0,3} \\ s'_{1,0} & s'_{1,1} & s'_{1,2} & s'_{1,3} \\ s'_{2,0} & s'_{2,1} & s'_{2,2} & s'_{2,3} \\ s'_{3,0} & s'_{3,1} & s'_{3,2} & s'_{3,3} \end{bmatrix}$$

AES Round - Mix Columns transformation



AES Round - Mix Columns

transformation

- can express each col as 4 equations
 - to derive each new byte in col
- decryption requires use of inverse matrix
 - with larger coefficients, hence a little harder
- have an alternate characterisation
 - each column a 4-term polynomial
 - with coefficients in $GF(2^8)$
 - and polynomials multiplied modulo (x^4+1)

AES Round - Mix Columns

transformation

e0	b8	1e
b4	41	27
52	11	98
ae	f1	e5

d4
bf
5d
30

•

02	03	01	01
01	02	03	01
01	01	02	03
03	01	01	02

=

04
66
81
e5

AES Round - Mix Columns

transformation

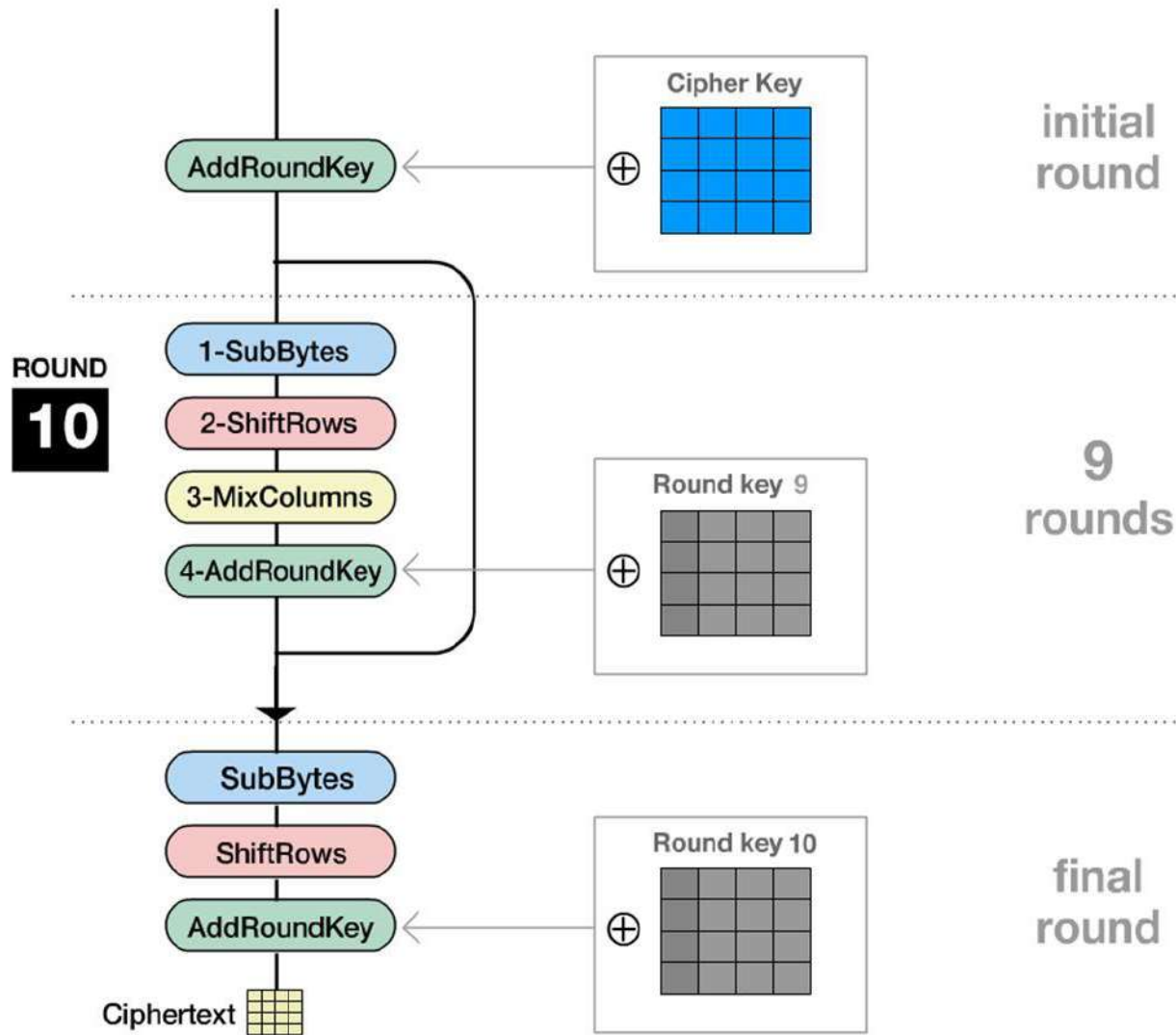
04	e0	b8	1e
66	cb	41	27
81	19	11	98
e5	9a	f1	e5

AES Round - Mix Columns

transformation

04	e0	48	28
66	cb	f8	06
81	19	d3	26
e5	9a	7a	4c

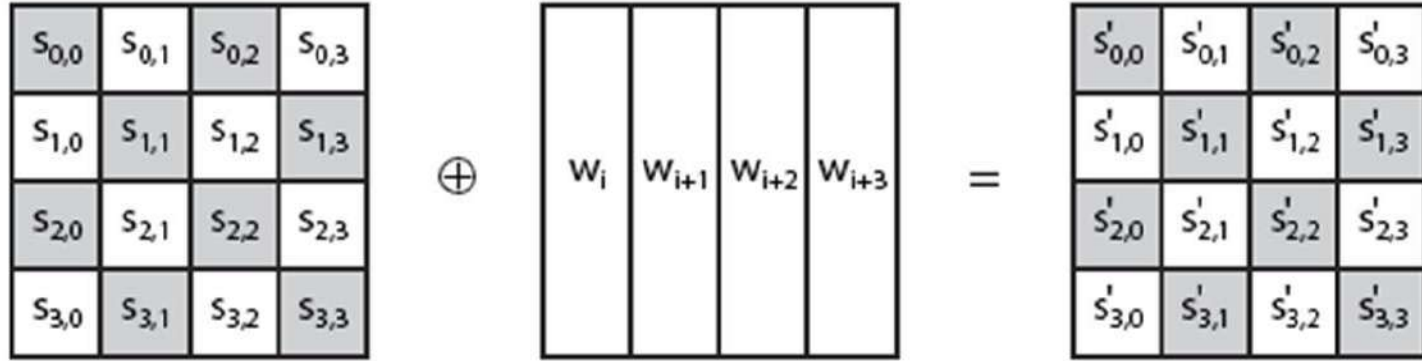
Recollecting AES phases.....



AES Round - Add Round Key

- XOR state with 128-bits of the round key
- again processed by column (though effectively a series of byte operations)
- inverse for decryption identical
 - since XOR own inverse, with reversed keys
- designed to be as simple as possible
 - a form of Vernam cipher on expanded key
 - requires other stages for complexity / security

AES Round - Add Round Key



AES Key schedule generation (contd)

2b	28	ab	09	a0	88	23	2a	f2	7a	23	73	3d	47	1e	6d
7e	ae	f7	cf	fa	54	a3	6c	c2	96	a3	59	80	16	23	7a
15	d2	15	4f	fe	2c	39	76	95	b9	39	f6	47	fe	7e	88
16	a6	88	3c	17	b1	39	05	f2	43	39	7f	7d	3e	44	3b

Cipher Key

Round key 1

Round key 2

Round key 3

...

d0	c9	e1	b6
14	ee	3f	63
f9	25	0c	0c
a8	89	c8	a6

Round key 10

AES Round - Add Round Key

04	e0	48	28
66	cb	f8	06
81	19	d3	26
e5	9a	7a	4c

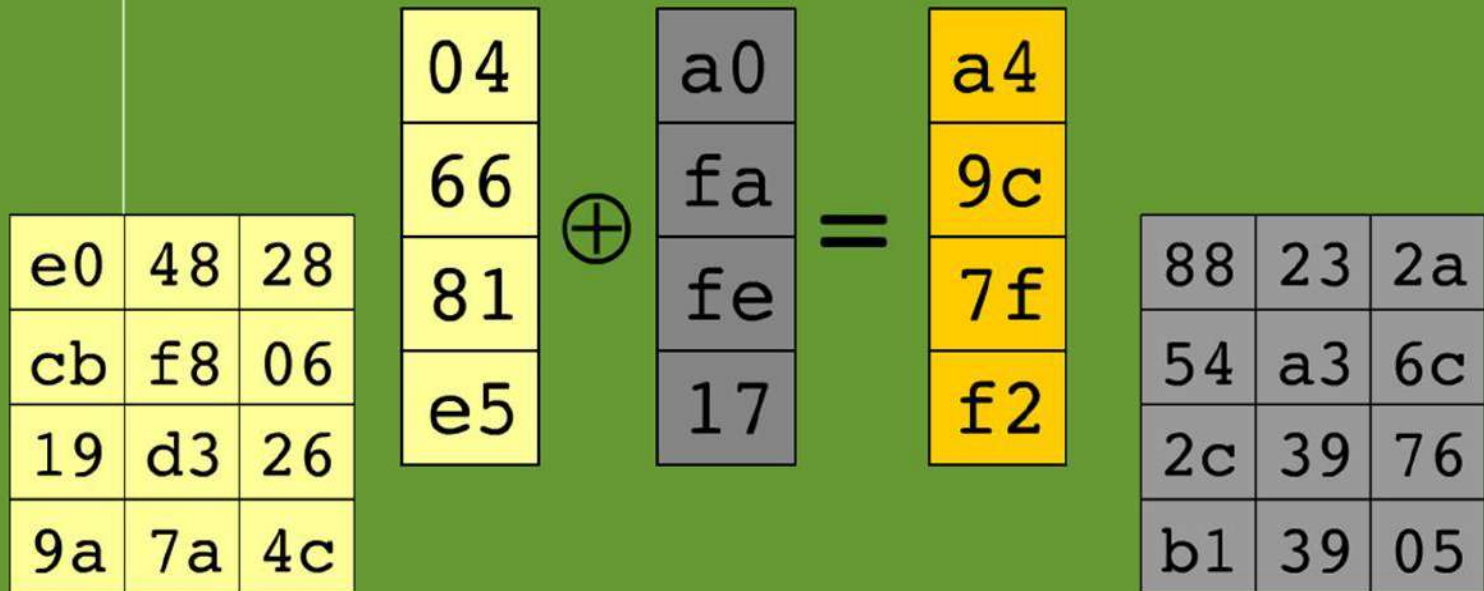
AES Round - Add Round Key

04	e0	48	28
66	cb	f8	06
81	19	d3	26
e5	9a	7a	4c

a0	88	23	2a
fa	54	a3	6c
fe	2c	39	76
17	b1	39	05

Round key

AES Round - Add Round Key



Round key

AES Round - Add Round Key

a4	68	48	28
9c	9f	f8	06
7f	35	d3	26
f2	2b	7a	4c

23	2a
a3	6c
39	76
39	05






Round key

AES Round - Add Round Key

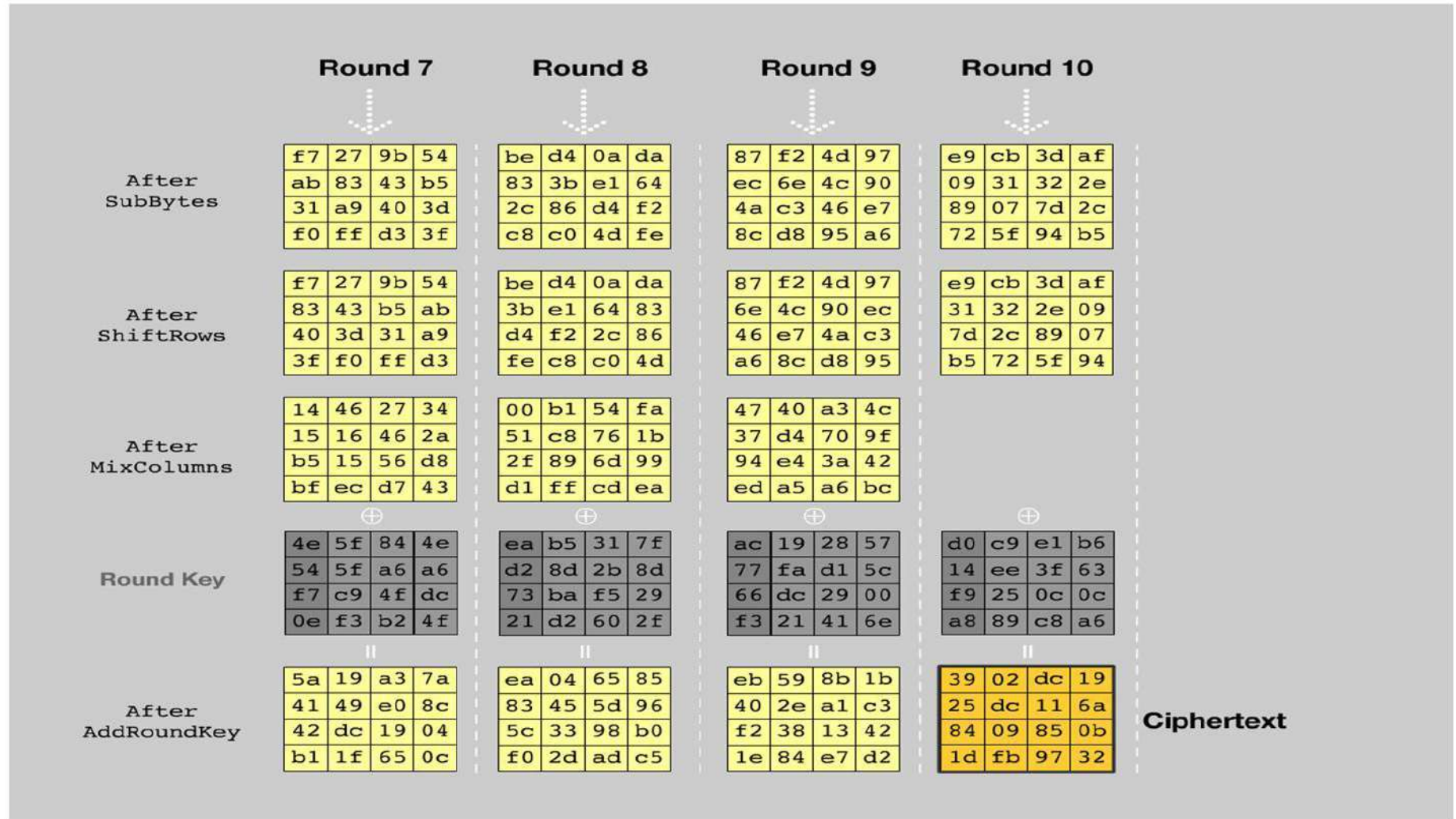
a4	68	6b	02
9c	9f	5b	6a
7f	35	ea	50
f2	2b	43	49

Round key

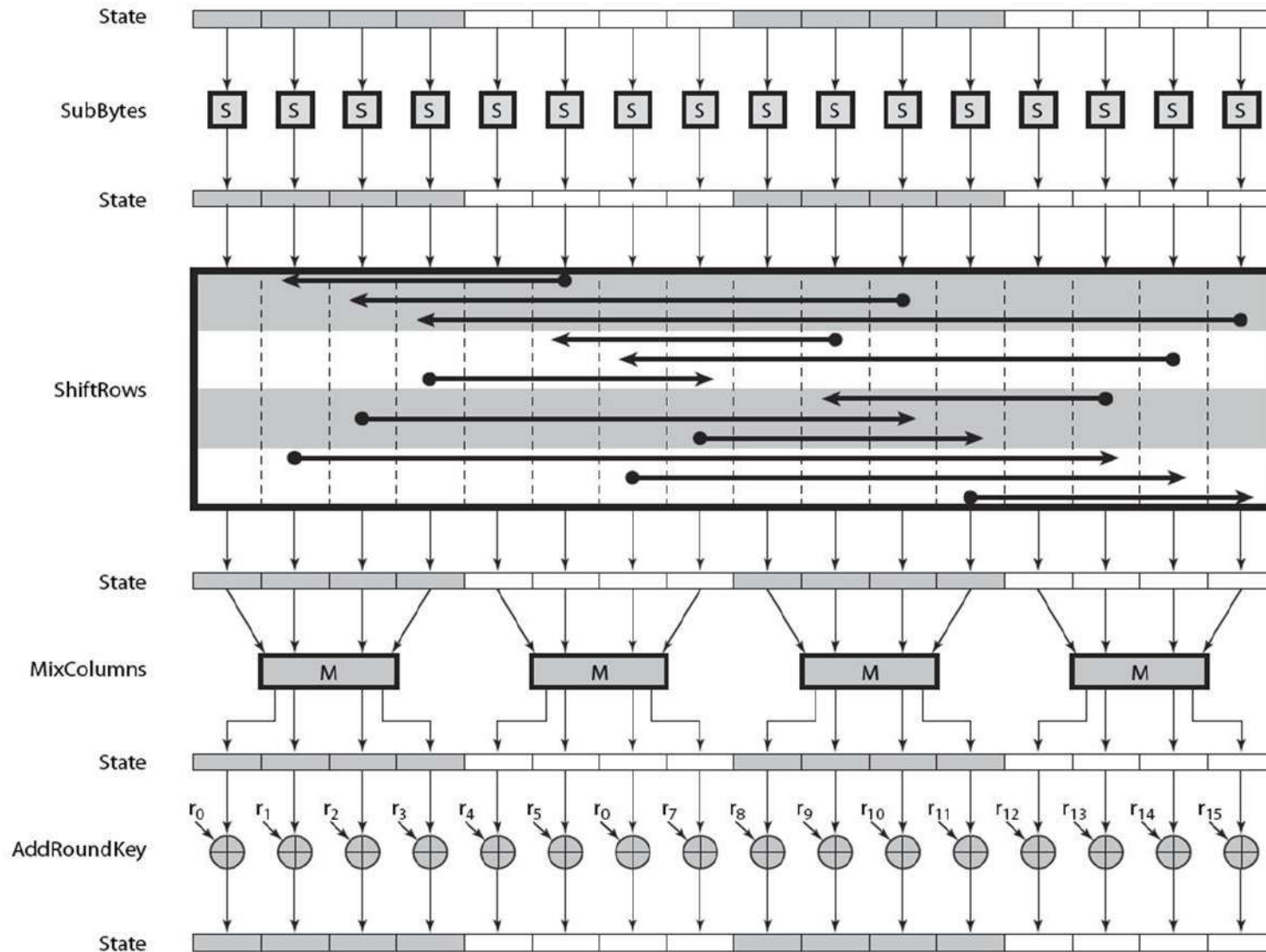
AES Round – ciphertext generation

	Round 2	Round 3	Round 4	Round 5	Round 6																																																																																
																																																																																					
After SubBytes	<table><tr><td>49</td><td>45</td><td>7f</td><td>77</td></tr><tr><td>de</td><td>db</td><td>39</td><td>02</td></tr><tr><td>d2</td><td>96</td><td>87</td><td>53</td></tr><tr><td>89</td><td>f1</td><td>1a</td><td>3b</td></tr></table>	49	45	7f	77	de	db	39	02	d2	96	87	53	89	f1	1a	3b	<table><tr><td>ac</td><td>ef</td><td>13</td><td>45</td></tr><tr><td>73</td><td>c1</td><td>b5</td><td>23</td></tr><tr><td>cf</td><td>11</td><td>d6</td><td>5a</td></tr><tr><td>7b</td><td>df</td><td>b5</td><td>b8</td></tr></table>	ac	ef	13	45	73	c1	b5	23	cf	11	d6	5a	7b	df	b5	b8	<table><tr><td>52</td><td>85</td><td>e3</td><td>f6</td></tr><tr><td>50</td><td>a4</td><td>11</td><td>cf</td></tr><tr><td>2f</td><td>5e</td><td>c8</td><td>6a</td></tr><tr><td>28</td><td>d7</td><td>07</td><td>94</td></tr></table>	52	85	e3	f6	50	a4	11	cf	2f	5e	c8	6a	28	d7	07	94	<table><tr><td>e1</td><td>e8</td><td>35</td><td>97</td></tr><tr><td>4f</td><td>fb</td><td>c8</td><td>6c</td></tr><tr><td>d2</td><td>fb</td><td>96</td><td>ae</td></tr><tr><td>9b</td><td>ba</td><td>53</td><td>7c</td></tr></table>	e1	e8	35	97	4f	fb	c8	6c	d2	fb	96	ae	9b	ba	53	7c	<table><tr><td>a1</td><td>78</td><td>10</td><td>4c</td></tr><tr><td>63</td><td>4f</td><td>e8</td><td>d5</td></tr><tr><td>a8</td><td>29</td><td>3d</td><td>03</td></tr><tr><td>fc</td><td>df</td><td>23</td><td>fe</td></tr></table>	a1	78	10	4c	63	4f	e8	d5	a8	29	3d	03	fc	df	23	fe
49	45	7f	77																																																																																		
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2f	5e	c8	6a																																																																																		
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49	45	7f	77																																																																																		
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4f	e8	d5	63																																																																																		
3d	03	a8	29																																																																																		
fe	fc	df	23																																																																																		
After MixColumns	<table><tr><td>58</td><td>1b</td><td>db</td><td>1b</td></tr><tr><td>4d</td><td>4b</td><td>e7</td><td>6b</td></tr><tr><td>ca</td><td>5a</td><td>ca</td><td>b0</td></tr><tr><td>f1</td><td>ac</td><td>a8</td><td>e5</td></tr></table>	58	1b	db	1b	4d	4b	e7	6b	ca	5a	ca	b0	f1	ac	a8	e5	<table><tr><td>75</td><td>20</td><td>53</td><td>bb</td></tr><tr><td>ec</td><td>0b</td><td>c0</td><td>25</td></tr><tr><td>09</td><td>63</td><td>cf</td><td>d0</td></tr><tr><td>93</td><td>33</td><td>7c</td><td>dc</td></tr></table>	75	20	53	bb	ec	0b	c0	25	09	63	cf	d0	93	33	7c	dc	<table><tr><td>0f</td><td>60</td><td>6f</td><td>5e</td></tr><tr><td>d6</td><td>31</td><td>c0</td><td>b3</td></tr><tr><td>da</td><td>38</td><td>10</td><td>13</td></tr><tr><td>a9</td><td>bf</td><td>6b</td><td>01</td></tr></table>	0f	60	6f	5e	d6	31	c0	b3	da	38	10	13	a9	bf	6b	01	<table><tr><td>25</td><td>bd</td><td>b6</td><td>4c</td></tr><tr><td>d1</td><td>11</td><td>3a</td><td>4c</td></tr><tr><td>a9</td><td>d1</td><td>33</td><td>c0</td></tr><tr><td>ad</td><td>68</td><td>8e</td><td>b0</td></tr></table>	25	bd	b6	4c	d1	11	3a	4c	a9	d1	33	c0	ad	68	8e	b0	<table><tr><td>4b</td><td>2c</td><td>33</td><td>37</td></tr><tr><td>86</td><td>4a</td><td>9d</td><td>d2</td></tr><tr><td>8d</td><td>89</td><td>f4</td><td>18</td></tr><tr><td>6d</td><td>80</td><td>e8</td><td>d8</td></tr></table>	4b	2c	33	37	86	4a	9d	d2	8d	89	f4	18	6d	80	e8	d8
58	1b	db	1b																																																																																		
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Round Key	<table><tr><td>f2</td><td>7a</td><td>59</td><td>73</td></tr><tr><td>c2</td><td>96</td><td>35</td><td>59</td></tr><tr><td>95</td><td>b9</td><td>80</td><td>f6</td></tr><tr><td>f2</td><td>43</td><td>7a</td><td>7f</td></tr></table>	f2	7a	59	73	c2	96	35	59	95	b9	80	f6	f2	43	7a	7f	<table><tr><td>3d</td><td>47</td><td>1e</td><td>6d</td></tr><tr><td>80</td><td>16</td><td>23</td><td>7a</td></tr><tr><td>47</td><td>fe</td><td>7e</td><td>88</td></tr><tr><td>7d</td><td>3e</td><td>44</td><td>3b</td></tr></table>	3d	47	1e	6d	80	16	23	7a	47	fe	7e	88	7d	3e	44	3b	<table><tr><td>ef</td><td>a8</td><td>b6</td><td>db</td></tr><tr><td>44</td><td>52</td><td>71</td><td>0b</td></tr><tr><td>a5</td><td>5b</td><td>25</td><td>ad</td></tr><tr><td>41</td><td>7f</td><td>3b</td><td>00</td></tr></table>	ef	a8	b6	db	44	52	71	0b	a5	5b	25	ad	41	7f	3b	00	<table><tr><td>d4</td><td>7c</td><td>ca</td><td>11</td></tr><tr><td>d1</td><td>83</td><td>f2</td><td>f9</td></tr><tr><td>c6</td><td>9d</td><td>b8</td><td>15</td></tr><tr><td>f8</td><td>87</td><td>bc</td><td>bc</td></tr></table>	d4	7c	ca	11	d1	83	f2	f9	c6	9d	b8	15	f8	87	bc	bc	<table><tr><td>6d</td><td>11</td><td>db</td><td>ca</td></tr><tr><td>88</td><td>0b</td><td>f9</td><td>00</td></tr><tr><td>a3</td><td>3e</td><td>86</td><td>93</td></tr><tr><td>7a</td><td>fd</td><td>41</td><td>fd</td></tr></table>	6d	11	db	ca	88	0b	f9	00	a3	3e	86	93	7a	fd	41	fd
f2	7a	59	73																																																																																		
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After AddRoundKey	<table><tr><td>aa</td><td>61</td><td>82</td><td>68</td></tr><tr><td>8f</td><td>dd</td><td>d2</td><td>32</td></tr><tr><td>5f</td><td>e3</td><td>4a</td><td>46</td></tr><tr><td>03</td><td>ef</td><td>d2</td><td>9a</td></tr></table>	aa	61	82	68	8f	dd	d2	32	5f	e3	4a	46	03	ef	d2	9a	<table><tr><td>48</td><td>67</td><td>4d</td><td>d6</td></tr><tr><td>6c</td><td>1d</td><td>e3</td><td>5f</td></tr><tr><td>4e</td><td>9d</td><td>b1</td><td>58</td></tr><tr><td>ee</td><td>0d</td><td>38</td><td>e7</td></tr></table>	48	67	4d	d6	6c	1d	e3	5f	4e	9d	b1	58	ee	0d	38	e7	<table><tr><td>e0</td><td>c8</td><td>d9</td><td>85</td></tr><tr><td>92</td><td>63</td><td>b1</td><td>b8</td></tr><tr><td>7f</td><td>63</td><td>35</td><td>be</td></tr><tr><td>e8</td><td>c0</td><td>50</td><td>01</td></tr></table>	e0	c8	d9	85	92	63	b1	b8	7f	63	35	be	e8	c0	50	01	<table><tr><td>f1</td><td>c1</td><td>7c</td><td>5d</td></tr><tr><td>00</td><td>92</td><td>c8</td><td>b5</td></tr><tr><td>6f</td><td>4c</td><td>8b</td><td>d5</td></tr><tr><td>55</td><td>ef</td><td>32</td><td>0c</td></tr></table>	f1	c1	7c	5d	00	92	c8	b5	6f	4c	8b	d5	55	ef	32	0c	<table><tr><td>26</td><td>3d</td><td>e8</td><td>fd</td></tr><tr><td>0e</td><td>41</td><td>64</td><td>d2</td></tr><tr><td>2e</td><td>b7</td><td>72</td><td>8b</td></tr><tr><td>17</td><td>7d</td><td>a9</td><td>25</td></tr></table>	26	3d	e8	fd	0e	41	64	d2	2e	b7	72	8b	17	7d	a9	25
aa	61	82	68																																																																																		
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2e	b7	72	8b																																																																																		
17	7d	a9	25																																																																																		

AES Round – ciphertext generation



AES Round summarizing



AES Decryption

- AES decryption is not identical to encryption since steps done in reverse
 - but can define an equivalent inverse cipher with steps as for encryption
 - but using inverses of each step with a different key schedule
- works since result is unchanged when
 - swap byte substitution & shift rows
 - swap mix columns & add (tweaked) round key

AES Decryption

