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Operations Research (Paper III) MSc. (Computer Science) Semester III 2022-23

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Aim: Use graphical method to solve the following LPP:

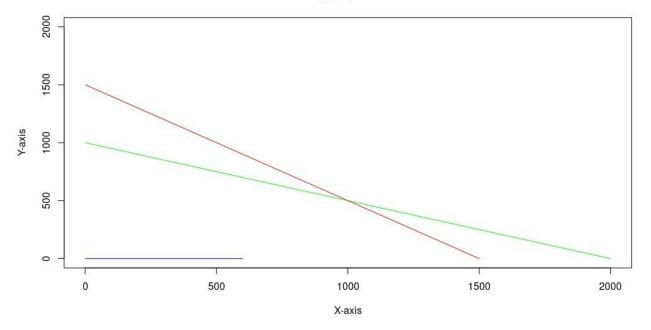
```
Max Z = 3x + 5y
w.r.t.
x + 2y \le 2000,
x + y \le 1500,
y \le 600,
x, y \ge 0
```

Source Code:

```
require(lpSolve)
C - c(3, 5)
A - matrix(c(1, 2,
              0, 1), nrow = 3, byrow = T)
B - c(2000, 1500, 600)
constraint_direction - c(" =", " =", " =")
plot.new()
plot.window(xlim = c(0, 2000), ylim = c(0, 2000))
axis(1)
axis(2)
title(main = "LPP using graphical method", xlab = "X-axis", ylab = "Y-
axis")
box()
segments(x0 = 2000, y0 = 0, x1 = 0, y1 = 1000, col = "green")
segments(x0 = 1500, y0 = 0, x1 = 0, y1 = 1500, col = "red")
segments(x0 = 0, y0 = 0, x1 = 600, y1 = 0, col = "blue")
z - lp(direction = "max",
```

```
> best_sol ← z$solution
> names(best_sol) ← c("x1", "x2")
> print(paste("Total cost: ", z$objval, sep = ""))
[1] "Total cost: 5500"
>
```

LPP using graphical method



Aim: Use simplex method to solve the following LPP:

from scipy.optimize import linprog

```
Max Z = 3x + 2y
w.r.t.
x + y \le 4,
x - y \le 2,
x, y \ge 0
```

Source Code:

```
obj = [-3, -2]
lhs_ineq = [[1, 1], [1, -1]]

In[1]:

rhs_ineq = [4, 2]

bound = [(0, float("inf")), (0, float("inf"))]

z = linprog(c = obj, A_ub = lhs_ineq, b_ub = rhs_ineq, bounds = bound, method = "revised simplex")

z
```

```
In [1]: 1 from scipy.optimize import linprog
          3 obj = [-3, -2]
          4 lhs_ineq = [[1, 1],
                        [1, -1]]
          6
          7 rhs_ineq = [4,
          10 bound = [(0, float("inf")),
11 (0, float("inf"))]
         1 z = linprog(c = obj, A_ub = lhs_ineq, b_ub = rhs_ineq,
2 bounds = bound, method = "revised simplex")
In [2]:
          3
          4 Z
Out[2]:
          con: array([], dtype=float64)
             fun: -11.0
          message: 'Optimization terminated successfully.'
              nit: 2
            slack: array([0., 0.])
          status: 0
          success: True
               x: array([3., 1.])
In [3]:
          1 print(z.fun)
          print(z.success)
          3 print(z.x)
         -11.0
         True
         [3. 1.]
```

Aim: Use simplex method to solve the following LPP:

```
Min Z = x_1 - 3x_2 + 2x_3
w.r.t
3x_1 - x_2 + 3x_3 \le 7,
-2x_1 + 4x_2 \le 12,
-4x_1 + 3x_2 + 8x_3 \le 10,
x_1, x_2, x_3 \ge 0
```

Source Code:

from scipy.optimize import linprog

Z

```
1 from scipy.optimize import linprog
In [1]:
           3 \text{ obj } = [1, -3, 2]
            5 lhs_ineq = [[3, -1, 3],
                             [-2, 4, 0],
            7
                              [-4, 3, 8]]
           8
           9 rhs_ineq = [7,
           10
                              12,
           11
                              10]
           12
          13 bound = [(0, float("inf")),
14 (0, float("inf")),
15 (0, float("inf"))]
          z = linprog(c = obj, A_ub = lhs_ineq, b_ub = rhs_ineq,
bounds = bound, method = "revised simplex")
In [2]:
            3
            4 z
Out[2]:
                con: array([], dtype=float64)
           fun: -11.0
message: 'Optimization terminated successfully.'
                nit: 2
              slack: array([ 0., 0., 11.])
            status: 0
           success: True
                  x: array([4., 5., 0.])
```

Aim: Use simplex method to solve the following LPP:

Max
$$Z = x + 2y$$

w.r.t.
 $2x + y \le 20$,
 $-4x + 5y \le 10$,
 $-x + 2y \ge -2$,
 $-x + 5y = 15$,
 $x, y \ge 0$

Source code:

Z

from scipy.optimize import linprog

```
1 from scipy.optimize import linprog
In [1]:
          3 obj = [-1, -2]
          4
          9 rhs_ineq = [20,
         10
                         10,
         11
                         2]
         12
         13 lhs_eq = [[-1, 5]]
14 rhs_eq = [15]
         15
         16 bound = [(0, float("inf")),
         17
                     (0, float("inf"))]
          1 z = linprog(c = obj, A_ub = lhs_ineq, b_ub = rhs_ineq,
In [2]:
                         A_eq = lhs_eq, b_eq = rhs_eq,
bounds = bound, method = "revised simplex")
          4
          5 z
Out[2]:
             con: array([0.])
             fun: -16.8181818181817
         message: 'Optimization terminated successfully.'
             nit: 3
           slack: array([ 0. , 18.18181818, 3.36363636])
          status: 0
         success: True
          __ x: array([7.72727273, 4.54545455])
```

Aim: Use Big M method to solve the following LPP:

```
Min Z = 4x_1 + x_2
w.r.t.
3x_1 + 4x_2 \ge 12,
x_1 + 5x_2 \ge 15,
x_1, x_2 \ge 0
```

Source code:

from scipy.optimize import linprog

```
from scipy.optimize import linprog
In [1]:
          2
          3
            obj = [4, 1]
          4 lhs_ineq = [[-3, -4],
          5
                         [-1, -5]]
          6
          7
            rhs_ineq = [-20,
          8
                         -15]
          9
         10
            bound = [(0, float("inf")),
         11
                      (0, float("inf"))]
In [2]:
            opt =linprog(c=obj,A_ub=lhs_ineq,b_ub=rhs_ineq,
          1
                            bounds=bound,method="interior-point")
          3
          4
            opt
Out[2]:
             con: array([], dtype=float64)
             fun: 5.0000000002364455
         message: 'Optimization terminated successfully.'
             nit: 5
           slack: array([1.64270375e-10, 1.00000000e+01])
          status: 0
         success: True
               x: array([6.01160437e-11, 5.00000000e+00])
```

Aim: Use any method to solve the following resource allocation problem:

$$\begin{aligned} &\text{Max Z} = 20x_1 + 12x_2 + 50x_3 + 25x_4 \dots \text{(profit)} \\ &\text{w.r.t.} \\ &x_1 + x_2 + x_3 + x_4 \leq 50 \dots \text{(manpower)} \\ &3x_1 + 2x_2 + x_3 \leq 100 \dots \text{(material A)} \\ &x_2 + 2x_3 \leq 90, \dots \text{(material B)} \\ &x_1, x_2, x_3 \geq 0 \end{aligned}$$

Source code:

from scipy.optimize import linprog

obj =
$$[-20, -12, -40, -25]$$

lhs_ineq = $[[1, 1, 1, 1], [3, 2, 1, 0], [0, 1, 2, 3]]$

rhs_ineq = $[50, 100, 90]$

opt = linprog(c = obj, A_ub = lhs_ineq, b_ub = rhs_ineq, method="revised simplex")

opt

```
In [1]: 1 from scipy.optimize import linprog
         3 obj = [-20, -12, -40, -25]
         9 rhs_ineq = [50,
        10
                     100,
        11
                     90]
        opt = linprog(c = obj, A_ub = lhs_ineq, b_ub = rhs_ineq, method="revised simplex")
In [2]:
         3 opt
Out[2]:
            con: array([], dtype=float64)
        fun: -1900.0
message: 'Optimization terminated successfully.'
            nit: 2
          slack: array([ 0., 40., 0.])
         status: 0
         success: True
              x: array([ 5., 0., 45., 0.])
```

Aim: Use simplex method to solve the following LPP:

```
Max Z = 200x + 300y
w.r.t.
2x + 3y \ge 1200,
x + y \le 400,
2x + 1.5y \ge 900,
x, y \ge 0
```

Source code:

```
from scipy.optimize import linprog
```

Aim: Use dual simplex method to solve the following LPP:

```
Max Z = 40x_1 + 50x_2
w.r.t.
2x_1 + 3x_2 \le 3,
8x_1 + 4x_2 \le 5,
x_1, x_2 \ge 0
```

Source code:

```
> lp("max", f.obj, f.con, f.dir, f.rhs, compute.sens = T)$duals
[1] 15.00 1.25 0.00 0.00
> lp("max", f.obj, f.con, f.dir, f.rhs, compute.sens = T)$duals.to
[1] 3.75e+00 1.20e+01 1.00e+30 1.00e+30
>
```

Aim: Solve following transportation problem in which each cell represents unit costs:

	Customers			Cumply	
	1	2	3	4	Supply
	10	2	20	11	15
Suppliers	12	7	9	20	25
	4	14	16	18	10
Demand	5	15	15	15	

Source code:

```
> total.cost ← lp.transport(cost, "min", row.signs, row.rhs, col.signs, col.rhs)
> total.cost$solution
      [,1] [,2] [,3] [,4]
[1,] 0 5 0 10
[2,] 0 10 15 0
[3,] 5 0 0 5
> print(total.cost)
Success: the objective function is 435
```

Aim: Solve following assignment problem represented in this matrix:

		Jobs			
		1	2	3	
	1	15	10	9	
Workers	2	9	15	10	
	3	10	12	8	

Source Code:

```
> answer ← lp.assign(cost)
> answer$solution
      [,1] [,2] [,3]
[1,] 0 1 0
[2,] 1 0 0
[3,] 0 0 1
> |
```