

Task 1: Dijkstra's Shortest Path Finder

Code Dijkstra's algorithm to find the shortest path from a start node to every other node in a weighted graph with positive Weight.

```
package com.wipro.graphalgo;
import java.util.*;

public class Dijkstra {

    public void dijkstra(List<List<int[]>> graph, int src) {
        int V = graph.size();
        int[] dist = new int[V];
        Arrays.fill(dist, Integer.MAX_VALUE);
        dist[src] = 0;

        boolean[] visited = new boolean[V];

        int[] minHeap = new int[V];
        int heapSize = 0;

        minHeap[heapSize++] = src;

        while (heapSize > 0) {

            int u = extractMin(minHeap, dist, heapSize);
            heapSize--;

            if (visited[u]) continue;
            visited[u] = true;

            for (int[] edge : graph.get(u)) {
                int v = edge[0], weight = edge[1];
                if (dist[u] + weight < dist[v]) {
                    dist[v] = dist[u] + weight;
                    if (!visited[v]) {
                        minHeap[heapSize++] = v;
                        heapifyUp(minHeap, dist, heapSize - 1);
                    }
                }
            }
        }

        printSolution(dist);
    }
}
```

```

    private int extractMin(int[] minHeap, int[] dist, int
heapSize) {
        int minIndex = 0;
        for (int i = 1; i < heapSize; i++) {
            if (dist[minHeap[i]] < dist[minHeap[minIndex]]) {
                minIndex = i;
            }
        }
        int minVertex = minHeap[minIndex];
        minHeap[minIndex] = minHeap[heapSize - 1];
        return minVertex;
    }

    private void heapifyUp(int[] minHeap, int[] dist, int index) {
        while (index > 0) {
            int parent = (index - 1) / 2;
            if (dist[minHeap[index]] < dist[minHeap[parent]]) {
                swap(minHeap, index, parent);
                index = parent;
            } else {
                break;
            }
        }
    }

    private void swap(int[] minHeap, int i, int j) {
        int temp = minHeap[i];
        minHeap[i] = minHeap[j];
        minHeap[j] = temp;
    }

    private void printSolution(int[] dist) {
        System.out.println("Shortest distances from source:");
        for (int i = 0; i < dist.length; i++) {
            System.out.println("Vertex " + i + ": " + dist[i]);
        }
    }

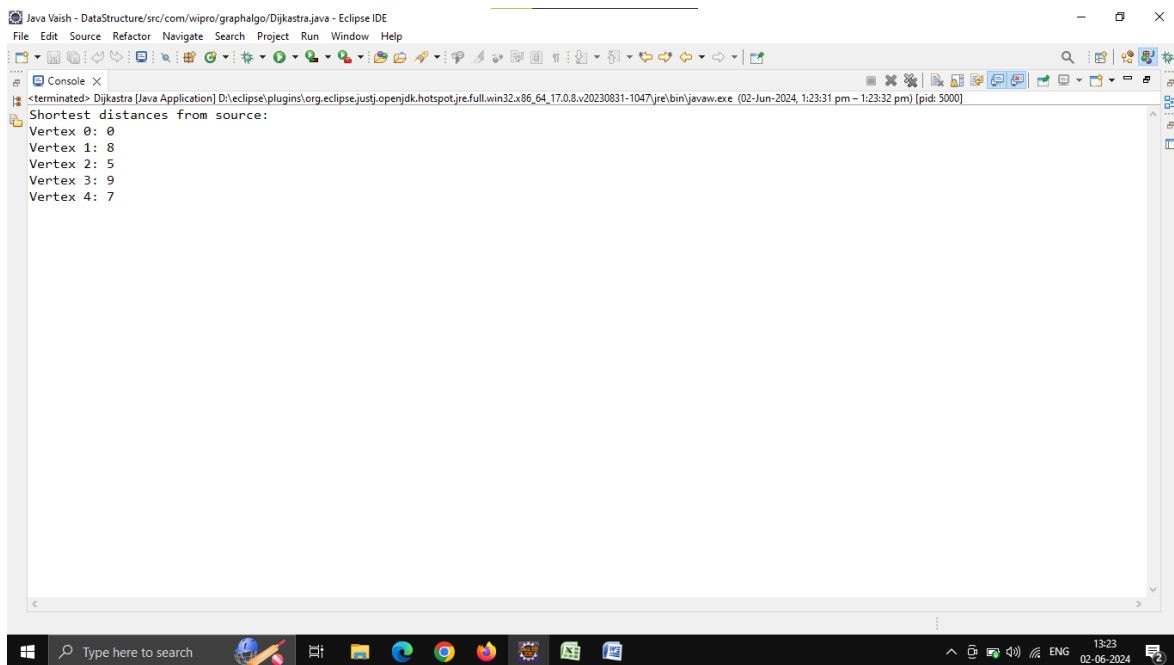
    public static void main(String[] args) {

        List<List<int[]>> graph = new ArrayList<>();
        int V = 5;
        for (int i = 0; i < V; i++) {
            graph.add(new ArrayList<>());
        }
        graph.get(0).add(new int[]{1, 10});
        graph.get(0).add(new int[]{2, 5});
    }

```

```
graph.get(1).add(new int[]{2, 2});  
graph.get(1).add(new int[]{3, 1});  
graph.get(2).add(new int[]{1, 3});  
graph.get(2).add(new int[]{3, 9});  
graph.get(2).add(new int[]{4, 2});  
graph.get(3).add(new int[]{4, 4});  
graph.get(4).add(new int[]{0, 7});
```

```
Dijkstra dijkstra = new Dijkstra();  
int src = 0;  
dijkstra.dijkstra(graph, src);  
}  
}
```



Task 2: Kruskal's Algorithm for MST

Implement Kruskal's algorithm to find the minimum spanning tree of a given connected, undirected graph with non-negative edge weights.

```
package com.wipro.graphalgo;
import java.util.*;
class Edge implements Comparable<Edge> {
    int source, destination, weight;

    public Edge(int source, int destination, int weight) {
        this.source = source;
        this.destination = destination;
        this.weight = weight;
    }

    @Override
    public int compareTo(Edge other) {
        return this.weight - other.weight;
    }
}

public class kruskal{
    private int V;
    private List<Edge> edges;

    public kruskal(int V) {
        this.V = V;
        this.edges = new ArrayList<>();
    }

    public void addEdge(int source, int destination, int weight) {
        edges.add(new Edge(source, destination, weight));
    }

    private int findParent(int[] parent, int vertex) {
        if (parent[vertex] == vertex)
            return vertex;
        return findParent(parent, parent[vertex]);
    }

    private void union(int[] parent, int x, int y) {
        int xSet = findParent(parent, x);
        int ySet = findParent(parent, y);
        parent[ySet] = xSet;
    }

    public List<Edge> findMinimumSpanningTree() {
        List<Edge> minimumSpanningTree = new ArrayList<>();
```

```

        Collections.sort(edges);

        int[] parent = new int[V];
        for (int i = 0; i < V; i++) {
            parent[i] = i;
        }

        int edgeCount = 0;
        for (Edge edge : edges) {
            if (edgeCount == V - 1)
                break;

            int x = findParent(parent, edge.source);
            int y = findParent(parent, edge.destination);

            if (x != y) {
                minimumSpanningTree.add(edge);
                union(parent, x, y);
                edgeCount++;
            }
        }

        return minimumSpanningTree;
    }

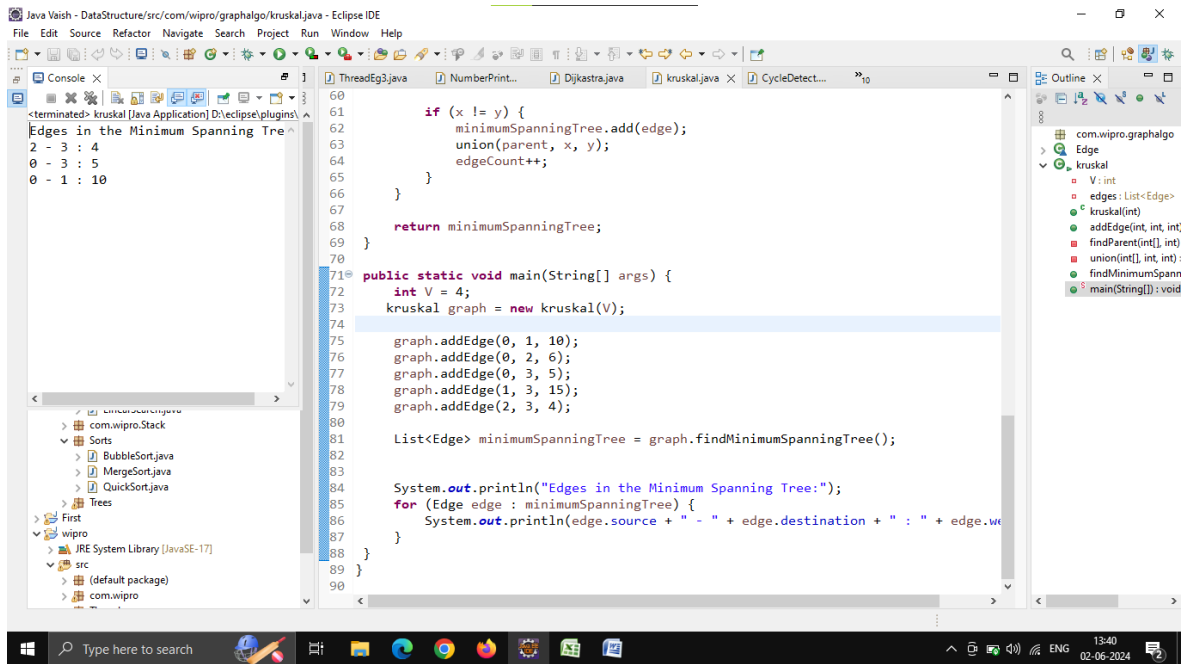
    public static void main(String[] args) {
        int V = 4;
        kruskal graph = new kruskal(V);

        graph.addEdge(0, 1, 10);
        graph.addEdge(0, 2, 6);
        graph.addEdge(0, 3, 5);
        graph.addEdge(1, 3, 15);
        graph.addEdge(2, 3, 4);

        List<Edge> minimumSpanningTree =
graph.findMinimumSpanningTree();

        System.out.println("Edges in the Minimum Spanning Tree:");
        for (Edge edge : minimumSpanningTree) {
            System.out.println(edge.source + " - " + edge.destination
+ " : " + edge.weight);
        }
    }
}

```



Task 3: Union-Find for Cycle Detection

Write a Union-Find data structure with path compression.
Use this data structure to detect a cycle in an undirected graph.

```
package com.wipro.graphalgo;
import java.util.Arrays;
class UnionFind{
    int[] parent;
    int[] rank;

    UnionFind(int n){
        parent=new int[n];
        rank=new int[n];
        Arrays.fill(rank,1);
        for(int i=0;i<n;i++) {
            parent[i]=i;
        }
    }
    int find(int i) {
        if(parent[i] != i) {
            parent[i]=find(parent[i]);
        }
        return parent[i];
    }
    void union(int x,int y) {
        int rootX = find(x);
        int rootY = find(y);

        if(rootX != rootY) {
            if (rank[rootX] < rank[rootY]) { // 1<2
                parent[rootX] = rootY;
            } else if (rank[rootX] > rank[rootY]) {
                parent[rootY] = rootX;
            } else {
                parent[rootY] = rootX;
                rank[rootX]++;
            }
        }
    }
}
```

```

class Graph {
    int V, E;
    Edge[] edges;

    class Edge {
        int src, dest;
    }

    Graph(int v, int e) {
        this.V = v;
        this.E = e;
        this.edges = new Edge[E];
        for (int i = 0; i < e; i++) {
            edges[i] = new Edge();
            System.out.println(edges[i].src + " -- " +
edges[i].dest);
        }

    }

    public boolean isCycleFound(Graph graph) {
        UnionFind uf = new UnionFind(V);
        for(int i=0;i<E;++i) {
            int x=find(uf,graph.edges[i].src);
            int y =find(uf,graph.edges[i].src);

            if(x==y) {
                return true;
            }
            uf.union(x,y);
        }
        return false;
    }

    private int find(UnionFind uf,int i) {
        return uf.find(i);
    }
}

public class CycleDetect {
    public static void main(String[] args){
        int V=3,E=2;

        Graph graph = new Graph(V, E);

        graph.edges[0].src = 0;
        graph.edges[0].dest = 1;

        graph.edges[1].src = 1;
        graph.edges[1].dest = 2;
    }
}

```

```

        System.out.println(graph.V + " -- " + graph.E);
        for (int i = 0; i < E; i++) {

            System.out.println(graph.edges[i].src + " -- " +
graph.edges[i].dest);
        }

        if(graph.isCycleFound(graph)) {
            System.out.println("Cycle Found");
        }else {
            System.out.println("Cycle Not Found...");
        }
    }
}

```

